

$$-u'' - u = \sin x \quad / \cdot v, \int_0^2 (-1) u(0) = 0$$

$$\int_0^2 u'' v dx - \int_0^2 u v dx = - \int_0^2 v \sin x dx \quad u'(2) - u(2) = 0$$

$$u'(2) = u(2)$$

$$u' v \Big|_0^2 - \int_0^2 u' v' dx + \int_0^2 u v dx = - \int_0^2 v \sin x dx$$

$$u'(2)v(2) - \underbrace{u'(0)v(0)}_{0 \text{ (Gibb)}} - \int_0^2 u' v' dx + \int_0^2 u v dx = - \int_0^2 v \sin x dx$$

$$\underbrace{u(2)v(2) + \int_0^2 (-u'v' + uv) dx}_{B(u,v)} = \underbrace{- \int_0^2 v \sin x dx}_{L(v)}$$

$$\begin{bmatrix} B(u_1, v_1) & \dots & B(u_1, v_m) \\ \vdots & & \vdots \\ B(u_n, v_1) & \dots & B(u_n, v_m) \end{bmatrix} \begin{bmatrix} c_1 \\ \vdots \\ c_m \end{bmatrix} = \begin{bmatrix} L_1 \\ \vdots \\ L_m \end{bmatrix}$$