1.) Given grammar:

$S \rightarrow \langle A \rangle a \langle B \rangle b$

$\langle A \rangle \rightarrow \langle A \rangle b \mid b$

$\langle B \rangle \rightarrow a \langle B \rangle \mid a$

a.) baab

$S \rightarrow \langle A \rangle a \langle B \rangle b$
$\rightarrow ba \langle B \rangle b$
$\rightarrow baab$

Valid Sentence

b.) bbbab

$S \rightarrow \langle A \rangle a \langle B \rangle b$
$\rightarrow \langle A \rangle ba \langle B \rangle b$ X won't work bc of $\langle B \rangle$

$S \rightarrow \langle A \rangle a \langle B \rangle b$
$\rightarrow ba \langle B \rangle b$ X won't work bc only one 'b' @ start

Invalid

c.) bbaaaaaa

- This is invalid since the sentences in this grammar must end in a 'b'.

d.) bbaab

$S \rightarrow \langle A \rangle a \langle B \rangle b$
$\rightarrow \langle A \rangle ba \langle B \rangle b$
$\rightarrow bba \langle B \rangle b$
$\rightarrow bbaab$

Valid Sentence

2.) Tokens for grammar: <assign> → <id> = <expr>
<id> → A | B | C
<expr> → <id> + <expr> | <id> * <expr>
| (<expr>) | <id>

Tokens	
Identifiers	A, B, C
Operators	=, +, *
Parantheses	(,)

3.) B = B + (C + (A * A))

<assign> → <id> = <expr>

<id> = <expr>

B = <expr>

B = <id> + <expr>

B = B + <expr>

B = B + (<expr>)

B = B + (<id> + <expr>)

B = B + (C + <expr>)

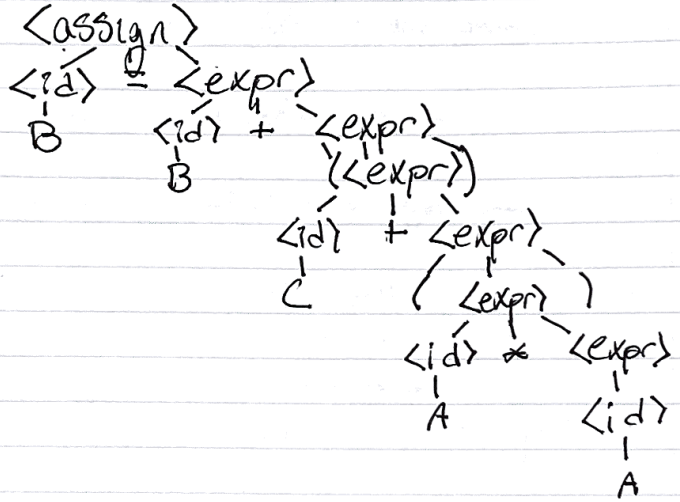
B = B + (C + (<expr>))

B = B + (C + (<id> * <expr>))

B = B + (C + (A * <expr>))

B = B + (C + (A * <id>))

B = B + (C + (A * A))



4.) Given: $S \to Aa \mid Bb$
$A \to Aa \mid AbC \mid C$
$B \to S \mid bb$
$C \to c$

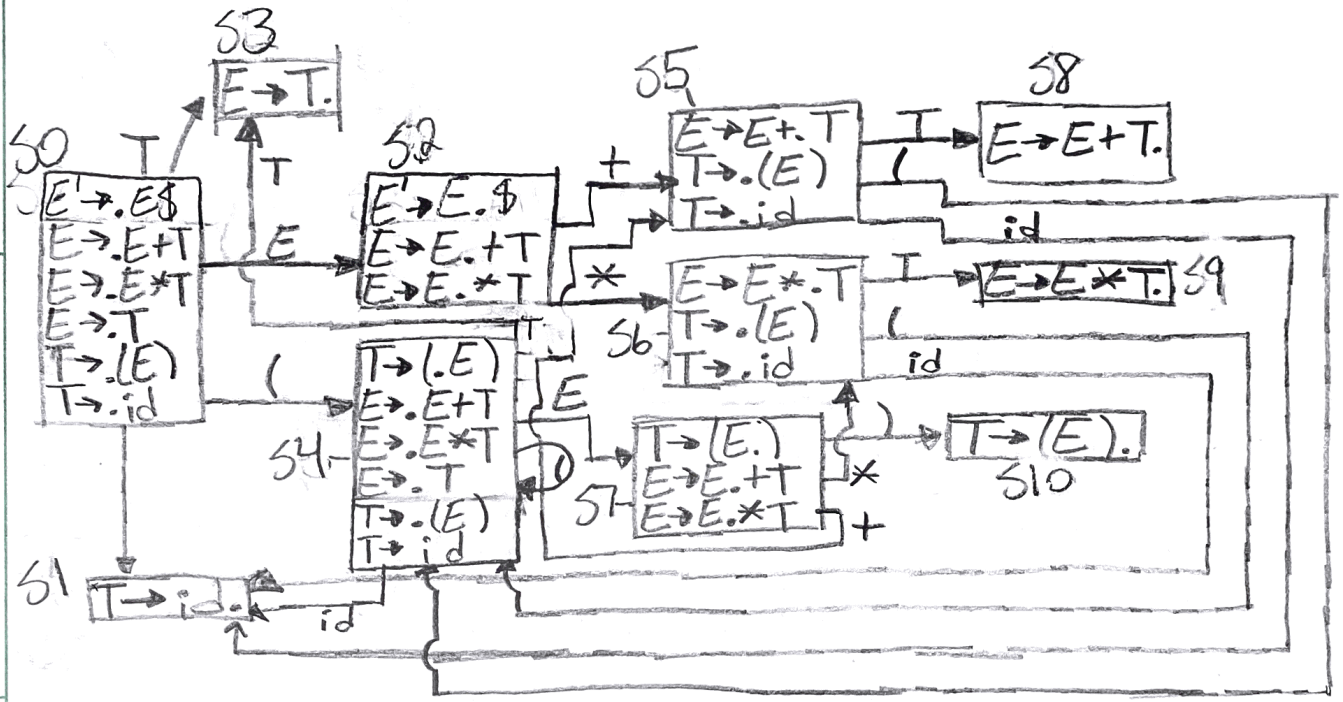
- Let's remove indirect recursion: $S \to Aa \mid Sb \mid bbb$
$A \to Aa \mid AbC \mid C$
$C \to c$

- Now apply rules: $S \to bS' \mid \varepsilon$
$S' \to AaS' \mid bbbS'$
$A \to aA' \mid bCA' \mid \varepsilon$
$A' \to CA'$
$C \to c$

5.) $A \to aBc \mid ac \mid a$
$A \to a \langle new \rangle c$
$\langle new \rangle \to \varepsilon$
$\langle new \rangle \to B$

$B \to b \mid aB$
$B \to a \langle new \rangle$
$\langle new \rangle \to \varepsilon$
$\langle new \rangle \to B$

6) r1: E → E+T
r2: E → E*T
r3: E → T
r4: T → (E)
r5: T → id



6.) Transition Table

	+	*	(	)	id	E	T
0			4		1	2	3
1							
2	5	6					
3							
4						7	3
5			4		1		8
6			4		1		9
7	5	6		10			
8							
9							
10							

6) Parse Table

	Action					GoTo	
	+	*	(	)	id	E	T
0			s4		s1	2	3
1	r5	r5	r5	r5	r5		
2	s5	s6					
3	r3	r3	r3	r3	r3		
4			s4		s1	7	3
5			s4		s1		8
6			s4		s1		9
7	s5	s6		s10			
8	r1	r1	r1	r1	r1		
9	r2	r2	r2	r2	r2		
10	r4	r4	r4	r4	r4		

r1: E → E+T
r2: E → E*T
r3: E → T
r4: T → (E)
r5: T → id

* If given a '$' in state 2, then ~~accept~~

7.) Bottom-Up parse for: (id + id) * id

r1: E → E + T
r2: E → E * T
r3: E → T
r4: T → (E)
r5: T → id

Start

input: .(id + id) * id $
Stack: 0
Output:

input: (.id + id) * id $
Stack: 0(4
Output:

input: (id. + id) * id $
Stack: 0(4 id
output:

input: (id.+ id) * id $
Stack: 0(4 id 1
Output:

input: (id. + id) * id $
Stack: 0(4T
output: 5,

input: (id. + id)* id $
Stack: 0(4T3
Output: 5,

input: (id.+id)* id $
Stack: 0(4E
output: 5,3,

input: (id.+id)* id $
Stack: 0(4E7
output: 5,3,

input: (id +.id) * id $
Stack: 0(4E7+
output: 5,3,

input: (id +. id) * id $
Stack: 0(4E7+5
Output: 5,3

input: (id + id.) * id $
Stack: 0(4E7+5 id
output: 5,3

input: (id + id.) * id $
Stack: 0(4E7+5T
output: 5,3,5

input: (id + id.) * id $
Stack: 0(4E7+5T8
output: 5,3,5

input: (id + id).* id $
Stack: 0(4E
output: 5,3,5,1

7.) Cont.

input: (id + id) * id $
Stack: 0(4E7

Output: 5, 3, 5, 1

input : (id + id). * id $
Stack: 0(4E7)

output: 5, 3, 5, 1

input : (id + id). * id $
Stack: 0(4E7) 10

output : 5, 3, 5, 1

input: (id + id). * id $
Stack : 0T

Output: 5, 3, 5, 1, 4

input : (id + id). * id $
Stack : 0T3

Output: 5, 3, 5, 1, 4

input: (id + id). * id $
Stack: 0E

Output: 5, 3, 5, 1, 4, 3

input : (id + id). * id $
Stack: 0E2

output: 5, 3, 5, 1, 4, 3

input : (id + id) * . id $
Stack: 0E2*

output: 5, 3, 5, 1, 4, 3

input: (id + id) * . id $
Stack: 0E2*6

output : 5, 3, 5, 1, 4, 3

input : (id + id) * id. $
Stack : 0E2*6 id

Output: 5, 3, 5, 1, 4, 3

input : (id + id) * id. $
Stack : 0E2*6 id 1

output:

input : (id + id) * id. $
Stack : 0E2*6T

output: 5, 3, 5, 1, 4, 3, 5

input : (id + id) * id. $
Stack : 0E2*6T9

output: 5, 3, 5, 1, 4, 3, 5

input : (id + id) * id. $
Stack : 0E

output : 5, 3, 5, 1, 4, 3, 5, 2

input : (id + id) * id $.
Stack : 0E2$

Output: 5, 3, 5, 1, 4, 3, 5, 2

Accept

8.) Rightmost Derivation for (id + id) * id

output: 5, 3, 5, 1, 4, 3, 5, 2

$E \rightarrow E * T$ by r2
$\rightarrow E * id$ by r5
$\rightarrow T * id$ by r3
$\rightarrow (E) * id$ by r4
$\rightarrow (E + T) * id$ by r1
$\rightarrow (E + id) * id$ by r5
$\rightarrow (T + id) * id$ by r3
$\rightarrow (id + id) * id$ by r5

The output from 7.) shows an equivalent output to the way we produced the rightmost derivation, just in reverse order, which means the output correctly finds all the handles.