

## ANNOUNCEMENTS

today is No Laptop Monday!

# Week08a

### WARMUP

"a chain is only as strong as its weakest link"

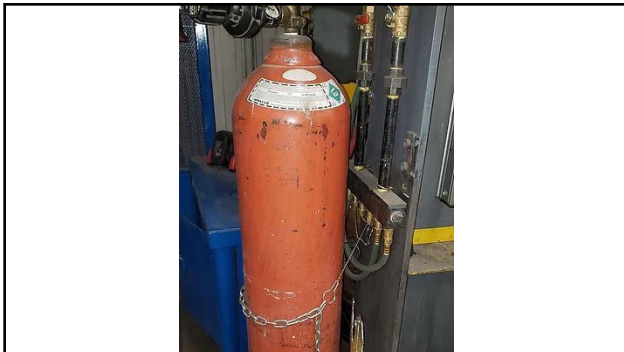
- what does this expression mean?
- what is a chain?
- what is a link?
- is this true for real-world metal chains? why or why not?

**TODAY** linked lists



1

2



3

# linked lists

record lecture

4

## (p)review: list interface

5

### list interface

```
- // Get the element with this index.
- ElementType get(int index);

- // Add (append) an element to the back of the list.
- void add();

- // Add (insert) an element into the list so it has this index
- void add(int index, ElementType element);

- // Remove (delete) the element in the list at this index.
- void remove(int index);

- // Get the number of elements currently in the list.
- int size();
```

6

### list interface (cont.)

```
- // NOTE: Many other functions could be included
  //       in this interface.
- void sort(); // Sort the list.
- void reverse(); // Reverse the list.

- List<ElementType> sorted(); // Get sorted copy of the list.
- List<ElementType> reversed(); // Get reversed copy of list.

- // Get index of first element with this value.
  int find(ElementType element);

- ...
```

7

a few weeks ago,  
we implemented the list interface  
using an array

the *array list*

8

this week, we will implement  
the list interface using nodes with  
"links" (references) to other nodes

this will be called a **linked list**

9

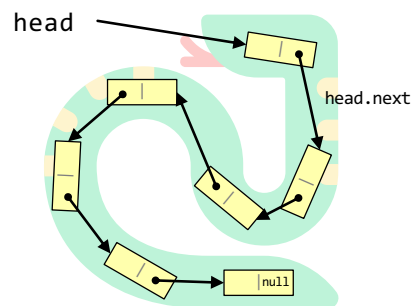
note

10

today we will be discussing the  
simplest possible linked list

(LinkedList literally just has a  
reference to Node head.)

11



12

some other implementations are possible.  
some will be faster than this one.

13

for linked lists, do NOT memorize  
big O runtimes out of context

14

why are we doing this?

15

**A:** it will be cool to see two  
very different implementations  
of the same interface 🤖

16

**B:** linked lists will prepare us for  
trees and graphs 🌳

17

**C:** linked lists are incredibly  
FUNdaMENTAL 🧠  
(for us, as fundamental as arrays)

18

**D:** linked lists are actually big O better  
(than array lists) in very specific cases

19

**E:** linked lists are actually really,  
really important  
(especially in the C programming language)

20



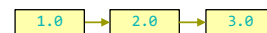
21

linked list

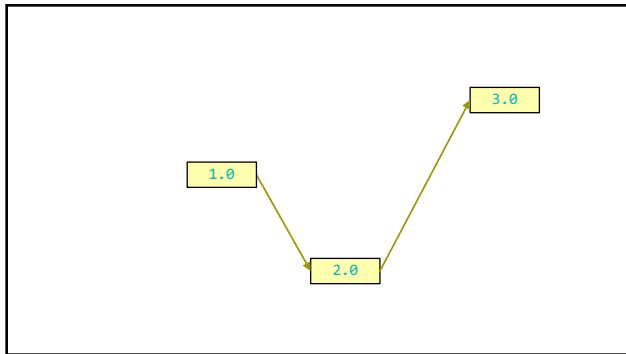
22



23



24



25

| linked list   |   |
|---|---|
| <pre> class LinkedList {     Node head; }  class Node {     Value value;     Node next;      Node(Value value) {         this.value = value;     } } </pre> | <pre> LinkedList list = new LinkedList();  list.head = new Node(1.0); 1.0  list.head.next = new Node(2.0); 1.0 → 2.0  list.head.next.next = new Node(3.0); 1.0 → 2.0 → 3.0 </pre> |

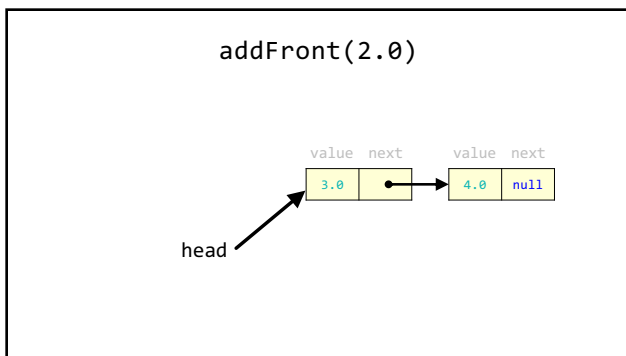
26

| linked list  |  |
|--|--|
| <pre> class LinkedList {     Node head;      void add(Value value) {         ...     } }  class Node {     Value value;     Node next;      Node(Value value) { </pre> | <pre> LinkedList list = new LinkedList();  list.add(1.0); 1.0  list.add(2.0); 1.0 → 2.0  list.add(3.0); 1.0 → 2.0 → 3.0 </pre> |

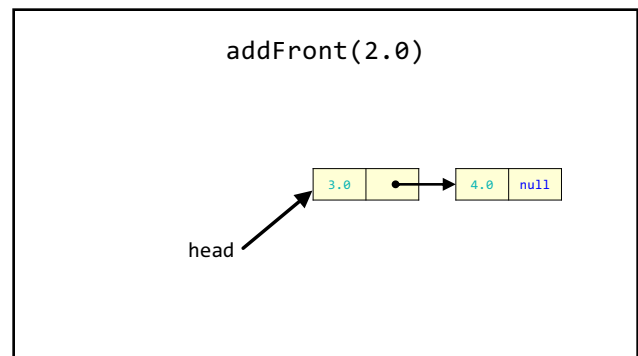
27

example: addFront(value)

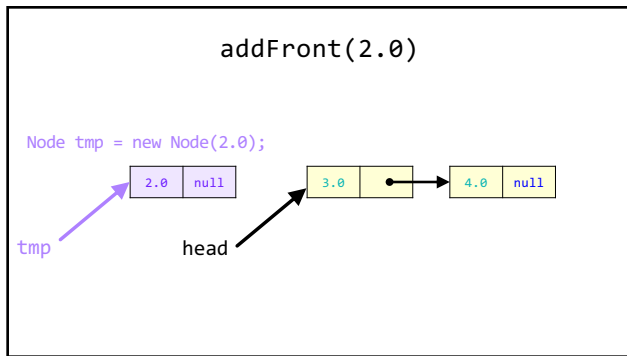
28



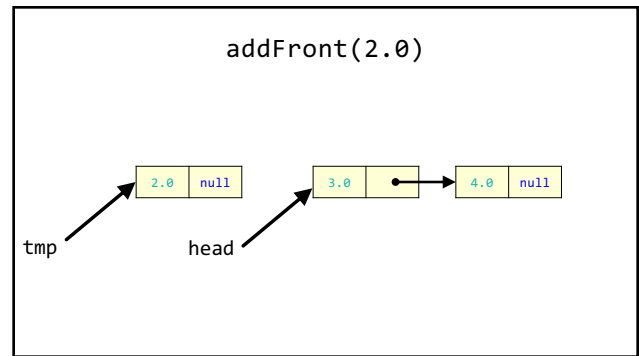
29



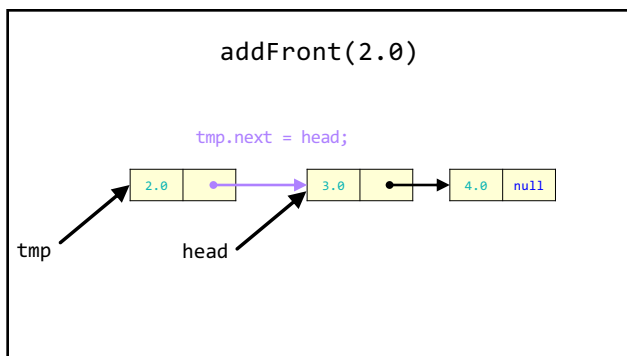
30



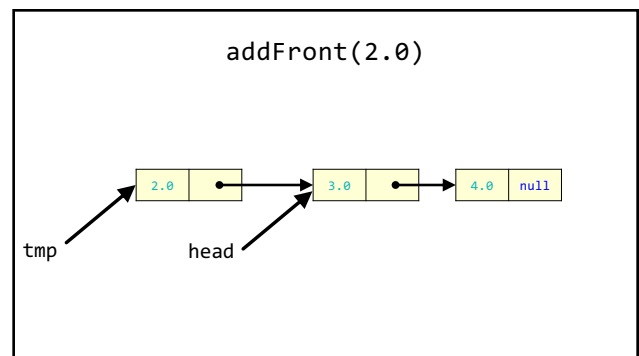
31



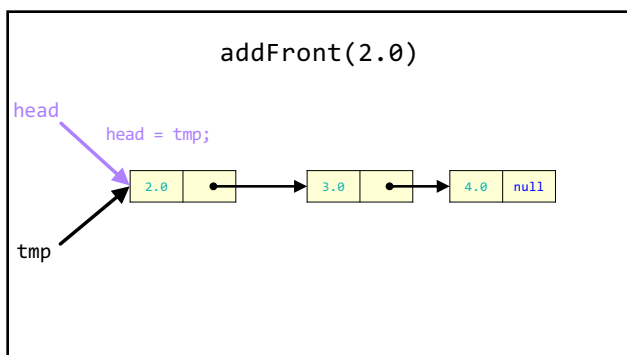
32



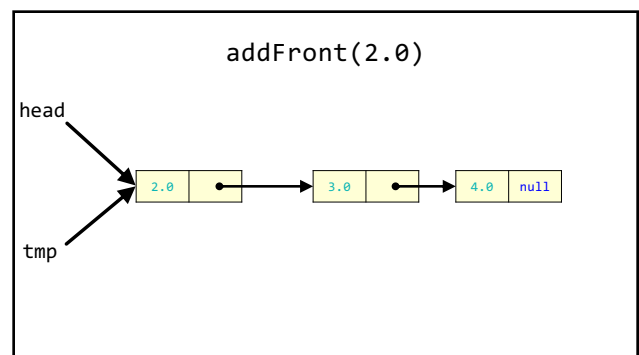
33



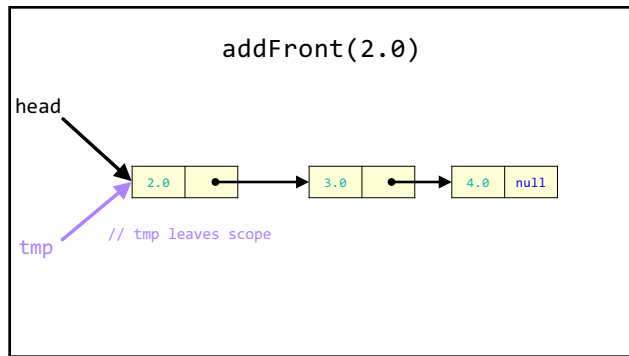
34



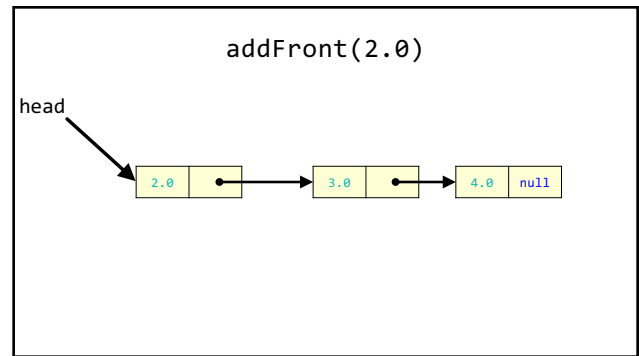
35



36



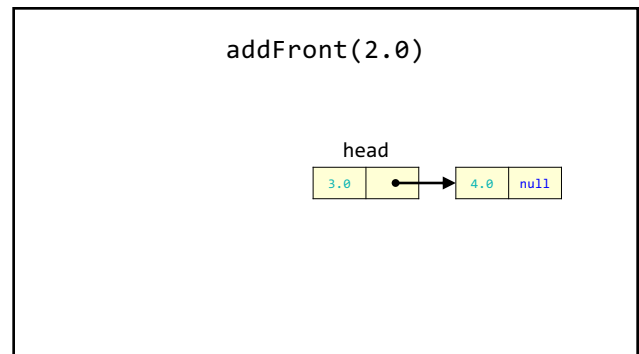
37



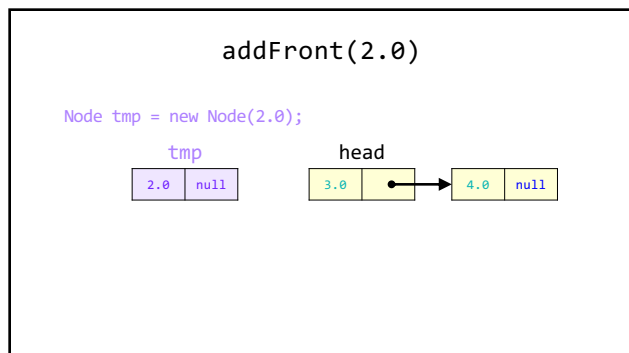
38

same thing but with  
labels instead of arrows  
for head and tmp

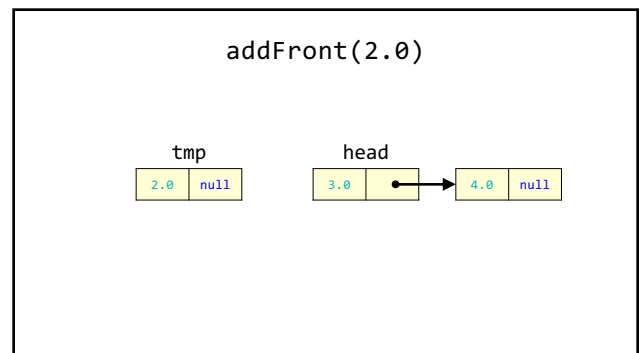
39



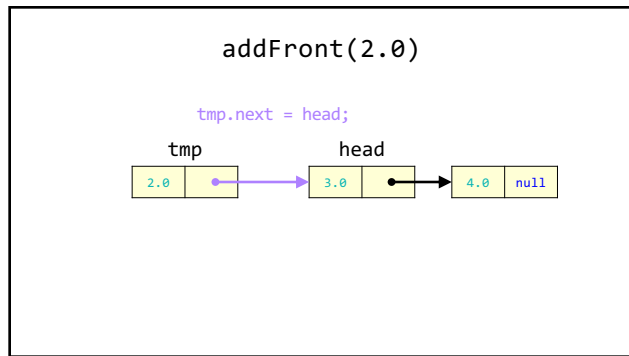
40



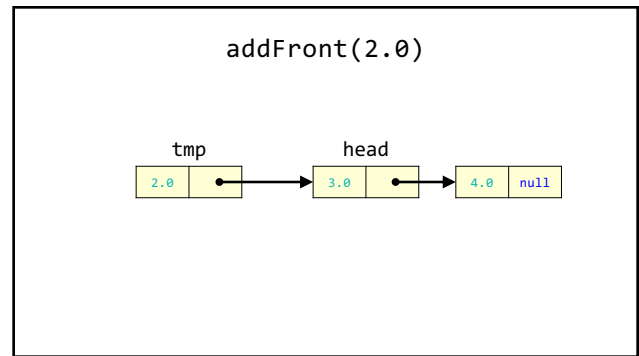
41



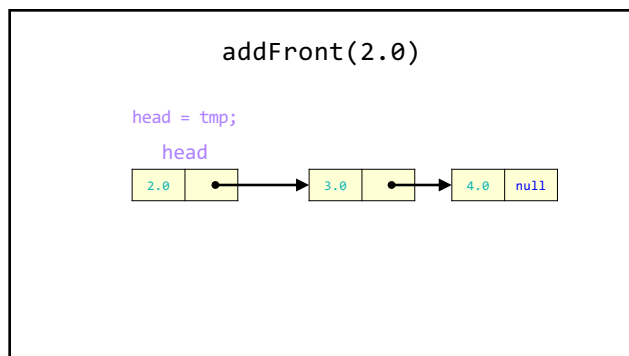
42



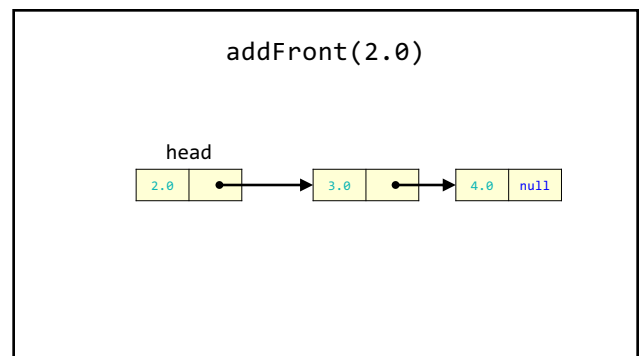
43



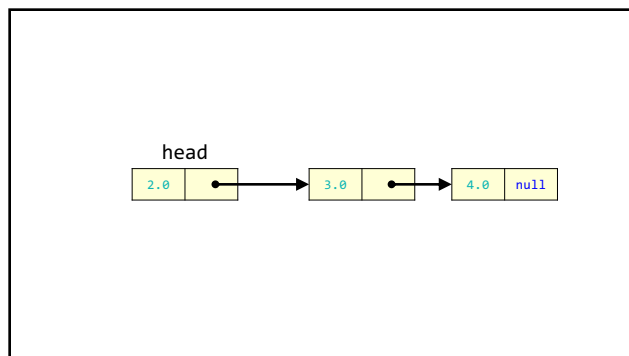
44



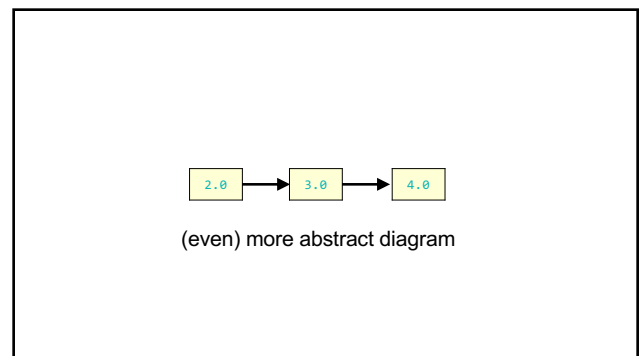
45



46



47



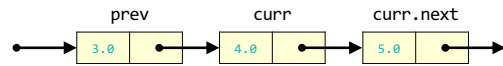
48



## example: remove

49

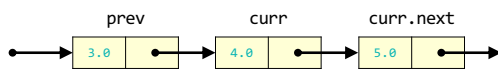
### remove



```
Node prev = null; // the previous node
Node curr = head; // the current node
while (...) {
    ...
    prev = curr;
    curr = curr.next;
}
```

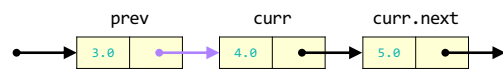
50

### remove



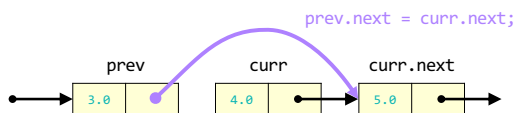
51

### remove



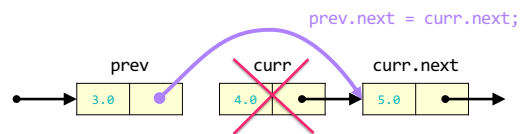
52

### remove

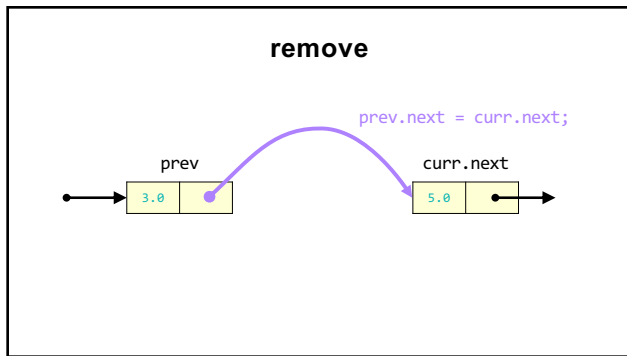


53

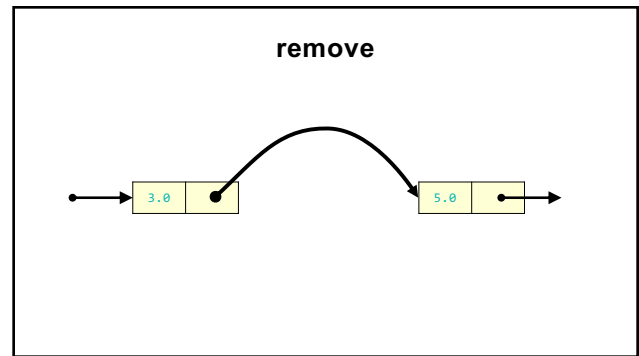
### remove



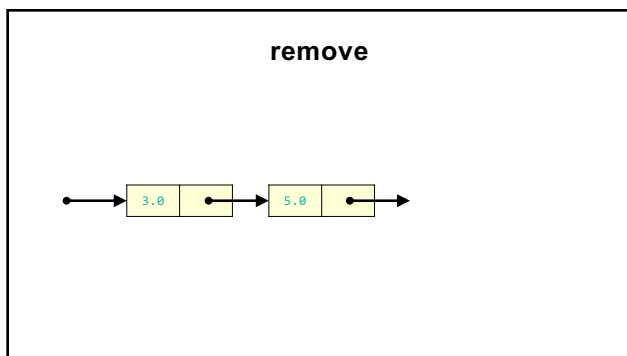
54



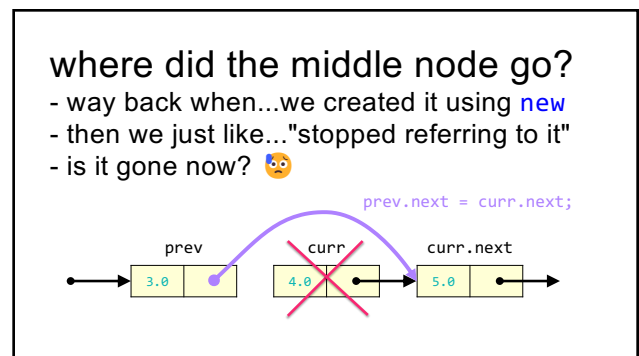
55




56



57



58

 it has been garbage collected

59

[board discussion of  
"no directed path from stack to the node"]

60

big O runtimes

61

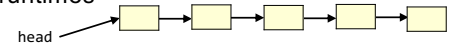
what is the big O runtime of size()?  
[pointing activity]

62

$O(n)$  🤔

63

singly-linked list  
worst case runtimes



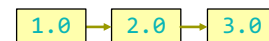
```
- list.add(index, value)      - list.addFront() // list.add(0, value)
  - // O(n)                  - // O(1)
- list.removeByIndex(index)  - list.removeFront() // list.removeByIndex(0)
  - // O(n)                  - // O(1)
- list.addBack()             - list.addBack()
  - // O(n)                  - // O(n)
- list.size()                - list.removeBack()
  - // O(n)                  - // O(n)
```

64

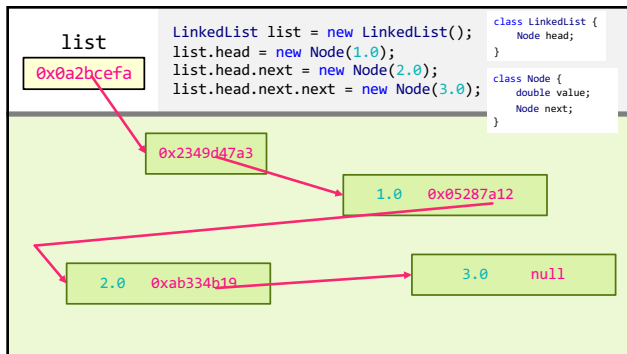
beyond big O runtime

65

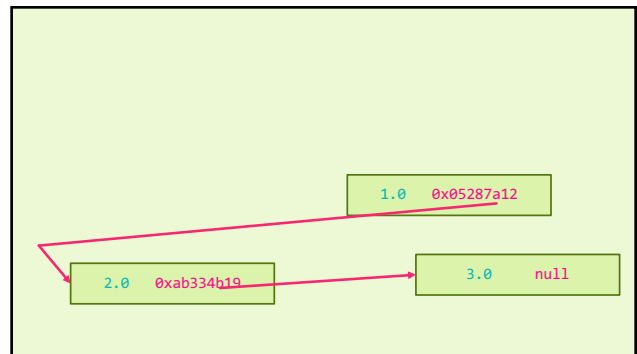
what does this actually look like  
in memory?



66



67



68

what does this *mean*?

cons? 😞

pros? 😊

(how is this very different than an array list?)

69

<https://x.com/kzr/status/1672497446705037312>

70



72

## ANNOUNCEMENTS

friday's colloquium will be cool!

my friend Pascal makes ✨underwater robotic spheres✨!  
midterms will be returned Fri

# Week08b

## WARMUP

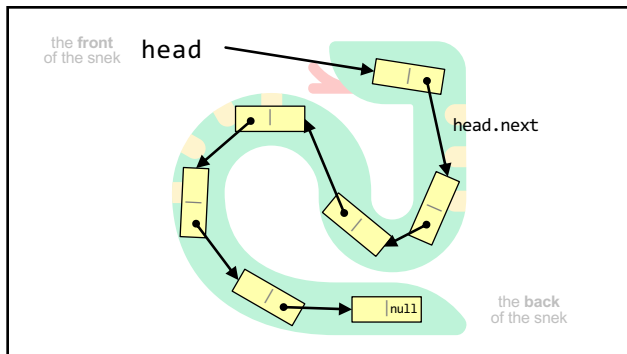
review: for a linked list, `size()` is  $O(n)$  runtime

- how could you make `size()` (or perhaps... `size`)  $O(1)$ ?

-- is this at all...spooky? 🧛

**TODAY** `size()` and riffs on linked lists

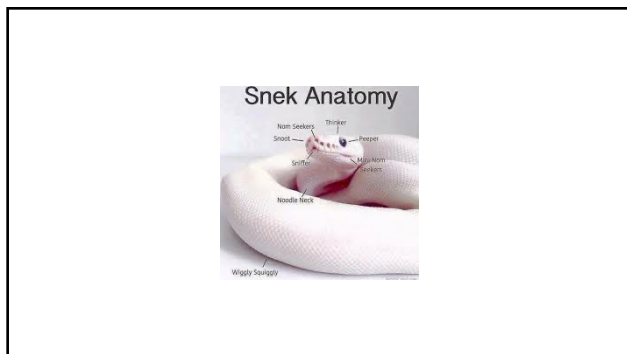
73



74

linked lisssssst

75



76

[record lecture]

77

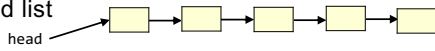
LinkedList  
review

78

runtimes

79

worst case  
singly-linked list  
runtimes



- |                             |                      |
|-----------------------------|----------------------|
| - list.add(index, value)    | - list.addFront()    |
| - // O(n)                   | - // O(1)            |
| - list.removeByIndex(index) | - list.removeFront() |
| - // O(n)                   | - // O(1)            |
| - list.size()               | - list.addBack()     |
| - // O(n)                   | - // O(n)            |
|                             | - list.removeBack()  |
|                             | - // O(n)            |

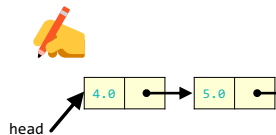
80

additional warmup:  
prepending a list

81

example

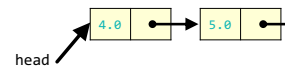
```
Node snap = new Node(1.0);
Node crackle = new Node(2.0);
Node pop = new Node(3.0);
snap.next = crackle;
crackle.next = pop;
pop.next = head;
head = snap;
```



82

example

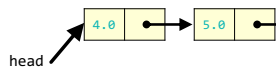
```
Node snap = new Node(1.0);
Node crackle = new Node(2.0);
Node pop = new Node(3.0);
snap.next = crackle;
crackle.next = pop;
pop.next = head;
head = snap;
```



83

example

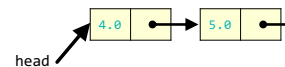
```
Node snap = new Node(1.0);
Node crackle = new Node(2.0);
Node pop = new Node(3.0);
snap.next = crackle;
crackle.next = pop;
pop.next = head;
head = snap;
```



84

example

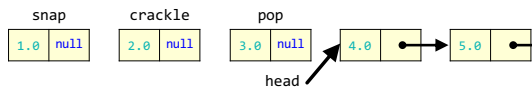
```
Node snap = new Node(1.0);
Node crackle = new Node(2.0);
Node pop = new Node(3.0);
snap.next = crackle;
crackle.next = pop;
pop.next = head;
head = snap;
```



85

### example

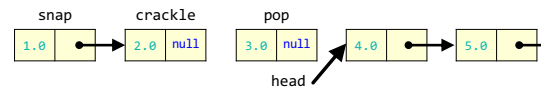
```
Node snap = new Node(1.0);
Node crackle = new Node(2.0);
Node pop = new Node(3.0);
snap.next = crackle;
crackle.next = pop;
pop.next = head;
head = snap;
```



86

### example

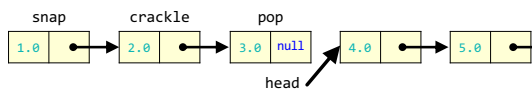
```
Node snap = new Node(1.0);
Node crackle = new Node(2.0);
Node pop = new Node(3.0);
snap.next = crackle;
crackle.next = pop;
pop.next = head;
head = snap;
```



87

### example

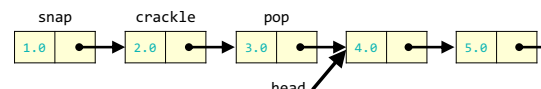
```
Node snap = new Node(1.0);
Node crackle = new Node(2.0);
Node pop = new Node(3.0);
snap.next = crackle;
crackle.next = pop;
pop.next = head;
head = snap;
```



88

### example

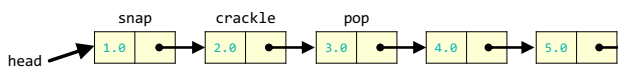
```
Node snap = new Node(1.0);
Node crackle = new Node(2.0);
Node pop = new Node(3.0);
snap.next = crackle;
crackle.next = pop;
pop.next = head;
head = snap;
```



89

### example

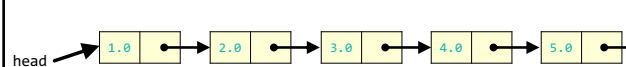
```
Node snap = new Node(1.0);
Node crackle = new Node(2.0);
Node pop = new Node(3.0);
snap.next = crackle;
crackle.next = pop;
pop.next = head;
head = snap;
```



90

### example

```
Node snap = new Node(1.0);
Node crackle = new Node(2.0);
Node pop = new Node(3.0);
snap.next = crackle;
crackle.next = pop;
pop.next = head;
head = snap;
```



91

```
Node snap = new Node(1.0);
Node crackle = new Node(2.0);
Node pop = new Node(3.0);
snap.next = crackle;
crackle.next = pop;
pop.next = head;
head = snap;
```

vs.

```
addFront(3.0);
addFront(2.0);
addFront(1.0);
```

🧠 was that faster than calling `addFront()`  $n$  times?

🧠 same big O or different big O?  
(if we were to call it many times)

92

🧠 was that faster than calling `addFront()`  $n$  times?

**yes**  
(only updated head once)

🧠 same big O or different big O?

**same**  
(still have to "hook up"  $O(n)$  references)

93

[implement LinkedList]

94

[implement LinkedList]

95

size()

96

[ implement size() poorly ]

97



[ implement size() poorly ]

98

joyful implementation of size

99

```
static class LinkedList {
    Node head;

    int size() {
        int result = 0;
        Node curr = head;
        while (curr != null) {
            ++result;
            curr = curr.next;
        }
        return result;
    }
}
```

100

size()

- what is the big O runtime of this method?
  - $O(n)$  😬
- this seems like a pretty steep cost to pay just to know the list's size...  
what would be a more efficient approach?
  - store size as an instance variable
    - update it every time you change the number of elements in the list  
(inside of add, remove, etc.)
- what is the runtime of this approach?
  - $O(1)$  😊

101

while way more efficient, this approach  
is perhaps a bit spooky 🐻

multiple functions are now also responsible  
for carefully modifying an instance variable  
(mess up, and any code that depends on size will be very weirdly broken)

102

**note:** the A homework doesn't use size at all

103

but if you *were* going to implement/use the list's size...  
 i would start with size() as a function,  
 get everything working perfectly,  
 and only then carefully turn it into an instance variable  
 😊👍

104

(it's this thing again)

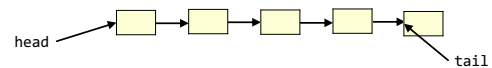


105

## tail reference

106

singly-linked list with reference to tail

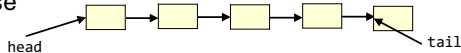


```
class LinkedList {
    Node head;
    Node tail;
}
```

```
class Node {
    Value value;
    Node next;
}
```

107

singly-linked list with reference to tail  
 worst case  
 runtimes



- |                             |                      |
|-----------------------------|----------------------|
| - list.add(index, value)    | - list.addFront()    |
| - // O(n)                   | - // O(1)            |
| - list.removeByIndex(index) | - list.removeFront() |
| - // O(n)                   | - // O(1)            |
| - list.size()               | - list.addBack()     |
| - // O(n)                   | - // O(1) 😊          |
|                             | - list.removeBack()  |
|                             | - // O(n) 😞          |

108

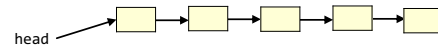
## doubly-linked list

109

## singly- vs. doubly-linked

110

### singly-linked list

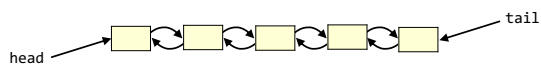


```
class LinkedList {  
    Node head;  
}
```

```
class Node {  
    Value value;  
    Node next;  
}
```

111

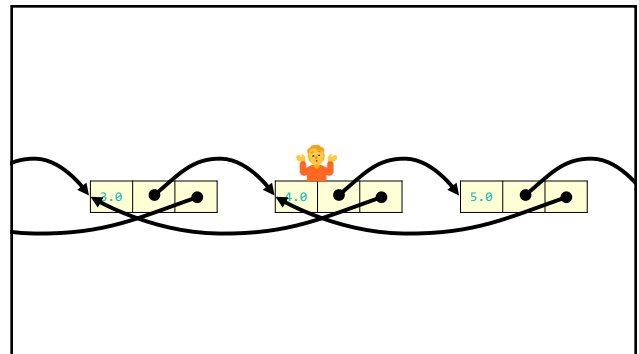
### doubly-linked list



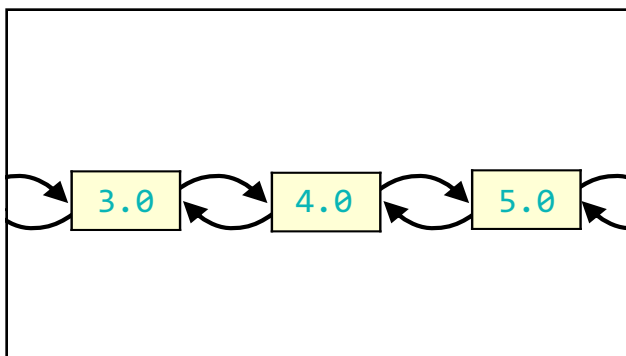
```
class LinkedList2 {  
    Node2 head;  
    Node2 tail;  
}
```

```
class Node2 {  
    Value value;  
    Node2 next;  
    Node2 prev;  
}
```

112



113

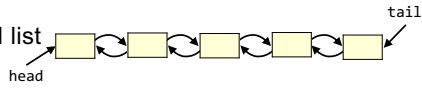


114

runtimes

115

### worst case doubly-linked list runtimes



- |                             |                      |
|-----------------------------|----------------------|
| - list.add(index, value)    | - list.addFront()    |
| - // $O(n)$                 | - // $O(1)$          |
| - list.removeByIndex(index) | - list.removeFront() |
| - // $O(n)$                 | - // $O(1)$          |
| - list.size()               | - list.addBack()     |
| - // $O(n)$                 | - // $O(1)$ 😊        |
|                             | - list.removeBack()  |
|                             | - // $O(1)$ 😊        |

116

### a doubly-linked list is a great way to implement a **deque** (double-ended queue)

- $O(1)$  addFront()
  - $O(1)$  removeFront()
  - $O(1)$  addBack()
  - $O(1)$  removeBack()
- 
- 🤔 could you pull this off with an **array list**?
  - no.
    - addFront() is  $O(n)$
- 
- 🤔 could you pull this off with an **array**?
  - sort of!—the **array deque** (amortized  $O(1)$  add)

117

something  
fun?

118