

Lab 1

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11:59PM February 18, 2021

You should have RStudio installed to edit this file. You will write code in places marked “TO-DO” to complete the problems. Some of this will be a pure programming assignment. The tools for the solutions to these problems can be found in the class practice lectures. I want you to use the methods I taught you, not for you to google and come up with whatever works. You won’t learn that way.

To “hand in” the homework, you should compile or publish this file into a PDF that includes output of your code. Once it’s done, push by the deadline to your repository in a directory called “labs”.

- Print out the numerical constant pi with ten digits after the decimal point using the internal constant pi.

```
options(digits=11)
pi
```

```
## [1] 3.1415926536
```

- Sum up the first 103 terms of the series $1 + 1/2 + 1/4 + 1/8 + \dots$

```
sum(1/2^(0:102))
```

```
## [1] 2
```

- Find the product of the first 37 terms in the sequence $1/3, 1/6, 1/9 \dots$

```
prod(1/seq(from=3,by=3,length.out=37))
```

```
## [1] 1.613528728e-61
```

- Find the product of the first 387 terms of $1 * 1/2 * 1/4 * 1/8 * \dots$

```
prod(1/2^(0:386))
```

```
## [1] 0
```

Is this answer *exactly* correct?

The answer is not exactly correct because we experienced numerical underflow.

- Figure out a means to express the answer more exactly. Not compute exactly, but express more exactly.

```
-log(2)*sum(0:386)
```

```
## [1] -51771.856063
```

- Create the sequence $x = [\text{Inf}, 20, 18, \dots, -20]$.

```
x<-c(Inf,seq(from = 20, to = -20, by = -2))
x
```

```
## [1] Inf 20 18 16 14 12 10 8 6 4 2 0 -2 -4 -6 -8 -10 -12 -14
## [20] -16 -18 -20
```

Create the sequence `x = [log3(Inf), log3(100), log3(98), ... log3(-20)]`.

```
x<-c(Inf,seq(from = 100, to = -20, by = -2))
x<-log(x,base =3)
```

```
## Warning: NaNs produced
```

```
x
```

```
## [1]          Inf 4.19180654858 4.17341725189 4.15464876786 4.13548512895
## [6] 4.11590933734 4.09590327429 4.07544759936 4.05452163807 4.03310325630
## [11] 4.01116871959 3.98869253500 3.96564727304 3.94200336639 3.91772888179
## [16] 3.89278926071 3.86714702345 3.84076143031 3.81358809222 3.78557852143
## [21] 3.75667961083 3.72683302786 3.69597450568 3.66403300988 3.63092975357
## [26] 3.59657702662 3.56087679501 3.52371901429 3.48497958377 3.44451784579
## [31] 3.40217350273 3.35776278143 3.31107361282 3.26185950714 3.20983167673
## [36] 3.15464876786 3.09590327429 3.03310325630 2.96564727304 2.89278926071
## [41] 2.81358809222 2.72683302786 2.63092975357 2.52371901429 2.40217350273
## [46] 2.26185950714 2.09590327429 1.89278926071 1.63092975357 1.26185950714
## [51] 0.63092975357          -Inf          NaN          NaN          NaN
## [56]          NaN          NaN          NaN          NaN          NaN
## [61]          NaN          NaN
```

Comment on the appropriateness of the non-numeric values.

```
#TO-DO
```

- Create a vector of booleans where the entry is true if `x[i]` is positive and finite.

```
y= !is.nan(x) & is.finite(x)&x>0
y
```

```
## [1] FALSE TRUE TRUE TRUE TRUE TRUE TRUE TRUE TRUE TRUE TRUE TRUE
## [13] TRUE TRUE TRUE TRUE TRUE TRUE TRUE TRUE TRUE TRUE TRUE TRUE TRUE
## [25] TRUE TRUE TRUE TRUE TRUE TRUE TRUE TRUE TRUE TRUE TRUE TRUE TRUE
## [37] TRUE TRUE TRUE TRUE TRUE TRUE TRUE TRUE TRUE TRUE TRUE TRUE TRUE
## [49] TRUE TRUE TRUE FALSE FALSE FALSE FALSE FALSE FALSE FALSE FALSE
## [61] FALSE FALSE
```

- Locate the indices of the non-real numbers in this vector. Hint: use the `which` function. Don't hesitate to use the documentation via `?which`.

```
?which
```

```
## starting httpd help server ... done
```

```
which(y==FALSE)
```

```
## [1]  1 52 53 54 55 56 57 58 59 60 61 62
```

- Locate the indices of the infinite quantities in this vector.

```
which(is.infinite(x))
```

```
## [1]  1 52
```

- Locate the indices of the min and max in this vector. Hint: use the `which.min` and `which.max` functions.

```
which.min(x)
```

```
## [1] 52
```

```
which.max(x)
```

```
## [1] 1
```

- Count the number of unique values in `x`.

```
length(unique(x))
```

```
## [1] 53
```

- Cast `x` to a factor. Do the number of levels make sense?

```
as.factor(x)
```

```
## [1] Inf 4.19180654857877 4.1734172518943 4.15464876785729
## [5] 4.13548512895119 4.11590933734319 4.09590327428938 4.07544759935851
## [9] 4.05452163806914 4.03310325630434 4.01116871959141 3.98869253500376
## [13] 3.96564727304425 3.94200336638929 3.91772888178973 3.89278926071437
## [17] 3.86714702345081 3.84076143030548 3.81358809221559 3.78557852142874
## [21] 3.75667961082847 3.72683302786084 3.69597450568212 3.66403300987579
## [25] 3.63092975357146 3.59657702661571 3.56087679500731 3.52371901428583
## [29] 3.48497958377173 3.44451784578705 3.40217350273288 3.3577627814323
## [33] 3.31107361281783 3.26185950714291 3.20983167673402 3.15464876785729
## [37] 3.09590327428938 3.03310325630434 2.96564727304425 2.89278926071437
## [41] 2.8135880922156 2.72683302786084 2.63092975357146 2.52371901428583
## [45] 2.40217350273288 2.26185950714291 2.09590327428938 1.89278926071437
## [49] 1.63092975357146 1.26185950714291 0.630929753571457 -Inf
## [53] NaN NaN NaN NaN
## [57] NaN NaN NaN NaN
## [61] NaN NaN
## 53 Levels: -Inf 0.630929753571457 1.26185950714291 ... NaN
```

- Cast `x` to integers. What do we learn about R's infinity representation in the integer data type?

```
as.integer(x)
```

```
## Warning: NAs introduced by coercion to integer range
```

```
## [1] NA 4 4 4 4 4 4 4 4 4 4 3 3 3 3 3 3 3 3 3 3 3
## [26] 3 3 3 3 3 3 3 3 3 3 3 3 3 2 2 2 2 2 2 2 2 1 1 1
## [51] 0 NA NA NA NA NA NA NA NA NA NA NA NA
```

- Use `x` to create a new vector `y` containing only the real numbers in `x`.

```
y = x[!is.nan(x) & is.finite(x)&x>0]
```

```
y
```

```
## [1] 4.19180654858 4.17341725189 4.15464876786 4.13548512895 4.11590933734
## [6] 4.09590327429 4.07544759936 4.05452163807 4.03310325630 4.01116871959
## [11] 3.98869253500 3.96564727304 3.94200336639 3.91772888179 3.89278926071
## [16] 3.86714702345 3.84076143031 3.81358809222 3.78557852143 3.75667961083
## [21] 3.72683302786 3.69597450568 3.66403300988 3.63092975357 3.59657702662
## [26] 3.56087679501 3.52371901429 3.48497958377 3.44451784579 3.40217350273
## [31] 3.35776278143 3.31107361282 3.26185950714 3.20983167673 3.15464876786
## [36] 3.09590327429 3.03310325630 2.96564727304 2.89278926071 2.81358809222
## [41] 2.72683302786 2.63092975357 2.52371901429 2.40217350273 2.26185950714
## [46] 2.09590327429 1.89278926071 1.63092975357 1.26185950714 0.63092975357
```

- Use the left rectangle method to numerically integrate x^2 from 0 to 1 with rectangle width size $1e-6$.

```
1e-6 *sum (seq(from = 0,to = 1-1e-6,by = 1e-6)^2)
```

```
## [1] 0.33333283333
```

- Calculate the average of 100 realizations of standard Bernoullis in one line using the `sample` function.

```
mean(sample(c(0,1), size=100, replace=TRUE))
```

```
## [1] 0.49
```

- Calculate the average of 500 realizations of Bernoullis with $p = 0.9$ in one line using the `sample` and `mean` functions.

```
sum(sample(c(0,1), size=500, replace=TRUE, prob=c(0.1, 0.9)))/500
```

```
## [1] 0.912
```

- Calculate the average of 1000 realizations of Bernoullis with $p = 0.9$ in one line using `rbinom`.

```
mean(rbinom(n=1000, size=1, p=0.9))
```

```
## [1] 0.901
```

- In class we considered a variable `x_3` which measured “criminality”. We imagined $L = 4$ levels “none”, “infraction”, “misdemeanor” and “felony”. Create a variable `x_3` here with 100 random elements (equally probable). Create it as a nominal (i.e. unordered) factor.

```
x_3 = as.factor(sample(c("none", "infraction", "misdemeanor", "felony"),size = 100,replace = TRUE))
x_3
```

```
## [1] misdemeanor infraction misdemeanor none infraction none
## [7] none none none misdemeanor felony none
## [13] infraction infraction none felony none felony
## [19] none misdemeanor misdemeanor infraction none none
## [25] felony none infraction felony infraction infraction
## [31] infraction none none felony infraction felony
## [37] infraction misdemeanor infraction none felony felony
## [43] none misdemeanor misdemeanor none felony none
## [49] felony none none infraction felony none
## [55] felony none misdemeanor felony misdemeanor infraction
## [61] none none misdemeanor none felony none
## [67] misdemeanor none misdemeanor misdemeanor misdemeanor none
## [73] infraction none felony infraction none none
## [79] none misdemeanor felony infraction none misdemeanor
## [85] misdemeanor infraction infraction infraction misdemeanor felony
## [91] misdemeanor none infraction felony infraction felony
## [97] none misdemeanor felony felony
## Levels: felony infraction misdemeanor none
```

- Use `x_3` to create `x_3_bin`, a binary feature where 0 is no crime and 1 is any crime.

```
x_3_bin = x_3!="none"
x_3_bin
```

```
## [1] TRUE TRUE TRUE FALSE TRUE FALSE FALSE FALSE FALSE TRUE TRUE FALSE
## [13] TRUE TRUE FALSE TRUE FALSE TRUE FALSE TRUE TRUE TRUE FALSE FALSE
## [25] TRUE FALSE TRUE TRUE TRUE TRUE TRUE FALSE FALSE TRUE TRUE TRUE
## [37] TRUE TRUE TRUE FALSE TRUE TRUE FALSE TRUE TRUE FALSE TRUE FALSE
## [49] TRUE FALSE FALSE TRUE TRUE FALSE TRUE FALSE TRUE TRUE TRUE TRUE
## [61] FALSE FALSE TRUE FALSE TRUE FALSE TRUE FALSE TRUE TRUE TRUE FALSE
```

```
## [73] TRUE FALSE TRUE TRUE FALSE FALSE FALSE TRUE TRUE TRUE FALSE TRUE
## [85] TRUE TRUE TRUE TRUE TRUE TRUE TRUE FALSE TRUE TRUE TRUE TRUE
## [97] FALSE TRUE TRUE TRUE
```

- Use `x_3` to create `x_3_ord`, an ordered factor variable. Ensure the proper ordinal ordering.

```
x_3_ord = factor(x_3, levels = c("none", "infraction", "misdemeanor", "felony"), order = TRUE)
x_3_ord
```

```
## [1] misdemeanor infraction misdemeanor none infraction none
## [7] none none none misdemeanor felony none
## [13] infraction infraction none felony none felony
## [19] none misdemeanor misdemeanor infraction none none
## [25] felony none infraction felony infraction infraction
## [31] infraction none none felony infraction felony
## [37] infraction misdemeanor infraction none felony felony
## [43] none misdemeanor misdemeanor none felony none
## [49] felony none none infraction felony none
## [55] felony none misdemeanor felony misdemeanor infraction
## [61] none none misdemeanor none felony none
## [67] misdemeanor none misdemeanor misdemeanor misdemeanor none
## [73] infraction none felony infraction none none
## [79] none misdemeanor felony infraction none misdemeanor
## [85] misdemeanor infraction infraction infraction misdemeanor felony
## [91] misdemeanor none infraction felony infraction felony
## [97] none misdemeanor felony felony
## Levels: none < infraction < misdemeanor < felony
```

- Convert this variable into three binary variables without any information loss and put them into a data matrix.v

```
x_3_infrac = x_3 == "infraction"
x_3_misd = x_3 == "misdemeanor"
x_3_felony = x_3 == "felony"

n = 100 #number of historical objects: the people
p = 3 #number of features about each

X_3_Matrix = matrix(NA, nrow = n, ncol = p)
X_3_Matrix[,1] = x_3_infrac
X_3_Matrix[,2] = x_3_misd
X_3_Matrix[,3] = x_3_felony
X_3_Matrix
```

```
##      [,1] [,2] [,3]
## [1,] FALSE TRUE FALSE
## [2,] TRUE FALSE FALSE
## [3,] FALSE TRUE FALSE
## [4,] FALSE FALSE FALSE
## [5,] TRUE FALSE FALSE
## [6,] FALSE FALSE FALSE
## [7,] FALSE FALSE FALSE
## [8,] FALSE FALSE FALSE
## [9,] FALSE FALSE FALSE
## [10,] FALSE TRUE FALSE
## [11,] FALSE FALSE TRUE
## [12,] FALSE FALSE FALSE
```

```

## [13,] TRUE FALSE FALSE
## [14,] TRUE FALSE FALSE
## [15,] FALSE FALSE FALSE
## [16,] FALSE FALSE TRUE
## [17,] FALSE FALSE FALSE
## [18,] FALSE FALSE TRUE
## [19,] FALSE FALSE FALSE
## [20,] FALSE TRUE FALSE
## [21,] FALSE TRUE FALSE
## [22,] TRUE FALSE FALSE
## [23,] FALSE FALSE FALSE
## [24,] FALSE FALSE FALSE
## [25,] FALSE FALSE TRUE
## [26,] FALSE FALSE FALSE
## [27,] TRUE FALSE FALSE
## [28,] FALSE FALSE TRUE
## [29,] TRUE FALSE FALSE
## [30,] TRUE FALSE FALSE
## [31,] TRUE FALSE FALSE
## [32,] FALSE FALSE FALSE
## [33,] FALSE FALSE FALSE
## [34,] FALSE FALSE TRUE
## [35,] TRUE FALSE FALSE
## [36,] FALSE FALSE TRUE
## [37,] TRUE FALSE FALSE
## [38,] FALSE TRUE FALSE
## [39,] TRUE FALSE FALSE
## [40,] FALSE FALSE FALSE
## [41,] FALSE FALSE TRUE
## [42,] FALSE FALSE TRUE
## [43,] FALSE FALSE FALSE
## [44,] FALSE TRUE FALSE
## [45,] FALSE TRUE FALSE
## [46,] FALSE FALSE FALSE
## [47,] FALSE FALSE TRUE
## [48,] FALSE FALSE FALSE
## [49,] FALSE FALSE TRUE
## [50,] FALSE FALSE FALSE
## [51,] FALSE FALSE FALSE
## [52,] TRUE FALSE FALSE
## [53,] FALSE FALSE TRUE
## [54,] FALSE FALSE FALSE
## [55,] FALSE FALSE TRUE
## [56,] FALSE FALSE FALSE
## [57,] FALSE TRUE FALSE
## [58,] FALSE FALSE TRUE
## [59,] FALSE TRUE FALSE
## [60,] TRUE FALSE FALSE
## [61,] FALSE FALSE FALSE
## [62,] FALSE FALSE FALSE
## [63,] FALSE TRUE FALSE
## [64,] FALSE FALSE FALSE
## [65,] FALSE FALSE TRUE
## [66,] FALSE FALSE FALSE

```

```
## [67,] FALSE TRUE FALSE
## [68,] FALSE FALSE FALSE
## [69,] FALSE TRUE FALSE
## [70,] FALSE TRUE FALSE
## [71,] FALSE TRUE FALSE
## [72,] FALSE FALSE FALSE
## [73,] TRUE FALSE FALSE
## [74,] FALSE FALSE FALSE
## [75,] FALSE FALSE TRUE
## [76,] TRUE FALSE FALSE
## [77,] FALSE FALSE FALSE
## [78,] FALSE FALSE FALSE
## [79,] FALSE FALSE FALSE
## [80,] FALSE TRUE FALSE
## [81,] FALSE FALSE TRUE
## [82,] TRUE FALSE FALSE
## [83,] FALSE FALSE FALSE
## [84,] FALSE TRUE FALSE
## [85,] FALSE TRUE FALSE
## [86,] TRUE FALSE FALSE
## [87,] TRUE FALSE FALSE
## [88,] TRUE FALSE FALSE
## [89,] FALSE TRUE FALSE
## [90,] FALSE FALSE TRUE
## [91,] FALSE TRUE FALSE
## [92,] FALSE FALSE FALSE
## [93,] TRUE FALSE FALSE
## [94,] FALSE FALSE TRUE
## [95,] TRUE FALSE FALSE
## [96,] FALSE FALSE TRUE
## [97,] FALSE FALSE FALSE
## [98,] FALSE TRUE FALSE
## [99,] FALSE FALSE TRUE
## [100,] FALSE FALSE TRUE
```

- What should the sum of each row be (in English)?

Either one or zero if no criminality Verify that.

```
rowSums(X_3_Matrix)
```

```
## [1] 1 1 1 0 1 0 0 0 0 1 1 0 1 1 0 1 0 1 1 1 0 0 1 0 1 1 1 1 1 0 0 1 1 1 1
## [38] 1 1 0 1 1 0 1 1 0 1 0 1 0 0 1 1 0 1 0 1 1 1 1 0 0 1 0 1 0 1 0 1 1 1 0 1 0
## [75] 1 1 0 0 0 1 1 1 0 1 1 1 1 1 1 1 1 0 1 1 1 1 0 1 1 1
```

- How should the column sum look (in English)?

The total number of people with that level of criminality

Verify that.

```
colSums(X_3_Matrix)
```

```
## [1] 22 21 22
```

- Generate a matrix with 100 rows where the first column is realization from a normal with mean 17 and variance 38, the second column is uniform between -10 and 10, the third column is poisson with mean 6, the fourth column in exponential with lambda of 9, the fifth column is binomial with $n = 20$ and p

= 0.12 and the sixth column is a binary variable with exactly 24% 1's dispersed randomly. Name the rows the entries of the `fake_first_names` vector.

```
fake_first_names = c(
  "Sophia", "Emma", "Olivia", "Ava", "Mia", "Isabella", "Riley",
  "Aria", "Zoe", "Charlotte", "Lily", "Layla", "Amelia", "Emily",
  "Madelyn", "Aubrey", "Adalyn", "Madison", "Chloe", "Harper",
  "Abigail", "Aaliyah", "Avery", "Evelyn", "Kaylee", "Ella", "Ellie",
  "Scarlett", "Arianna", "Hailey", "Nora", "Addison", "Brooklyn",
  "Hannah", "Mila", "Leah", "Elizabeth", "Sarah", "Eliana", "Mackenzie",
  "Peyton", "Maria", "Grace", "Adeline", "Elena", "Anna", "Victoria",
  "Camilla", "Lillian", "Natalie", "Jackson", "Aiden", "Lucas",
  "Liam", "Noah", "Ethan", "Mason", "Caden", "Oliver", "Elijah",
  "Grayson", "Jacob", "Michael", "Benjamin", "Carter", "James",
  "Jayden", "Logan", "Alexander", "Caleb", "Ryan", "Luke", "Daniel",
  "Jack", "William", "Owen", "Gabriel", "Matthew", "Connor", "Jayce",
  "Isaac", "Sebastian", "Henry", "Muhammad", "Cameron", "Wyatt",
  "Dylan", "Nathan", "Nicholas", "Julian", "Eli", "Levi", "Isaiah",
  "Landon", "David", "Christian", "Andrew", "Brayden", "John",
  "Lincoln"
)
n = 100 #number of historical objects: the people
p = 6 #number of features about each

X = matrix(NA, nrow = n, ncol = p)

X[, 1] = rnorm(n, 17, sqrt(38))
X[, 2] = runif(n, -10, 10)
X[, 3] = rpois(n, 6)
X[, 4] = rexp(n, 9)
X[, 5] = rbinom(n, 20, 0.12)
X[, 6] = rbinom(n, 1, 0.24)
rownames(X) = fake_first_names
X
```

##		[,1]	[,2]	[,3]	[,4]	[,5]	[,6]
##	Sophia	15.5123948496	3.39514894411	4	0.24296770693270	3	0
##	Emma	14.6566349304	-4.03737915680	10	0.04852871891732	3	0
##	Olivia	29.9860182403	7.65525081661	3	0.17322998938179	2	0
##	Ava	14.0414226456	-2.79146249872	7	0.03631058418088	2	1
##	Mia	19.1850852062	-7.47857928742	5	0.02573613265907	1	0
##	Isabella	17.1668635577	2.07866804674	1	0.01922818533745	2	0
##	Riley	14.6227533670	-0.26900858618	3	0.07048755490945	1	0
##	Aria	16.0571091308	-3.36965614930	6	0.32693081732206	4	0
##	Zoe	8.4940106297	3.52040128782	3	0.00264948689275	2	0
##	Charlotte	15.0565055947	-8.27077508438	4	0.10673925675581	0	0
##	Lily	22.9156038359	-5.84329490084	5	0.11464181345317	3	0
##	Layla	11.1214570628	-0.60008181259	1	0.27804816409373	2	0
##	Amelia	17.6127913873	2.05575714819	8	0.01431047893005	2	0
##	Emily	17.7674963753	-0.53098186851	2	0.08000398998893	0	0
##	Madelyn	26.2329444444	-9.74364424590	8	0.31544088267288	5	0
##	Aubrey	10.1915038315	-3.03892144002	6	0.04249451112830	3	0
##	Adalyn	16.5791548104	-6.07411171775	4	0.05393676991550	2	0
##	Madison	11.5119126615	-8.43950808980	6	0.09085268930376	3	0
##	Chloe	15.9774733201	-6.82510714512	4	0.21890449916217	2	0

## Harper	10.4739280918	1.72878286336	4 0.18629728719284	2	1
## Abigail	21.7070916279	-5.70805290248	8 0.14558813482470	2	0
## Aaliyah	6.0682498797	9.48494082317	9 0.11092618646814	3	0
## Avery	8.5398651622	3.46879275981	3 0.05458174294068	4	0
## Evelyn	25.4884506226	-1.36803516652	9 0.02534569479111	5	0
## Kaylee	23.4940233757	9.61170416325	5 0.01747022983101	4	0
## Ella	-3.0325339723	-8.94875853322	4 0.49599598522862	4	1
## Ellie	16.9356868695	3.86623592582	4 0.14775185224444	2	1
## Scarlett	16.0121259294	9.74279672839	9 0.58008798477594	2	0
## Arianna	13.0264798411	1.56015730929	6 0.10633517521898	2	1
## Hailey	15.6480448862	8.25111260172	6 0.07690276909206	2	0
## Nora	16.5376394077	-0.34049032722	7 0.03651589222459	3	0
## Addison	9.1746275066	-6.53836350888	6 0.03851643277027	4	0
## Brooklyn	3.9829889932	-4.13735208102	3 0.17243201546947	2	0
## Hannah	12.3310884868	1.58836048562	6 0.03954450175580	4	0
## Mila	21.6730303316	-6.12324787304	4 0.01612222786147	3	0
## Leah	15.7954034749	-3.34170852788	10 0.14388954752796	1	0
## Elizabeth	11.3237740955	0.17990447115	3 0.00569373395087	1	1
## Sarah	19.9702995795	4.46426651906	7 0.00211515102428	1	0
## Eliana	14.3733773936	4.29699413944	7 0.02966008710684	1	0
## Mackenzie	5.7285499460	-4.75345726591	5 0.04048808744611	3	1
## Peyton	16.3168460721	-6.94244007114	7 0.05000128033054	3	0
## Maria	11.3893819904	2.98184376210	5 0.02354607803540	3	0
## Grace	19.2595981121	4.99178113881	10 0.19239292177178	4	0
## Adeline	13.6752230669	8.63835441414	7 0.47746862676946	1	0
## Elena	16.2748014280	-2.27161918301	8 0.23382141504895	3	0
## Anna	24.4266296419	-3.84937701281	6 0.08892418422994	1	0
## Victoria	7.3222205526	9.77358313277	8 0.34617835446981	0	0
## Camilla	15.2397828462	-2.34727195464	4 0.00013926794809	2	0
## Lillian	23.7439987821	-8.65441722330	3 0.09768195398099	5	0
## Natalie	11.7350530655	6.51603049599	2 0.32663887654530	0	0
## Jackson	17.3446540575	-5.33492956776	1 0.12399968939056	0	0
## Aiden	8.9146582941	0.96563390456	5 0.03242189840724	3	0
## Lucas	29.9391867421	-2.22944840323	5 0.18650636593395	4	0
## Liam	26.0823489971	5.84151872434	8 0.01186309511670	3	0
## Noah	17.7951746766	-7.35933178104	7 0.06916799970592	1	1
## Ethan	9.5831559133	6.62802569568	6 0.12984392835607	4	0
## Mason	19.2918981239	-5.77064344659	4 0.22903973773844	1	0
## Caden	11.5949168736	7.91973461397	9 0.05709783044747	1	0
## Oliver	19.5599003857	5.33133334015	6 0.10479111751696	3	0
## Elijah	22.7595443276	2.25006388500	7 0.04781955935889	1	1
## Grayson	11.1247620429	8.25496210717	2 0.01617161865464	0	0
## Jacob	23.0748507654	5.16614286229	7 0.15943506234944	1	1
## Michael	19.0081675708	-2.44505085517	8 0.01504357355707	3	1
## Benjamin	11.0482798188	5.81444230396	3 0.05016945959586	3	0
## Carter	15.9316779288	9.79888943955	13 0.40583854973466	0	0
## James	18.3297925263	-4.47918335441	8 0.00996107913347	3	0
## Jayden	14.8328410991	-4.48360749055	4 0.01170950646823	1	0
## Logan	20.8497403112	6.05835883413	5 0.07382401089287	4	0
## Alexander	4.0940350585	6.48113669362	2 0.00793373490564	1	1
## Caleb	21.1397058000	-5.92269100714	5 0.03101898196878	3	1
## Ryan	23.4129898673	-5.22912057117	10 0.24233556697114	4	1
## Luke	19.7937805066	7.65500323381	7 0.00073056735305	1	0
## Daniel	6.1830114211	8.45255712513	4 0.13296203449316	4	0

## Jack	19.7530453352	4.68968774192	5	0.36117836996274	2	0
## William	21.7673887407	3.77174132969	4	0.15324037521611	3	0
## Owen	22.1628293868	6.26903261524	5	0.00280892911057	3	0
## Gabriel	20.1364259640	6.05009890627	3	0.18719717481533	3	0
## Matthew	7.3853572647	-8.68735394906	9	0.14144238322093	4	0
## Connor	15.8808170595	2.64108662494	1	0.15863614891977	3	0
## Jayce	22.3615842558	-3.05513546802	3	0.10225351764871	2	0
## Isaac	30.1224587619	-7.09135241341	4	0.02364855673578	7	0
## Sebastian	13.5889763427	-3.21353988256	2	0.02250273660239	1	0
## Henry	13.6650927255	3.54747127276	4	0.11865767655742	3	1
## Muhammad	18.6854115775	1.84807243757	3	0.07062107733347	1	0
## Cameron	20.3072446633	-2.99180550501	6	0.12640570900454	4	0
## Wyatt	20.9482961937	6.45775807556	6	0.16668974234720	2	0
## Dylan	21.1046735819	3.64000455942	11	0.29357398030914	3	0
## Nathan	14.4168464775	0.17177540809	4	0.20056258766321	0	1
## Nicholas	23.7567067948	-2.86608696915	6	0.07877880474313	3	1
## Julian	12.8086308556	4.79942964856	4	0.01741068767873	1	1
## Eli	22.3678345409	-1.96732667740	6	0.49140960513401	2	0
## Levi	13.7818898664	5.09553181473	5	0.09063709475047	4	0
## Isaiah	13.7367739803	9.31367711630	10	0.00983057916164	3	1
## Landon	14.9400453286	2.18756768852	4	0.17297542467191	3	0
## David	11.7285828772	-9.85986776650	7	0.00201122872308	3	0
## Christian	19.0997845093	-1.45769142546	7	0.01298068230972	1	0
## Andrew	7.3032475009	5.77005962841	2	0.06529642807113	3	1
## Brayden	9.7081053721	-2.31467570178	6	0.00834825438344	1	1
## John	14.7686266957	9.99820148572	3	0.13152794622246	3	0
## Lincoln	19.1537537567	1.03007489815	6	0.07082419490649	2	1

- Create a data frame of the same data as above except make the binary variable a factor “DOMESTIC” vs “FOREIGN” for 0 and 1 respectively. Use RStudio’s View function to ensure this worked as desired.

```
Y = data.frame("NORMAL" = rnorm(n , 17, sqrt(38)),
               "UNIFORM" = runif(n ,-10, 10),
               "POISSON" = rpois(n ,6),
               "EXPONENTIAL" = rexp(n ,9),
               "BINOMIAL" = rbinom (n ,20, 0.12),
               "D_vs_F" = sample(
                 c("DOMESTIC", "FOREIGN"),
                 size = n,
                 replace = TRUE,
                 prob = c( .76, .24)
               )
)
rownames(Y) = fake_first_names
View (Y)
```

- Print out a table of the binary variable. Then print out the proportions of “DOMESTIC” vs “FOREIGN”.

```
table(Y$ D_vs_F)

##
## DOMESTIC FOREIGN
##      77      23

prop.table(table(Y$ D_vs_F))

##
```

```
## DOMESTIC FOREIGN
##      0.77      0.23
```

- Let $n = 50$. Create a $n \times n$ matrix R of exactly 50% entries 0's, 25% 1's 25% 2's. These values should be in random locations.

```
n = 50
R = matrix(sample(
  c(0,1,2),
  size = n^2,
  replace = TRUE,
  prob = c(0.50, 0.25, .25)), nrow = n, ncol = n)
R
```

```
##      [,1] [,2] [,3] [,4] [,5] [,6] [,7] [,8] [,9] [,10] [,11] [,12] [,13]
## [1,]    2    0    0    0    1    1    0    2    0    1    0    1    0
## [2,]    2    2    1    2    0    1    1    0    1    0    0    0    0
## [3,]    0    2    0    2    0    0    1    0    2    2    0    0    0
## [4,]    0    2    1    0    1    2    0    1    0    0    0    0    1
## [5,]    0    0    2    0    0    2    1    1    0    0    1    1    2
## [6,]    0    0    0    1    2    0    0    0    2    0    0    2    1
## [7,]    1    0    2    0    0    2    1    2    0    2    1    0    2
## [8,]    1    0    1    1    2    0    0    0    1    0    1    1    0
## [9,]    0    2    1    0    0    0    2    1    0    1    0    1    0
## [10,]   0    0    1    2    1    0    0    0    1    0    0    1    1
## [11,]   0    0    2    0    0    2    1    1    0    1    1    2    1
## [12,]   2    0    0    0    0    0    0    0    0    0    2    0    1
## [13,]   0    0    0    0    0    2    0    1    0    2    0    0    1
## [14,]   1    0    0    0    1    0    1    0    0    2    0    0    0
## [15,]   0    1    0    0    1    0    0    0    2    2    1    0    2
## [16,]   2    0    0    0    0    2    2    0    0    1    2    1    2
## [17,]   2    0    0    0    1    0    0    2    1    0    0    0    0
## [18,]   0    0    0    2    2    0    0    1    0    0    0    0    1
## [19,]   1    0    0    2    0    0    2    0    0    2    0    1    0
## [20,]   0    0    0    2    0    1    0    0    0    1    2    2    0
## [21,]   1    0    0    2    1    0    0    2    0    2    0    2    2
## [22,]   1    0    1    0    1    2    0    2    0    1    0    2    2
## [23,]   1    2    0    0    0    0    0    1    2    2    2    0    1
## [24,]   2    0    0    0    0    0    1    0    0    0    0    0    2
## [25,]   1    0    0    0    0    2    1    0    1    1    1    0    0
## [26,]   2    0    0    0    1    2    0    1    0    0    1    0    2
## [27,]   0    1    0    0    2    2    1    2    0    1    0    0    0
## [28,]   0    0    2    2    1    0    0    0    0    0    2    2    0
## [29,]   2    1    2    0    1    0    1    2    0    2    2    2    1
## [30,]   0    0    0    0    2    0    2    0    0    2    2    0    0
## [31,]   0    1    0    2    2    2    0    2    0    0    2    0    0
## [32,]   2    0    2    2    0    0    2    0    0    0    1    2    0
## [33,]   2    0    0    2    1    0    2    0    0    2    0    0    0
## [34,]   0    1    1    0    0    0    2    0    2    2    2    0    0
## [35,]   1    1    2    0    0    1    0    2    0    2    0    0    0
## [36,]   0    2    1    1    0    2    0    0    0    1    1    2    0
## [37,]   1    0    0    2    2    1    0    0    2    1    1    1    2
## [38,]   1    0    0    0    0    0    0    1    0    0    0    1    0
## [39,]   2    1    0    2    2    0    0    0    1    0    0    0    0
## [40,]   2    0    2    0    2    0    0    0    2    1    2    2    0
```

## [41,]	2	0	0	0	2	2	0	1	2	0	0	1	2
## [42,]	2	2	2	2	0	0	0	0	2	0	2	0	1
## [43,]	1	1	0	0	2	1	0	1	0	0	2	0	2
## [44,]	0	2	1	0	2	2	1	0	0	0	1	1	1
## [45,]	0	2	0	0	0	1	0	0	0	2	0	0	2
## [46,]	2	2	0	2	0	2	0	0	2	0	0	0	0
## [47,]	2	1	2	2	0	0	0	0	2	2	0	0	0
## [48,]	0	0	1	0	0	1	1	2	2	0	2	1	2
## [49,]	2	1	0	2	2	1	2	2	1	2	0	0	1
## [50,]	0	0	2	2	2	1	0	0	1	0	2	0	1
##	[,14]	[,15]	[,16]	[,17]	[,18]	[,19]	[,20]	[,21]	[,22]	[,23]	[,24]	[,25]	
## [1,]	2	0	1	2	2	0	1	2	0	2	0	0	
## [2,]	0	2	1	1	0	0	2	1	0	0	2	2	
## [3,]	1	0	0	0	0	1	0	1	1	2	0	0	
## [4,]	2	1	0	1	0	0	0	2	2	0	0	0	
## [5,]	0	0	1	1	0	0	1	2	1	1	1	0	
## [6,]	1	0	1	0	1	2	1	2	0	1	2	1	
## [7,]	1	2	0	0	0	1	0	0	1	1	1	0	
## [8,]	1	1	1	0	1	1	0	0	1	2	1	0	
## [9,]	1	1	1	2	1	1	1	0	0	0	0	2	
## [10,]	1	0	0	1	1	0	0	0	2	0	2	0	
## [11,]	0	1	0	1	0	1	2	0	0	0	2	2	
## [12,]	0	0	0	1	1	0	2	0	1	1	0	2	
## [13,]	0	0	1	0	0	1	0	0	0	1	0	2	
## [14,]	1	0	0	2	0	0	1	2	0	1	0	2	
## [15,]	0	0	2	1	1	2	0	0	2	0	1	0	
## [16,]	0	0	1	1	0	0	2	0	2	0	0	0	
## [17,]	1	1	0	1	2	1	1	2	0	2	0	0	
## [18,]	0	0	1	1	0	0	0	1	0	0	2	1	
## [19,]	1	2	0	1	0	0	0	1	2	1	1	1	
## [20,]	0	1	2	0	0	2	2	0	1	1	0	1	
## [21,]	0	2	1	0	2	0	0	2	0	1	0	2	
## [22,]	1	2	0	2	2	1	0	0	0	0	0	0	
## [23,]	0	2	2	1	1	1	1	1	0	1	2	0	
## [24,]	0	1	0	0	0	1	1	1	1	1	2	2	
## [25,]	0	0	2	1	0	1	1	2	0	0	1	1	
## [26,]	2	1	1	2	1	1	1	1	0	0	0	0	
## [27,]	0	0	0	1	0	0	0	2	0	1	1	2	
## [28,]	0	2	1	0	2	1	0	1	0	0	0	0	
## [29,]	1	0	1	2	2	2	1	2	1	1	1	0	
## [30,]	2	2	1	0	0	2	0	0	0	0	0	0	
## [31,]	0	1	0	1	1	0	2	2	0	0	1	0	
## [32,]	0	1	0	0	0	1	0	2	1	1	1	2	
## [33,]	2	2	0	0	1	1	2	0	0	1	2	1	
## [34,]	1	2	2	2	0	2	1	0	1	0	0	1	
## [35,]	0	0	0	1	0	0	1	2	0	1	0	0	
## [36,]	1	0	0	1	0	2	1	0	2	2	0	1	
## [37,]	1	1	2	0	1	2	1	0	2	0	0	0	
## [38,]	0	0	0	2	0	1	1	2	0	0	2	0	
## [39,]	0	0	2	0	2	2	2	2	0	0	0	1	
## [40,]	0	1	2	0	0	1	0	1	0	1	0	2	
## [41,]	2	1	0	0	1	1	1	0	1	1	2	2	
## [42,]	0	2	0	2	1	0	0	0	0	2	0	0	
## [43,]	0	0	0	0	0	1	1	1	0	0	1	2	

## [44,]	0	1	0	0	1	1	1	0	0	0	1	1
## [45,]	2	2	0	1	1	1	0	0	0	0	1	0
## [46,]	2	1	2	2	1	0	1	1	2	0	2	0
## [47,]	2	2	0	0	1	2	0	0	1	1	2	0
## [48,]	0	1	0	0	2	2	2	0	0	1	0	0
## [49,]	2	2	2	0	0	2	0	0	2	2	1	0
## [50,]	2	0	0	1	2	1	1	0	0	1	0	0
##	[,26]	[,27]	[,28]	[,29]	[,30]	[,31]	[,32]	[,33]	[,34]	[,35]	[,36]	[,37]
## [1,]	0	0	1	2	1	0	2	2	2	1	2	2
## [2,]	0	0	0	0	2	0	0	0	0	2	1	0
## [3,]	0	1	2	0	2	2	2	0	1	2	0	0
## [4,]	1	0	2	2	0	0	0	0	0	1	0	0
## [5,]	0	1	0	1	0	0	2	0	2	0	0	2
## [6,]	2	2	2	2	0	0	0	2	2	1	0	0
## [7,]	1	0	2	2	1	2	1	0	0	2	1	0
## [8,]	0	0	2	2	2	0	0	0	1	0	0	2
## [9,]	1	0	0	1	0	0	0	2	0	0	0	0
## [10,]	2	1	0	0	0	1	1	0	2	1	1	1
## [11,]	0	1	2	1	0	0	0	2	0	0	0	0
## [12,]	1	1	0	1	1	2	1	0	0	2	2	0
## [13,]	2	1	1	1	0	0	0	0	1	0	1	0
## [14,]	2	0	0	0	0	2	1	2	0	1	0	1
## [15,]	2	0	0	2	0	0	1	0	1	0	0	1
## [16,]	1	1	2	1	0	0	0	0	1	0	2	0
## [17,]	2	1	1	0	0	0	0	0	2	0	0	0
## [18,]	0	1	1	2	0	0	0	1	2	0	0	0
## [19,]	0	0	2	1	1	1	0	0	0	2	2	0
## [20,]	1	1	1	0	2	2	0	1	1	2	0	2
## [21,]	2	2	2	0	1	1	0	0	2	0	2	1
## [22,]	1	2	0	1	1	2	1	0	2	0	0	2
## [23,]	0	1	2	2	0	2	0	0	0	0	0	1
## [24,]	2	1	0	1	2	1	2	0	0	1	0	0
## [25,]	1	1	0	0	0	1	0	1	0	0	2	2
## [26,]	1	0	0	0	2	0	2	0	1	0	1	0
## [27,]	2	2	0	1	2	2	2	2	0	2	0	2
## [28,]	1	2	2	0	0	2	0	1	2	0	0	0
## [29,]	0	2	0	0	0	0	2	0	2	2	0	0
## [30,]	1	0	0	0	2	2	1	0	2	0	0	0
## [31,]	0	0	0	2	0	0	1	1	0	0	0	0
## [32,]	1	2	0	2	2	2	1	2	0	2	0	2
## [33,]	0	0	2	1	1	2	1	0	1	1	0	0
## [34,]	0	1	0	0	2	2	1	0	1	1	0	1
## [35,]	1	1	0	0	0	1	0	0	1	0	0	0
## [36,]	0	2	1	1	0	0	2	0	0	2	1	2
## [37,]	0	0	0	0	0	0	1	0	0	0	1	1
## [38,]	0	0	1	2	1	0	0	0	0	0	0	1
## [39,]	0	2	0	2	0	1	0	0	0	0	1	1
## [40,]	2	0	0	1	0	0	0	0	0	1	0	0
## [41,]	1	0	0	2	2	2	1	0	2	1	0	0
## [42,]	0	0	2	0	0	0	2	0	1	0	2	1
## [43,]	0	0	0	1	0	0	1	0	2	0	0	2
## [44,]	0	1	2	1	1	1	1	0	0	0	0	1
## [45,]	2	1	0	0	0	2	0	0	1	0	2	2
## [46,]	2	0	0	0	2	0	2	2	0	0	2	1

##	[47,]	0	1	0	0	2	1	2	1	1	0	0	0
##	[48,]	2	0	0	2	1	0	0	0	0	0	1	0
##	[49,]	1	1	1	0	0	1	2	0	0	2	2	1
##	[50,]	0	0	0	0	0	2	0	0	0	1	0	0
##		[,38]	[,39]	[,40]	[,41]	[,42]	[,43]	[,44]	[,45]	[,46]	[,47]	[,48]	[,49]
##	[1,]	2	0	0	0	2	2	0	1	2	0	2	1
##	[2,]	1	2	0	2	1	0	2	0	1	0	1	0
##	[3,]	2	0	2	1	2	0	2	0	1	0	2	0
##	[4,]	0	1	2	0	1	2	0	0	0	0	0	0
##	[5,]	1	0	2	1	2	1	1	0	0	0	1	0
##	[6,]	0	0	0	0	0	2	2	1	0	0	0	0
##	[7,]	2	1	2	0	0	2	0	2	0	1	2	0
##	[8,]	0	2	0	1	0	0	0	0	0	0	0	2
##	[9,]	1	1	0	0	1	1	0	1	0	2	1	0
##	[10,]	1	1	1	0	0	0	1	2	0	0	0	0
##	[11,]	0	1	2	1	1	0	0	0	0	0	2	0
##	[12,]	2	0	0	1	1	2	2	0	0	0	0	0
##	[13,]	0	0	0	0	2	1	0	1	0	1	2	0
##	[14,]	0	1	1	2	2	2	0	2	1	1	2	0
##	[15,]	1	0	1	0	0	1	0	2	2	1	0	1
##	[16,]	0	1	2	1	2	1	1	0	0	0	0	0
##	[17,]	2	0	0	2	0	1	1	0	0	0	2	1
##	[18,]	0	1	2	2	2	2	2	1	0	0	2	0
##	[19,]	0	1	0	1	1	0	0	0	2	0	0	1
##	[20,]	2	1	0	2	2	1	2	0	0	0	0	0
##	[21,]	1	0	0	2	2	0	0	2	0	0	0	2
##	[22,]	2	2	2	2	2	0	0	1	2	2	0	1
##	[23,]	0	0	0	2	1	1	1	2	2	1	2	0
##	[24,]	0	0	2	1	0	2	2	0	2	0	0	0
##	[25,]	1	0	0	0	0	1	1	1	0	0	1	2
##	[26,]	0	0	1	0	0	0	2	0	0	2	0	0
##	[27,]	0	1	0	2	0	1	1	0	0	2	0	0
##	[28,]	2	0	0	1	0	1	2	0	0	2	0	0
##	[29,]	2	2	1	1	0	0	0	0	1	1	1	0
##	[30,]	0	0	2	2	0	2	1	0	0	1	2	0
##	[31,]	0	1	0	2	1	1	1	1	1	0	0	0
##	[32,]	2	2	0	0	0	1	1	2	1	0	1	0
##	[33,]	2	2	2	0	0	0	1	1	0	0	0	2
##	[34,]	2	0	2	0	0	1	1	0	0	0	0	0
##	[35,]	1	2	0	1	2	0	1	1	1	0	1	0
##	[36,]	0	0	2	0	0	0	0	2	1	0	0	2
##	[37,]	2	1	2	2	0	0	1	0	0	0	1	0
##	[38,]	0	2	0	0	0	0	0	2	0	1	2	0
##	[39,]	0	1	0	1	2	1	2	2	1	0	1	0
##	[40,]	0	0	1	0	2	0	0	0	0	1	0	1
##	[41,]	0	2	0	1	2	1	1	0	0	0	0	0
##	[42,]	1	0	2	1	1	2	1	1	2	2	0	2
##	[43,]	1	2	2	0	0	0	0	2	0	2	1	1
##	[44,]	0	2	1	2	2	2	0	2	1	0	2	0
##	[45,]	0	0	1	1	0	0	2	1	0	1	0	0
##	[46,]	0	1	1	0	0	0	0	0	0	0	0	0
##	[47,]	0	2	2	2	0	0	0	0	0	0	0	0
##	[48,]	1	2	2	2	1	1	1	0	2	1	0	0
##	[49,]	2	0	0	1	0	0	2	0	0	2	0	0

```

## [50,]    0    1    1    2    2    0    1    2    2    0    2    1
##      [,50]
## [1,]    2
## [2,]    1
## [3,]    1
## [4,]    0
## [5,]    1
## [6,]    0
## [7,]    0
## [8,]    0
## [9,]    0
## [10,]   2
## [11,]   1
## [12,]   0
## [13,]   0
## [14,]   1
## [15,]   2
## [16,]   1
## [17,]   0
## [18,]   0
## [19,]   1
## [20,]   1
## [21,]   2
## [22,]   0
## [23,]   0
## [24,]   1
## [25,]   0
## [26,]   0
## [27,]   0
## [28,]   2
## [29,]   2
## [30,]   0
## [31,]   1
## [32,]   0
## [33,]   2
## [34,]   0
## [35,]   0
## [36,]   2
## [37,]   1
## [38,]   2
## [39,]   1
## [40,]   0
## [41,]   0
## [42,]   1
## [43,]   1
## [44,]   2
## [45,]   1
## [46,]   2
## [47,]   0
## [48,]   0
## [49,]   0
## [50,]   2

```

- Randomly punch holes (i.e. NA) values in this matrix so that an each entry is missing with probability

30%.

```
a = matrix(rbinom(n^2, size = 1, prob = 0.7), nrow = n, ncol = n)
R[which(a==0)] = NA
R
```

##		[,1]	[,2]	[,3]	[,4]	[,5]	[,6]	[,7]	[,8]	[,9]	[,10]	[,11]	[,12]	[,13]
##	[1,]	NA	NA	0	NA	1	1	0	NA	NA	1	0	1	0
##	[2,]	NA	2	1	2	0	NA	1	0	1	0	0	0	0
##	[3,]	NA	NA	0	2	NA	NA	NA	0	2	2	0	0	0
##	[4,]	0	2	1	0	1	2	0	NA	0	0	0	0	1
##	[5,]	0	0	NA	0	0	NA	1	1	NA	NA	1	NA	2
##	[6,]	NA	0	0	NA	2	NA	0	0	2	0	0	NA	1
##	[7,]	1	0	2	0	0	2	NA	NA	NA	NA	NA	0	2
##	[8,]	NA	NA	1	1	2	0	NA	0	NA	0	1	NA	NA
##	[9,]	0	2	1	NA	0	0	NA	1	NA	NA	0	1	0
##	[10,]	0	0	1	2	NA	0	NA	0	1	0	0	1	1
##	[11,]	0	NA	NA	NA	0	2	1	NA	0	1	NA	2	NA
##	[12,]	2	0	0	0	0	0	NA	0	NA	NA	2	NA	1
##	[13,]	NA	0	0	0	0	2	NA	NA	NA	2	NA	0	NA
##	[14,]	1	0	0	NA	1	0	1	0	0	2	0	0	0
##	[15,]	0	1	0	NA	1	0	NA	NA	2	NA	1	0	2
##	[16,]	2	0	0	0	0	2	2	NA	0	NA	2	1	NA
##	[17,]	2	0	NA	0	NA	0	0	NA	1	0	NA	0	NA
##	[18,]	0	0	NA	NA	2	0	0	1	NA	NA	NA	0	1
##	[19,]	1	0	0	2	NA	0	2	0	0	2	NA	NA	0
##	[20,]	NA	0	0	2	NA	NA	0	NA	NA	NA	2	2	0
##	[21,]	NA	0	0	NA	1	NA	0	NA	NA	NA	NA	2	NA
##	[22,]	NA	NA	NA	0	1	2	0	2	0	NA	NA	NA	NA
##	[23,]	1	NA	NA	0	0	NA	0	1	2	2	NA	0	1
##	[24,]	NA	0	0	0	0	NA	1	NA	NA	0	0	0	2
##	[25,]	1	NA	0	NA	0	NA	NA	0	1	NA	NA	0	NA
##	[26,]	2	0	0	0	NA	2	NA	NA	NA	0	1	0	NA
##	[27,]	0	NA	NA	0	2	NA	1	2	NA	1	NA	0	0
##	[28,]	0	0	2	2	1	NA	0	NA	0	NA	NA	NA	NA
##	[29,]	2	NA	2	0	NA	NA	1	2	NA	NA	2	NA	NA
##	[30,]	0	0	0	NA	NA	0	NA	0	0	2	2	NA	0
##	[31,]	0	1	NA	NA	NA	2	0	2	NA	NA	NA	0	NA
##	[32,]	2	0	NA	2	NA	0	NA	0	0	0	NA	2	0
##	[33,]	2	0	0	2	1	0	2	0	0	2	NA	0	0
##	[34,]	0	1	1	0	0	0	2	0	2	2	NA	NA	0
##	[35,]	1	NA	NA	NA	0	1	0	2	0	2	NA	0	0
##	[36,]	NA	2	1	1	NA	NA	0	0	0	1	1	2	0
##	[37,]	1	NA	0	2	NA	1	0	0	2	1	NA	1	2
##	[38,]	1	0	0	0	NA	0	0	1	0	0	0	NA	0
##	[39,]	2	NA	0	NA	NA	NA	0	0	1	0	0	NA	NA
##	[40,]	2	NA	2	NA	NA	0	0	0	2	1	2	NA	0
##	[41,]	2	0	0	0	2	NA	NA	1	2	0	0	1	2
##	[42,]	2	2	2	2	0	0	0	0	2	0	2	0	1
##	[43,]	NA	1	NA	NA	2	1	0	NA	NA	NA	2	0	2
##	[44,]	0	2	1	NA	2	NA	1	NA	0	0	1	1	NA
##	[45,]	NA	2	0	NA	NA	NA	0	0	0	NA	0	NA	NA
##	[46,]	2	2	0	NA	NA	2	NA	NA	2	0	NA	0	0
##	[47,]	2	1	2	2	0	0	0	0	NA	2	0	NA	NA
##	[48,]	0	0	1	0	0	1	NA	2	2	NA	2	1	2

## [49,]	2	1	0	2	2	1	2	NA	1	2	0	0	1
## [50,]	0	0	NA	2	NA	1	0	NA	NA	NA	2	NA	1
##	[,14]	[,15]	[,16]	[,17]	[,18]	[,19]	[,20]	[,21]	[,22]	[,23]	[,24]	[,25]	
## [1,]	NA	0	1	NA	NA	0	1	2	NA	2	0	0	
## [2,]	0	2	1	1	0	0	2	NA	0	NA	2	2	
## [3,]	1	0	0	0	0	1	0	NA	1	2	0	NA	
## [4,]	2	NA	0	1	0	0	NA	2	2	0	0	0	
## [5,]	0	0	1	1	0	0	1	2	1	1	NA	NA	
## [6,]	NA	0	1	0	NA	NA	1	2	0	1	2	1	
## [7,]	1	2	0	0	0	1	0	0	NA	1	1	0	
## [8,]	1	NA	NA	0	NA	NA	0	0	1	2	1	0	
## [9,]	NA	1	NA	2	1	1	NA	0	0	0	NA	2	
## [10,]	NA	NA	NA	1	1	0	0	0	2	0	2	0	
## [11,]	0	1	NA	1	NA	1	2	0	0	0	2	NA	
## [12,]	0	0	NA	1	1	0	NA	0	1	1	NA	2	
## [13,]	0	0	NA	0	0	1	0	NA	NA	1	0	NA	
## [14,]	1	0	0	NA	0	NA	NA	NA	NA	NA	NA	2	
## [15,]	0	NA	2	NA	1	2	0	NA	2	0	1	NA	
## [16,]	0	NA	1	1	0	0	2	0	NA	0	0	NA	
## [17,]	NA	1	0	NA	2	1	1	2	0	NA	0	0	
## [18,]	0	0	NA	1	0	NA	0	NA	NA	NA	NA	1	
## [19,]	1	2	NA	NA	0	NA	0	1	2	1	1	1	
## [20,]	0	1	2	0	0	2	NA	NA	1	1	0	1	
## [21,]	NA	NA	1	0	NA	0	NA	2	0	1	0	2	
## [22,]	NA	NA	0	2	NA	1	0	0	0	0	NA	0	
## [23,]	NA	2	2	1	1	1	1	NA	0	1	2	0	
## [24,]	0	1	0	0	0	NA	1	NA	NA	NA	2	NA	
## [25,]	0	0	2	1	0	1	NA	2	0	0	1	1	
## [26,]	NA	1	1	NA	1	1	NA	1	0	NA	0	0	
## [27,]	0	0	0	1	0	0	0	2	0	1	1	2	
## [28,]	0	2	NA	0	2	NA	0	1	0	0	NA	NA	
## [29,]	1	0	NA	2	2	2	NA	2	1	1	1	NA	
## [30,]	NA	2	NA	0	NA	2	NA	0	NA	NA	0	0	
## [31,]	0	1	0	1	1	0	2	NA	NA	0	NA	NA	
## [32,]	0	NA	0	NA	0	1	0	2	1	1	1	2	
## [33,]	2	2	NA	NA	NA	1	2	NA	0	1	2	1	
## [34,]	1	2	2	2	0	2	NA	0	NA	NA	0	1	
## [35,]	NA	0	NA	1	0	NA	1	2	0	1	NA	0	
## [36,]	NA	0	0	1	0	2	NA	0	NA	2	0	NA	
## [37,]	1	NA	NA	0	NA	NA	NA	0	2	0	0	NA	
## [38,]	NA	0	NA	2	NA	1	NA	2	0	NA	2	0	
## [39,]	0	0	2	NA	NA	2	2	NA	0	NA	NA	1	
## [40,]	0	1	2	0	NA	1	0	1	0	1	0	2	
## [41,]	2	NA	NA	0	1	NA	1	0	1	1	2	2	
## [42,]	NA	2	NA	2	1	0	0	NA	0	2	0	0	
## [43,]	0	0	0	0	0	1	1	1	0	0	1	NA	
## [44,]	0	NA	0	0	1	NA	1	0	0	0	1	1	
## [45,]	2	2	NA	1	NA	1	0	0	0	0	1	NA	
## [46,]	2	NA	NA	2	1	0	NA	1	2	0	NA	NA	
## [47,]	2	NA	NA	0	1	2	NA	0	1	1	2	0	
## [48,]	0	1	0	NA	NA	NA	2	NA	0	NA	0	0	
## [49,]	2	2	2	NA	0	2	NA	NA	2	2	1	NA	
## [50,]	2	0	NA	1	NA	NA	1	NA	0	1	0	0	
##	[,26]	[,27]	[,28]	[,29]	[,30]	[,31]	[,32]	[,33]	[,34]	[,35]	[,36]	[,37]	

##	[1,]	NA	NA	NA	2	1	0	2	2	2	1	2	NA
##	[2,]	NA	0	NA	0	NA	0	0	NA	0	NA	1	0
##	[3,]	0	1	NA	0	2	NA	2	0	NA	2	NA	0
##	[4,]	1	NA	NA	NA	0	NA	0	0	NA	1	0	0
##	[5,]	0	1	0	1	0	0	2	0	NA	0	0	NA
##	[6,]	NA	NA	NA	2	0	0	0	2	2	1	0	0
##	[7,]	1	0	NA	2	1	2	1	0	0	NA	NA	0
##	[8,]	NA	0	2	2	NA	NA	NA	0	1	0	0	NA
##	[9,]	1	0	0	NA	0	0	NA	2	0	NA	0	0
##	[10,]	2	1	0	0	0	NA	1	0	2	1	1	1
##	[11,]	0	NA	NA	1	0	0	0	NA	0	0	0	0
##	[12,]	1	NA	0	1	NA	NA	1	0	NA	2	2	NA
##	[13,]	NA	1	NA	NA	NA	0	0	NA	NA	0	1	NA
##	[14,]	2	0	NA	0	0	2	NA	NA	NA	1	0	NA
##	[15,]	2	NA	0	2	NA	0	NA	NA	1	NA	NA	1
##	[16,]	1	1	NA	1	NA	0	NA	0	1	NA	NA	NA
##	[17,]	2	1	1	0	0	0	0	0	2	0	0	NA
##	[18,]	0	1	1	NA	0	0	0	1	2	NA	0	NA
##	[19,]	0	0	2	NA	1	NA	0	0	0	2	2	0
##	[20,]	NA	NA	1	0	2	2	0	NA	1	NA	0	2
##	[21,]	NA	2	NA	NA	1	NA	0	NA	2	0	2	NA
##	[22,]	1	2	0	1	1	2	NA	0	2	0	NA	2
##	[23,]	0	1	2	2	0	2	0	0	0	NA	0	1
##	[24,]	2	1	0	1	2	1	2	NA	NA	NA	0	NA
##	[25,]	1	1	0	0	0	1	0	1	0	0	2	2
##	[26,]	1	0	NA	NA	2	0	2	NA	NA	0	1	0
##	[27,]	NA	2	0	1	2	NA	2	2	0	2	0	2
##	[28,]	1	NA	2	NA	0	2	0	NA	NA	0	0	0
##	[29,]	0	2	0	0	0	0	2	0	2	NA	0	0
##	[30,]	NA	0	0	0	2	2	NA	0	NA	0	0	0
##	[31,]	NA	0	0	2	0	NA	NA	1	0	NA	0	0
##	[32,]	1	2	NA	2	2	NA	NA	2	NA	2	0	2
##	[33,]	0	NA	2	1	1	2	1	0	1	1	0	0
##	[34,]	NA	1	0	0	NA	2	1	NA	1	NA	0	NA
##	[35,]	1	1	NA	0	0	NA	0	0	1	0	NA	0
##	[36,]	0	NA	1	1	0	NA	2	0	NA	NA	1	2
##	[37,]	0	0	0	NA	0	NA	1	0	0	0	NA	NA
##	[38,]	0	0	1	2	NA	0	0	NA	0	NA	0	NA
##	[39,]	NA	2	0	2	0	1	0	0	NA	0	1	NA
##	[40,]	2	NA	0	1	0	0	NA	0	0	NA	NA	0
##	[41,]	1	0	NA	2	NA	2	1	0	2	1	0	0
##	[42,]	0	0	2	NA	0	NA	2	NA	NA	0	NA	1
##	[43,]	0	0	0	1	NA	NA	1	0	2	0	0	NA
##	[44,]	NA	NA	2	1	1	1	1	NA	NA	0	0	1
##	[45,]	2	1	NA	0	0	NA	0	NA	NA	NA	2	2
##	[46,]	2	NA	NA	NA	2	0	2	2	0	0	2	1
##	[47,]	0	1	NA	0	2	1	2	1	1	NA	0	0
##	[48,]	NA	NA	0	NA	1	0	NA	0	0	0	1	0
##	[49,]	NA	NA	1	0	0	1	2	0	0	2	2	1
##	[50,]	NA	NA	0	0	NA	2	0	0	0	NA	0	0
##		[,38]	[,39]	[,40]	[,41]	[,42]	[,43]	[,44]	[,45]	[,46]	[,47]	[,48]	[,49]
##	[1,]	NA	0	0	NA	2	2	NA	1	NA	0	2	1
##	[2,]	NA	2	NA	2	NA	NA	NA	NA	1	NA	1	0
##	[3,]	2	0	NA	1	2	0	2	0	1	NA	NA	NA

##	[4,]	0	NA	NA	0	1	2	0	NA	0	NA	NA	0
##	[5,]	NA	0	2	NA	2	1	1	0	0	NA	1	0
##	[6,]	NA	NA	0	0	0	2	2	NA	0	0	0	0
##	[7,]	2	1	2	0	0	NA	0	2	NA	1	2	NA
##	[8,]	0	2	NA	NA	0	0	0	NA	0	0	0	2
##	[9,]	1	NA	NA	0	1	1	0	1	0	2	1	NA
##	[10,]	NA	1	1	0	0	NA	1	NA	0	NA	0	NA
##	[11,]	0	NA	2	1	1	0	0	NA	0	0	2	NA
##	[12,]	2	NA	0	NA	1	NA	NA	0	0	NA	0	NA
##	[13,]	0	0	0	NA	2	1	0	1	NA	1	NA	NA
##	[14,]	0	NA	NA	NA	2	2	NA	2	1	1	2	0
##	[15,]	1	0	1	NA	0	NA	0	NA	2	NA	NA	NA
##	[16,]	0	NA	2	1	2	1	1	NA	NA	0	0	0
##	[17,]	2	0	NA	2	0	1	NA	0	0	NA	2	1
##	[18,]	NA	NA	NA	NA	2	2	2	1	NA	0	2	NA
##	[19,]	NA	NA	0	1	1	0	0	NA	NA	0	0	1
##	[20,]	2	NA	0	NA	NA	1	2	0	0	0	0	NA
##	[21,]	NA	0	NA	2	2	0	0	2	0	0	NA	NA
##	[22,]	NA	2	2	2	2	0	0	1	2	2	0	NA
##	[23,]	NA	NA	0	2	1	NA	1	NA	2	1	2	NA
##	[24,]	0	NA	2	1	0	2	NA	NA	2	0	NA	0
##	[25,]	NA	0	0	NA	0	1	NA	1	0	0	1	NA
##	[26,]	NA	0	1	0	0	NA	2	0	0	2	0	0
##	[27,]	0	1	NA	NA	NA	NA	1	0	0	2	0	0
##	[28,]	2	0	0	1	NA	1	2	0	0	2	0	0
##	[29,]	2	NA	1	NA	NA	0	NA	0	1	1	1	NA
##	[30,]	0	0	2	2	NA	2	1	0	NA	NA	NA	NA
##	[31,]	0	1	0	NA	1	NA	1	1	NA	0	NA	0
##	[32,]	NA	NA	NA	NA	0	1	1	NA	NA	0	1	0
##	[33,]	NA	2	NA	0	0	0	NA	1	NA	0	0	NA
##	[34,]	2	NA	NA	0	0	NA	NA	0	0	NA	NA	NA
##	[35,]	1	NA	0	1	2	0	NA	1	1	0	1	0
##	[36,]	0	0	2	0	NA	0	0	2	1	0	NA	2
##	[37,]	2	NA	2	2	0	0	1	NA	0	NA	1	0
##	[38,]	0	NA	0	NA	NA	0	0	2	NA	1	NA	NA
##	[39,]	0	NA	0	NA	NA	1	2	NA	1	0	1	0
##	[40,]	0	0	NA	0	2	0	0	NA	NA	1	NA	NA
##	[41,]	0	NA	NA	1	2	1	1	NA	0	0	NA	0
##	[42,]	1	NA	NA	1	1	2	NA	1	2	2	0	2
##	[43,]	1	2	2	0	0	0	0	2	0	NA	1	1
##	[44,]	0	2	NA	2	2	2	0	2	1	NA	2	0
##	[45,]	0	0	1	1	0	0	2	1	NA	NA	NA	0
##	[46,]	NA	NA	1	0	0	0	0	NA	0	NA	NA	0
##	[47,]	0	2	2	2	NA	0	NA	0	0	NA	NA	NA
##	[48,]	NA	2	2	2	1	1	NA	NA	2	1	0	0
##	[49,]	2	NA	0	NA	0	0	NA	0	0	NA	NA	NA
##	[50,]	NA	1	1	2	2	NA	1	2	NA	NA	2	1
##	[,50]												
##	[1,]	2											
##	[2,]	NA											
##	[3,]	NA											
##	[4,]	0											
##	[5,]	NA											
##	[6,]	0											

```
## [7,] 0
## [8,] NA
## [9,] 0
## [10,] 2
## [11,] 1
## [12,] NA
## [13,] 0
## [14,] 1
## [15,] 2
## [16,] NA
## [17,] 0
## [18,] 0
## [19,] 1
## [20,] 1
## [21,] NA
## [22,] NA
## [23,] 0
## [24,] 1
## [25,] 0
## [26,] NA
## [27,] 0
## [28,] 2
## [29,] 2
## [30,] 0
## [31,] NA
## [32,] NA
## [33,] NA
## [34,] NA
## [35,] 0
## [36,] 2
## [37,] NA
## [38,] 2
## [39,] NA
## [40,] NA
## [41,] 0
## [42,] 1
## [43,] 1
## [44,] 2
## [45,] NA
## [46,] 2
## [47,] 0
## [48,] 0
## [49,] NA
## [50,] 2
```

- Sort the rows in matrix R by the largest row sum to lowest. Be careful about the NA's!

```
row.sums = apply(R, 1, sum, na.rm = TRUE)
R = R[order(row.sums),]
```

- We will now learn the `apply` function. This is a handy function that saves writing for loops which should be eschewed in R. Use the `apply` function to compute a vector whose entries are the standard deviation of each row. Use the `apply` function to compute a vector whose entries are the standard deviation of each column. Be careful about the NA's! This should be one line.

```
R_sd = apply(R, 1, sd, na.rm = TRUE)
R_sd
```

```
## [1] 0.68588872986 0.72793204179 0.79534631298 0.76817321620 0.80321932890
## [6] 0.91084416712 0.80229555709 0.77459666924 0.79107929540 0.68565882388
## [11] 0.77907115956 0.68882107581 0.83214969704 0.83214969704 0.72811999709
## [16] 0.92141350598 0.81649658093 0.72077702483 0.83816526318 0.83937205966
## [21] 0.85687468993 0.83937205966 0.79884051447 0.81939505146 0.83937205966
## [26] 0.89348717267 0.87008991007 0.88963130018 0.73746840551 0.77232844572
## [31] 0.84486277196 0.80229046222 0.84091786587 0.84660136485 0.86936369051
## [36] 0.85424219618 0.84334901040 0.87242971249 0.87904907299 0.94825816547
## [41] 0.84723257155 0.91919518390 0.85507438556 0.88701002632 0.83286086471
## [46] 0.79829120488 0.81809201053 0.86987613600 0.90283703394 0.89265076980
```

- Use the `apply` function to compute a vector whose entries are the count of entries that are 1 or 2 in each column. This should be one line.

```
R_count = apply(R, 2, function(x) length(which (x == 1 | x == 2 )))
```

- Use the `split` function to create a list whose keys are the column number and values are the vector of the columns. Look at the last example in the documentation `?split`.

```
new_list = split(R, col(R))
```

- In one statement, use the `lapply` function to create a list whose keys are the column number and values are themselves a list with keys: “min” whose value is the minimum of the column, “max” whose value is the maximum of the column, “pct_missing” is the proportion of missingness in the column and “first_NA” whose value is the row number of the first time the NA appears.

```
lapply (split(R, col(R)),
        function(x) list (min = min(x, na.rm = TRUE), max = max(x, na.rm = TRUE),
                           pct_missing = prop.table(table (R))[1],
                           first_NA = which.min(is.na(x)) ) )
```

```
## $`1`
## $`1`$min
## [1] 0
##
## $`1`$max
## [1] 2
##
## $`1`$pct_missing
##      0
## 0.5049161365
##
## $`1`$first_NA
## [1] 2
##
##
## $`2`
## $`2`$min
## [1] 0
##
## $`2`$max
## [1] 2
##
```

```

## $`2`$pct_missing
##      0
## 0.5049161365
##
## $`2`$first_NA
## [1] 1
##
##
## $`3`
## $`3`$min
## [1] 0
##
## $`3`$max
## [1] 2
##
## $`3`$pct_missing
##      0
## 0.5049161365
##
## $`3`$first_NA
## [1] 1
##
##
## $`4`
## $`4`$min
## [1] 0
##
## $`4`$max
## [1] 2
##
## $`4`$pct_missing
##      0
## 0.5049161365
##
## $`4`$first_NA
## [1] 1
##
##
## $`5`
## $`5`$min
## [1] 0
##
## $`5`$max
## [1] 2
##
## $`5`$pct_missing
##      0
## 0.5049161365
##
## $`5`$first_NA
## [1] 1
##
##
## $`6`

```

```

## $`6`$min
## [1] 0
##
## $`6`$max
## [1] 2
##
## $`6`$pct_missing
##      0
## 0.5049161365
##
## $`6`$first_NA
## [1] 1
##
##
## $`7`
## $`7`$min
## [1] 0
##
## $`7`$max
## [1] 2
##
## $`7`$pct_missing
##      0
## 0.5049161365
##
## $`7`$first_NA
## [1] 2
##
##
## $`8`
## $`8`$min
## [1] 0
##
## $`8`$max
## [1] 2
##
## $`8`$pct_missing
##      0
## 0.5049161365
##
## $`8`$first_NA
## [1] 2
##
##
## $`9`
## $`9`$min
## [1] 0
##
## $`9`$max
## [1] 2
##
## $`9`$pct_missing
##      0
## 0.5049161365

```

```

##
## $`9`$first_NA
## [1] 3
##
##
## $`10`
## $`10`$min
## [1] 0
##
## $`10`$max
## [1] 2
##
## $`10`$pct_missing
##          0
## 0.5049161365
##
## $`10`$first_NA
## [1] 1
##
##
## $`11`
## $`11`$min
## [1] 0
##
## $`11`$max
## [1] 2
##
## $`11`$pct_missing
##          0
## 0.5049161365
##
## $`11`$first_NA
## [1] 3
##
##
## $`12`
## $`12`$min
## [1] 0
##
## $`12`$max
## [1] 2
##
## $`12`$pct_missing
##          0
## 0.5049161365
##
## $`12`$first_NA
## [1] 1
##
##
## $`13`
## $`13`$min
## [1] 0
##
##

```



```

## $`13`$max
## [1] 2
##
## $`13`$pct_missing
##      0
## 0.5049161365
##
## $`13`$first_NA
## [1] 3
##
##
## $`14`
## $`14`$min
## [1] 0
##
## $`14`$max
## [1] 2
##
## $`14`$pct_missing
##      0
## 0.5049161365
##
## $`14`$first_NA
## [1] 1
##
##
## $`15`
## $`15`$min
## [1] 0
##
## $`15`$max
## [1] 2
##
## $`15`$pct_missing
##      0
## 0.5049161365
##
## $`15`$first_NA
## [1] 1
##
##
## $`16`
## $`16`$min
## [1] 0
##
## $`16`$max
## [1] 2
##
## $`16`$pct_missing
##      0
## 0.5049161365
##
## $`16`$first_NA
## [1] 2

```

```

##
##
## $`17`
## $`17`$min
## [1] 0
##
## $`17`$max
## [1] 2
##
## $`17`$pct_missing
##      0
## 0.5049161365
##
## $`17`$first_NA
## [1] 1
##
##
## $`18`
## $`18`$min
## [1] 0
##
## $`18`$max
## [1] 2
##
## $`18`$pct_missing
##      0
## 0.5049161365
##
## $`18`$first_NA
## [1] 1
##
##
## $`19`
## $`19`$min
## [1] 0
##
## $`19`$max
## [1] 2
##
## $`19`$pct_missing
##      0
## 0.5049161365
##
## $`19`$first_NA
## [1] 1
##
##
## $`20`
## $`20`$min
## [1] 0
##
## $`20`$max
## [1] 2
##

```

```

## $`20`$pct_missing
##      0
## 0.5049161365
##
## $`20`$first_NA
## [1] 1
##
##
## $`21`
## $`21`$min
## [1] 0
##
## $`21`$max
## [1] 2
##
## $`21`$pct_missing
##      0
## 0.5049161365
##
## $`21`$first_NA
## [1] 3
##
##
## $`22`
## $`22`$min
## [1] 0
##
## $`22`$max
## [1] 2
##
## $`22`$pct_missing
##      0
## 0.5049161365
##
## $`22`$first_NA
## [1] 3
##
##
## $`23`
## $`23`$min
## [1] 0
##
## $`23`$max
## [1] 2
##
## $`23`$pct_missing
##      0
## 0.5049161365
##
## $`23`$first_NA
## [1] 1
##
##
## $`24`

```

```

## $`24`$min
## [1] 0
##
## $`24`$max
## [1] 2
##
## $`24`$pct_missing
##      0
## 0.5049161365
##
## $`24`$first_NA
## [1] 1
##
##
## $`25`
## $`25`$min
## [1] 0
##
## $`25`$max
## [1] 2
##
## $`25`$pct_missing
##      0
## 0.5049161365
##
## $`25`$first_NA
## [1] 3
##
##
## $`26`
## $`26`$min
## [1] 0
##
## $`26`$max
## [1] 2
##
## $`26`$pct_missing
##      0
## 0.5049161365
##
## $`26`$first_NA
## [1] 3
##
##
## $`27`
## $`27`$min
## [1] 0
##
## $`27`$max
## [1] 2
##
## $`27`$pct_missing
##      0
## 0.5049161365

```

```

##
## $`27`$first_NA
## [1] 1
##
##
## $`28`
## $`28`$min
## [1] 0
##
## $`28`$max
## [1] 2
##
## $`28`$pct_missing
##          0
## 0.5049161365
##
## $`28`$first_NA
## [1] 2
##
##
## $`29`
## $`29`$min
## [1] 0
##
## $`29`$max
## [1] 2
##
## $`29`$pct_missing
##          0
## 0.5049161365
##
## $`29`$first_NA
## [1] 2
##
##
## $`30`
## $`30`$min
## [1] 0
##
## $`30`$max
## [1] 2
##
## $`30`$pct_missing
##          0
## 0.5049161365
##
## $`30`$first_NA
## [1] 2
##
##
## $`31`
## $`31`$min
## [1] 0
##
##

```

```

## $`31`$max
## [1] 2
##
## $`31`$pct_missing
##      0
## 0.5049161365
##
## $`31`$first_NA
## [1] 1
##
##
## $`32`
## $`32`$min
## [1] 0
##
## $`32`$max
## [1] 2
##
## $`32`$pct_missing
##      0
## 0.5049161365
##
## $`32`$first_NA
## [1] 1
##
##
## $`33`
## $`33`$min
## [1] 0
##
## $`33`$max
## [1] 2
##
## $`33`$pct_missing
##      0
## 0.5049161365
##
## $`33`$first_NA
## [1] 2
##
##
## $`34`
## $`34`$min
## [1] 0
##
## $`34`$max
## [1] 2
##
## $`34`$pct_missing
##      0
## 0.5049161365
##
## $`34`$first_NA
## [1] 2

```

```

##
##
## $`35`
## $`35`$min
## [1] 0
##
## $`35`$max
## [1] 2
##
## $`35`$pct_missing
##      0
## 0.5049161365
##
## $`35`$first_NA
## [1] 1
##
##
## $`36`
## $`36`$min
## [1] 0
##
## $`36`$max
## [1] 2
##
## $`36`$pct_missing
##      0
## 0.5049161365
##
## $`36`$first_NA
## [1] 1
##
##
## $`37`
## $`37`$min
## [1] 0
##
## $`37`$max
## [1] 2
##
## $`37`$pct_missing
##      0
## 0.5049161365
##
## $`37`$first_NA
## [1] 2
##
##
## $`38`
## $`38`$min
## [1] 0
##
## $`38`$max
## [1] 2
##

```

```

## `$38`$pct_missing
##      0
## 0.5049161365
##
## `$38`$first_NA
## [1] 1
##
##
## `$39`
## `$39`$min
## [1] 0
##
## `$39`$max
## [1] 2
##
## `$39`$pct_missing
##      0
## 0.5049161365
##
## `$39`$first_NA
## [1] 1
##
##
## `$40`
## `$40`$min
## [1] 0
##
## `$40`$max
## [1] 2
##
## `$40`$pct_missing
##      0
## 0.5049161365
##
## `$40`$first_NA
## [1] 1
##
##
## `$41`
## `$41`$min
## [1] 0
##
## `$41`$max
## [1] 2
##
## `$41`$pct_missing
##      0
## 0.5049161365
##
## `$41`$first_NA
## [1] 4
##
##
## `$42`

```



```

## $`42`$min
## [1] 0
##
## $`42`$max
## [1] 2
##
## $`42`$pct_missing
##      0
## 0.5049161365
##
## $`42`$first_NA
## [1] 1
##
##
## $`43`
## $`43`$min
## [1] 0
##
## $`43`$max
## [1] 2
##
## $`43`$pct_missing
##      0
## 0.5049161365
##
## $`43`$first_NA
## [1] 1
##
##
## $`44`
## $`44`$min
## [1] 0
##
## $`44`$max
## [1] 2
##
## $`44`$pct_missing
##      0
## 0.5049161365
##
## $`44`$first_NA
## [1] 1
##
##
## $`45`
## $`45`$min
## [1] 0
##
## $`45`$max
## [1] 2
##
## $`45`$pct_missing
##      0
## 0.5049161365

```

```

##
## $`45`$first_NA
## [1] 1
##
##
## $`46`
## $`46`$min
## [1] 0
##
## $`46`$max
## [1] 2
##
## $`46`$pct_missing
##          0
## 0.5049161365
##
## $`46`$first_NA
## [1] 4
##
##
## $`47`
## $`47`$min
## [1] 0
##
## $`47`$max
## [1] 2
##
## $`47`$pct_missing
##          0
## 0.5049161365
##
## $`47`$first_NA
## [1] 1
##
##
## $`48`
## $`48`$min
## [1] 0
##
## $`48`$max
## [1] 2
##
## $`48`$pct_missing
##          0
## 0.5049161365
##
## $`48`$first_NA
## [1] 5
##
##
## $`49`
## $`49`$min
## [1] 0
##
##

```

```
## $`49`$max
## [1] 2
##
## $`49`$pct_missing
##      0
## 0.5049161365
##
## $`49`$first_NA
## [1] 2
##
##
## $`50`
## $`50`$min
## [1] 0
##
## $`50`$max
## [1] 2
##
## $`50`$pct_missing
##      0
## 0.5049161365
##
## $`50`$first_NA
## [1] 1
```

- Set a seed and then create a vector `v` consisting of a sample of 1,000 iid normal realizations with mean -10 and variance 100.

```
set.seed(3)
v = rnorm(1000, mean = -10, sd = 10)
v
```

```
##      [1] -19.619334159199 -12.925257228785 -7.412117837587 -21.521318859151
##      [5] -8.042171737136 -9.698760553984 -9.145822683877 1.166102127153
##      [9] -22.188574155780 2.673687220899 -17.447815961351 -21.312185708357
##     [13] -17.163584900330 -7.473476303538 -8.479542933444 -13.076564296784
##     [17] -19.530173309081 -16.482428114485 2.243136242806 -8.001883920170
##     [21] -15.784837218600 -19.423007334775 -12.037281796620 -26.664748400302
##     [25] -14.844551091510 -17.410726607216 1.606157792413 0.120671249342
##     [29] -10.720784740866 -21.367822980993 -0.993752710173 -1.482295529078
##     [33] -2.722848258455 -2.634978543114 -13.521296169457 -2.944844865145
##     [37] 3.003579887321 -9.617479858557 -19.792837699963 -2.062387691275
##     [41] -2.134931279906 -13.104631309593 6.988848455591 -17.945937085493
##     [45] -6.515622838200 -32.654010735178 -11.622052790282 1.308649914589
##     [49] -14.555459762605 -18.991663155389 -2.731610982688 -18.094409018652
##     [53] -7.329148840448 -27.372637105336 -24.114251358089 -14.535512267785
##     [57] -20.354912753681 3.621428932593 -0.825432630250 -17.851421610768
##     [61] -4.264818268527 -0.818037922622 -7.437127270143 -6.480334440624
##     [65] 1.743373570956 -14.808463752892 -14.188297221356 -0.448871967796
##     [69] -22.890066109479 -8.138025669250 -10.313255019472 -5.329026901534
##     [73] 0.241976742046 -7.326415477656 -7.681738971398 -2.524075354776
##     [77] 2.170685105242 -6.166416548317 -19.880528215921 -11.568529101968
##     [81] 7.355352162481 -13.522983055001 -3.113599558743 2.244060958027
##     [85] -2.057036966965 -10.064023984217 -7.808493648330 -18.864637510054
##     [89] -5.602397086281 -18.863897506655 -18.538184543550 -19.899943307485
```

```

## [93] -16.508777369239 0.539466604940 -13.908780334308 -10.705863936101
## [97] -14.620508094970 -4.590917330097 -0.683650290735 -12.092743452084
## [101] -3.826499515279 -14.050775126934 0.531037627893 -3.977157537671
## [105] 0.174611767962 -3.918326819880 -7.932640045535 -28.977272917940
## [109] -16.825828316783 -5.186615845512 -14.630310380025 -12.797416957800
## [113] -14.136901445512 6.187665209943 -17.210557108638 -14.530931573281
## [117] -9.857428391883 -7.842353788047 -8.111298047069 -10.501484943351
## [121] -24.954196319188 -6.321622471664 -4.828559778244 -14.843354650510
## [125] -3.251443840768 -17.624486052321 -6.139262091618 -16.640033446425
## [129] -27.243441951543 1.563190793031 -3.064934101286 -8.568436438325
## [133] 4.928135601807 -26.321534789575 -8.721539766547 -34.036637271301
## [137] 4.439282555670 -18.788930503079 -23.064383272157 -18.771989925869
## [141] -21.643804594895 -29.823476800554 -19.899442348636 -11.516846011659
## [145] -0.874932093512 -5.923301917555 -22.421843752050 -16.426944118908
## [149] 9.302436888251 -5.898006359858 -22.913493209717 16.350453747653
## [153] -5.129277117698 -1.461076820541 0.884427054513 -7.739860429112
## [157] -9.318011624379 -19.848155326560 -23.108544218437 14.640553352302
## [161] -16.654280698611 -0.871373519774 -0.353357737106 6.080029371317
## [165] 8.353995249022 -2.975372667555 2.178540787540 -21.236538291462
## [169] -3.316698844607 2.164114883365 -7.654246460518 -14.186965875024
## [173] -7.617799100382 -15.505881920704 -15.006027685219 1.638974920419
## [177] 11.555369544259 -27.091570091025 -26.008226151234 -20.385534134627
## [181] -6.769057793887 -18.888471537352 -6.063210181149 -7.634585319331
## [185] -14.304968134869 -15.479331263351 -23.222516588355 -3.178732506188
## [189] 11.627894815320 -14.166696492927 -23.573178969266 -16.712264619195
## [193] -3.500817565471 -2.287088252289 16.766319271840 -23.708714212538
## [197] -9.422408545042 -11.970675081676 -22.615176255222 -16.624425616365
## [201] -23.323523244824 -7.226763792140 0.855338489135 -26.427184894733
## [205] -14.571802584416 4.611718454525 -26.725326023575 5.610959964386
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## [997] -22.261248768625 -40.563282335631 4.506577754392 -2.820231411514
```

- Repeat this exercise by resetting the seed to ensure you obtain the same results.

```
set.seed(3)
v = rnorm(1000, mean = -10, sd = 10)
v
```

```
## [1] -19.619334159199 -12.925257228785 -7.412117837587 -21.521318859151
## [5] -8.042171737136 -9.698760553984 -9.145822683877 1.166102127153
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## [897] -3.400403025122 -18.382010761344 -6.053109403551 -13.796259943018
## [901] 10.667798958086 -20.297497694303 -11.230955037009 -8.260422933721
## [905] -4.468093996811 -17.590686777527 -9.641704059606 -10.034950627904
## [909] -12.201904159497 -25.576802463945 -12.380459555889 -5.750175183680
## [913] -14.467797149752 -24.018547804707 -15.474142566073 -7.520582310342
## [917] -23.517025392188 2.853746702425 10.966329943241 -20.757166707862
## [921] -3.561814448109 -1.888929140086 -13.733691622783 -11.177557024666
## [925] -0.604906994514 -12.235444861136 -21.888657515816 -4.000388370744
## [929] -18.633060179970 -16.691361117331 -2.419190873591 -0.227876773458
## [933] 4.869604274728 -1.908179766512 0.495912980797 -23.783173148779
## [937] -21.663797316684 -5.494683374552 -4.460132607085 -8.284662147239
## [941] -18.068814703931 -0.211471217982 1.710354977120 -12.547509988794
## [945] -12.617794736045 3.570085370016 0.481954276737 12.288984855557
## [949] -24.705188119154 -20.312500413812 -8.351864725618 -22.438381562496
## [953] -8.836918261815 1.975473701615 -16.981309875727 -7.063950518001
## [957] -5.627022561804 -3.722374274922 -21.605435144943 -10.207884184738
## [961] 0.447240893840 3.115945847123 -10.824390282046 -0.807752382709
## [965] -12.432699212984 -6.489056233583 -23.403841721078 -5.741539055199
## [969] -18.143537334408 -3.066259193262 -2.944554440704 -7.216494611977
## [973] -22.026921419860 -3.572381826061 -16.059739450465 -23.772576133374
## [977] -19.259926871761 -4.327561431147 15.954812602946 -12.399845474462
## [981] -3.124635989125 -11.517889862396 -7.724557399724 -16.686480380507
## [985] -9.691709334165 -9.715704423793 -13.654550736339 -32.080121952053
## [989] -7.029605727864 11.297006585474 3.250411425943 -11.161714466792
## [993] -24.701462210519 -13.792718345032 -24.650059312925 0.751482628703
## [997] -22.261248768625 -40.563282335631 4.506577754392 -2.820231411514

```

- Find the average of v and the standard error of v .

```
mean (v)
```

```
## [1] -9.9360346452
```

```
sd(v)/sqrt(length(v))
```

```
## [1] 0.31561915962
```

- Find the 5%ile of `v` and use the `qnorm` function to compute what it theoretically should be. Is the estimate about what is expected by theory?

```
quantile(v,0.05)
```

```
##           5%
```

```
## -25.753712238
```

- What is the percentile of `v` that corresponds to the value 0? What should it be theoretically? Is the estimate about what is expected by theory?

```
ecdf(v)(0)
```

```
## [1] 0.839
```