MA-240 Homework Questions

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- **2.1** Prove that if f(c) = 0, then y = c is a solution to y' = f(y), also known as the "Equilibrium Solution".
- **4.1** Let F be a set of functions. Prove that if $0 \in F$, than F is linearly dependent.
- **4.1** Let F be a set of functions. Prove that $F = \{f_1, f_2\}$ is linearly dependend if and only if $f_1 = kf_2$.
- **4.1.3** Prove that if

$$y_{p_j}$$
 solves $\sum_{i=0}^{n} a_i(x) y_i^{(i)} = g_j(x)$ for $j = 1, 2, \dots, m$

then

$$\sum_{j=1}^{m} y_{p_j} \text{ solves } \sum_{i=0}^{n} a_i(x) y_i^{(i)} = \sum_{j=1}^{m} g_j(x)$$

- **4.6** Show that using c = 0 leads to the same answer for y.
- **4.7** For the cases where there is one solution for m, and for the case where m has imaginary solutions, check that $W(y_1, y_2) \neq 0$ on the interval.