Predication and Speculation

Compilers for High Performance Computers

Stefano Petrilli stefano.petrilli@upc.edu Jakob Eberhardt

jakob.eberhardt@estudiantat.upc.edu

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1 Introduction

Superscalar processors with deep pipelines and out-of-order execution represent the state of the art in processor architecture.

Superscalar processors have multiple execution unit which allows them to fetch, decode, and execute multiple instructions in parallel through separate pipeline stages within a single clock cycle. This increases the instructions throughput and allows for an Instructions Per Cycle (IPC) count that is greater than 1. The latest main vendor's architectures, AMD Zen5 and Intel Alder Lake, feature cores that are respectively 8 and 6 instructions wide.

When talking about deep pipelines, we refer to the number of stages that the instructions have to go through from the fetch to the moment they are retired. High performance design employ different pipelines for different classes of instructions. For both the last generation of AMD and Intel desktop processors, the depth of the integer pipeline is estimated to be 19 stages.

When talking about Out of Order Execution, we refer to architecture design where instructions can be executed as soon as their input operands are ready, rather than strictly in the original program order. By executing instructions out of order, the processor can keep its execution units busy even when some instructions are stalled due to delays like cache misses or data dependencies.

These design choices proved to deliver unmatched performances when provided with enough Instruction Level Parallelism (ILP). Based on the work of August et al. [1], the main obstacles to high ILP are difficult to predict control flows and ambiguous memory dependencies.

1.1 The cost of branch misprediction

The reason why branch mispredictions represent a big obstacle for modern machines has to do with the design choices described so far.

Another central component of modern designs are branch predictors. Branch predictors allow for one side of conditional branches to be speculatively executed before the branch is evaluated. When the speculated side and the evaluated side coincide, we have the benefit of keeping the pipeline full and executing instructions ahead of time. When these speculations fail, tough, the instructions speculatively executed will need to be discarded and the right side will need to be executed. Due to out of order execution, between the time the branch is speculatively executed and the time it is evaluated, a high number of instruction might have been retired. In addition to this, as the pipelines are deep, several cycles have to pass before the pipeline is filled again and start retiring new instruction. Based on the work of Kwan Lin et al. [6], branch misprediction account for 20% of the IPC in modern processor and is representing the main limit to having deeper, more efficient pipelines. A good empirical average measure of the cost of a branch misprediction comes from the weight used in the heuristics of llvm [5].

Architecture	Misprediction	Optimistic
	Penalty	Load Cost
Sapphire Rapids	14	5
Alder Lake-P	14	5
Ice Lake	14	5
Broadwell	16	5
Haswell	16	5
Cortex A57	14	4
Cortex R52	8	1
Cortex M4	2	2

Table 1: Branch Misprediction Penalty and Optimistic Load Cost used in *llvm*'s heuristics for various Intel and ARM architectures.

From the weight used in *llvm* for both branch misprediction and optimistic load cost reported in Table 1, we can conclude that a branch misprediction, in a modern high performance architecture, is three times more expensive than a load operation that hits the L1 cache. Certain design choices peculiar to the embedded field make the cost of branch misprediction higher or lower. The data regarding Cortex R52 and Cortex M4 have been cherry-picked precisely to describe this. The Cortex R52 is a design that implements advanced safety features like lockstep redundancy which introduces further overhead in case of misprediction. Due to these characteristics, it has a misprediction penalty to load cost ratio of 8:1. Cortex M4 is also an embedded processor but has a 3 stages pipeline and execute instructions in order. This results in a ratio of branch misprediction cost to load cost of 1:1. The way the weights reported are used by the compiler's heuristics are treated in more detail in Sections ??, ?? and ??.

1.2 Compilation techniques to improve IPC

Two techniques have been introduced into compilers to try to mitigate the obstacles to high IPC described so far:

- Speculation: Is a technique where the compiler makes assumptions about the program's behavior to generate optimized code paths, potentially executing certain operations early or avoiding them entirely. If the speculated outcomes are incorrect at runtime, mechanisms like rollback or patching are used to maintain correctness. This has not to be confused with branch speculation, which is executed at the architectural level with the aid of the branch predictor.
- **Predication**: Instead of using conditional branches to decide which instructions to execute, predicated instructions execute all possible paths but only commit the results of the path that meets a specific condition, known as the predicate. This is only possible when the Instruction Set Architecture (ISA) supports predicated instructions.

We discuss in more detail how Speculation and Predication help delivery higher performances respectively in Section 2 and in Section 3. Additionally, we discuss in Section 4 how these techniques can be combined to achieve even greater benefit in Section 3

2 Speculation

Whenever we move an instruction above a branch it is control-flow dependent on, we consider this instruction to be *speculatively* executed [3]. When speculating during compilation, we typically try to tailor the control-flow of the program towards the actual behavior we expect during runtime. The most common types of speculations include loads, computations and stores. While these may increase performance in certain cases, they each come with considerations and hazards one has to be aware of. In this section, we will study the concepts and heuristics behind speculative execution.

2.1 Example

```
if (x > 0) {
    y = array[x];
}
```

Listing 1: Setting the value of y depends on x being positive.

```
LDR r3, [r0]
CMP r3, #0
BLE skip_load_and_store
LDR r1, [r2, r3, LSL #2]
STR r1, [r4]
skip_load_and_store:
```

Listing 3: Once we know the branch is not taken, we issue a load of data[x] into r1

```
int temp = array[x];
if (x > 0) {
    y = temp;
}
```

Listing 2: We can speculatively load the value of array[x] into a additional variable.

```
LDR r3, [r0]
LDR r1, [r2, r3, LSL #2]
CMP r3, #0
BLE skip_store
STR r1, [r4]
skip_store:
```

Listing 4: We immediately issue a load for data[x], even tough we do not know yet if it will be needed.

2.2 Superblock Structure

If we consider the control flow of a program, a superblock [7] is a consecutive sequence of instruction which is always entered at the top-most basic block but may be left at arbitrary and multiple points. When forming superblock, we try to anticipate the future control flow of the program during run time by either profiling it with synthetic data or other means [4]. An example of how the profile of a loop execution may look like can be seen in figure 1. Note that most iterations consist of BB2, BB3 and BB5. Blocks which are frequently executed together are also called traces. To create a superblock from this trace, we need to remove the side entrance from BB4 to BB5 and hence to the trace section. Typically, this done with tail duplication. In this case, we need to add BB5' to remove the side entrance, as can be seen in figure 2. By forming superblocks, we can avoid bookkeeping complexity which typically arises during trace scheduling when we move instructions across side entrances. Note that also BB4 and BB5' now form a superblock. Superblocks are not exclusively tools of speculation, rather they are also important for enabling other optimizations in compilers.

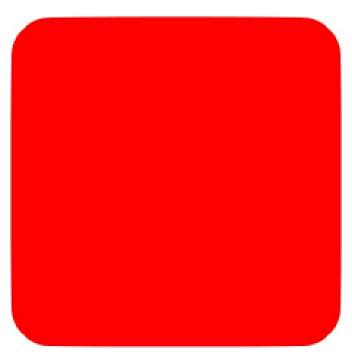
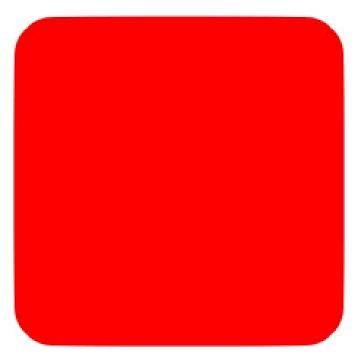


Figure 1: Trace with Side Entrance
The edge from BB4 to BB5 is a so-called side entrance into thew the most important trace consisting of BB2, BB3, and BB5.



 $\label{eq:Figure 2: Superblock Example} In this example, we removed the side entrance into the trace by duplicating BB5 (BB5') for the case where BB2 is branching to BB4.$

2.3 Superblock Scheduling

After the trace selection and the formation of superblocks, the compiler has to schedule the instructions with the goal of enabling as much ILP as possible and the constraint of producing a save and correct program. This is done by building a graph which represents the dependencies among the instructions. The dependency graph is used during and a subsequent list scheduling. The compiler may use heuristics and given instruction latencies to assign priorities to instructions which are *ready* to produce a schedule which will use the available resources as efficient as possible [3]. To this end, the compiler needs to be able to move instructions above previous branches which is considered a speculation.

2.4 Speculative Code Motion Models

In many cases, higher performance can be achieved by moving certain instructions either down or upward. However, in both cases we have to retain the correctness of the original program. A variable or register is called *live* if it holds a value that will be needed by other instructions. For branching instructions, we can define live-out(Br) as the set of variables which may be used before being defined in case Br will be taken. Downward code motion, meaning moving a instruction I beneath a later instruction Br can always be applied if Br is not dependent on the result of I. In case the destination register of I is in live-out(Br), we have to insert a copy of I between Br and its target to insure correctness, as can be seen in listing 5

```
LDR r1, [R2]

CMP r3, #0

BEQ Target

ADD r4, r1, r5

; ...

Target:

SUB r6, r1, r7
```

Listing 5: Since r1 is needed in the branch target of the BEQ instruction, live-out(BEQ) contains r1.

```
CMP r3, #0
BEQ Target
LDR r1, [R2]
ADD r4, r1, r5
; ...
Target:
LDR r1, [r2]
SUB r6, r1, r7
```

Listing 6: We can delay the LDR instruction by moving it downward. However, in case the BEQ-branch is taken, we need to load the correct value using a copy of the LDR instruction.

Although downward motion can be easily done, the cases where we will gain performance are limited. Moving an instruction from a point after a branch to a point before the branch is refereed to as upward motion. Typically, one may try to schedule long-latency instructions early to reduce the critical path, for example in a superblock. Similar to other architectures, the division instruction SDIV is a example of such a long-latency instruction. As can be seen in listing 7, depending on the input data, we may have to execute SDIV. Therefore it would we preferable to speculatively execute the division as can be seen in listing 8. However, the destination of SDIV (r1) is in live-out(BEQ) if it is taken, hence the speculation would alter the result if the compiler does not introduce compensation code, e.g. a copy of r1 for the taken case. Additionally, SDIV may cause an exception since it was moved above the branch which checks the loaded value in r1 to be zero.

```
LDR r1, [address]

CMP r1, #0

BEQ taken

SDIV r1, #5, r1

B end

taken:

ADD r1, r1, #2

end:
```

Listing 7: Depending on the input data, we may have to execute a division which typically takes many cycles in most architectures.

```
LDR r1, [address2]

SDIV r1, #5, r1

CMP r1, #0

BEQ taken

B end
taken:

ADD r1, r1, #2
end:
```

Listing 8: The long-latency division was naively moved upwards. Depending on the input data, the program will now compute wrong results, because the destination register of the speculatively executed division r1 is in live-out(BEQ). In addition, SDIV may cause a unnecessary a divide-by-zero exception.

Restriction 1: The destination register of I is not part of live-out(Br). Hence, the result of I is not used before it is redefined when the branch was taken.

Restriction 2: Instruction I will not cause an exception which will alter the program execution if Br was taken.

Restricted Percolation is a conservative code motion technique where the compiler moves instructions across basic blocks or control-flow boundaries under strict safety conditions. Instructions are only moved when it is guaranteed that such movement will not alter the program's observable behavior. Minimal or no speculation is involved, and the movement is based on provable safety. The technique strictly respects data dependencies (ensuring that an instruction's operands are ready) and control dependencies (ensuring the instruction is only executed when it should be).

3 Predication

For the reasons outlined in Section 1.1, we can conclude that branches are expensive. Even when using state of the art branch predictors, certain branches are systematically hard to predict or have such low occurrences that not enough data are collected to perform a good prediction [6]. Predication is used to replace conditional branches with other instructions. In LLVM and in GCC, this is usually done during the backend optimization phase where the compiler works on the machine level representation of the code. The name that is generally given to this code optimization pass is if-conversion.

Figure 3: Replacing a conditional branch with arithmetic operations.

An example of this is presented in Figure 3 where code containing a conditional branch is replaced with code that performs exactly the same operation without the use of conditional branches. The example presented uses arithmetic properties to replace the branch and is usually referred to as **Arithmetic Predication** or **Branchless Programming**. Using Arithmetic Predication to replace branches presents limitations: multiplications are also expensive, and it's difficult to apply most of the time.

One way to overcome these limitations is by utilizing predicated instructions supported by the architecture, when these are available. A predicated instruction in ARMv7 is an

instruction which attaches conditions directly to instructions, allowing them to either execute or skip based on the condition's outcome.

```
MOV RO, R1 2 MOVGT RO, R1
```

Listing 9: Standard MOV in ARMv7 assembly

Listing 10: Predicated MOV in ARMv7 assembly

The ARMv7 architecture supports several predicated instructions. For example, the standard MOV instructions in Listing 3 takes the value in R1 and moves it into R0 while, the predicated version, MOVGT, showed in Listing 3 moves the value in R1 to R0 only when the last comparison was "greater than".

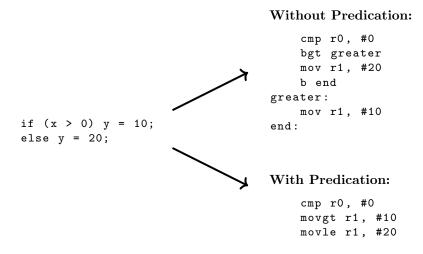


Figure 4: Branching versus predication in ARM assembly

In Figure 4 two assembly translation of the code in Figure 3 are displayed. The top one is when no predication is used, while the bottom one uses predicated instructions. By comparing the two versions in Figure 4, the benefits of predication are staggering. The code size is reduced from 5 instructions to 3, while removing one conditional branch and one unconditional branch. Another benefit that is outlined by this example is **Deterministic Execution**. It's difficult to predict how many cycles an assembly code needs to be executed when branch predictions and other form of speculations are involved. As we removed all the branches and as we have no memory accesses in our snippet of code, we can determine exactly how long it's going to take to execute the operation. Deterministic Execution is crucial in certain fields where software needs to have a predictable behavior and respond within strict timing constraints. This is necessary for instance in flight control systems, in medical devices and other mission-critical software. Section 3.1 focuses on a more in depth analysis of how ARMv7 and IA64 architectures introduce support for predication.

It's also necessary to mention some limitations of predication.

- Increased Instruction Executions: predication can lead to unnecessary execution of both paths in a conditional statement. In certain cases this may lead to a very inefficient use of the CPU and to wasting several cycles. This is particularly true when the predicated code has long conditional chains.
- **Higher register pressure**: as we might need to hold intermediate results in registers, the register pressure increases. Registers are a highly contented resource, and allocating them efficiently is a difficult problem in compilers [2]. If the increased pressure introduced by predication results in spilling to memory, performance degradation is to be expected.

• Code Size: While the example presented, demonstrates how predication can result in code size reduction, this is not necessary the case. In fact, as a more complex control flow is taken into account, code size is more likely to increment.

For these reasons, if predication is applied in discriminately, performance regression happen. Production compilers like LLVM and GCC use heuristics to decide at compile time whether predication is beneficial or not. In Subsection 3.3 we will treat this in more detail reporting and analyzing some of these heuristics.

Finding whether predication is applicable is per se a challenge. The logic that *LLVM* uses to find basic blocks where predication is applicable is reported in Subsection 3.2.

Finally, in Subsection 3.5, a series of micro benchmarks will be proposed to showcase in which cases and what impact predication has.

3.1 How is predication achieved in the architecture

Various ways to support predication at ISA level have been developed.

In the case of ARMv7, predication is achieved through condition flags in the *Program Status Register* (PSR) and the instruction's condition field, This is a special register used to set various bits which describe the execution state, among these bits, there are the Zero (Z), Negative (N), Carry (C), and Overflow (V) bits which are set whenever an arithmetic instruction is executed. When the CPU encounters a predicated instruction, it evaluates the condition field against the current PSR flags. If the condition is met, the instruction executes; otherwise, it is treated as a no-op.

	Condition GT: 1100	Opcode MOV: 1101	S 0	Rn 0000	Rd Dest	Operand2	Pad
0	ļ	1 1	I I 8 9	1	1 3	I 17	I 29 3
ſ	Condition	Opcode	S	Rn	Rd	Operand2	Pad
	AL: 1110	MOV: 1101	0	0000	Dest		
	AL: 1110		U I I 8 9		Dest 1 3] 1 29 3

Figure 5: Bit-level encoding of ARMv7's MOVGT (on top) and of MOV (on the bottom) instructions, illustrating fields for condition codes, opcode, status bit, register operands, and operand values.

In Figure 5 we can observe how MOV and MOVG bit encoding only differ for the first 4 bits. The condition field in ARMv7 applies to almost all instructions. In ARM's architecture, most instructions have a 4-bit condition field. This makes non predicated instructions a particular case of predication where the condition field is set to 1110.

Another architecture design that offer predication support is the Itanium IA-64. The IA-64 has 64 predicate registers (p0 to 63) that allow each instruction to be conditionally executed based on specific predicate values. Each instruction can specify a predicate register, offering highly granular control over conditional execution. Thanks to this approach, entire sections of code can be totally predicated, minimizing the dependency on branch predictors.

Listing 11: Predicated MOV in Itanium

In Listing 11, it's possible to see the IA-64 equivalent of the assembly code showed in Listing 4.

3.2 Detecting Predicable Regions

Some operations are difficult to predicate. Interruption, Exceptions and System Calls have side effects that expand beyond the local execution and might trigger events that are impossible to revert. Certain Control Flow Instructions like jmp and call alter the program's execution path, predicating this requires hardware to simulate both the taken and non-taken paths simultaneously. Additionally, predicating large blocks results in executing many unnecessary instructions when the predicate is false. The performance penalty of executing unnecessary instructions outweighs the benefit of avoiding a branch. A set of basic block is therefore considered not predicable if it exceeds certain sizes.

The discovery of predicable regions is the beginning of the if-conversion step. This optimization pass starts by iterating through all the basic blocks in a function's control flow graph (CFG).

```
/// Analyze the structure of the sub-CFG starting from the specified block.
  /// Record its successors and whether it looks like an if-conversion candidate
  void IfConverter::AnalyzeBlock(
      MachineBasicBlock &MBB, std::vector<std::unique_ptr<IfcvtToken>> &Tokens)
    // Initialize stack with the starting block.
    SmallVector < MachineBasicBlock *, 16 > BBStack = {&MBB};
6
    while (!BBStack.empty()) {
      MachineBasicBlock *BB = BBStack.pop_back_val();
9
      BBInfo &BBI = BBAnalysis[BB->getNumber()];
11
      // Skip blocks already analyzed.
      if (BBI.IsAnalyzed)
13
         continue;
14
16
      // Analyze branches and instructions in the block.
      AnalyzeBranches(BBI);
17
18
      ScanInstructions(BBI, BB->begin(), BB->end());
19
      // Skip blocks unsuitable for if-conversion.
20
      if (!BBI.IsBrAnalyzable || BBI.BrCond.empty()) {
        BBI.IsAnalyzed = true;
23
         continue;
24
25
      // Push successors for further analysis.
26
      if (BBI.TrueBB && BBI.FalseBB) {
27
        BBStack.push_back(BBI.TrueBB);
28
29
        BBStack.push_back(BBI.FalseBB);
30
31
      // Check for if-conversion patterns (e.g., diamonds, triangles).
32
      if (ValidDiamond(BBI)) {
33
        {\tt Tokens.push\_back(std::make\_unique < IfcvtToken > (BBI, ICDiamond));}
34
35
        else if (ValidTriangle(BBI)) {
        Tokens.push_back(std::make_unique < IfcvtToken > (BBI, ICTriangle));
36
37
        else if (ValidSimple(BBI)) {
38
         Tokens.push_back(std::make_unique < IfcvtToken > (BBI, ICSimple));
39
40
      BBI. Is Analyzed = true;
41
    }
42
  }
```

Figure 6: Simplified version of *LLVM*'s AnalyzeBlock implementation for ARM architectures.

For each block, the function AnalyzeBlock is called. A simplified version of this function is shown in Listing 6.

A Machine Basic Block is a basic block after being translated to machine instructions. This function analyzes the structure of a sub-CFG starting from a given Machine Basic Block. It evaluates branches and records successors to determine if the block is suitable for if-conversion. The function Analyze Branches, determines if its branches can be analyzed or reversed, and checks if it has fall-through behavior. The data collected when this function runs are then stored in the Machine Basic Block struct and used later. The function Scan Instruction scans all the instructions in the block to determine if the block is predicable. In most cases, a block is predicable if all the instructions in the block are predicable. When this analysis grants that the current basic block is predicable, the function verifies if common predication patterns exists with other basic blocks. The common predication patterns are described in Subsection 3.4

The analysis, described so far, finds a set of basic blocks that are predicable and calculate

the penalty for predication. if there is one.

3.3 Compiler's Heuristics

As already showed in Section 3, predication is versatile and can bring different advantages depending on the situation, at the same time, if applied without caution, it can result in performance degradation. In order to decide whether to use this technique or not, modern compilers apply heuristics. These heuristics are highly architecture dependent (as Table 1 points out). In the rest of this section, the heuristics used by the production state of the art compiler *LLVM* are analyzed.

Knowing that a set of blocks, once predicated, will take a higher amount of cycles to execute is not enough to rule out predication. Two more factors have to be taken into account. The cost of misprediction and the code size.

Another crucial information that is calculated in ScanInstruction is whether there is an additional cost to pay when predicating the Basic Block being analyzed. The logic used to do so is reported in Listing 7

```
BBI.NonPredSize++;
unsigned ExtraPredCost = TII->getPredicationCost(MI);
unsigned NumCycles = SchedModel.computeInstrLatency(&MI, false);
if (NumCycles > 1)
BBI.ExtraCost += NumCycles-1;
BBI.ExtraCost2 += ExtraPredCost;
```

Figure 7: Portion of code where the cost of predicating a Basic Block is calculated in LLVM.

The cost of predicating a Basic Block consists of two components: architecture-dependent predication cost and instruction latency. These costs vary based on the specific instruction and the architecture. Some architectures impose a fixed cost for predicating any instruction, while others either avoid this cost entirely or apply it selectively to certain instructions. Taking as reference the ARMv7 architecture, calls have an additional latency of 1 cycle to be predicated, while predicating any other instruction does not introduce any other cost.

```
bool ARMBaseInstrInfo::
  isProfitableToIfCvt(MachineBasicBlock &TBB,
                       unsigned TCycles, unsigned TExtra,
                       {\tt MachineBasicBlock} &FBB,
                       unsigned FCycles, unsigned FExtra,
                       BranchProbability Probability) const {
    if (!TCycles)
      return false;
10
    // Attempt to estimate the relative costs of predication versus branching.
    // Here we scale up each component of UnpredCost to avoid precision issue
11
        when
    // scaling TCycles/FCycles by Probability.
12
    const unsigned ScalingUpFactor = 1024;
13
14
    unsigned PredCost = (TCycles + FCycles + TExtra + FExtra) * ScalingUpFactor;
15
    unsigned UnpredCost;
16
17
    if (!Subtarget.hasBranchPredictor()) {
      // This code block contains the case where a pranch predictor
18
19
      \ensuremath{//} is not available. For the sake of brevity is not reported
    } else {
20
      unsigned TUnpredCost = Probability.scale(TCycles * ScalingUpFactor);
21
      unsigned FUnpredCost =
23
        Probability.getCompl().scale(FCycles * ScalingUpFactor);
      UnpredCost = TUnpredCost + FUnpredCost;
24
25
      UnpredCost += 1 * ScalingUpFactor; // The branch itself
26
      UnpredCost += Subtarget.getMispredictionPenalty() * ScalingUpFactor / 10;
27
    return PredCost <= UnpredCost;</pre>
29
```

Figure 8: LLVM's isProfitableToIfCvt implementation for ARM architectures.

3.4 Common Predication Patterns

3.5 Predication Benchmarks

4 Predication and Speculation

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