Lecture 3: The Principal-Agent Model

Compensation in Organizations

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Discussion: Lazear (2000)

Why a Model? (Clarity of Thought)

- ▶ "All models are wrong, but some are useful." -George Box
- Maps are useful precisely because they ignore some features.
- ▶ A good model has what we need to study one question, and nothing more.
- Under the model's assumptions, we know the truth.
- ▶ If the outcome is unrealistic, we can argue about which precise assumptions led to it.

Why THIS Model?

- ▶ The model we study in this lecture will be the main model of this class.
- ▶ We will slightly change it to study different questions.
- ▶ It was developed in the 1970s and has framed theoretical and empirical research for decades.

The Principal-Agent Model

Players

- There is a firm (the principal) who is risk neutral (exponential utility with parameter r = 0).
- There is a worker (the agent) who is risk averse (exponential utility with parameter $r = r \ge 0$).

Actions

- Firm chooses a linear wage which depends on effort (w(e)) or output (w(y))
- ► After seeing the wage, the worker either accepts or rejects the job.
- If they accept, worker chooses effort e at an increasing, convex cost c(e)

The Principal-Agent Model

Output

- Output is effort (e) plus noise/luck (ϵ): $y = e + \epsilon$ where $\epsilon \sim N(0, \sigma^2)$
- ▶ This implies output is normal with mean e and variance σ^2

Payoffs

- ▶ If accepted, firm's payoff π is expected output minus expected wages: E[y w|e]
- ▶ If accepted, worker's payoff is expected utility of the wage minus effort cost: E[u(w) c(e)|e]
- ▶ If rejected, worker has "outside option" of \bar{u} and firm has "outside option" of 0.¹
- 1. We will assume throughout that the firm prefers to hire the worker ex-ante.

Timing

See the board!

Effort-Based Pay

- Suppose the firm can pay based on the worker's effort.
- ▶ Then wage is a linear function of effort: $w(e) = \alpha + \beta e$
- ▶ We now go to the board to solve!

Effort-Based Pay

Theorem 1

When wages depend directly on effort, effort is e^* which solves $c'(e^*) = 1$ and $\beta^* = 1, \alpha^* = \bar{u} + c(e^*) - 1$

- We reward the worker for more effort.
- Question: What is the worker's expected payoff?
- Question: Why is the marginal cost set equal to 1?
- Let's compute the firm's payoff and total surplus on the board.

Effort-Based Pay

- ▶ We showed that this is the first-best: the firm could not do better even if they did the work themselves!
- ▶ The firm gets everything, but if the worker proposed they would get everything
- Question: What assumption did we bake in that got us here?
- Question: Is this assumption realistic?

Selling the Firm

Theorem 2

When wages depend directly on effort, effort is e^* which solves $c'(e^*) = 1$ and $\beta^* = 1, \alpha^* = \bar{u} + c(e^*) - 1$

- ightharpoonup Consider our result: $\beta = 1$ and the average return to effort is 1
- ► The firm gives the worker everything they produce.
- ▶ This is called selling the firm: the worker pays α but keeps everything they make!
- ► These are extremely strong incentives (why?)

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- Does this ever happen?
- Question: Can you give some examples?