# THE 18.821 MATHEMATICS PROJECT LAB REPORT [PROOFS]

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### 1. Theorems

### 1.1. Notation.

t: Time

l: Path length

s: Speed

 $a_T$ : Tangential acceleration  $a_C$ : Centripetal acceleration

 $\vec{x}$ : Position  $\vec{v}$ : Velocity

 $\vec{a}$ : Acceleration

### 2. Cylindrical Coordinates Calculus

(1) 
$$\mathbf{r} = r\hat{\mathbf{r}}$$

(2) 
$$\dot{\mathbf{r}} = \dot{r}\hat{\mathbf{r}} + r\dot{\phi}\hat{\phi}$$

(3) 
$$\ddot{\mathbf{r}} = \left(\ddot{r} - r\dot{\phi}^2\right)\hat{\mathbf{r}} + \frac{1}{r}\frac{d}{dt}\left(r^2\dot{\phi}\right)\hat{\phi}$$

## 3. Theorems

**Theorem 3.1.** For a given speed and bounded centripetal acceleration, it is always optimal to minimize the turning radius. This turning radius is

Proof. Well, yes.  $\Box$ 

#### REFERENCES

[1] http://en.wikipedia.org/wiki/Polar\_coordinate\_system

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