

- **Do not turn this page until time is called.**
- We will read through the info below together. 😊👍
- The exam is 8 questions long.
- Each question is 1 page long; Some questions will have helpful code above them.
- The exam is 90 points total.
- The exam is scheduled for 120 minutes.
- No notes are allowed.
- Partial credit will be given. Make sure you try answering all questions!  
**Especially Question 8 (the coding question).** 😊👍
- Just like in the homework, we are compiling with Java 8 and importing `java.util.*`
- Assume code snippets are inside of suitable main methods.
- This exam may be curved, but only up (the curve cannot make your grade worse).
- This exam will be primarily graded on correctness.
- This exam may also be graded (to a lesser extent) on speed, clarity, and robustness.
- `char c = (char) ('A' + 3); // 'D'`
- In PostScript, **def** is "define," **mul** is "multiply," **dup** is "duplicate," **exch** is "exchange," **sqrt** is "square root"
- We can use `ArrayDeque` queue; as a single-ended (regular, typical) queue.  
`queue.add(...)` adds to the back  
`queue.remove()` removes from the front and returns it
- `isEmpty()` returns whether an `ArrayList`, `Stack` or `ArrayDeque` is empty  
`foo.isEmpty()` it is equivalent to `(foo.size() == 0)`

Please sign below.

*I am the person whose name is listed at the top of this page.  
I have neither given nor received unauthorized help on this exam.*

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1. (10 points) Draw the state of the stack and map after these PostScript functions run.  
NOTE: Functions **ARE** separate.

1.0 3.0 add sqrt

-----  
stack + map { }

---

/side 2.0 def /area side side mul def /volume side area mul def

-----  
stack + map { }

2. (10 points) What could this code print?

**NOTE:** Assume `buildFrequencyTables(...)` does **NOT** "wrap around."

The last window to consider is:

**aabbbbbaa**

--^ ("ba" followed by 'a')

```
String sourceText = "aabbbbbaa";  
int windowLength = 2;  
HashMap<String, HashMap<Character, Integer>> frequencyTables;  
frequencyTables = buildFrequencyTables(sourceText, windowLength);  
System.out.println(frequencyTables);
```

// Answer goes below here. vvv

```

class LinkedList {
    Node head;
    // list of nodes with values 1, 2, 3 prints as
    // 1 -> 2 -> 3
    String toString();
}

class Node {
    int value;
    Node next;
    Node(int value); // Constructor.
}

```

3. (10 Points) What does this code print?

**NOTE:** The blocks of code are NOT separate.

```
LinkedList list = new LinkedList();
```

```
list.head = new Node(3);
```

```
System.out.println(list); // <- Answer goes here.
```

```
Node node = new Node(5);
```

```
System.out.println(list); // <- Answer goes here.
```

```
list.head.next = node;
```

```
System.out.println(list); // <- Answer goes here.
```

```
node.next = new Node(7);
```

```
System.out.println(list); // <- Answer goes here.
```

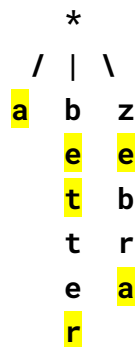
```
list.head = list.head.next.next;
```

```
System.out.println(list); // <- Answer goes here.
```

4. (10 points) Tries and Traversal.

a. What words are stored in this trie?

NOTE: Terminal nodes are highlighted in yellow.



```
//                                     <- Answer goes here.
```

b. Say root is the root node of the trie shown above. What does this code print?

NOTE: This code uses the same trie `Node` from HW09.

**// HINT: This is a breadth-first traversal (using a queue).**

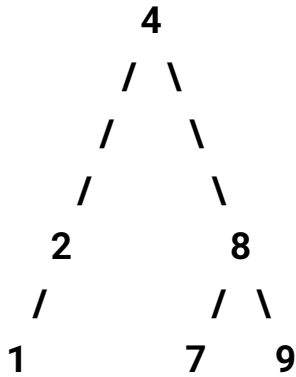
```
ArrayDeque<Node> queue = new ArrayDeque<>();
queue.add(root);
while (!queue.isEmpty()) {
    Node curr = queue.remove();
    for (int i = 0; i < 26; ++i) {
        if (curr.children[i] != null) {
            if (curr.children[i].isTerminal) {
                char c = (char)('A' + i);
                System.out.println(c);
            }
            queue.add(curr.children[i]);
        }
    }
}
```

```
// Answer goes below here. vvv
```

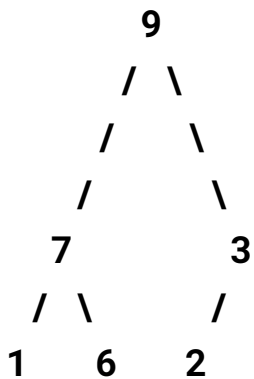
5. (10 points) Binary Search Trees and Max Binary Heaps.

a. Draw the state of this **binary search tree** after calling `tree.add(5)`.

NOTE: Use the naive `add(int i)` from HW10 (**NOT** self-balancing).



b. Draw the state of this **max binary heap** after calling `heap.remove()`.



```

class ToyMap {
    ArrayList<KeyValuePair>[] buckets;
    ToyMap() {
        buckets = (ArrayList<KeyValuePair>[]) new ArrayList[5];
        for (int i = 0; i < buckets.length; ++i) {
            buckets[i] = new ArrayList<>();
        }
    }
    void put(String key, bool value) {
        int bucketIndex = (2 * key.length()) % buckets.length;
        ArrayList<KeyValuePair> bucket = buckets[bucketIndex];
        for (KeyValuePair pair : bucket) {
            if (key.equals(pair.key)) {
                pair.value = value;
                return;
            }
        }
        bucket.add(new KeyValuePair(key, value));
    }
}

class KeyValuePair {
    String key;
    bool value;
    KeyValuePair(String key, bool value) {
        this.key = key;
        this.value = value;
    }
    public String toString() { return key + "=" + value; }
}

```

**6. (10 Points) What does this code print?**

```

ToyMap map = new ToyMap();
map.put("Mew", true);
map.put("Arbok", true);
map.put("Muk", true);
map.put("Arbok", false);
System.out.println(Arrays.toString(map.buckets));

```

```
//
```

**<- Answer goes here.**

7. (10 Points) Write the worst case big O runtime in terms of n.

NOTE: The blocks of code ARE separate.

```
// Worst-case big O runtime: ?
int result = 0;
while (n > 0) {
    result += n;
    n /= 2;
}
```

```
// Worst-case big O runtime: ?
int result = n;
for (int i = 0; i < 742; ++i) {
    result += i;
}
```

```
// Worst-case big O runtime: ?
String result = "";
for (int i = 0; i < n; ++i) {
    result = result + "asdf";
}
```

```
// Worst-case big O runtime: ?
Stack<Integer> stack = new Stack<>();
stack.push(n);
while (!stack.isEmpty()) {
    int tmp = stack.pop();
    for (int i = 1; i < tmp; ++i) {
        stack.push(i);
    }
}
```



8. (20 Points) Implement this function.

HINT: `HashMap<Integer, Integer> map = new HashMap<>();`

HINT: You can use for-each loops to iterate through...

- the array's elements: `for (int i : array) { ... }`
- the map's keys: `for (int i : map.keySet()) { ... }`

HINT: `HashMap` functions:

- `map.containsKey(i)`
- `map.get(i)`
- `map.put(i, ...)`

// Returns the number that shows up most often in array (the **mode**).

// If there are multiple modes, returns (any) one of them.

// If array is empty, crashes.

// { 7, 5, -4, -4, 9 } -> -4

// { 1, 1, 2, 2, 3 } -> 1 (or 2)

// { 8 } -> 8

// **Worst-case Runtime:  $O(n)$**

`int getMode(int[] array) {`

`}`