Image Analysis

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# **Chapter 1**

# Namespace Index

# 1.1 Packages

Here are the packages with brief descriptions (if available):

imagetools		 					 															Ş
imagetools.ml		 					 														 	ç
imagetools.plotting		 					 														 	10
imagetools.signals		 					 														 	11
inverse_problems		 					 															13
lgd																						
seament		 					 															30

2 Namespace Index

# Chapter 2

# **Hierarchical Index**

# 2.1 Class Hierarchy

This inheritance list is sorted roughly, but not completely, alphabetically:

imagetools.ml.KMeans_Custom	35
nn.Module	
lgd.LGD_net	38
lad.prox net	40

4 Hierarchical Index

# **Chapter 3**

# **Class Index**

# 3.1 Class List

Here are the classes, structs, unions and interfaces with brief descriptions:

imagetools.ml.KMeans_Custom	
Implements a class that handles KMeans Clustering	35
lgd.LGD_net	38
lad prov. net	40

6 Class Index

# **Chapter 4**

# File Index

# 4.1 File List

Here is a list of all files with brief descriptions:

/home/jhughes2712/projects/image_analysis/jh2284/src/inverse_problems.py	
Script running code for questions 2.1, 2.2, 2.3, and 3.1	45
/home/jhughes2712/projects/image_analysis/jh2284/src/lgd.py	
Script for training LGD	47
/home/jhughes2712/projects/image_analysis/jh2284/src/segment.py	
Script running code for segmentation problems	48
/home/jhughes2712/projects/image_analysis/jh2284/src/imagetools/initpy	43
/home/jhughes2712/projects/image_analysis/jh2284/src/imagetools/ml.py	
Module containing implementations of machine learning algorithms	43
/home/jhughes2712/projects/image_analysis/jh2284/src/imagetools/plotting.py	
Module building on matplotlib to provide image-specific plotting functions	44
/home/jhughes2712/projects/image_analysis/jh2284/src/imagetools/signals.py	
Module providing useful functions for image processing when employing Fourier and Wavelet	
transforms	44

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# **Chapter 5**

# **Namespace Documentation**

# 5.1 imagetools Namespace Reference

# **Namespaces**

- ml
- plotting
- signals

# 5.2 imagetools.ml Namespace Reference

#### **Classes**

• class KMeans\_Custom

Implements a class that handles KMeans Clustering.

#### **Functions**

• def gradient\_descent (obj, grad, x0, obj\_min, eps, lr, max\_iters, filename)

Implements vanilla gradient descent for scalar functions on R2.

#### 5.2.1 Function Documentation

#### 5.2.1.1 gradient\_descent()

```
def imagetools.ml.gradient_descent (
    obj,
    grad,
    x0,
    obj_min,
    eps,
    lr,
    max_iters,
    filename )
```

Implements vanilla gradient descent for scalar functions on R2.

```
@param obj The objective function to minimise.
@param grad The gradient of the objective function (R^2-->R^2)
@param x0 The initial iterate
@param obj_min The minimal value of the objective function
@param eps The threshold error for the stopping criterion
@param lr The learning rate
@param max_iters The maximum number of iterations to run before terminating
@param filename Determines the name of the trajectory and loss plot file
@return x estimated argmin (in R^2) of the objective
```

# 5.3 imagetools.plotting Namespace Reference

#### **Functions**

• def plot\_image (ax\_sp, img, title, cmap, gt=None)

#### 5.3.1 Function Documentation

#### 5.3.1.1 plot\_image()

# 5.4 imagetools.signals Namespace Reference

# **Functions**

```
    def iterative_soft_thresholding (data_sampled, lam, n_iters, gt=None)
        Implements ISTA in 1D.

    def fft1c (x)
    def ifft1c (y)
```

- def ComplexSoftThresh (y, lam)
- def coeffs2img (LL, coeffs)
- def img2coeffs (Wim, levels=4)
- def unstack\_coeffs (Wim)
- def dwt2 (im)
- def idwt2 (Wim)

#### 5.4.1 Function Documentation

#### 5.4.1.1 coeffs2img()

# 5.4.1.2 ComplexSoftThresh()

```
def imagetools.signals.ComplexSoftThresh ( \emph{y}, \emph{lam} )
```

# 5.4.1.3 dwt2()

# 5.4.1.4 fft1c()

```
\begin{tabular}{ll} $\operatorname{def imagetools.signals.fftlc} & ( \\ & x \end{tabular} \label{eq:constraints}
```

# 5.4.1.5 idwt2()

```
\begin{tabular}{ll} $\tt def imagetools.signals.idwt2 ( \\ $\tt \textit{Wim} )$ \\ \end{tabular}
```

# 5.4.1.6 ifft1c()

```
def imagetools.signals.ifft1c ( y )
```

#### 5.4.1.7 img2coeffs()

```
def imagetools.signals.img2coeffs ( \it Wim, \it levels = 4 )
```

# 5.4.1.8 iterative\_soft\_thresholding()

# Implements ISTA in 1D.

```
<code>@param data_sampled The subsampled measurement vector</code> <code>@param lam The soft-thresholding (regularisation) parameter</code> <code>@param n_iters Number of iterations</code> <code>@param gt Ground truth measurements to compare to</code> <code>@return predictions (N, P) array of centroids</code>
```

# 5.4.1.9 unstack\_coeffs()

```
\label{eq:coeffs} \mbox{def imagetools.signals.unstack\_coeffs (} $\mbox{\it Wim}$ )
```

# 5.5 inverse problems Namespace Reference

#### **Variables**

```
    file_list = f.read().split("\n")[:-1]

    y noisy = np.array([float(x) for x in file list])

• y_outlier = np.array([float(x) for x in file_list])
x = np.arange(len(y noisy))
• a noisy 12 = \text{np.sum}(x * y \text{ noisy}) / \text{np.sum}(x * x)
b_noisy_l2 = np.mean(y_noisy) - a_noisy_l2 * np.mean(x)
a_outlier_I2 = np.sum(x * y_outlier) / np.sum(x * x)
• b_outlier_l2 = np.mean(y_outlier) - a_outlier_l2 * np.mean(x)
• fig

    ax

· figsize
• list B coefs = []
• obj_l1 = lambda B: np.sum(np.abs(B[0] \times x + B[1] - y))
• B0 = np.array([0.1, 0.1])
• float lr = 0.0001
rng = np.random.default_rng(seed=42)
• signal = np.zeros(100)
• data = fft1c(signal)
• int sample freq = 4
• mask random = rng.uniform(0, 1, 100)
mask unif = np.zeros(100)
• start index = rng.integers(0, sample freq)
• sample_random = mask_random * data
sample_unif = mask_unif * data
int signal_random = ifft1c(sample_random) * sample_freq
• int signal_unif = ifft1c(sample_unif) * sample_freq
data_random_recon
· mse random

    lam

n_iters = 1000

    gt

· data_unif_recon

    mse unif

    int signal random recon = ifft1c(data random recon) * sample freq

• int signal_unif_recon = ifft1c(data_unif_recon) * sample_freq

    label

· title

    xlabel

    ylabel

    river img = skimage.io.imread("data/river side.jpeg")

river img dw = dwt2(river img)
river_img_recon = idwt2(river_img_dw)
th = np.quantile(abs(river_img_dw), 0.85)
• river_img_dw_th = abs(river_img_dw) > th

    tuple plotrange

• aximg0 = ax[0].imshow(abs(river img dw), vmin=plotrange[0], vmax=plotrange[1])
• aximg1 = ax[1].imshow(abs(river img dw th), cmap="grey")
• float obj = lambda x: 0.5 * (x[0] ** 2) + (x[1] ** 2)
• grad = lambda x: np.array([x[0], 2.0 * x[1]])
• x0 = np.array([1.0, 1.0])
• float eps = 0.01
float obj_min = 0.0
```

# 5.5.1 Variable Documentation

```
5.5.1.1 a_noisy_I2
inverse_problems.a_noisy_12 = np.sum(x * y_noisy) / np.sum(x * x)
5.5.1.2 a_outlier_I2
inverse_problems.a_outlier_12 = np.sum(x * y_outlier) / np.sum(x * x)
5.5.1.3 ax
inverse_problems.ax
5.5.1.4 aximg0
inverse_problems.aximg0 = ax[0].imshow(abs(river_img_dw), vmin=plotrange[0], vmax=plotrange[1])
5.5.1.5 aximg1
inverse_problems.aximg1 = ax[1].imshow(abs(river_img_dw_th), cmap="grey")
5.5.1.6 B
```

inverse\_problems.B = gradient\_descent(obj\_l1, grad\_l1, B0, 0, 0.01, lr, 100, "gd\_l1")

# 5.5.1.7 B0

```
inverse_problems.B0 = np.array([0.1, 0.1])
```

# 5.5.1.8 B\_coefs

```
list inverse_problems.B_coefs = []
```

# 5.5.1.9 b\_noisy\_l2

```
inverse\_problems.b\_noisy\_12 = np.mean(y\_noisy) - a\_noisy\_12 * np.mean(x)
```

# 5.5.1.10 b\_outlier\_I2

```
inverse_problems.b_outlier_12 = np.mean(y_outlier) - a_outlier_12 * np.mean(x)
```

#### 5.5.1.11 data

```
inverse_problems.data = fft1c(signal)
```

# 5.5.1.12 data\_random\_recon

 $\verb|inverse_problems.data_random_recon|\\$ 

#### 5.5.1.13 data\_unif\_recon

inverse\_problems.data\_unif\_recon

# 5.5.1.14 eps

float inverse\_problems.eps = 0.01

# 5.5.1.15 fig

inverse\_problems.fig

# 5.5.1.16 figsize

inverse\_problems.figsize

# 5.5.1.17 file\_list

```
inverse_problems.file_list = f.read().split("\n")[:-1]
```

#### 5.5.1.18 grad

```
inverse_problems.grad = lambda x: np.array([x[0], 2.0 * x[1]])
```

# 5.5.1.19 grad\_l1

inverse\_problems.grad\_11

#### Initial value:

# 5.5.1.20 gt

inverse\_problems.gt

#### 5.5.1.21 label

inverse\_problems.label

#### 5.5.1.22 lam

inverse\_problems.lam

# 5.5.1.23 Ir

float inverse\_problems.lr = 0.0001

# 5.5.1.24 mask\_random

inverse\_problems.mask\_random = rng.uniform(0, 1, 100)

# 5.5.1.25 mask\_unif

 $inverse\_problems.mask\_unif = np.zeros(100)$ 

#### 5.5.1.26 mse\_random

inverse\_problems.mse\_random

# 5.5.1.27 mse\_unif

inverse\_problems.mse\_unif

#### 5.5.1.28 n\_iters

int inverse\_problems.n\_iters = 1000

# 5.5.1.29 obj

float inverse\_problems.obj = lambda x: 0.5 \* (x[0] \*\* 2) + (x[1] \*\* 2)

# 5.5.1.30 obj\_l1

inverse\_problems.obj\_l1 = lambda B: np.sum(np.abs(B[0] \* x + B[1] - y))

#### 5.5.1.31 obj\_min

```
float inverse_problems.obj_min = 0.0
```

#### 5.5.1.32 plotrange

tuple inverse\_problems.plotrange

#### Initial value:

```
1 = (
2     np.quantile(abs(river_img_dw), 0.005),
3     np.quantile(abs(river_img_dw), 0.995),
4 )
```

# 5.5.1.33 river\_img

```
inverse_problems.river_img = skimage.io.imread("data/river_side.jpeg")
```

# 5.5.1.34 river\_img\_dw

```
inverse_problems.river_img_dw = dwt2(river_img)
```

# 5.5.1.35 river\_img\_dw\_th

```
{\tt inverse\_problems.river\_img\_dw\_th = abs(river\_img\_dw) > th}
```

# 5.5.1.36 river\_img\_recon

```
inverse_problems.river_img_recon = idwt2(river_img_dw)
```

# 5.5.1.37 rng

```
inverse_problems.rng = np.random.default_rng(seed=42)
```

# 5.5.1.38 sample\_freq

```
int inverse_problems.sample_freq = 4
```

#### 5.5.1.39 sample\_random

```
inverse_problems.sample_random = mask_random * data
```

# 5.5.1.40 sample\_unif

```
inverse_problems.sample_unif = mask_unif * data
```

#### 5.5.1.41 signal

```
inverse_problems.signal = np.zeros(100)
```

# 5.5.1.42 signal\_random

```
int inverse_problems.signal_random = ifft1c(sample_random) * sample_freq
```

#### 5.5.1.43 signal\_random\_recon

```
int inverse_problems.signal_random_recon = ifftlc(data_random_recon) * sample_freq
```

#### 5.5.1.44 signal\_unif

```
int inverse_problems.signal_unif = ifftlc(sample_unif) * sample_freq
```

# 5.5.1.45 signal\_unif\_recon

```
int inverse_problems.signal_unif_recon = ifftlc(data_unif_recon) * sample_freq
```

#### 5.5.1.46 start\_index

```
inverse_problems.start_index = rng.integers(0, sample_freq)
```

#### 5.5.1.47 th

```
inverse_problems.th = np.quantile(abs(river_img_dw), 0.85)
```

#### 5.5.1.48 title

inverse\_problems.title

#### 5.5.1.49 x

```
inverse_problems.x = np.arange(len(y_noisy))
```

#### 5.5.1.50 x0

```
inverse\_problems.x0 = np.array([1.0, 1.0])
```

#### 5.5.1.51 xlabel

inverse\_problems.xlabel

# 5.5.1.52 y\_noisy

```
inverse\_problems.y\_noisy = np.array([float(x) for x in file\_list])
```

# 5.5.1.53 y\_outlier

```
inverse_problems.y_outlier = np.array([float(x) for x in file_list])
```

#### 5.5.1.54 ylabel

```
inverse_problems.ylabel
```

# 5.6 Igd Namespace Reference

#### **Classes**

```
    class prox_net
```

· class LGD net

#### **Variables**

```
• parser = argparse.ArgumentParser()
type
• str

    choices

    required

• args = parser.parse_args()
• int img size = 256
• reco_space
• int num_angles = 30
• geometry = odl.tomo.parallel_beam_geometry(reco_space, num_angles=num_angles)

    fwd_op_odl = odl.tomo.RayTransform(reco_space, geometry)

· fbp_op_odl
• adj_op_odl = fwd_op_odl.adjoint

    phantom_odl = odl.phantom.shepp_logan(reco_space, modified=True)

data_odl = fwd_op_odl(phantom_odl)
• fbp_odl = fbp_op_odl(data_odl)
phantom_np = phantom_odl.__array__()
• fbp_np = fbp_odl.__array__()
data_np = data_odl.__array__()
• fig

    ax

• figsize
• grad = odl.Gradient(reco space)

    L = odl.BroadcastOperator(fwd_op_odl, grad)

    data_fit = odl.solvers.L2NormSquared(fwd_op_odl.range).translated(data_odl)

• float lam = 0.015

    float reg_func = lam * odl.solvers.L1Norm(grad.range)

• g = odl.solvers.SeparableSum(data fit, reg func)
• f = odl.solvers.ZeroFunctional(L.domain)
• float op_norm = 1.1 * odl.power_method_opnorm(L, maxiter=20)
• int niter = 200
• float sigma = 2.0
• float tau = sigma / op_norm**2
· callback
x_admm_odl = L.domain.zero()
x_admm_np = x_admm_odl.__array__()
```

tuple device

- int step\_size = 1 / op\_norm
- lgd\_net = LGD\_net().to(device)
- num\_learnable\_params
- tuple y
- tuple x\_init
- tuple ground\_truth
- mse\_loss = torch.nn.MSELoss()
- optimizer = torch.optim.Adam(lgd\_net.parameters(), lr=1e-4)
- int num\_epochs = 2000
- ckpt = torch.load("outputs/weights\_1990.pth", map\_location=device)
- int start\_idx = 1989
- losses = ckpt["losses"]
- int save\_interval = 1
- int verbose\_interval = 1
- recon = lgd\_net(y, x\_init)
- loss = mse\_loss(recon, ground\_truth)
- · dictionary checkpoint
- string checkpoint filepath = f"outputs/weights {epoch+1:03d}.pth"
- tuple lgd\_recon\_np

#### 5.6.1 Variable Documentation

#### 5.6.1.1 adj\_op\_odl

```
lgd.adj_op_odl = fwd_op_odl.adjoint
```

#### 5.6.1.2 args

```
lgd.args = parser.parse_args()
```

#### 5.6.1.3 ax

lgd.ax

#### 5.6.1.4 callback

lgd.callback

#### Initial value:

```
1 = odl.solvers.CallbackPrintIteration(
2 step=10
     step=10
3 ) & odl.solvers.CallbackShow(step=10)
```

#### 5.6.1.5 checkpoint

dictionary lgd.checkpoint

#### Initial value:

```
"epoch": epoch + 1,
"state_dict": lgd_net.state_dict(),
"optimizer": optimizer.state_dict(),
"losses": losses,
```

#### 5.6.1.6 checkpoint\_filepath

```
string lgd.checkpoint_filepath = f"outputs/weights_{epoch+1:03d}.pth"
```

#### 5.6.1.7 choices

lgd.choices

# 5.6.1.8 ckpt

```
lgd.ckpt = torch.load("outputs/weights_1990.pth", map_location=device)
```

# 5.6.1.9 data\_fit

```
lgd.data_fit = odl.solvers.L2NormSquared(fwd_op_odl.range).translated(data_odl)
```

#### 5.6.1.10 data\_np

```
lgd.data_np = data_odl.__array__()
```

#### 5.6.1.11 data\_odl

```
lgd.data_odl = fwd_op_odl(phantom_odl)
```

# 5.6.1.12 device

tuple lgd.device

# Initial value:

```
1 = (
2    torch.device("cuda") if torch.cuda.is_available() else torch.device("cpu")
3 )
```

# 5.6.1.13 f

```
lgd.f = odl.solvers.ZeroFunctional(L.domain)
```

#### 5.6.1.14 fbp\_np

```
lgd.fbp_np = fbp_odl.__array__()
```

# 5.6.1.15 fbp\_odl

```
lgd.fbp_odl = fbp_op_odl(data_odl)
```

# 5.6.1.16 fbp\_op\_odl

```
lgd.fbp_op_odl
```

#### Initial value:

```
1 = odl.tomo.fbp_op(
    fwd_op_odl, filter_type="Ram-Lak", frequency_scaling=0.6
3 )
```

# 5.6.1.17 fig

lgd.fig

#### 5.6.1.18 figsize

lgd.figsize

# 5.6.1.19 fwd\_op\_odl

```
lgd.fwd_op_odl = odl.tomo.RayTransform(reco_space, geometry)
```

# 5.6.1.20 g

```
lgd.g = odl.solvers.SeparableSum(data_fit, reg_func)
```

#### 5.6.1.21 geometry

```
lgd.geometry = odl.tomo.parallel_beam_geometry(reco_space, num_angles=num_angles)
```

# 5.6.1.22 grad

```
lgd.grad = odl.Gradient(reco_space)
```

# 5.6.1.23 ground\_truth

```
tuple lgd.ground_truth
```

#### Initial value:

```
1 = (
2          torch.from_numpy(phantom_np).to(device).unsqueeze(0)
3 )
```

# 5.6.1.24 gt

lgd.gt

# 5.6.1.25 img\_size

```
int lgd.img_size = 256
```

# 5.6.1.26 L

```
lgd.L = odl.BroadcastOperator(fwd_op_odl, grad)
```

#### 5.6.1.27 lam

```
float lgd.lam = 0.015
```

# 5.6.1.28 lgd\_net

```
lgd.lgd_net = LGD_net().to(device)
```

# 5.6.1.29 lgd\_recon\_np

```
tuple lgd.lgd_recon_np
```

#### Initial value:

```
1 = (
2          recon.detach().cpu().numpy().squeeze()
3 )
```

#### 5.6.1.30 loss

```
lgd.loss = mse_loss(recon, ground_truth)
```

# 5.6.1.31 losses

```
list lgd.losses = ckpt["losses"]
```

# 5.6.1.32 mse\_loss

```
lgd.mse_loss = torch.nn.MSELoss()
```

# 5.6.1.33 niter

```
lgd.niter = 200
```

# 5.6.1.34 num\_angles

```
int lgd.num_angles = 30
```

#### 5.6.1.35 num\_epochs

```
int lgd.num_epochs = 2000
```

#### 5.6.1.36 num\_learnable\_params

lgd.num\_learnable\_params

# Initial value:

```
1 = sum(
2    p.numel() for p in lgd_net.parameters() if p.requires_grad
3 )
```

#### 5.6.1.37 op\_norm

```
float lgd.op_norm = 1.1 * odl.power_method_opnorm(L, maxiter=20)
```

# 5.6.1.38 optimizer

```
lgd.optimizer = torch.optim.Adam(lgd_net.parameters(), lr=1e-4)
```

#### 5.6.1.39 parser

```
lgd.parser = argparse.ArgumentParser()
```

#### 5.6.1.40 phantom\_np

```
lgd.phantom_np = phantom_odl.__array__()
```

#### 5.6.1.41 phantom\_odl

```
lgd.phantom_odl = odl.phantom.shepp_logan(reco_space, modified=True)
```

#### 5.6.1.42 reco\_space

lgd.reco\_space

#### Initial value:

```
1 = odl.uniform_discr(
2     min_pt=[-20, -20],
3     max_pt=[20, 20],
4     shape=[img_size, img_size],
5     dtype="float32",
6 )
```

# 5.6.1.43 recon

```
lgd.recon = lgd_net(y, x_init)
```

# 5.6.1.44 reg\_func

```
float lgd.reg_func = lam * odl.solvers.L1Norm(grad.range)
```

# 5.6.1.45 required

lgd.required

# 5.6.1.46 save\_interval

```
int lgd.save_interval = 1
```

#### 5.6.1.47 sigma

```
lgd.sigma = 2.0
```

#### 5.6.1.48 start\_idx

```
int lgd.start_idx = 1989
```

#### 5.6.1.49 step\_size

```
int lgd.step_size = 1 / op_norm
```

#### 5.6.1.50 str

lgd.str

#### 5.6.1.51 tau

```
lgd.tau = sigma / op_norm**2
```

#### 5.6.1.52 type

lgd.type

#### 5.6.1.53 verbose\_interval

```
int lgd.verbose_interval = 1
```

#### 5.6.1.54 x\_admm\_np

```
lgd.x_admm_np = x_admm_odl.__array__()
```

#### 5.6.1.55 x\_admm\_odl

```
lgd.x_admm_odl = L.domain.zero()
```

#### 5.6.1.56 x\_init

```
tuple lgd.x_init
```

#### Initial value:

```
1 = (
2     torch.from_numpy()
3         fbp_op_od1(y.detach().cpu().numpy().squeeze()).__array__()
4     )
5     .to(device)
6     .unsqueeze(0)
7     )
```

#### 5.6.1.57 y

```
tuple lgd.y
```

#### Initial value:

```
1 = (
2    torch.from_numpy(data_np).to(device).unsqueeze(0)
3 )
```

#### 5.7 segment Namespace Reference

#### **Variables**

- fig
- ax
- figsize
- ct\_img = skimage.io.imread("data/CT.png")
- ct\_threshold = threshold\_otsu(ct\_img)
- ct\_segmented = ct\_img > ct\_threshold
- se = disk(4)
- ct\_mask = remove\_small\_objects(binary\_opening(ct\_segmented, se))
- ct\_labelled = label(ct\_mask == 0)
- ct\_props = regionprops(ct\_labelled)
- lung\_idx = sorted(list(range(3)), key=lambda i: ct\_props[i].area)[:2]
- cmap
- coins\_img = skimage.io.imread("data/coins.png")
- coins\_marked = coins\_img.copy()
- coins\_pre = rank.median(coins\_img, np.ones((1, 7)))
- int coins\_segmented = 1 chan\_vese(coins\_pre, mu=0.1)
- coins\_labelled = label(coins\_segmented)
- list desired\_coins\_idx
- flowers\_img = skimage.io.imread("data/noisy\_flower.jpg")
- flowers\_pre = denoise\_tv\_bregman(flowers\_img, weight=0.5)
- km = KMeans\_Custom(K=6)
- flowers\_data = flowers\_pre[::8, ::8, :].reshape(-1, 3)
- verbose
- flowers\_flat = flowers\_pre.reshape(-1, 3)
- flowers\_segmented = km.predict\_cluster(flowers\_flat)
- int flowers\_purple = 0

#### 5.7.1 Variable Documentation

# 5.7.1.1 ax segment.ax

#### 5.7.1.2 cmap

segment.cmap

#### 5.7.1.3 coins\_img

```
tuple segment.coins_img = skimage.io.imread("data/coins.png")
```

#### 5.7.1.4 coins\_labelled

```
segment.coins_labelled = label(coins_segmented)
```

#### 5.7.1.5 coins\_marked

```
segment.coins_marked = coins_img.copy()
```

#### 5.7.1.6 coins\_pre

```
segment.coins_pre = rank.median(coins_img, np.ones((1, 7)))
```

#### 5.7.1.7 coins\_segmented

```
segment.coins_segmented = 1 - chan_vese(coins_pre, mu=0.1)
```

#### 5.7.1.8 ct\_img

```
segment.ct_img = skimage.io.imread("data/CT.png")
```

#### 5.7.1.9 ct\_labelled

```
float segment.ct_labelled = label(ct_mask == 0)
```

#### 5.7.1.10 ct\_mask

```
segment.ct_mask = remove_small_objects(binary_opening(ct_segmented, se))
```

#### 5.7.1.11 ct\_props

```
segment.ct_props = regionprops(ct_labelled)
```

#### 5.7.1.12 ct\_segmented

```
segment.ct\_segmented = ct\_img > ct\_threshold
```

#### 5.7.1.13 ct\_threshold

```
segment.ct_threshold = threshold_otsu(ct_img)
```

#### 5.7.1.14 desired\_coins\_idx

list segment.desired\_coins\_idx

#### Initial value:

#### 5.7.1.15 fig

```
segment.fig
```

#### 5.7.1.16 figsize

```
segment.figsize
```

#### 5.7.1.17 flowers\_data

```
segment.flowers_data = flowers_pre[::8, ::8, :].reshape(-1, 3)
```

#### 5.7.1.18 flowers\_flat

```
segment.flowers_flat = flowers_pre.reshape(-1, 3)
```

#### 5.7.1.19 flowers\_img

```
segment.flowers_img = skimage.io.imread("data/noisy_flower.jpg")
```

#### 5.7.1.20 flowers\_pre

```
segment.flowers_pre = denoise_tv_bregman(flowers_img, weight=0.5)
```

#### 5.7.1.21 flowers\_purple

```
segment.flowers_purple = 0
```

#### 5.7.1.22 flowers\_segmented

```
segment.flowers_segmented = km.predict_cluster(flowers_flat)
```

#### 5.7.1.23 km

```
segment.km = KMeans_Custom(K=6)
```

#### 5.7.1.24 lung\_idx

```
segment.lung_idx = sorted(list(range(3)), key=lambda i: ct_props[i].area)[:2]
```

#### 5.7.1.25 se

```
segment.se = disk(4)
```

#### 5.7.1.26 verbose

segment.verbose

### **Chapter 6**

### **Class Documentation**

#### 6.1 imagetools.ml.KMeans\_Custom Class Reference

Implements a class that handles KMeans Clustering.

#### **Public Member Functions**

- def init (self, K)
- def assignment (self, data)

Assigns a matrix where each row represents the assigned centroid.

• def fit (self, data, verbose=10, limit=1e5)

Fits the KMeans clusters.

• def predict (self, data)

Returns an array whose rows are the closest centroid to each datum.

• def predict\_cluster (self, data)

Returns an array whose entries are the closest centroid to each datum, mapped to a single identifying integer.

#### **Public Attributes**

- K
- · centroids

#### 6.1.1 Detailed Description

Implements a class that handles KMeans Clustering.

#### 6.1.2 Constructor & Destructor Documentation

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#### 6.1.2.1 \_\_init\_\_()

#### 6.1.3 Member Function Documentation

#### 6.1.3.1 assignment()

```
def imagetools.ml.KMeans_Custom.assignment ( self, data )
```

Assigns a matrix where each row represents the assigned centroid.

#### **Parameters**

```
data The data to assign labels to. Must be an (N, P) array.
```

Returns

labels

#### 6.1.3.2 fit()

#### Fits the KMeans clusters.

```
 \hbox{\tt @details Uses the KMeans++ algorithm to initialise centroids,} \\ \hbox{\tt and then iteratively updates them using Lloyd's algorithm.}
```

<code>@param</code> data The data to assign labels to. Must be an  $(N,\ P)$  array. <code>@param</code> verbose How often to print out number of reassigned labels. <code>@param</code> limit Maximum number of iterations before stopping. Prevents an indefinite loop.

#### 6.1.3.3 predict()

Returns an array whose rows are the closest centroid to each datum.

#### **Parameters**

data The data to assign labels to. Must be an (N, P) array.

#### Returns

predictions (N, P) array of centroids

#### 6.1.3.4 predict\_cluster()

Returns an array whose entries are the closest centroid to each datum, mapped to a single identifying integer.

#### **Parameters**

data The data to assign labels to. Must be an (N, P) array.

#### Returns

predictions (N, 1) array of predicted clusters

#### 6.1.4 Member Data Documentation

#### 6.1.4.1 centroids

imagetools.ml.KMeans\_Custom.centroids

#### 6.1.4.2 K

```
imagetools.ml.KMeans\_Custom.K
```

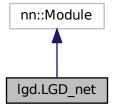
The documentation for this class was generated from the following file:

/home/jhughes2712/projects/image\_analysis/jh2284/src/imagetools/ml.py

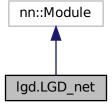
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### 6.2 lgd.LGD\_net Class Reference

Inheritance diagram for lgd.LGD\_net:



Collaboration diagram for lgd.LGD\_net:



#### **Public Member Functions**

- def \_\_init\_\_ (self, niter=5, step\_size=step\_size)
- def forward (self, y, x\_init)

#### **Public Attributes**

- niter
- prox
- step\_size
- fwd\_op\_torch
- adj\_op\_torch

#### 6.2.1 Constructor & Destructor Documentation

#### 6.2.1.1 \_\_init\_\_()

#### 6.2.2 Member Function Documentation

#### 6.2.2.1 forward()

```
def lgd.LGD_net.forward ( self, \\ y, \\ x\_init )
```

#### 6.2.3 Member Data Documentation

#### 6.2.3.1 adj\_op\_torch

```
lgd.LGD_net.adj_op_torch
```

#### 6.2.3.2 fwd\_op\_torch

```
{\tt lgd.LGD\_net.fwd\_op\_torch}
```

#### 6.2.3.3 niter

```
lgd.LGD_net.niter
```

#### 6.2.3.4 prox

```
lgd.LGD_net.prox
```

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#### 6.2.3.5 step\_size

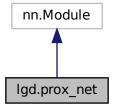
```
lgd.LGD_net.step_size
```

The documentation for this class was generated from the following file:

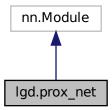
• /home/jhughes2712/projects/image\_analysis/jh2284/src/lgd.py

#### 6.3 Igd.prox\_net Class Reference

Inheritance diagram for lgd.prox\_net:



Collaboration diagram for lgd.prox\_net:



#### **Public Member Functions**

- def \_\_init\_\_ (self, n\_in\_channels=2, n\_out\_channels=1, n\_filters=32, kernel\_size=3)
- def forward (self, x, u)

#### **Public Attributes**

- pad
- conv1
- conv2
- conv3
- act1
- act2

#### 6.3.1 Constructor & Destructor Documentation

#### 6.3.1.1 \_\_init\_\_()

#### 6.3.2 Member Function Documentation

#### 6.3.2.1 forward()

#### ######### YOUR CODE HERE

#### 6.3.3 Member Data Documentation

#### 6.3.3.1 act1

```
lgd.prox_net.act1
```

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#### 6.3.3.2 act2

lgd.prox\_net.act2

#### 6.3.3.3 conv1

lgd.prox\_net.conv1

#### 6.3.3.4 conv2

lgd.prox\_net.conv2

#### 6.3.3.5 conv3

lgd.prox\_net.conv3

#### 6.3.3.6 pad

lgd.prox\_net.pad

The documentation for this class was generated from the following file:

• /home/jhughes2712/projects/image\_analysis/jh2284/src/lgd.py

### **Chapter 7**

### **File Documentation**

7.1 /home/jhughes2712/projects/image\_
analysis/jh2284/src/imagetools/\_\_init\_\_.py File Reference

#### **Namespaces**

· imagetools

## 7.2 /home/jhughes2712/projects/image\_ analysis/jh2284/src/imagetools/ml.py File Reference

Module containing implementations of machine learning algorithms.

#### **Classes**

class imagetools.ml.KMeans\_Custom
 Implements a class that handles KMeans Clustering.

#### **Namespaces**

· imagetools.ml

#### **Functions**

• def imagetools.ml.gradient\_descent (obj, grad, x0, obj\_min, eps, lr, max\_iters, filename)

Implements vanilla gradient descent for scalar functions on R2.

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#### 7.2.1 Detailed Description

Module containing implementations of machine learning algorithms.

Uses numpy to implement KMeans and Gradient Descent, in a way which is not as optimised as, say, scikit-learn, but is readable.

**Author** 

Created by J. Hughes on 8th June 2024.

## 7.3 /home/jhughes2712/projects/image\_← analysis/jh2284/src/imagetools/plotting.py File Reference

Module building on matplotlib to provide image-specific plotting functions.

#### **Namespaces**

· imagetools.plotting

#### **Functions**

• def imagetools.plotting.plot\_image (ax\_sp, img, title, cmap, gt=None)

#### 7.3.1 Detailed Description

Module building on matplotlib to provide image-specific plotting functions.

Author

Created by J. Hughes on 8th June 2024.

## 7.4 /home/jhughes2712/projects/image\_ analysis/jh2284/src/imagetools/signals.py File Reference

Module providing useful functions for image processing when employing Fourier and Wavelet transforms.

#### **Namespaces**

· imagetools.signals

#### **Functions**

- def imagetools.signals.iterative\_soft\_thresholding (data\_sampled, lam, n\_iters, gt=None)
   Implements ISTA in 1D.
- def imagetools.signals.fft1c (x)
- def imagetools.signals.ifft1c (y)
- · def imagetools.signals.ComplexSoftThresh (y, lam)
- def imagetools.signals.coeffs2img (LL, coeffs)
- def imagetools.signals.img2coeffs (Wim, levels=4)
- def imagetools.signals.unstack coeffs (Wim)
- def imagetools.signals.dwt2 (im)
- · def imagetools.signals.idwt2 (Wim)

#### 7.4.1 Detailed Description

Module providing useful functions for image processing when employing Fourier and Wavelet transforms.

Many of the functions are taken from the 'helper' module provided on the Image Analysis course GitLab page.

**Author** 

Created by J. Hughes on 8th June 2024.

## 7.5 /home/jhughes2712/projects/image\_analysis/jh2284/src/inverse\_← problems.py File Reference

Script running code for questions 2.1, 2.2, 2.3, and 3.1.

#### **Namespaces**

· inverse problems

#### **Variables**

- inverse problems.file list = f.read().split("\n")[:-1]
- inverse\_problems.y\_noisy = np.array([float(x) for x in file\_list])
- inverse\_problems.y\_outlier = np.array([float(x) for x in file\_list])
- inverse\_problems.x = np.arange(len(y\_noisy))
- inverse\_problems.a\_noisy\_l2 = np.sum(x \* y\_noisy) / np.sum(x \* x)
- inverse\_problems.b\_noisy\_l2 = np.mean(y\_noisy) a\_noisy\_l2 \* np.mean(x)
- inverse\_problems.a\_outlier\_l2 = np.sum(x \* y\_outlier) / np.sum(x \* x)
- inverse\_problems.b\_outlier\_I2 = np.mean(y\_outlier) a\_outlier\_I2 \* np.mean(x)
- · inverse\_problems.fig
- inverse\_problems.ax
- inverse\_problems.figsize
- list inverse problems.B coefs = []
- inverse problems.obj I1 = lambda B: np.sum(np.abs(B[0] \* x + B[1] y))
- inverse problems.grad I1
- inverse\_problems.B0 = np.array([0.1, 0.1])

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- float inverse\_problems.lr = 0.0001
- inverse\_problems.B = gradient\_descent(obj\_l1, grad\_l1, B0, 0, 0.01, lr, 100, "gd\_l1")
- inverse problems.rng = np.random.default rng(seed=42)
- inverse problems.signal = np.zeros(100)
- inverse problems.data = fft1c(signal)
- int inverse\_problems.sample\_freq = 4
- inverse\_problems.mask\_random = rng.uniform(0, 1, 100)
- inverse problems.mask unif = np.zeros(100)
- inverse problems.start index = rng.integers(0, sample freq)
- inverse problems.sample random = mask random \* data
- inverse problems.sample unif = mask unif \* data
- int inverse\_problems.signal\_random = ifft1c(sample\_random) \* sample\_freq
- int inverse\_problems.signal\_unif = ifft1c(sample\_unif) \* sample\_freq
- inverse\_problems.data\_random\_recon
- inverse problems.mse random
- · inverse problems.lam
- inverse\_problems.n\_iters = 1000
- · inverse problems.gt
- inverse\_problems.data\_unif\_recon
- · inverse problems.mse unif
- int inverse\_problems.signal\_random\_recon = ifft1c(data\_random\_recon) \* sample\_freq
- int inverse\_problems.signal\_unif\_recon = ifft1c(data\_unif\_recon) \* sample\_freq
- · inverse problems.label
- inverse\_problems.title
- inverse\_problems.xlabel
- inverse problems.ylabel
- inverse\_problems.river\_img = skimage.io.imread("data/river\_side.jpeg")
- inverse problems.river img dw = dwt2(river img)
- inverse\_problems.river\_img\_recon = idwt2(river\_img\_dw)
- inverse\_problems.th = np.quantile(abs(river\_img\_dw), 0.85)
- inverse\_problems.river\_img\_dw\_th = abs(river\_img\_dw) > th
- tuple inverse\_problems.plotrange
- inverse\_problems.aximg0 = ax[0].imshow(abs(river\_img\_dw), vmin=plotrange[0], vmax=plotrange[1])
- inverse\_problems.aximg1 = ax[1].imshow(abs(river\_img\_dw\_th), cmap="grey")
- float inverse\_problems.obj = lambda x: 0.5 \* (x[0] \*\* 2) + (x[1] \*\* 2)
- inverse\_problems.grad = lambda x: np.array([x[0], 2.0 \* x[1]])
- inverse problems.x0 = np.array([1.0, 1.0])
- float inverse\_problems.eps = 0.01
- float inverse problems.obj min = 0.0

#### 7.5.1 Detailed Description

Script running code for questions 2.1, 2.2, 2.3, and 3.1.

This script solves various inverse problems related to signal and image processing, employing various iterative strategies and signal transforms.

Author

Created by J. Hughes on 8th June 2024.

## 7.6 /home/jhughes2712/projects/image\_analysis/jh2284/src/lgd.py File Reference

Script for training LGD.

#### Classes

- class lgd.prox\_net
- class lgd.LGD\_net

#### **Namespaces**

• lgd

#### **Variables**

```
• lgd.parser = argparse.ArgumentParser()
```

- lgd.type
- · lgd.str
- lgd.choices
- · lgd.required
- lgd.args = parser.parse args()
- int lgd.img\_size = 256
- · lgd.reco\_space
- int lgd.num\_angles = 30
- lgd.geometry = odl.tomo.parallel\_beam\_geometry(reco\_space, num\_angles=num\_angles)
- lgd.fwd\_op\_odl = odl.tomo.RayTransform(reco\_space, geometry)
- lgd.fbp\_op\_odl
- lgd.adj\_op\_odl = fwd\_op\_odl.adjoint
- lgd.phantom\_odl = odl.phantom.shepp\_logan(reco\_space, modified=True)
- lgd.data\_odl = fwd\_op\_odl(phantom\_odl)
- lgd.fbp\_odl = fbp\_op\_odl(data\_odl)
- lgd.phantom\_np = phantom\_odl.\_\_array\_\_()
- lgd.fbp\_np = fbp\_odl.\_\_array\_\_()
- lgd.data\_np = data\_odl.\_\_array\_\_()
- lgd.fig
- lgd.ax
- lgd.figsize
- lgd.gt
- lgd.grad = odl.Gradient(reco\_space)
- lgd.L = odl.BroadcastOperator(fwd op odl, grad)
- lgd.data fit = odl.solvers.L2NormSquared(fwd op odl.range).translated(data odl)
- float lgd.lam = 0.015
- float lgd.reg\_func = lam \* odl.solvers.L1Norm(grad.range)
- lgd.g = odl.solvers.SeparableSum(data\_fit, reg\_func)
- lgd.f = odl.solvers.ZeroFunctional(L.domain)
- float lgd.op\_norm = 1.1 \* odl.power\_method\_opnorm(L, maxiter=20)
- int lgd.niter = 200
- float lgd.sigma = 2.0
- float lgd.tau = sigma / op\_norm\*\*2

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- · lgd.callback
- lgd.x\_admm\_odl = L.domain.zero()
- lgd.x\_admm\_np = x\_admm\_odl.\_\_array\_\_()
- tuple lgd.device
- int lgd.step\_size = 1 / op\_norm
- lgd.lgd\_net = LGD\_net().to(device)
- lgd.num\_learnable\_params
- · tuple lgd.y
- tuple lgd.x\_init
- · tuple lgd.ground truth
- lgd.mse loss = torch.nn.MSELoss()
- lgd.optimizer = torch.optim.Adam(lgd\_net.parameters(), Ir=1e-4)
- int lgd.num\_epochs = 2000
- lgd.ckpt = torch.load("outputs/weights\_1990.pth", map\_location=device)
- int lgd.start idx = 1989
- lgd.losses = ckpt["losses"]
- int lgd.save\_interval = 1
- int lgd.verbose\_interval = 1
- lgd\_recon = lgd\_net(y, x\_init)
- lgd.loss = mse\_loss(recon, ground\_truth)
- · dictionary lgd.checkpoint
- string lgd.checkpoint\_filepath = f"outputs/weights\_{epoch+1:03d}.pth"
- tuple lgd.lgd\_recon\_np

#### 7.6.1 Detailed Description

Script for training LGD.

Reconstructs CT images using FBP and ADMM, and compares to a data-driven LGD algorithm. Can be run in 'demo' mode, just performing the last 10 epochs of training from a checkpoint, or 'full' mode which runs all 2000 training epochs.

**Author** 

Created by J. Hughes on 8th June 2024.

## 7.7 /home/jhughes2712/projects/image\_analysis/jh2284/src/segment.py File Reference

Script running code for segmentation problems.

#### **Namespaces**

segment

#### **Variables**

- · segment.fig
- · segment.ax
- · segment.figsize
- segment.ct\_img = skimage.io.imread("data/CT.png")
- segment.ct threshold = threshold otsu(ct img)
- segment.ct\_segmented = ct\_img > ct\_threshold
- segment.se = disk(4)
- segment.ct mask = remove small objects(binary opening(ct segmented, se))
- segment.ct\_labelled = label(ct\_mask == 0)
- segment.ct props = regionprops(ct labelled)
- segment.lung\_idx = sorted(list(range(3)), key=lambda i: ct\_props[i].area)[:2]
- · segment.cmap
- segment.coins\_img = skimage.io.imread("data/coins.png")
- segment.coins marked = coins img.copy()
- segment.coins\_pre = rank.median(coins\_img, np.ones((1, 7)))
- int segment.coins\_segmented = 1 chan\_vese(coins\_pre, mu=0.1)
- segment.coins\_labelled = label(coins\_segmented)
- · list segment.desired coins idx
- segment.flowers img = skimage.io.imread("data/noisy flower.jpg")
- segment.flowers\_pre = denoise\_tv\_bregman(flowers\_img, weight=0.5)
- segment.km = KMeans Custom(K=6)
- segment.flowers\_data = flowers\_pre[::8, ::8, :].reshape(-1, 3)
- · segment.verbose
- segment.flowers flat = flowers pre.reshape(-1, 3)
- segment.flowers segmented = km.predict cluster(flowers flat)
- int segment.flowers\_purple = 0

#### 7.7.1 Detailed Description

Script running code for segmentation problems.

This script segments the three images given on the question sheet using three different segmentation algorithms.

Author

Created by J. Hughes on 8th June 2024.

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