

# Problem Set 2

Jacob Kohlhepp

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The purpose of this homework is to work through a multitasking problem and a relative performance evaluation problem. There are only minor differences between these problems and the ones we did in class, so your notes should be very helpful in completing this problem set.

## 1 Meaning and Performance

### 1.1 Setup

- The cost of effort is:  $c_{ij}(e) = \frac{e^2}{2(1+\lambda_i m_{ij})}$ .
- Output is given by:  $y_{ij} = \theta_i e + \epsilon_{ij}$ .
- The contract is based on output:  $w_{ij}(y_{ij}) = \alpha_{ij} + \beta_{ij} y_{ij} = \alpha_{ij} + \beta_{ij}(\theta_i e_{ij} + \epsilon_{ij})$
- The timing is as usual: the firm designs the contract and the worker then decides how much effort to exert.

### 1.2 Questions

1. Show the model captures the idea that “if you enjoy your job you will never work a day in your life.”
2. Explain how we can return to our standard effort-based pay model by setting primitives to certain values.
3. Taking the contract as given (and assuming the worker takes the job), solve for the worker’s effort.
4. Explain why the “take the job” step from our standard performance pay or effort based-pay model does not make sense in this setting. Make sure to connect it to the reading.
5. Given your earlier answers, maximize firm  $j$ ’s profit with respect to  $\beta_{ij}$ , and solve for the firm’s profit maximizing bonus.
6. Write down and simplify the worker’s utility from taking the job assuming some given base pay  $\alpha_{ij}$ .<sup>1</sup>
7. Write down and simplify an inequality that represents the worker choosing between two jobs  $p$  and  $a$ .
8. The experiment in the paper changed  $\lambda_i$  from 0 to 1. Use the model to show how this should impact effort of some fixed worker  $i$  who stays. Hint: Verification 2 in the paper will help.

## 2 Multitasking

There are two key differences in the setup of this problem vs. what we did in class:

1. Task 1 effort is measured in different “units.”
2. I am telling you specific values for  $a, b$  in the last part of the problem.

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<sup>1</sup>Remember we do not allow the firm to choose the base pay in this model so it is just a primitive.

## 2.1 Setup

- Output is  $y = ae_1 + be_2$
- Cost of effort is:

$$c(e_1, e_2) = \begin{cases} 0 & \text{if } e_1 + e_2 \leq 2\bar{e} \\ (e_1 + e_2 - 2\bar{e})^2/2 & \text{if } e_1 + e_2 > 2\bar{e} \end{cases}$$

- We assume that without incentives the worker supplies all 0 cost effort and splits effort evenly:

$$e_1 = e_2 = \bar{e}$$

- Only task 1 effort is measured:  $m = k \cdot e_1$ , where  $k > 0$ .
- The firm can only pay based on task 1:  $w(m) = \alpha + \beta m = \alpha + \beta k e_1$
- The firm's and worker's outside options are 0.

## 2.2 Questions

1. Setup the firm's problem in the first-best, that is when the firm can just choose effort directly and we do not care about wages.
2. Solve for the first-best  $e_1, e_2$  when  $a > b, a > 0$ . Only assume that  $a > b$  for this problem.
3. From now on we are solving for equilibrium, meaning the firm cannot choose effort directly but just chooses a compensation scheme. Setup the worker's effort choice problem.
4. Solve for worker's choice of effort assuming for now until told otherwise that  $\beta > 0$ .
5. Write down the inequality that determines whether the worker takes the job. Argue that it must be an equality.
6. Setup the firm's profit maximization problem. Substitute past work in so that it is only a function of  $\beta$ .
7. Solve for  $\beta, e_1, e_2$ .
8. Now, solve for  $e_1, e_2$  when  $\beta = 0$ . You may use the same steps we just did or do it your own way.
9. From now until I say otherwise assume that  $a = -1, b = 2, \bar{e} = 1$ . Provide an interpretation for  $a$  being negative.
10. Using the work you have already done, should the firm set  $\beta = 0$  or  $\beta > 0$ ? Find  $\beta, e_1, e_2$ .
11. Now assume that  $a = 2, b = 1, \bar{e} = 1$ . Using the work you have already done, should the firm set  $\beta = 0$  or  $\beta > 0$ ? Find  $\beta, e_1, e_2$ .
12. Do your answers to any of these questions depend on  $k$ ? Interpret your answer.