

Results: [20, 35] Crossings

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The same CNN and ViT used in our initial study were fine-tuned on a new dataset \mathcal{D} , where:

$$\mathcal{D} = \mathcal{D}_{\text{train}} \cup \mathcal{D}_{\text{val}} \cup \mathcal{D}_{\text{test}},$$

$$|\mathcal{D}| = 560,000 \text{ diagrams},$$

$$|\mathcal{D}_{\text{train}}| = 448,000 \text{ diagrams},$$

$$|\mathcal{D}_{\text{val}}| = |\mathcal{D}_{\text{test}}| = 56,000 \text{ diagrams}.$$

Each split included knots with n crossings, where $n \in \{20, 21, \dots, 35\}$. For every n , the number of diagrams per split was identical, with an equal number of unknots and non-trivial knots.

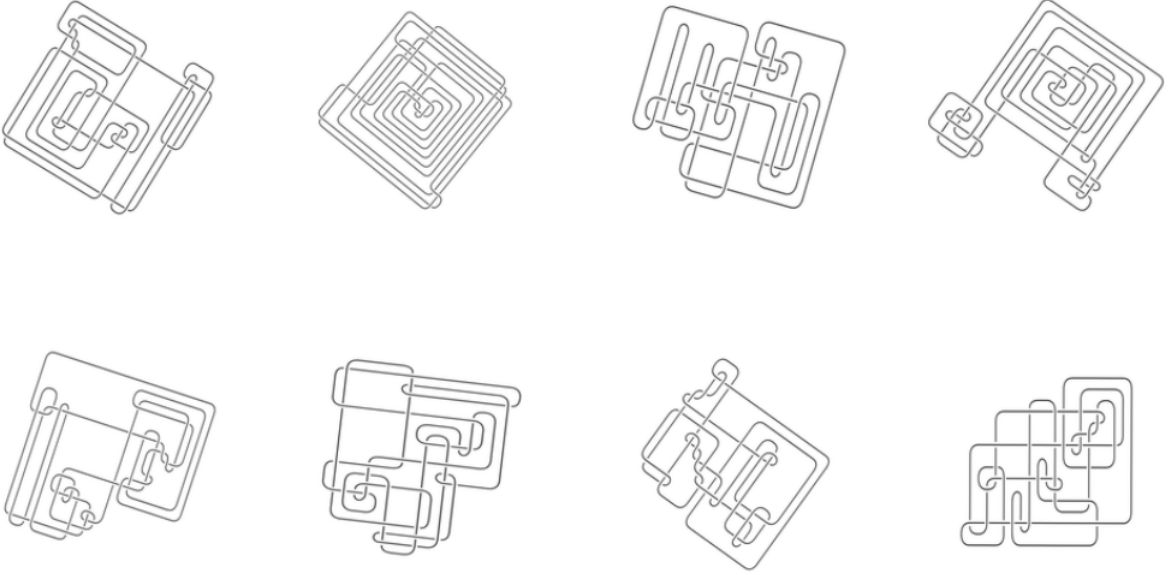


Figure 1: 35-crossing unknots (top row) and non-trivial knots (bottom row) in $\mathcal{D}_{\text{test}}$.

CNN Results

CNN TP: True Unknots Predicted as Unknots

CNN FN: True Unknots Predicted as Knots

CNN TN: True Knots Predicted as Knots

CNN FP: True Knots Predicted as Unknots

ViT Results

ViT TP: True Unknots Predicted as Unknots

ViT FN: True Unknots Predicted as Knots

ViT TN: True Knots Predicted as Knots

ViT FP: True Knots Predicted as Unknots