

Graph  $G = (U \cup V, E)$ , want maximum matching  $M$

(1)

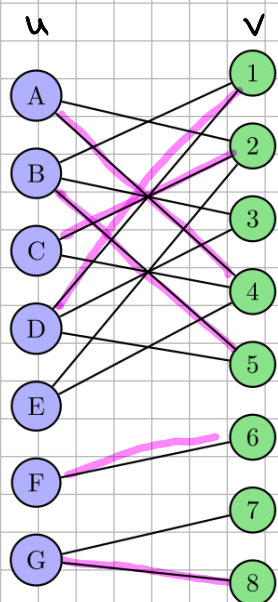
$x_{i,j}$  true if  $(i,j) \in M$

(2)

$$\min \sum_{(i,j) \in E} \bar{x}_{i,j}$$

s.t.  $\bar{x}_{i,j} + \bar{x}_{i,k} \geq 1$  for  $(i,j), (i,k) \in E$

e.g.  $\bar{x}_{B,1} + \bar{x}_{B,3} \geq 1$  (1)  
 $\bar{x}_{B,1} + \bar{x}_{B,5} \geq 1$  (2)  
 $\bar{x}_{B,3} + \bar{x}_{B,5} \geq 1$  (3)  
 $\bar{x}_{G,7} + \bar{x}_{G,8} \geq 1$  (4)



Rule

Annotation

Result

Lit

$$\bar{x}_{F,6}$$

$$\bar{x}_{F,6} \geq 0$$

(5)

Add

$$(1) + (2)$$

$$2\bar{x}_{B,1} + \bar{x}_{B,3} + \bar{x}_{B,5} \geq 2$$

(6)

Add

$$(6) + (3)$$

$$2\bar{x}_{B,1} + 2\bar{x}_{B,3} + 2\bar{x}_{B,5} \geq 3$$

(7)

Div

$$(7) / 2$$

$$\bar{x}_{B,1} + \bar{x}_{B,3} + \bar{x}_{B,5} \geq 2 \quad (\text{AMo-B})$$

(5)

derive similar to AMo-B

$$\bar{x}_{D,1} + \bar{x}_{D,3} + \bar{x}_{D,5} \geq 2 \quad (\text{AMo-D})$$

(5)

$$\bar{x}_{2,A} + \bar{x}_{2,C} + \bar{x}_{2,D} \geq 2 \quad (\text{AMo-2})$$

(5)

$$\bar{x}_{4,A} + \bar{x}_{4,C} + \bar{x}_{4,D} \geq 2 \quad (\text{AMo-4})$$

(5)

Dom

$$\omega = \{x_{F,6} \mapsto 1\}$$

$$x_{F,6} \geq 1$$

(6)

Red

$$\omega = \{x_{G,7} \mapsto x_{G,8}, x_{G,8} \mapsto x_{G,7}\}$$

$$\bar{x}_{G,7} + x_{G,8} \geq 1$$

(7)

Add

$$(\text{AMo-B}) + (\text{AMo-D}) + (\text{AMo-2}) + (\text{AMo-4}) + (4) + (5)$$

$$\sum_{(i,j) \in E} \bar{x}_{i,j} \geq 9 \quad (\text{from 15}) \quad (8)$$

(8)

Bound

Matching method (sets 6 variables to true)

$$\sum_{(i,j) \in E} x_{i,j} \geq 7$$

(3)

(3)

Add

$$(8) + (3)$$

$$0 \geq 1$$