

# Implementation of the Belle Model for $D^0 \rightarrow K_S^0 \pi^+ \pi^-$ and $\bar{D}^0 \rightarrow K_S^0 \pi^+ \pi^-$ decay in ampGen

Jake Lane

July 5, 2019

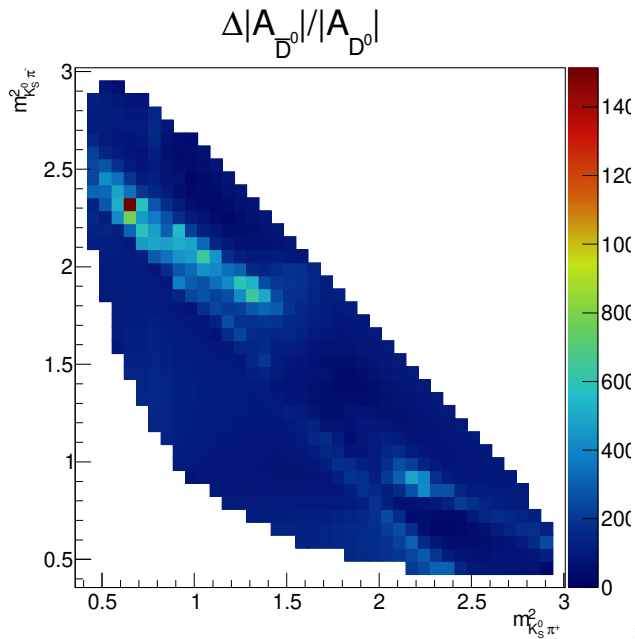
# Belle in Cartesian

```
CouplingConstant::Coordinates cartesian
Import $AMPGENROOT/options/kMatrix.opt
Particle::DefaultModifier BL
Particle::SpinFormalism Canonical
```

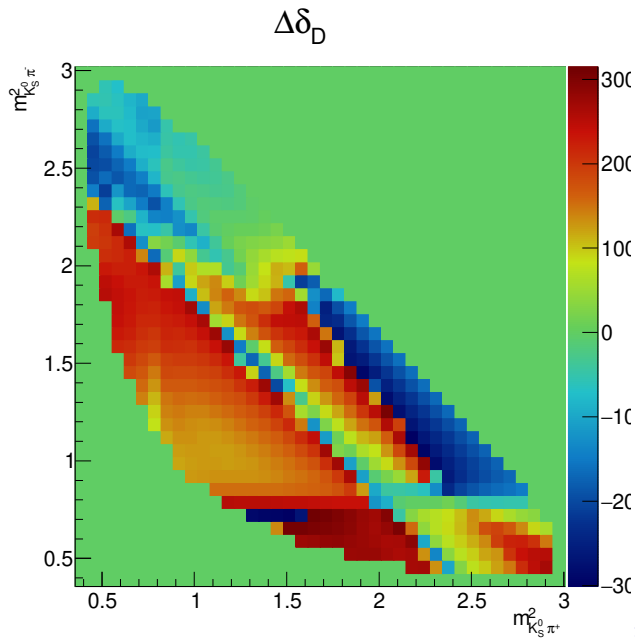
```
D0{K(0)*(1430)+[GLASS]{K0S0,pi+},pi-} 0 0.0095653 0.000827718 0 0.00601207 0.000843
D0{K(0)*(1430)bar-[GLASS]{K0S0,pi-},pi+} 0 0.0255993 0.00122597 0 -0.194327 0.001053
D0{K(2)*(1430)+{K0S0,pi+},pi-} 0 0.0133101 0.00135651 0 0.0170886 0.00123279
D0{K(2)*(1430)bar-{K0S0,pi-},pi+} 0 -0.107163 0.00146194 0 0.104979 0.00164431
D0{K*(1410)+{K0S0,pi+},pi-} 0 0.00296544 0.00225542 0 0.014186 0.00247679
D0{K*(1410)bar-{K0S0,pi-},pi+} 0 -0.0339155 0.00309512 0 0.0613357 0.0037167
D0{K*(1680)bar-{K0S0,pi-},pi+} 0 -0.0535469 0.00651378 0 0.0272353 0.0073212
D0{K*(892)+{K0S0,pi+},pi-} 0 0.126313 0.00245399 0 -0.140858 0.00235595
D0{K*(892)bar-{K0S0,pi-},pi+} 0 -1.37962 0.00769138 0 1.49371 0.00800201
D0{K0S0,PiPi00} 2 1 0 2 0 0
D0{K0S0,f(2)(1270)0{pi+,pi-}} 0 -0.125526 0.00221442 0 0.0943573 0.00286431
D0{K0S0,omega(782)0{pi+,pi-}} 0 -0.0640864 0.00196373 0 0.12832 0.00170606
D0{K0S0,rho(1450)0{pi+,pi-}} 0 0.160532 0.00460311 0 0.0886014 0.00646564
D0{K0S0,rho(770)0{pi+,pi-}} 2 1 0 2 0 0
```

```
Dbar0{K(0)*(1430)bar-[GLASS]{K0S0,pi-},pi+} 0 0.0095653 0.000827718 0 0.00601207 0
Dbar0{K(0)*(1430)+[GLASS]{K0S0,pi+},pi-} 0 0.0255993 0.00122597 0 -0.194327 0.001053
Dbar0{K(2)*(1430)bar-{K0S0,pi-},pi+} 0 0.0133101 0.00135651 0 0.0170886 0.00123279
Dbar0{K(2)*(1430)+{K0S0,pi+},pi-} 0 -0.107163 0.00146194 0 0.104979 0.00164431
Dbar0{K*(1410)bar-{K0S0,pi-},pi+} 0 0.00296544 0.00225542 0 0.014186 0.00247679
Dbar0{K*(1410)+{K0S0,pi+},pi-} 0 -0.0339155 0.00309512 0 0.0613357 0.0037167
Dbar0{K*(1680)+{K0S0,pi+},pi-} 0 -0.0535469 0.00651378 0 0.0272353 0.0073212
Dbar0{K*(892)bar-{K0S0,pi-},pi+} 0 0.126313 0.00245399 0 -0.140858 0.00235595
Dbar0{K*(892)+{K0S0,pi+},pi-} 0 -1.37962 0.00769138 0 1.49371 0.00800201
Dbar0{K0S0,PiPi00} 2 1 0 2 0 0
Dbar0{K0S0,f(2)(1270)0{pi+,pi-}} 0 -0.125526 0.00221442 0 0.0943573 0.00286431
Dbar0{K0S0,omega(782)0{pi+,pi-}} 0 -0.0640864 0.00196373 0 0.12832 0.00170606
Dbar0{K0S0,rho(1450)0{pi+,pi-}} 0 0.160532 0.00460311 0 0.0886014 0.00646564
Dbar0{K0S0,rho(770)0{pi+,pi-}} 2 1 0 2 0 0
```

# Belle in Cartesian



# Belle in Cartesian



# Belle in Cartesian

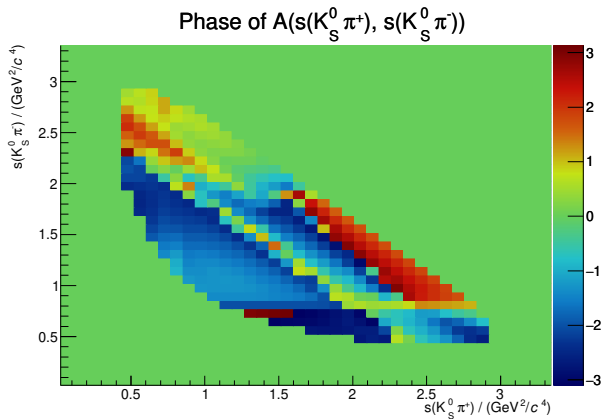


Figure: Argument for Belle in Cartesian

# Belle in Cartesian

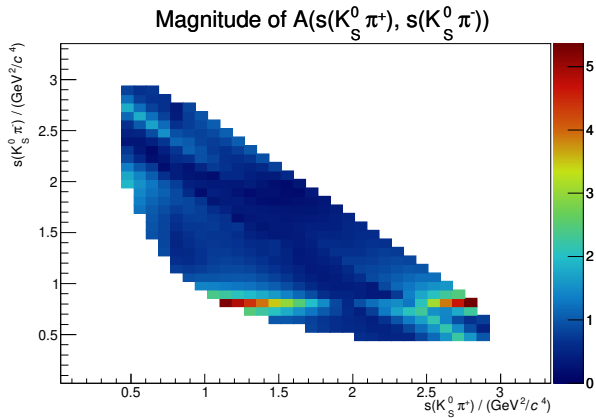


Figure: Magnitude for Belle in Cartesian

# Belle in Cartesian

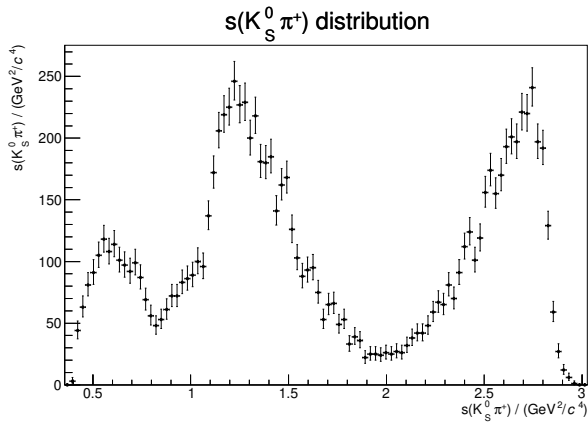


Figure:  $m_+^2$  for Belle in Cartesian

# Belle in Cartesian

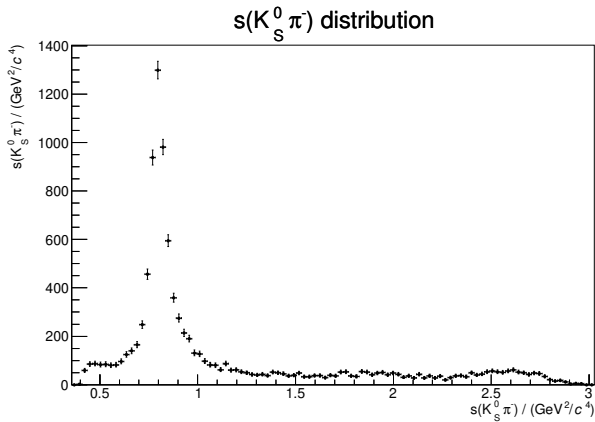


Figure:  $m_-^2$  for Belle in Cartesian



# Belle in Cartesian

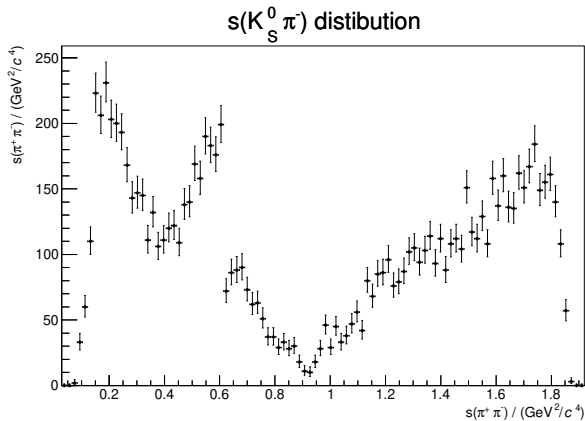


Figure:  $m_0^2$  for Belle in Cartesian

# Belle in Cartesian

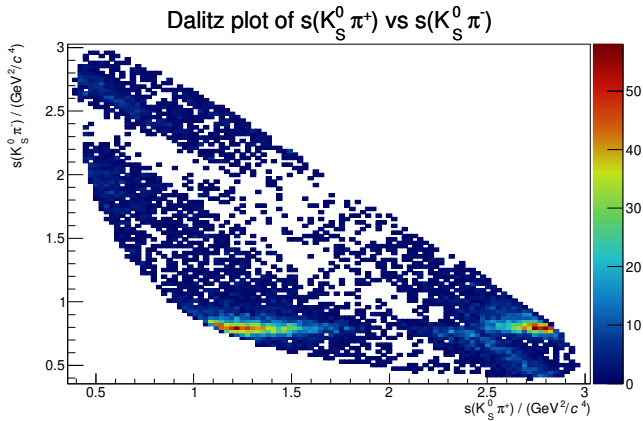


Figure:  $m_+^2$  vs  $m_-^2$  for Belle in Cartesian

# Belle in Cartesian

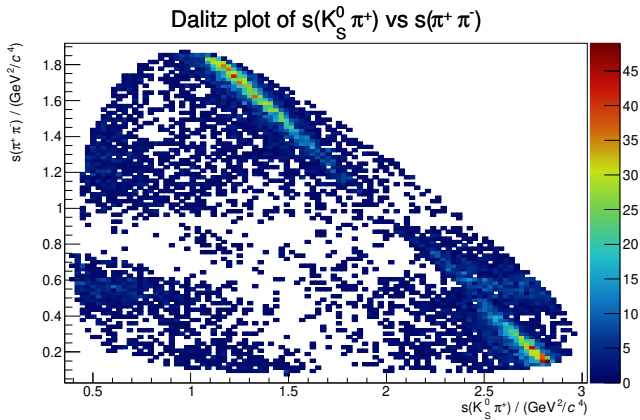


Figure:  $m_+^2 \text{ vs } m_0^2$  for Belle in Cartesian

# Belle in Cartesian

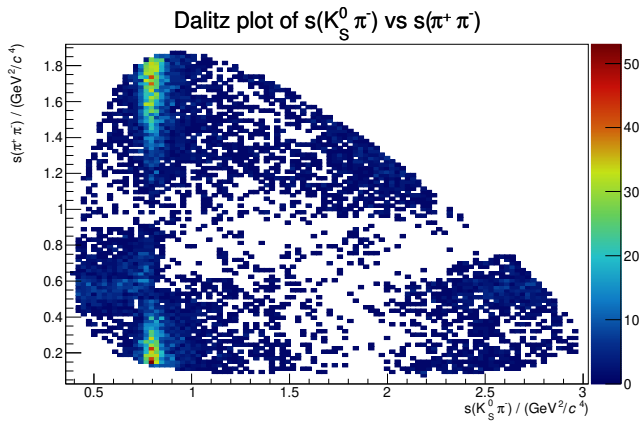


Figure:  $m_+^2$  vs  $m_0^2$  for Belle in Cartesian

# Belle in Cartesian

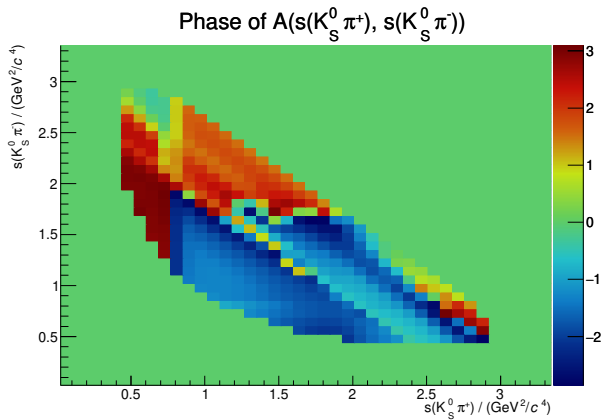


Figure: Argument for Belle in Cartesian

# Belle in Cartesian

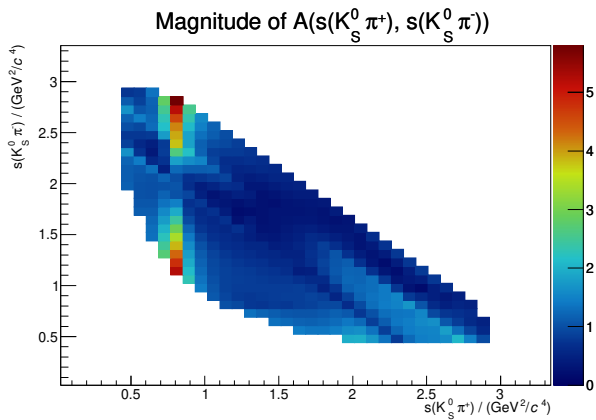


Figure: Magnitude for Belle in Cartesian

# Belle in Cartesian

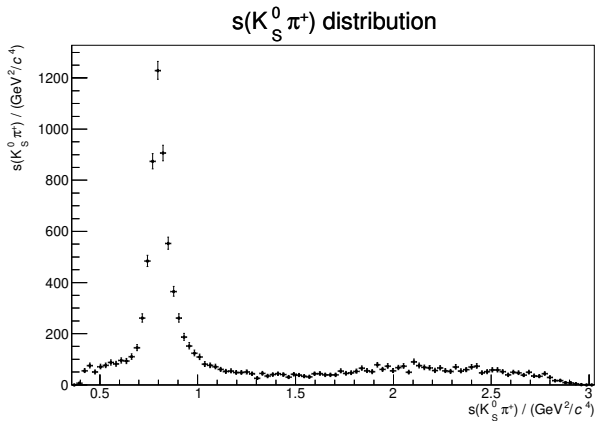


Figure:  $m_+^2$  for Belle in Cartesian

# Belle in Cartesian

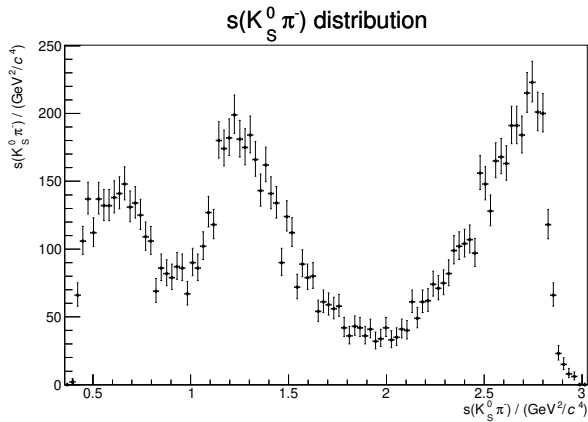


Figure:  $m_-^2$  for Belle in Cartesian



# Belle in Cartesian

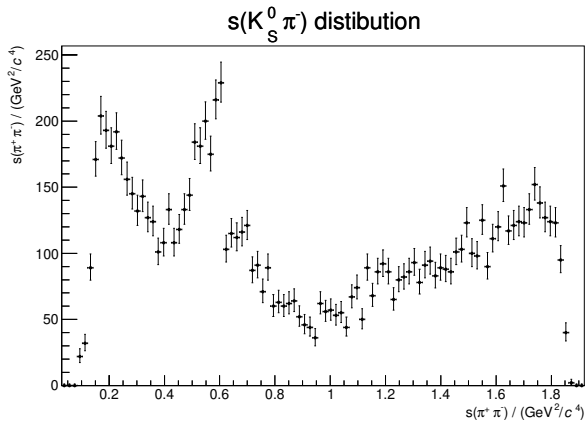


Figure:  $m_0^2$  for Belle in Cartesian

# Belle in Cartesian

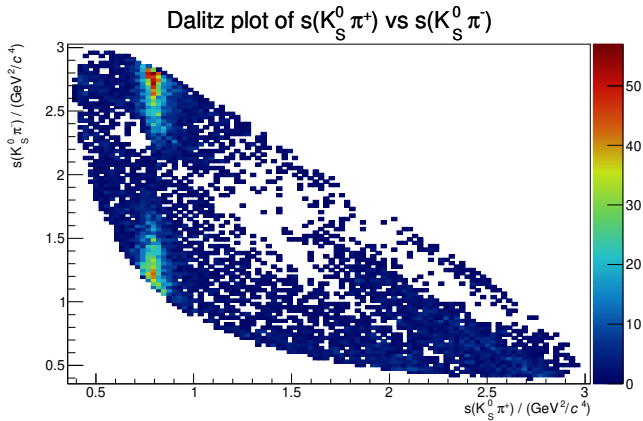


Figure:  $m_+^2$  vs  $m_-^2$  for Belle in Cartesian

# Belle in Cartesian

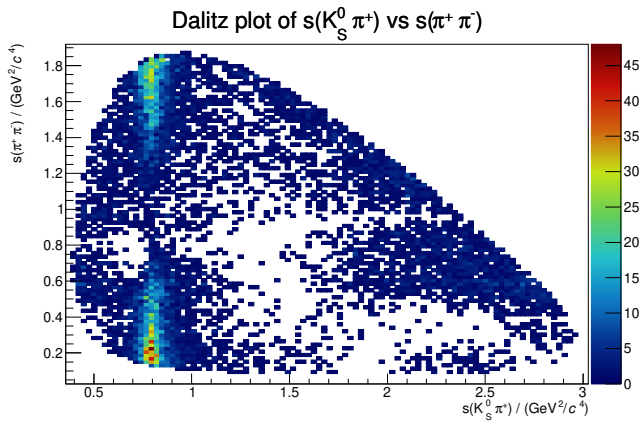


Figure:  $m_+^2$  vs  $m_0^2$  for Belle in Cartesian

# Belle in Cartesian

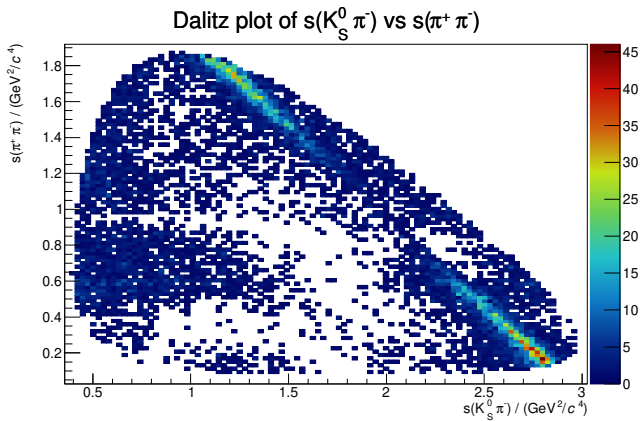


Figure:  $m_+^2$  vs  $m_0^2$  for Belle in Cartesian

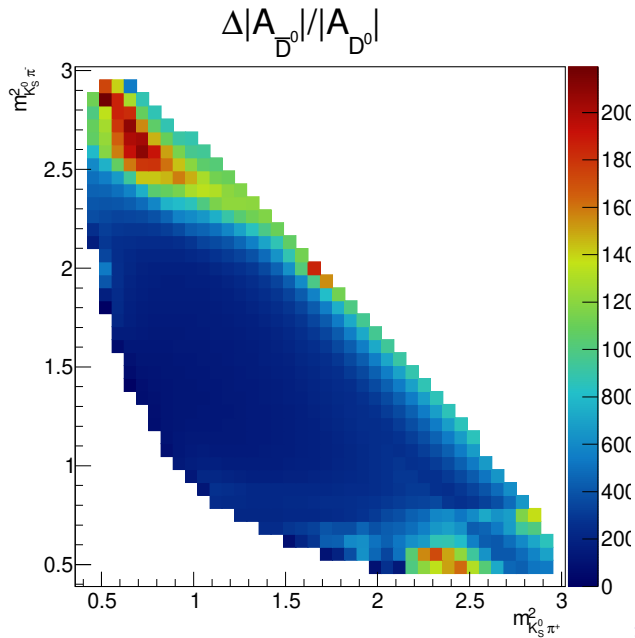
# Belle in Polar

#Belle Model from <https://arxiv.org/pdf/1804.06153v1.pdf>

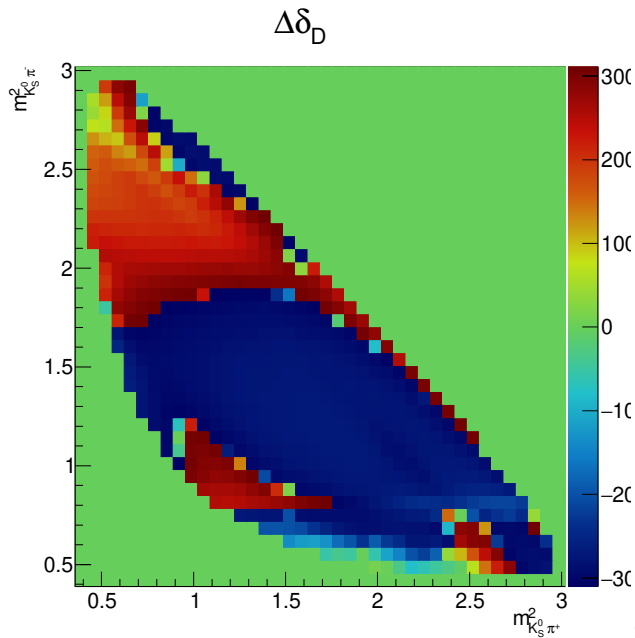
```
#EventType D0 K0S0 pi+ pi-
CouplingConstant::Coordinates polar
CouplingConstant::AngularUnits deg
Import "$AMPGEN"/kspipi/kMatrix.opt
Particle::DefaultModifier BL
Particle::SpinFormalism Canonical
```

```
D0{K*(892)bar-{K0S0,pi-},pi+} 0 1.72 0.006 0 136.8 0.2
D0{K(0)*(1430)bar-[GLASS]{K0S0,pi-},pi+} 0 2.36 0.06 0 99.4 1.7
D0{K(2)*(1430)bar-{K0S0,pi-},pi+} 0 1.27 0.02 0 -44.1 0.8
D0{K*(1410)bar-{K0S0,pi-},pi+} 0 0.29 0.03 0 99.4 5.5
D0{K*(1680)bar-{K0S0,pi-},pi+} 0 3.31 0.2 0 -118.2 3.1
D0{K*(892)+{K0S0,pi+},pi-} 0 0.0164 0.003 0 -42.2 0.9
D0{K*(1410)+{K0S0,pi+},pi-} 0 0.21 0.02 0 150.2 5.3
D0{K(0)*(1430)+[GLASS]{K0S0,pi+},pi-} 0 0.11 0.01 0 162.3 6.6
D0{K(2)*(1430)+{K0S0,pi+},pi-} 0 0.1 0.01 0 -89.6 7.6
D0{K0S0,rho(770)0{pi+,pi-}} 2 1 0 2 0 0
D0{K0S0,omega(782)0{pi+,pi-}} 0 0.0388 0.0005 0 120.7 0.7
D0{K0S0,f(2)(1270)0{pi+,pi-}} 0 1.43 0.03 0 -36.3 1.1
D0{K0S0,rho(1450)0{pi+,pi-}} 0 2.85 0.1 0 102.1 1.9
D0{K0S0,PiPi00} 0 0.1 0 0 0 0
Dbar0{K*(892)+{K0S0,pi+},pi-} 0 1.72 0.006 0 136.8 0.2
Dbar0{K(0)*(1430)+[GLASS]{K0S0,pi+},pi-} 0 2.36 0.06 0 99.4 1.7
Dbar0{K(2)*(1430)+{K0S0,pi+},pi-} 0 1.27 0.02 0 -44.1 0.8
Dbar0{K*(1410)+{K0S0,pi+},pi-} 0 0.29 0.03 0 99.4 5.5
Dbar0{K*(1680)+{K0S0,pi+},pi-} 0 3.31 0.2 0 -118.2 3.1
Dbar0{K*(892)bar-{K0S0,pi-},pi+} 0 0.164 0.003 0 -42.2 0.9
Dbar0{K*(1410)bar-{K0S0,pi-},pi+} 0 0.21 0.02 0 150.2 5.3
Dbar0{K(0)*(1430)bar-[GLASS]{K0S0,pi-},pi+} 0 0.11 0.01 0 162.3 6.6
Dbar0{K(2)*(1430)bar-{K0S0,pi-},pi+} 0 0.1 0.01 0 -89.6 7.6
Dbar0{K0S0,rho(770)0{pi+,pi-}} 2 1 0 2 0 0
Dbar0{K0S0,omega(782)0{pi+,pi-}} 0 0.0388 0.0005 0 120.7 0.7
Dbar0{K0S0,f(2)(1270)0{pi+,pi-}} 0 1.43 0.03 0 -36.3 1.1
```

# Belle in Polar



# Belle in Polar



# Belle in Polar

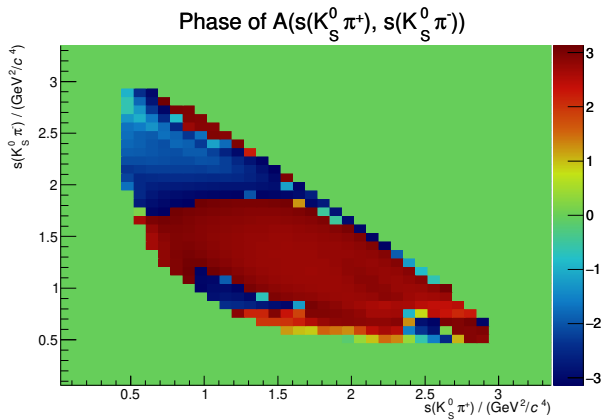


Figure: Argument for Belle in Polar



# Belle in Polar

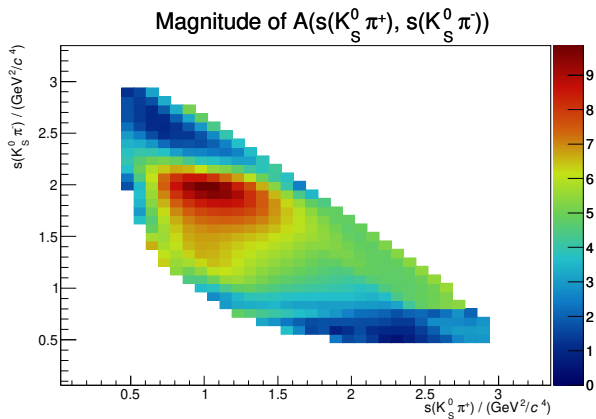


Figure: Magnitude for Belle in Polar

# Belle in Polar

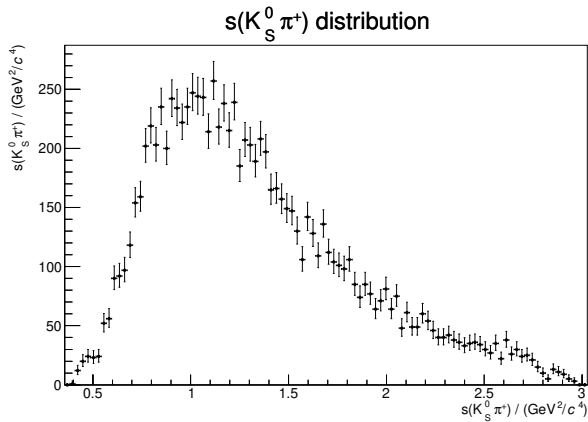


Figure:  $m_+^2$  for Belle in Polar

# Belle in Polar

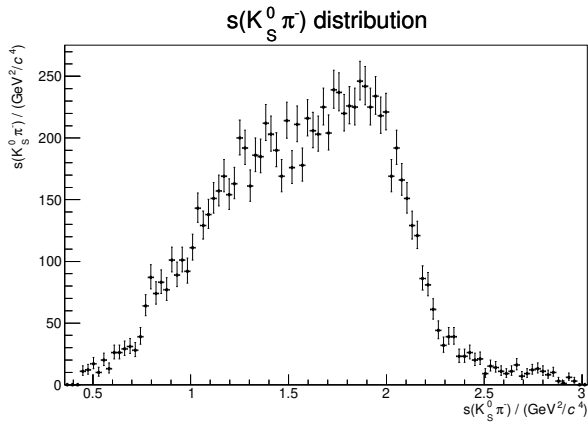


Figure:  $m_-^2$  for Belle in Polar

# Belle in Polar

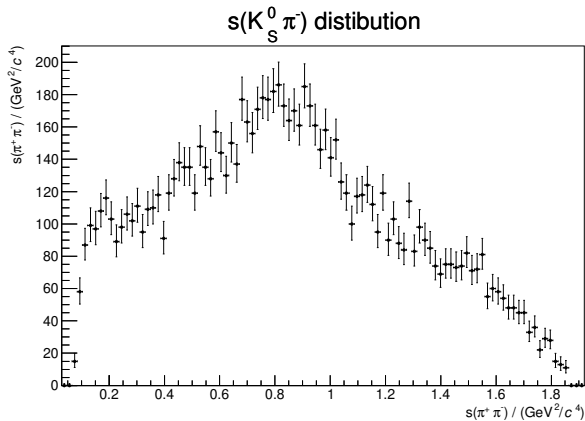


Figure:  $m_0^2$  for Belle in Polar

# Belle in Polar

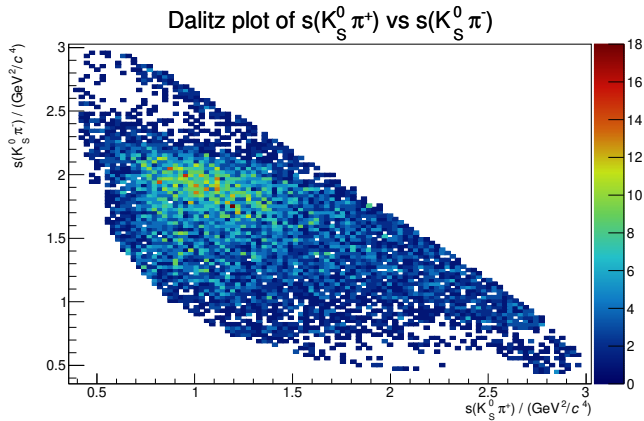


Figure:  $m_+^2$  vs  $m_-^2$  for Belle in Polar

# Belle in Polar

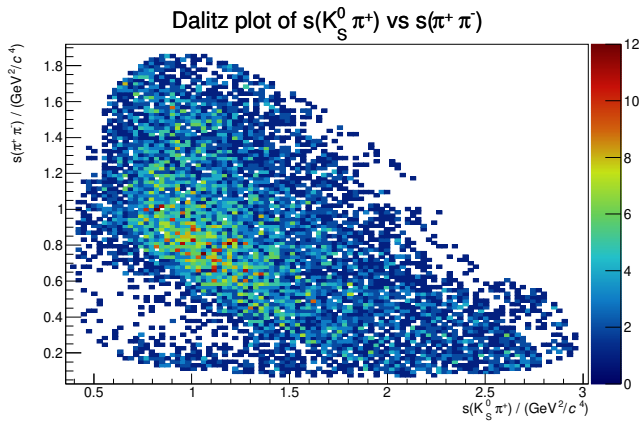


Figure:  $m_+^2$  vs  $m_0^2$  for Belle in Polar

# Belle in Polar

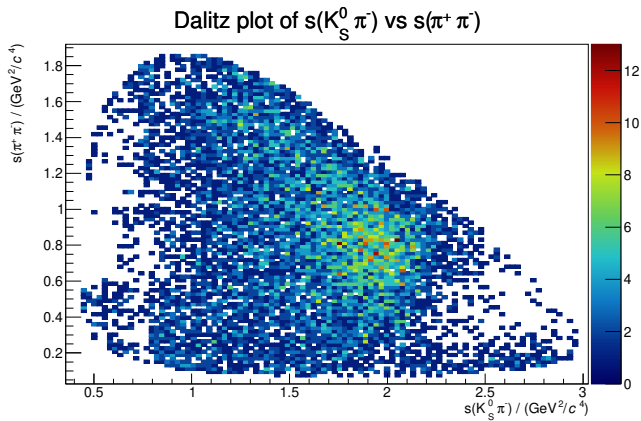


Figure:  $m_+^2$  vs  $m_0^2$  for Belle in Polar

# Belle in Polar

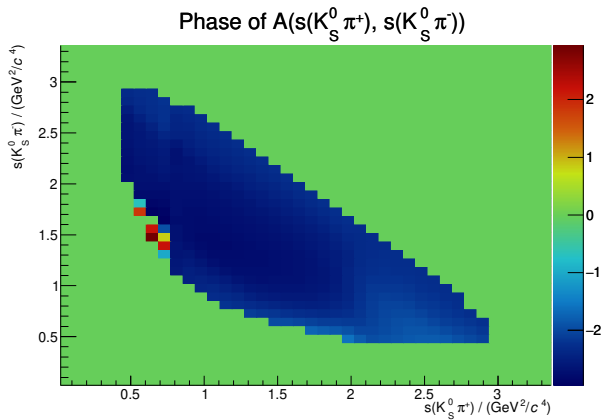


Figure: Argument for Belle in Polar



# Belle in Polar

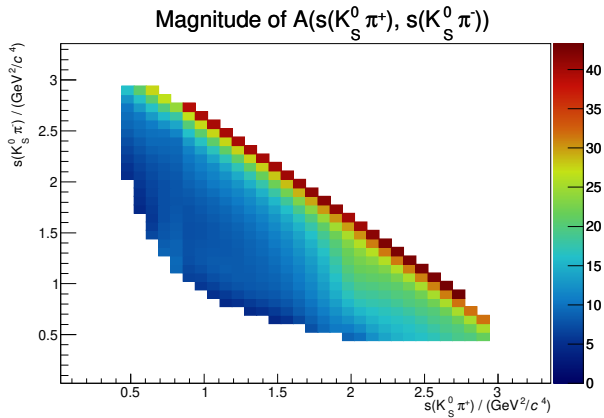


Figure: Magnitude for Belle in Polar

# Belle in Polar

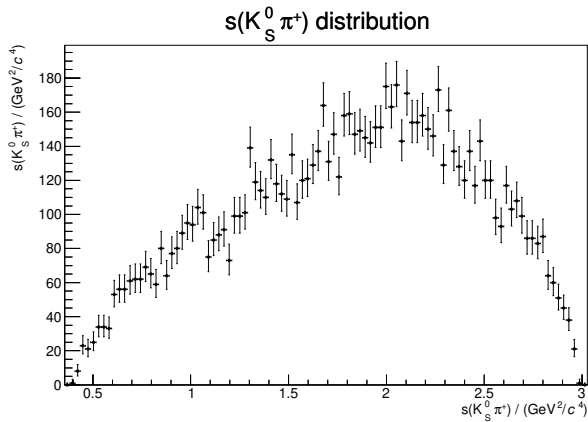


Figure:  $m_+^2$  for Belle in Polar

# Belle in Polar

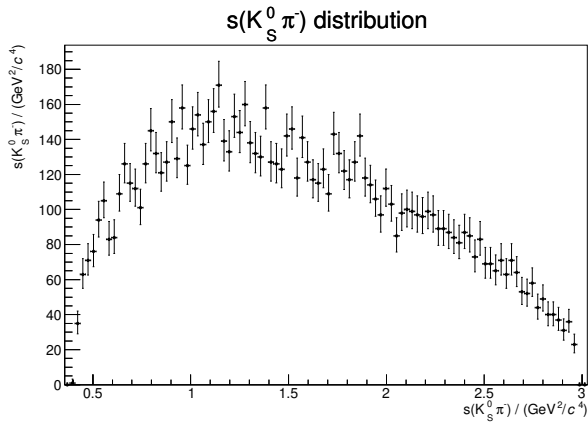


Figure:  $m_-^2$  for Belle in Polar

# Belle in Polar

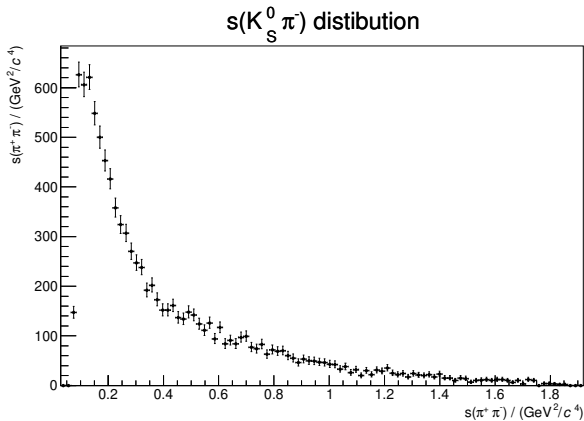


Figure:  $m_0^2$  for Belle in Polar

# Belle in Polar

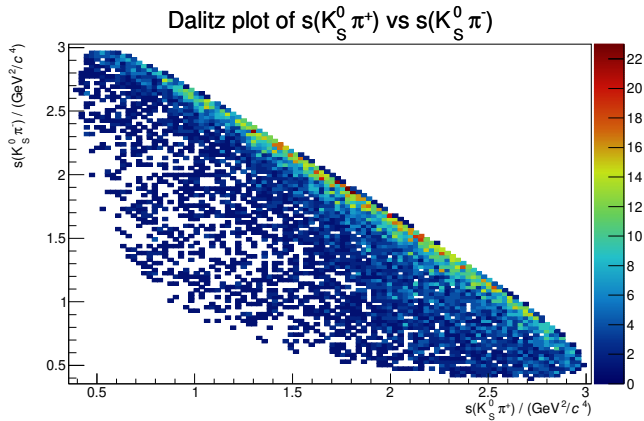


Figure:  $m_+^2$  vs  $m_-^2$  for Belle in Polar

# Belle in Polar

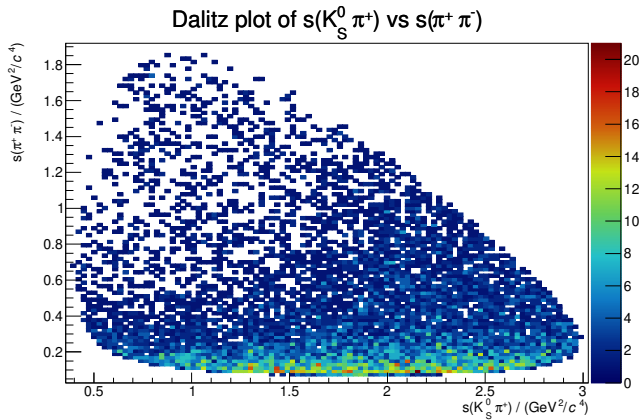


Figure:  $m_+^2$  vs  $m_0^2$  for Belle in Polar

# Belle in Polar

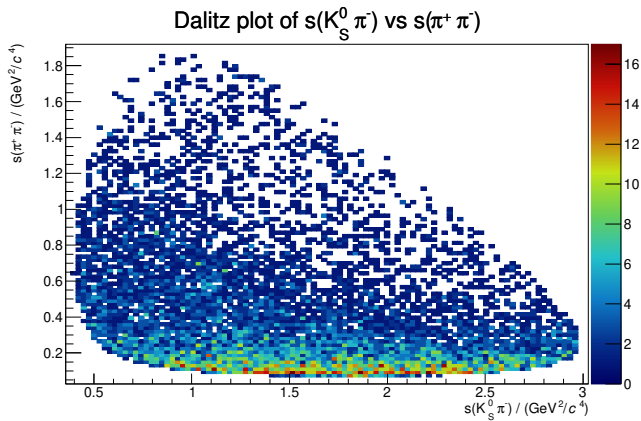


Figure:  $m_+^2$  vs  $m_0^2$  for Belle in Polar

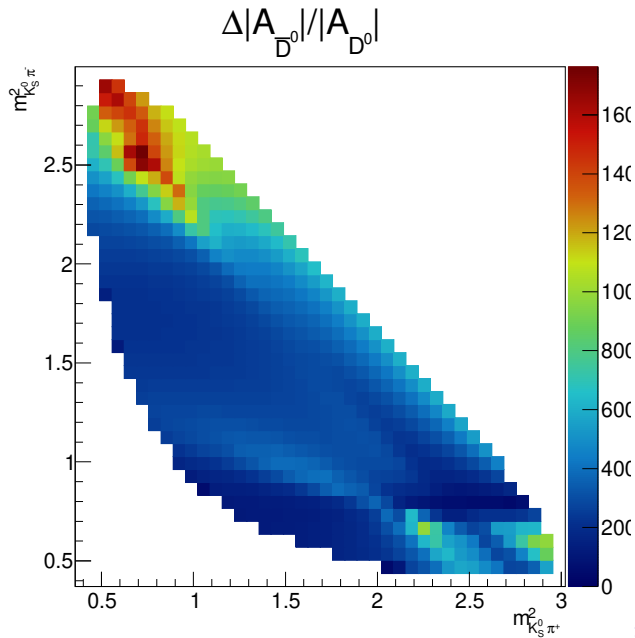
# Belle in Polar times Fit Fractions

```
#EventType D0 K0S0 pi+ pi-
CouplingConstant::Coordinates polar
CouplingConstant::AngularUnits deg
Import "$AMPGEN"/kspipi/kMatrix.opt
Particle::DefaultModifier BL
Particle::SpinFormalism Canonical
```

```
D0{K*(892)bar-{K0S0,pi-},pi+} 0 1.03028 0.00359 0 136.8 0.2
D0{K(0)*(1430)bar-[GLASS]{K0S0,pi-},pi+} 0 0.16520 0.00420 0 99.4 1.7
D0{K(2)*(1430)bar-{K0S0,pi-},pi+} 0 0.01651 0.00026 0 -44.1 0.8
D0{K*(1410)bar-{K0S0,pi-},pi+} 0 0.00029 0.00003 0 99.4 5.5
D0{K*(1680)bar-{K0S0,pi-},pi+} 0 0.01655 0.00100 0 -118.2 3.1
D0{K*(892)+{K0S0,pi+},pi-} 0 0.00098 0.00002 0 -42.2 0.9
D0{K*(1410)+{K0S0,pi+},pi-} 0 0.00021 0.00002 0 150.2 5.3
D0{K(0)*(1430)+[GLASS]{K0S0,pi+},pi-} 0 0.00011 0.00001 0 162.3 6.6
D0{K(2)*(1430)+{K0S0,pi+},pi-} 0 0.00010 0.00001 0 -89.6 7.6
D0{K0S0,rho(770)0{pi+,pi-}} 0 0.20400 0.00000 2 0 0
D0{K0S0,omega(782)0{pi+,pi-}} 0 0.00019 0.00000 0 120.7 0.7
D0{K0S0,f(2)(1270)0{pi+,pi-}} 0 0.01144 0.00024 0 -36.3 1.1
D0{K0S0,rho(1450)0{pi+,pi-}} 0 0.01710 0.00060 0 102.1 1.9
D0{K0S0,PiPi00} 0 0.010000 0.00000 0 0 0
PiPi00[kMatrix.pole.0]{pi+,pi-} 0 8.5 0.5 0 68.5 3.4
PiPi00[kMatrix.pole.1]{pi+,pi-} 0 12.2 0.3 0 24 1.4
PiPi00[kMatrix.pole.2]{pi+,pi-} 0 29.2 1.6 0 -0.1 2.5
PiPi00[kMatrix.pole.3]{pi+,pi-} 0 10.8 0.5 0 -51.9 2.4
PiPi00[kMatrix.prod.0]{pi+,pi-} 0 8 0.4 0 -126 2.5
PiPi00[kMatrix.prod.1]{pi+,pi-} 0 26.3 1.6 0 -152.3 3
PiPi00[kMatrix.prod.2]{pi+,pi-} 0 33 1.8 0 -93.2 3.1
PiPi00[kMatrix.prod.3]{pi+,pi-} 0 26.2 1.3 0 -121.4 2.7
PiPi00_s0_prod 0 -0.07 0 0
K(0)*(1430)bar-_mass 0 1.441 0.002 0.002
K(0)*(1430)bar-_width 0 0.193 0.004 0.004
K(0)*(1430)+::GLASS::F 0 0.96 0.07 0.07
```

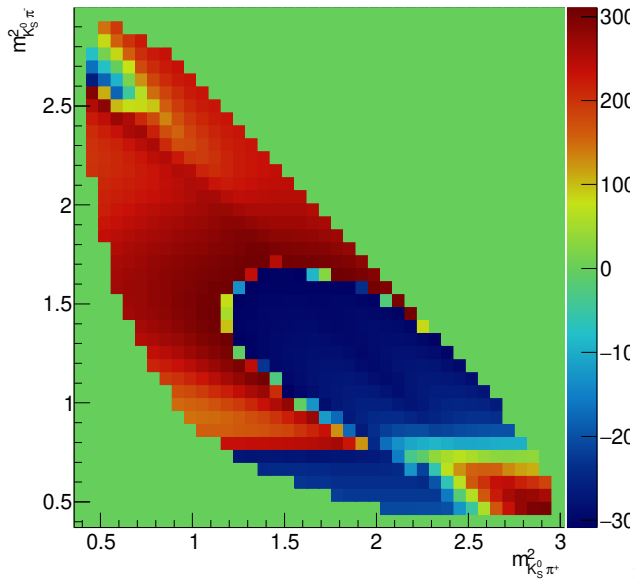


# Belle in Polar times Fit Fractions



# Belle in Polar times Fit Fractions

$$\Delta\delta_D$$



# Belle in Polar times Fit Fractions

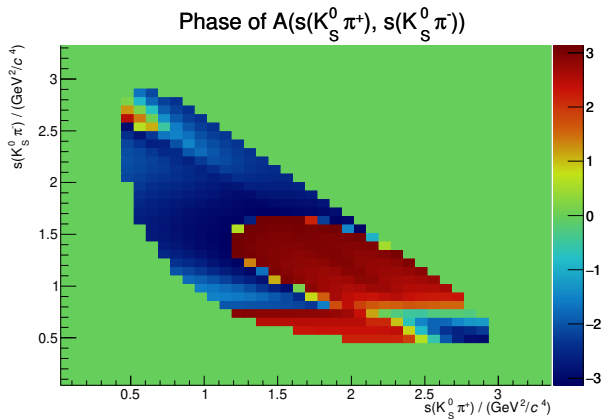


Figure: Argument for Belle in Polar times Fit Fractions

# Belle in Polar times Fit Fractions

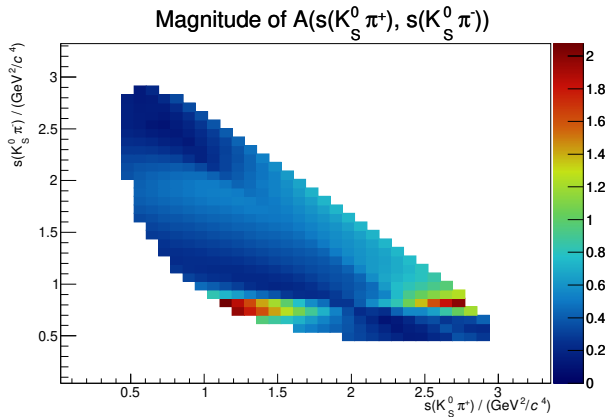


Figure: Magnitude for Belle in Polar times Fit Fractions

# Belle in Polar times Fit Fractions

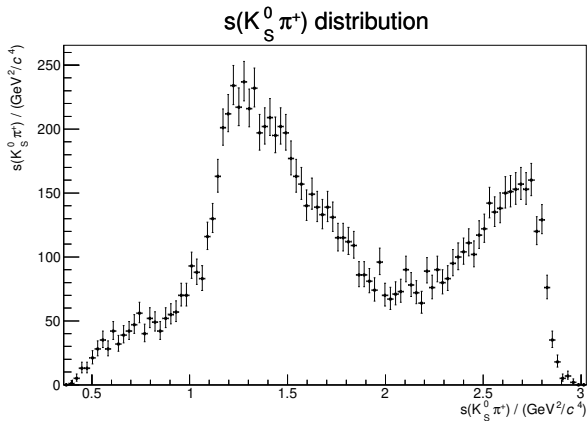


Figure:  $m_+^2$  for Belle in Polar times Fit Fractions

# Belle in Polar times Fit Fractions

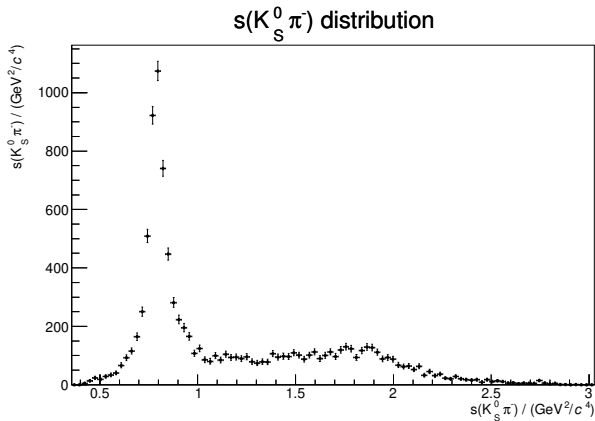


Figure:  $m_-^2$  for Belle in Polar times Fit Fractions

# Belle in Polar times Fit Fractions

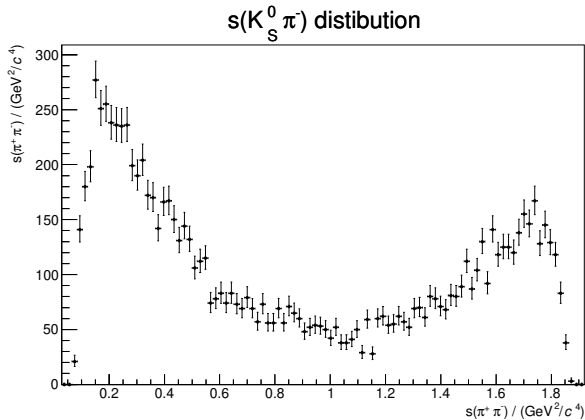


Figure:  $m_0^2$  for Belle in Polar times Fit Fractions

# Belle in Polar times Fit Fractions

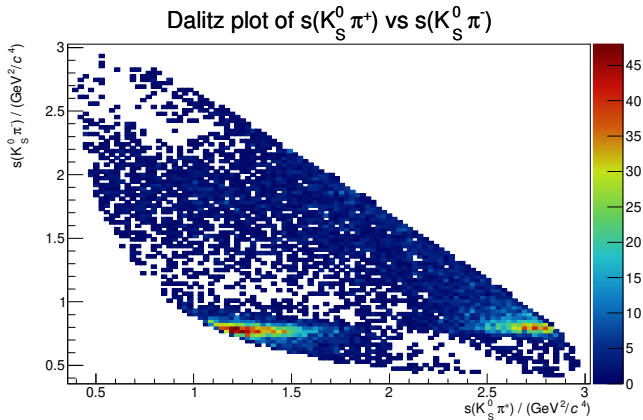


Figure:  $m_+^2$  vs  $m_-^2$  for Belle in Polar times Fit Fractions



# Belle in Polar times Fit Fractions

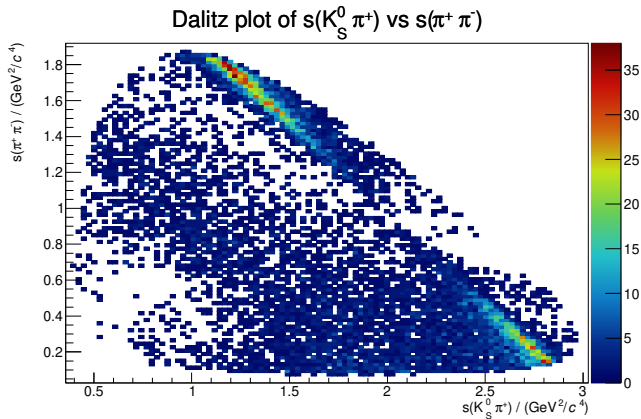


Figure:  $m_+^2$  vs  $m_0^2$  for Belle in Polar times Fit Fractions

# Belle in Polar times Fit Fractions

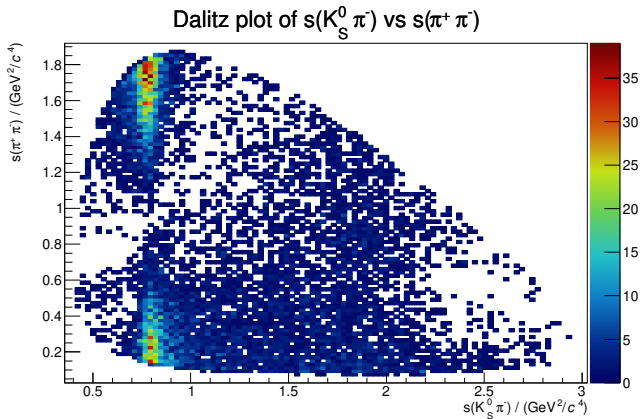


Figure:  $m_+^2$  vs  $m_0^2$  for Belle in Polar times Fit Fractions

# Belle in Polar times Fit Fractions

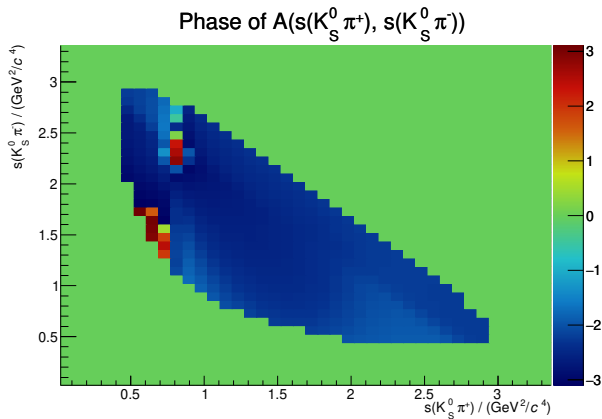


Figure: Argument for Belle in Polar times Fit Fractions

# Belle in Polar times Fit Fractions

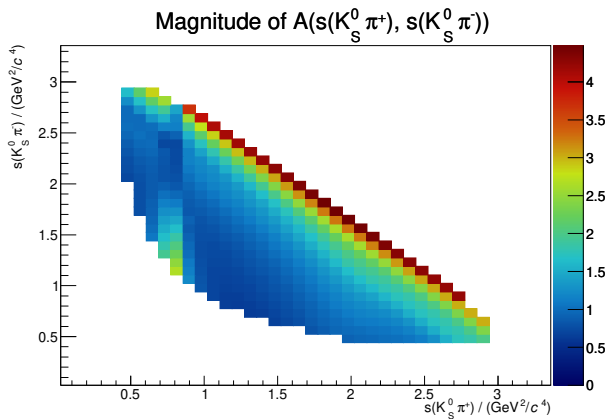


Figure: Magnitude for Belle in Polar times Fit Fractions

# Belle in Polar times Fit Fractions

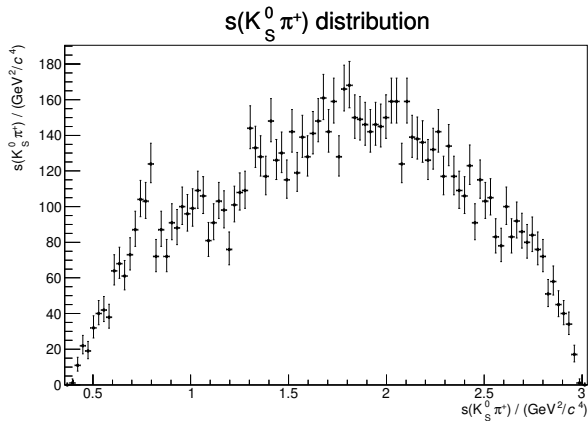


Figure:  $m_+^2$  for Belle in Polar times Fit Fractions

# Belle in Polar times Fit Fractions

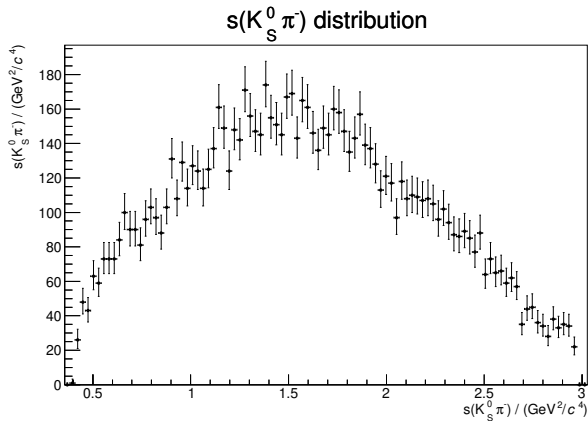


Figure:  $m_-^2$  for Belle in Polar times Fit Fractions

# Belle in Polar times Fit Fractions

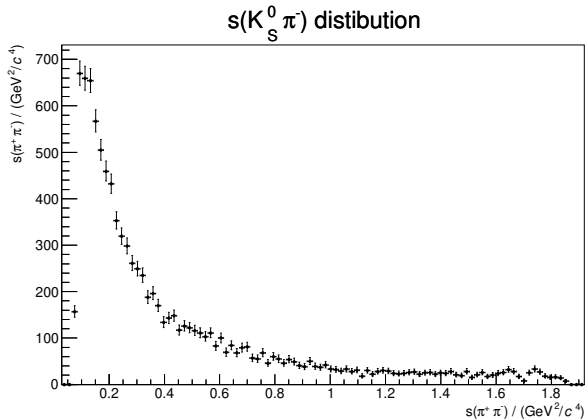


Figure:  $m_0^2$  for Belle in Polar times Fit Fractions

# Belle in Polar times Fit Fractions

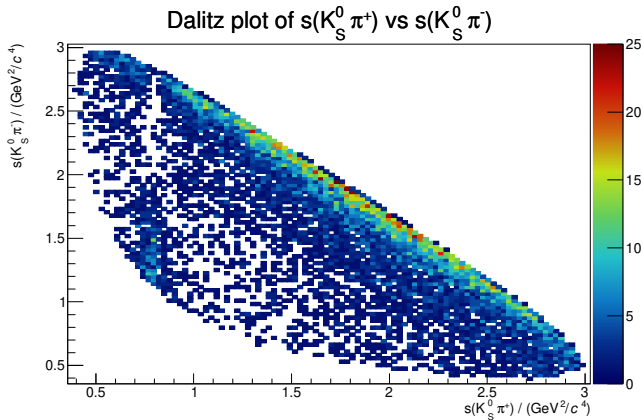


Figure:  $m_+^2$  vs  $m_-^2$  for Belle in Polar times Fit Fractions



# Belle in Polar times Fit Fractions

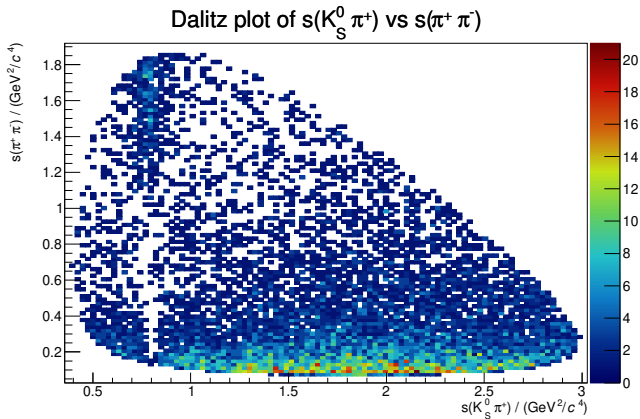


Figure:  $m_+^2$  vs  $m_0^2$  for Belle in Polar times Fit Fractions

# Belle in Polar times Fit Fractions

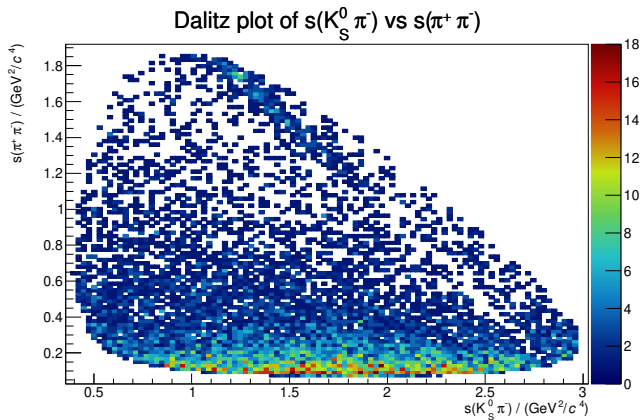


Figure:  $m_+^2$  vs  $m_0^2$  for Belle in Polar times Fit Fractions

# To Do

- ▶ Cartesian times Fit Fraction
- ▶ Convert any model (Belle, BaBar) to Re,Im (use excel?)
- ▶ Fitting is also done in Re-Im, it might be an ampGen error?