

Counterfactuals and Directed acyclic graphs in epidemiology

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23 mei, 2018

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- ▶ So $Y^{a=1}$ is the value Y would take if we set $a = 1$ (N.B.: this is not $Y|A=1$)
- ▶ In a dataset we observe *at most* half of the Y^a (an RCT of a binary A)
- ▶ We write the causal effect we're interested in as $Y^{a=1} - Y^{a=0}$

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- ▶ Counterfactual notation has been used to achieve insight into estimation of longitudinal causal effects, instrumental variables and a number of other topics
- ▶ Some of the insight provided by counterfactuals can also be depicted in graphical form

Directed Acyclic Graphs (DAGs)

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 1    

Can someone explain in simple terms to me what a Directed acyclic graph is?

Ask Question



70



30

Can someone explain in simple terms to me what a Directed acyclic graph is? I have looked on Wikipedia but it doesn't really make me see its use in programming.

directed-acyclic-graphs

share edit

edited Mar 2 '10 at 2:15



polygenelubricants
257k • 92 • 491 • 583

asked Feb 17 '10 at 19:26



Zubair
20.2k • 46 • 190 • 327

17 Wikipedia frequently contains overwhelming technical content that would take beginners a great deal of studying to comprehend. Many of the math help sites are superior in this regard, but they tend not to get into computation related subjects, unfortunately. – Jonathon Faust Feb 17 '10 at 19:41

add a comment

asked 7 years, 11 months ago

viewed 37,741 times

active 7 months ago



dots with lines pointing to other dots

25



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answered Dec 14 '12 at 11:46




smartcaveman
24.1k • 17 • 94 • 184

1 +1 FOR A FUNNY ANSWER! :) – Zubair Dec 14 '12 at 12:03

11 This is one of the best answers because it is a simple way of describing what is a simple concept buried in complex terminology (if we're asking this question, we might not know graph theory... or even need to know). My variant would be something like "bar-hopping where you can never go to the same bar twice". Although the family-tree example from another answer is probably conceptually simpler, especially for those of us who aren't college students or alcoholics. – Tom Harrison Jr Jul 23 '16 at 16:48

4 ... in one direction – Mark Robson Jul 4 '17 at 12:34

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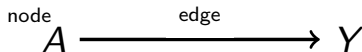
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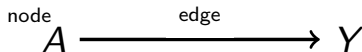
Directed Acyclic Graphs (DAGs)

- ▶ DAGs are diagrams with simple rules that allow us to clearly think about our causal questions to determine what sources of bias we might have and how we can avoid them



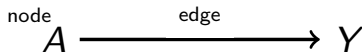
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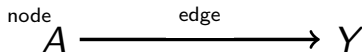
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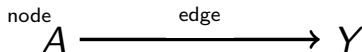
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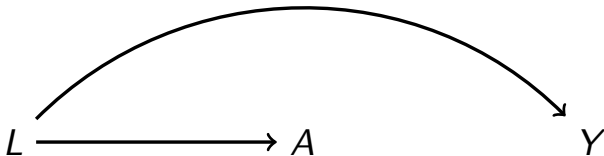
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- ▶ Edges are directed (i.e. one causes the other)
- ▶ DAGs must be acyclic, no feedback loops are allowed
- ▶ The edges are not deterministic



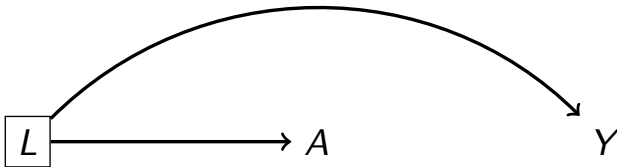
Directed Acyclic Graphs (DAGs)

- ▶ $Y \not\perp\!\!\!\perp A$ but $Y^a \perp\!\!\!\perp A$



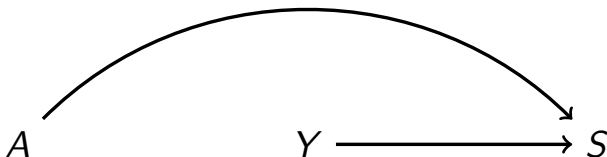
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- $Y \perp\!\!\!\perp A|L$ but $Y^a \perp\!\!\!\perp A|L$



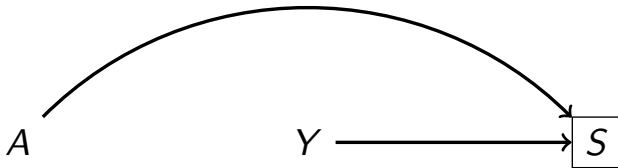
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Directed Acyclic Graphs (DAGs)

- $Y \not\perp\!\!\!\perp A|S$ but $Y^a \perp\!\!\!\perp A|S$



Directed acyclic graphs (DAGs)



george davey smith

@mendel_random

Following



Epidemiologists rejoice! "the task of selecting an appropriate set of covariates to control for confounding has been reduced to a simple "roadblocks" puzzle manageable by a simple algorithm" arxiv.org/abs/1801.04016 and



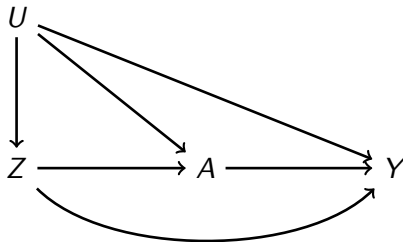
Comments on: The tale wagged by the DAG | International ...

I am grateful to the editors for the opportunity to comment on Nancy Krieger and George Davey Smith's article, 'The tale wagged by the DAG', which appeared in academic.oup.com

This is true! But the DAG has to be correctly specified which is the hard (impossible) part.

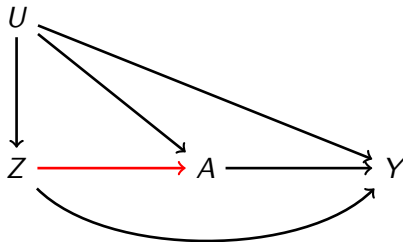
Showing the IV assumptions in a DAG

- This DAG makes the least amount of assumptions about the observed data. Every node is connected to every other



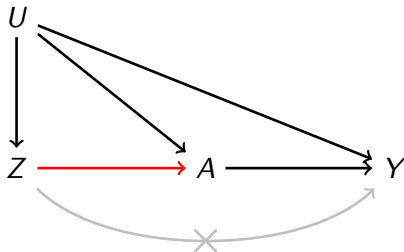
Showing the IV assumptions in a DAG

- The relevance assumption is represented by the red arrow, showing that there is a relationship between Z and A



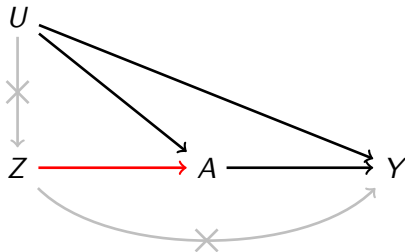
Showing the IV assumptions in a DAG

- The exclusion restriction (ER) assumption assumes that the direct edge between Z and A is not present



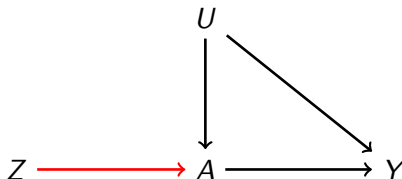
Showing the IV assumptions in a DAG

- The exchangeability assumption assumes that Z is not confounded with Y



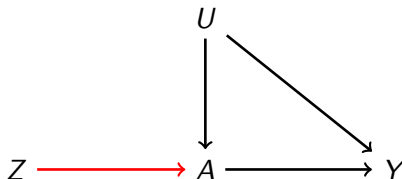
Showing the IV assumptions in a DAG

- ▶ With our three assumptions, we end up with our classic IV DAG



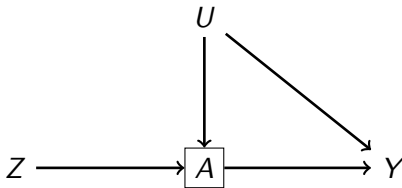
Showing the IV assumptions in a DAG

- ▶ With our three assumptions, we end up with our classic IV DAG
- ▶ Note: monotonicity and homogeneity cannot be drawn on a DAG because they are parametric concepts



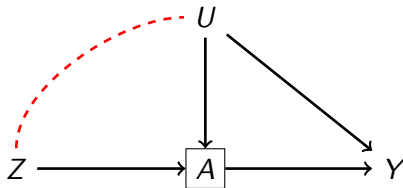
Conditioning on exposure in IV analyses

- Sometimes people like to stratify or restrict on exposure



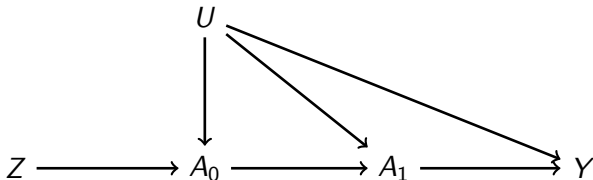
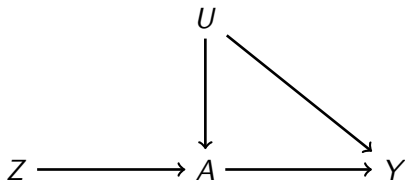
Conditioning on exposure in IV analyses

- ▶ But we create a new association between Z and U therefore violating the exchangeability assumption



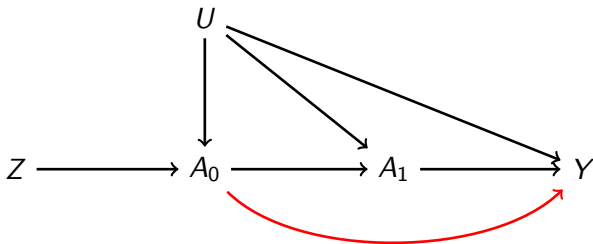
Using DAGs to think about IV longitudinally

- We can depict a time-varying exposure by splitting the A node into separate nodes for each time point



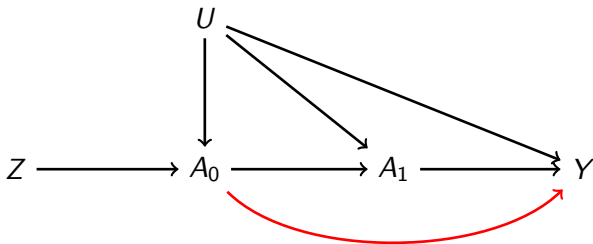
Using DAGs to think about IV longitudinally

- We have assumed that A_0 does not have a direct effect on Y



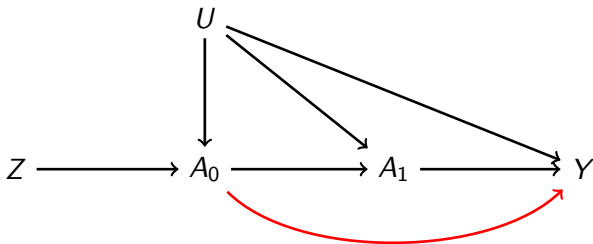
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- ▶ We have assumed that A_0 does not have a direct effect on Y
- ▶ If A_0 does affect Y then we can no longer estimate the effect of A_1 on Y



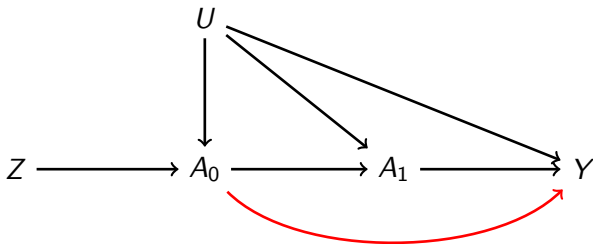
Using DAGs to think about IV longitudinally

- ▶ We have assumed that A_0 does not have a direct effect on Y
- ▶ If A_0 does affect Y then we can no longer estimate the effect of A_1 on Y
- ▶ This is because, although the ER holds for A as a whole, it does not hold for A_1



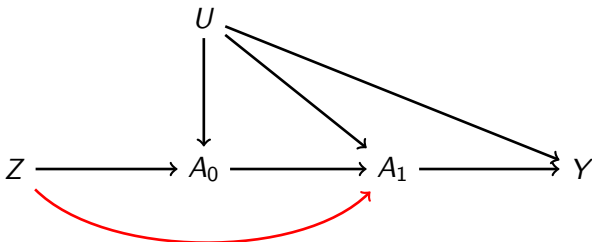
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- ▶ So if we measure A_0 we're alright?



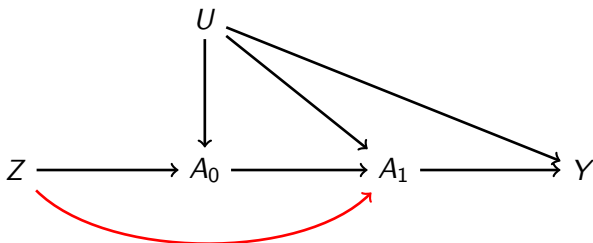
Using DAGs to think about IV longitudinally

- ▶ We have also assumed that Z does not have a direct effect on A_1



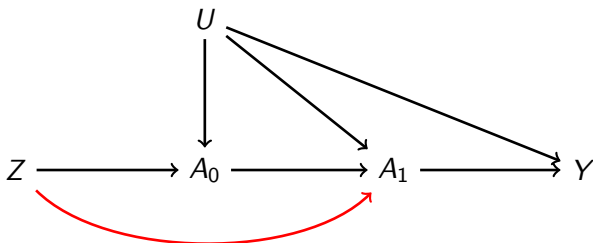
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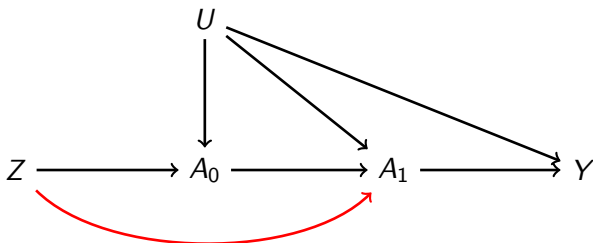
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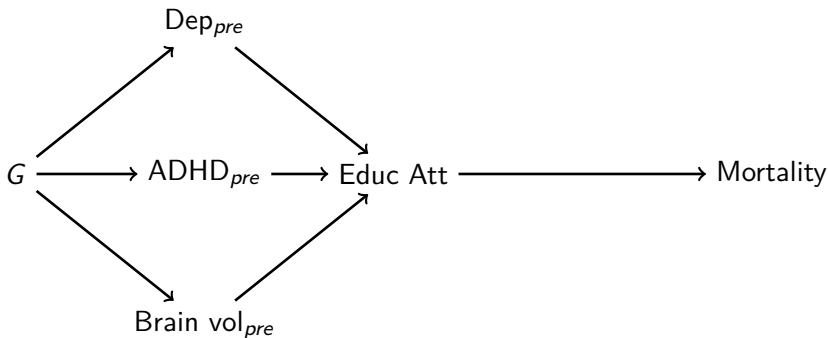
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- ▶ If Z does affect A_1 then we can no longer estimate the effect of A_0 on Y
- ▶ This is because, although the ER still holds for A as a whole, it does not hold for A_0
- ▶ All this to illustrate that, in contexts such as Mendelian randomization, important thought must be given to how exposures change longitudinally



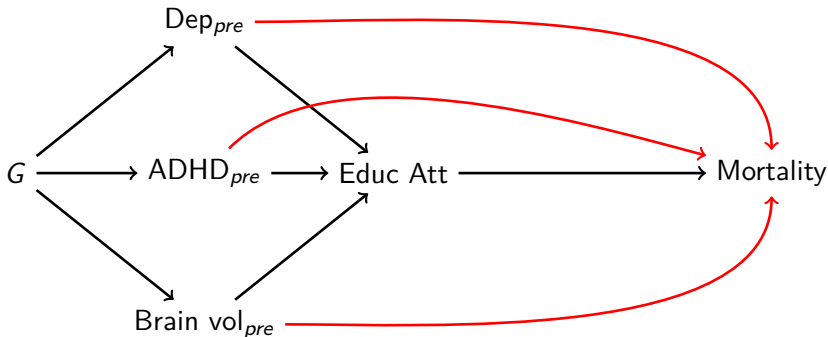
Using DAGs to think about Mendelian randomization

- ▶ DAG for a MR study of the effect of educational attainment on mortality



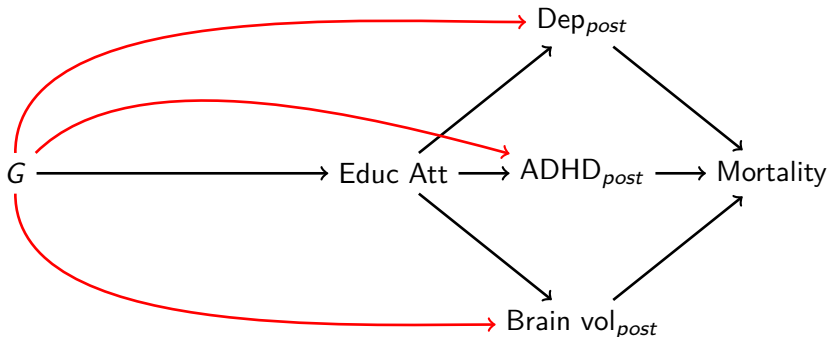
Using DAGs to think about Mendelian randomization

- ▶ But what if the intermediates between G and education attainment have a direct effect on mortality?



Using DAGs to think about Mendelian randomization

- Or what if G has a direct affect on the intermediates after educational attainment



Using DAGs to think about Mendelian randomization

- ▶ We have also assumed that Z does not have a direct effect on A_1

