

Business Analytics & Machine Learning

Tutorial sheet 1: Statistics

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Exercise T1.1 *Effect of tax on consumption*

The following table contains data of 10 individuals' consumption levels before and after a tax increase, measured by an index value. High index values correspond to high consumption levels. The rows represent individuals' identifiers i , their index values prior to the tax increase a_i , and after the tax increase b_i .

i	1	2	3	4	5	6	7	8	9	10
a_i	27	31	23	35	26	27	26	18	22	21
b_i	40	36	43	34	25	41	32	29	21	36
$d_i = a_i - b_i$	-13	-5	-20	1	1	-14	-6	-11	1	-15

- Perform a hypothesis test in order to find out whether there is a significant ($\alpha = 0.05$) difference between consumption levels prior to the tax increase and consumption levels after the tax increase. Assume, that the difference is normally distributed.
- Verify your result by applying `stats.ttest_rel()` in Python using the *SciPy* package.

Exercise T1.2 *Masks during Covid19*

In the context of the COVID-19 pandemic, 8 men and 10 women were asked how many hours per day they wear a mask. The following table shows their answers. The hypothesis is "On average, women wear their mask longer per day than men". It can be assumed, that the average time people wear their mask is normally distributed.

Individual no. (i)	1	2	3	4	5	6	7	8	9	10	11	12	13	14	15	16	17	18
Hours per day	4	2	3	5	7	2	7	3	5	2	2	1	5	3	1	3	2	3
Gender	f	f	f	f	f	f	f	f	f	f	m	m	m	m	m	m	m	m

- Test the hypothesis "by hand" with a significance level of $\alpha = 0.05$ and 16 degrees of freedom.
- Search for the corresponding functions in Python and use them to verify your result.

Exercise T1.3 *Research Methods*

You are a researcher investigating whether a new study technique improves the average test scores of students. You have collected data on the test scores of 15 students who used the new technique (group *NT*) and 15 students who did not (group *OT*). The following table contains the test scores, where i is the index of a student in a specific group. We can assume that the differences are normally distributed.

i	1	2	3	4	5	6	7	8	9	10	11	12	13	14	15
NT_i	85	89	92	88	91	90	87	93	86	91	84	88	89	90	92
OT_i	79	81	75	82	77	80	78	84	76	80	78	83	82	79	85

- State the null hypothesis (H_0) and the alternative hypothesis (H_1) for this scenario.
- Explain whether this is a one-sided or two-sided test and justify your choice.
- Conduct the t-test in Python using the SciPy library to compare the means of the two groups using a significance level of $\alpha = 0.05$. You can leverage the provided notebook.
- Given the test result, would you reject the null hypothesis H_0 ? Explain the result in the context of the research question.
- Determine and interpret the corresponding 95% confidence interval in Python.