

Image Analysis

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Chapter 1

Namespace Index

1.1 Packages

Here are the packages with brief descriptions (if available):

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| imagetools.signals | 11 |
| inverse_problems | 13 |
| lgd | 21 |
| segment | 30 |

Chapter 2

Hierarchical Index

2.1 Class Hierarchy

This inheritance list is sorted roughly, but not completely, alphabetically:

| | |
|---------------------------------------|----|
| imagetools.ml.KMeans_Custom | 35 |
| nn.Module | |
| lgd.LGD_net | 38 |
| lgd.prox_net | 40 |

Chapter 3

Class Index

3.1 Class List

Here are the classes, structs, unions and interfaces with brief descriptions:

| | | |
|---|-------|--------------------|
| imagetools.ml.KMeans_Custom | | |
| Implements a class that handles KMeans Clustering | | 35 |
| lgd.LGD_net | | 38 |
| lgd.prox_net | | 40 |

Chapter 4

File Index

4.1 File List

Here is a list of all files with brief descriptions:

| | |
|--|----|
| /home/jhughes2712/projects/image_analysis/jh2284/src/ inverse_problems.py | |
| Script running code for questions 2.1, 2.2, 2.3, and 3.1 | 45 |
| /home/jhughes2712/projects/image_analysis/jh2284/src/ lgd.py | |
| Script for training LGD | 47 |
| /home/jhughes2712/projects/image_analysis/jh2284/src/ segment.py | |
| Script running code for segmentation problems | 48 |
| /home/jhughes2712/projects/image_analysis/jh2284/src/imagetools/ __init__.py | 43 |
| /home/jhughes2712/projects/image_analysis/jh2284/src/imagetools/ ml.py | |
| Module containing implementations of machine learning algorithms | 43 |
| /home/jhughes2712/projects/image_analysis/jh2284/src/imagetools/ plotting.py | |
| Module building on matplotlib to provide image-specific plotting functions | 44 |
| /home/jhughes2712/projects/image_analysis/jh2284/src/imagetools/ signals.py | |
| Module providing useful functions for image processing when employing Fourier and Wavelet transforms | 44 |

Chapter 5

Namespace Documentation

5.1 imagetools Namespace Reference

Namespaces

- [ml](#)
- [plotting](#)
- [signals](#)

5.2 imagetools.ml Namespace Reference

Classes

- class [KMeans_Custom](#)
Implements a class that handles KMeans Clustering.

Functions

- def [gradient_descent](#) (obj, grad, x0, obj_min, eps, lr, max_iters, filename)
Implements vanilla gradient descent for scalar functions on R2, where the true global minimum is known.

5.2.1 Function Documentation

5.2.1.1 [gradient_descent\(\)](#)

```
def imagetools.ml.gradient_descent (
    obj,
    grad,
    x0,
    obj_min,
    eps,
    lr,
    max_iters,
    filename )
```

Implements vanilla gradient descent for scalar functions on R2, where the true global minimum is known.

Parameters

| | |
|------------------|--|
| <i>obj</i> | The objective function to minimise. |
| <i>grad</i> | The gradient of the objective function ($R^2 \rightarrow R^2$) |
| <i>x0</i> | The initial iterate |
| <i>obj_min</i> | The minimal value of the objective function |
| <i>eps</i> | The threshold error for the stopping criterion |
| <i>lr</i> | The learning rate |
| <i>max_iters</i> | The maximum number of iterations to run before terminating |
| <i>filename</i> | Determines the name of the trajectory and loss plot file |

Returns

x estimated argmin (in R^2) of the objective

5.3 imagetools.plotting Namespace Reference

Functions

- def [plot_image](#) (ax_sp, img, title, cmap, gt=None)
Plots an image and compares to GT.

5.3.1 Function Documentation

5.3.1.1 plot_image()

```
def imagetools.plotting.plot_image (
    ax_sp,
    img,
    title,
    cmap,
    gt = None )
```

Plots an image and compares to GT.

```
@param ax_sp Specified matplotlib.pyplot.Axes object
@param img Image to be displayed
@param title Image title string
@param cmap String defining matplotlib colormap for image
@param gt Ground truth measurements to compare to
```

5.4 imagetools.signals Namespace Reference

Functions

- def [iterative_soft_thresholding](#) (data_sampled, lam, n_iters, gt=None)
Implements ISTA in 1D.
- def [fft1c](#) (x)
- def [ifft1c](#) (y)
- def [ComplexSoftThresh](#) (y, lam)
- def [coeffs2img](#) (LL, coeffs)
- def [img2coeffs](#) (Wim, levels=4)
- def [unstack_coeffs](#) (Wim)
- def [dwt2](#) (im)
- def [idwt2](#) (Wim)

5.4.1 Function Documentation

5.4.1.1 coeffs2img()

```
def imagetools.signals.coeffs2img (
    LL,
    coeffs )
```

5.4.1.2 ComplexSoftThresh()

```
def imagetools.signals.ComplexSoftThresh (
    Y,
    lam )
```

5.4.1.3 dwt2()

```
def imagetools.signals.dwt2 (
    im )
```

5.4.1.4 fft1c()

```
def imagetools.signals.fft1c (
    x )
```

5.4.1.5 idwt2()

```
def imagetools.signals.idwt2 (
    Wim )
```

5.4.1.6 ifft1c()

```
def imagetools.signals.ifft1c (
    y )
```

5.4.1.7 img2coeffs()

```
def imagetools.signals.img2coeffs (
    Wim,
    levels = 4 )
```

5.4.1.8 iterative_soft_thresholding()

```
def imagetools.signals.iterative_soft_thresholding (
    data_sampled,
    lam,
    n_iters,
    gt = None )
```

Implements ISTA in 1D.

```
@param data_sampled The subsampled measurement vector
@param lam The soft-thresholding (regularisation) parameter
@param n_iters Number of iterations
@param gt Ground truth measurements to compare to
@return data Approximated reconstructed measurements
@return mse_values Series of mse values per iteration to enable
performance plot
```

5.4.1.9 unstack_coeffs()

```
def imagetools.signals.unstack_coeffs (
    Wim )
```

5.5 inverse_problems Namespace Reference

Variables

- `file_list` = `f.read().split("\n")[:-1]`
- `y_noisy` = `np.array([float(x) for x in file_list])`
- `y_outlier` = `np.array([float(x) for x in file_list])`
- `x` = `np.arange(len(y_noisy))`
- `a_noisy_l2` = `np.sum(x * y_noisy) / np.sum(x * x)`
- `b_noisy_l2` = `np.mean(y_noisy) - a_noisy_l2 * np.mean(x)`
- `a_outlier_l2` = `np.sum(x * y_outlier) / np.sum(x * x)`
- `b_outlier_l2` = `np.mean(y_outlier) - a_outlier_l2 * np.mean(x)`
- `fig`
- `ax`
- `figsize`
- list `B_coefs` = `[]`
- `obj_l1` = `lambda B: np.sum(np.abs(B[0] * x + B[1] - y))`
- `grad_l1`
- `B0` = `np.array([0.1, 0.1])`
- float `lr` = `0.0001`
- `B` = `gradient_descent(obj_l1, grad_l1, B0, 0, 0.01, lr, 100, "gd_l1")`
- `rng` = `np.random.default_rng(seed=42)`
- `signal` = `np.zeros(100)`
- `data` = `fft1c(signal)`
- int `sample_freq` = `4`
- `mask_random` = `rng.uniform(0, 1, 100)`
- `mask_unif` = `np.zeros(100)`
- `start_index` = `rng.integers(0, sample_freq)`
- `sample_random` = `mask_random * data`
- `sample_unif` = `mask_unif * data`
- int `signal_random` = `ifft1c(sample_random) * sample_freq`
- int `signal_unif` = `ifft1c(sample_unif) * sample_freq`
- `data_random_recon`
- `mse_random`
- `lam`
- `n_iters` = `1000`
- `gt`
- `data_unif_recon`
- `mse_unif`
- int `signal_random_recon` = `ifft1c(data_random_recon) * sample_freq`
- int `signal_unif_recon` = `ifft1c(data_unif_recon) * sample_freq`
- `label`
- `title`
- `xlabel`
- `ylabel`
- `river_img` = `skimage.io.imread("data/river_side.jpeg")`
- `river_img_dw` = `dwt2(river_img)`
- `river_img_recon` = `idwt2(river_img_dw)`
- `th` = `np.quantile(abs(river_img_dw), 0.85)`
- `river_img_dw_th` = `abs(river_img_dw) > th`
- tuple `plotrange`
- `aximg0` = `ax[0].imshow(abs(river_img_dw), vmin=plotrange[0], vmax=plotrange[1])`
- `aximg1` = `ax[1].imshow(abs(river_img_dw_th), cmap="grey")`
- float `obj` = `lambda x: 0.5 * (x[0] ** 2) + (x[1] ** 2)`
- `grad` = `lambda x: np.array([x[0], 2.0 * x[1]])`
- `x0` = `np.array([1.0, 1.0])`
- float `eps` = `0.01`
- float `obj_min` = `0.0`

5.5.1 Variable Documentation

5.5.1.1 a_noisy_l2

```
inverse_problems.a_noisy_l2 = np.sum(x * y_noisy) / np.sum(x * x)
```

5.5.1.2 a_outlier_l2

```
inverse_problems.a_outlier_l2 = np.sum(x * y_outlier) / np.sum(x * x)
```

5.5.1.3 ax

```
inverse_problems.ax
```

5.5.1.4 aximg0

```
inverse_problems.aximg0 = ax[0].imshow(abs(river_img_dw), vmin=plotrange[0], vmax=plotrange[1])
```

5.5.1.5 aximg1

```
inverse_problems.aximg1 = ax[1].imshow(abs(river_img_dw_th), cmap="grey")
```

5.5.1.6 B

```
inverse_problems.B = gradient_descent(obj_l1, grad_l1, B0, 0, 0.01, lr, 100, "gd_l1")
```

5.5.1.7 B0

```
inverse_problems.B0 = np.array([0.1, 0.1])
```

5.5.1.8 B_coefs

```
list inverse_problems.B_coefs = []
```

5.5.1.9 b_noisy_l2

```
inverse_problems.b_noisy_l2 = np.mean(y_noisy) - a_noisy_l2 * np.mean(x)
```

5.5.1.10 b_outlier_l2

```
inverse_problems.b_outlier_l2 = np.mean(y_outlier) - a_outlier_l2 * np.mean(x)
```

5.5.1.11 data

```
inverse_problems.data = fftlc(signal)
```

5.5.1.12 data_random_recon

```
inverse_problems.data_random_recon
```

5.5.1.13 data_unif_recon

```
inverse_problems.data_unif_recon
```

5.5.1.14 eps

```
float inverse_problems.eps = 0.01
```

5.5.1.15 fig

```
inverse_problems.fig
```

5.5.1.16 figsize

```
inverse_problems.figsize
```

5.5.1.17 file_list

```
inverse_problems.file_list = f.read().split("\n")[:-1]
```

5.5.1.18 grad

```
inverse_problems.grad = lambda x: np.array([x[0], 2.0 * x[1]])
```

5.5.1.19 grad_l1

```
inverse_problems.grad_l1
```

Initial value:

```
1 = lambda B: np.array(  
2     [  
3         np.dot(x, np.sign(B[0] * x + B[1] - y)),  
4         np.sum(np.sign(B[0] * x + B[1] - y)),  
5     ]  
6 )
```

5.5.1.20 gt

```
inverse_problems.gt
```

5.5.1.21 label

```
inverse_problems.label
```

5.5.1.22 lam

```
inverse_problems.lam
```


5.5.1.23 lr

```
float inverse_problems.lr = 0.0001
```

5.5.1.24 mask_random

```
inverse_problems.mask_random = rng.uniform(0, 1, 100)
```

5.5.1.25 mask_unif

```
inverse_problems.mask_unif = np.zeros(100)
```

5.5.1.26 mse_random

```
inverse_problems.mse_random
```

5.5.1.27 mse_unif

```
inverse_problems.mse_unif
```

5.5.1.28 n_iters

```
int inverse_problems.n_iters = 1000
```

5.5.1.29 obj

```
float inverse_problems.obj = lambda x: 0.5 * (x[0] ** 2) + (x[1] ** 2)
```

5.5.1.30 obj_l1

```
inverse_problems.obj_l1 = lambda B: np.sum(np.abs(B[0] * x + B[1] - y))
```

5.5.1.31 obj_min

```
float inverse_problems.obj_min = 0.0
```

5.5.1.32 plotrange

```
tuple inverse_problems.plotrange
```

Initial value:

```
1 = (  
2     np.quantile(abs(river_img_dw), 0.005),  
3     np.quantile(abs(river_img_dw), 0.995),  
4 )
```

5.5.1.33 river_img

```
inverse_problems.river_img = skimage.io.imread("data/river_side.jpeg")
```

5.5.1.34 river_img_dw

```
inverse_problems.river_img_dw = dwt2(river_img)
```

5.5.1.35 river_img_dw_th

```
inverse_problems.river_img_dw_th = abs(river_img_dw) > th
```

5.5.1.36 river_img_recon

```
inverse_problems.river_img_recon = idwt2(river_img_dw)
```

5.5.1.37 rng

```
inverse_problems.rng = np.random.default_rng(seed=42)
```

5.5.1.38 sample_freq

```
int inverse_problems.sample_freq = 4
```

5.5.1.39 sample_random

```
inverse_problems.sample_random = mask_random * data
```

5.5.1.40 sample_unif

```
inverse_problems.sample_unif = mask_unif * data
```

5.5.1.41 signal

```
inverse_problems.signal = np.zeros(100)
```

5.5.1.42 signal_random

```
int inverse_problems.signal_random = ifft1c(sample_random) * sample_freq
```

5.5.1.43 signal_random_recon

```
int inverse_problems.signal_random_recon = ifft1c(data_random_recon) * sample_freq
```

5.5.1.44 signal_unif

```
int inverse_problems.signal_unif = ifft1c(sample_unif) * sample_freq
```

5.5.1.45 signal_unif_recon

```
int inverse_problems.signal_unif_recon = ifft1c(data_unif_recon) * sample_freq
```

5.5.1.46 start_index

```
inverse_problems.start_index = rng.integers(0, sample_freq)
```

5.5.1.47 th

```
inverse_problems.th = np.quantile(abs(river_img_dw), 0.85)
```

5.5.1.48 title

```
inverse_problems.title
```

5.5.1.49 x

```
inverse_problems.x = np.arange(len(y_noisy))
```

5.5.1.50 x0

```
inverse_problems.x0 = np.array([1.0, 1.0])
```

5.5.1.51 xlabel

```
inverse_problems.xlabel
```

5.5.1.52 y_noisy

```
inverse_problems.y_noisy = np.array([float(x) for x in file_list])
```

5.5.1.53 y_outlier

```
inverse_problems.y_outlier = np.array([float(x) for x in file_list])
```

5.5.1.54 ylabel

`inverse_problems.ylabel`

5.6 Igd Namespace Reference

Classes

- class `prox_net`
- class `LGD_net`

Variables

- `parser` = `argparse.ArgumentParser()`
- `type`
- `str`
- `choices`
- `required`
- `args` = `parser.parse_args()`
- `img_size` = 256
- `reco_space`
- `num_angles` = 30
- `geometry` = `odl.tomo.parallel_beam_geometry(reco_space, num_angles=num_angles)`
- `fwd_op_odl` = `odl.tomo.RayTransform(reco_space, geometry)`
- `fbp_op_odl`
- `adj_op_odl` = `fwd_op_odl.adjoint`
- `phantom_odl` = `odl.phantom.shepp_logan(reco_space, modified=True)`
- `data_odl` = `fwd_op_odl(phantom_odl)`
- `fbp_odl` = `fbp_op_odl(data_odl)`
- `phantom_np` = `phantom_odl.__array__()`
- `fbp_np` = `fbp_odl.__array__()`
- `data_np` = `data_odl.__array__()`
- `fig`
- `ax`
- `figsize`
- `gt`
- `grad` = `odl.Gradient(reco_space)`
- `L` = `odl.BroadcastOperator(fwd_op_odl, grad)`
- `data_fit` = `odl.solvers.L2NormSquared(fwd_op_odl.range).translated(data_odl)`
- `lam` = 0.015
- `reg_func` = `lam * odl.solvers.L1Norm(grad.range)`
- `g` = `odl.solvers.SeparableSum(data_fit, reg_func)`
- `f` = `odl.solvers.ZeroFunctional(L.domain)`
- `op_norm` = `1.1 * odl.power_method_opnorm(L, maxiter=20)`
- `niter` = 200
- `sigma` = 2.0
- `tau` = `sigma / op_norm**2`
- `callback`
- `x_admm_odl` = `L.domain.zero()`
- `x_admm_np` = `x_admm_odl.__array__()`
- `device`

- int `step_size` = 1 / `op_norm`
- `lgd_net` = `LGD_net().to(device)`
- `num_learnable_params`
- tuple `y`
- tuple `x_init`
- tuple `ground_truth`
- `mse_loss` = `torch.nn.MSELoss()`
- `optimizer` = `torch.optim.Adam(lgd_net.parameters(), lr=1e-4)`
- int `num_epochs` = 2000
- `ckpt` = `torch.load("outputs/weights_1990.pth", map_location=device)`
- int `start_idx` = 1989
- `losses` = `ckpt["losses"]`
- int `save_interval` = 1
- int `verbose_interval` = 1
- `recon` = `lgd_net(y, x_init)`
- `loss` = `mse_loss(recon, ground_truth)`
- dictionary `checkpoint`
- string `checkpoint_filepath` = `f"outputs/weights_{epoch+1:03d}.pth"`
- tuple `lgd_recon_np`

5.6.1 Variable Documentation

5.6.1.1 `adj_op_odl`

```
lgd.adj_op_odl = fwd_op_odl.adjoint
```

5.6.1.2 `args`

```
lgd.args = parser.parse_args()
```

5.6.1.3 `ax`

```
lgd.ax
```

5.6.1.4 `callback`

```
lgd.callback
```

Initial value:

```
1 = odl.solvers.CallbackPrintIteration(
2     step=10
3 ) & odl.solvers.CallbackShow(step=10)
```

5.6.1.5 checkpoint

dictionary lgd.checkpoint

Initial value:

```
1 = {  
2     "epoch": epoch + 1,  
3     "state_dict": lgd_net.state_dict(),  
4     "optimizer": optimizer.state_dict(),  
5     "losses": losses,  
6 }
```

5.6.1.6 checkpoint_filepath

string lgd.checkpoint_filepath = `f"outputs/weights_{epoch+1:03d}.pth"`

5.6.1.7 choices

lgd.choices

5.6.1.8 ckpt

lgd.ckpt = torch.load("outputs/weights_1990.pth", map_location=`device`)

5.6.1.9 data_fit

lgd.data_fit = odl.solvers.L2NormSquared(fwd_op_odl.range).translated(`data_odl`)

5.6.1.10 data_np

lgd.data_np = data_odl.__array__()

5.6.1.11 data_odl

lgd.data_odl = `fwd_op_odl`(`phantom_odl`)

5.6.1.12 device

```
tuple lgd.device
```

Initial value:

```
1 = (  
2     torch.device("cuda") if torch.cuda.is_available() else torch.device("cpu")  
3 )
```

5.6.1.13 f

```
lgd.f = odl.solvers.ZeroFunctional(L.domain)
```

5.6.1.14 fbp_np

```
lgd.fbp_np = fbp_odl.__array__()
```

5.6.1.15 fbp_odl

```
lgd.fbp_odl = fbp_op_odl(data_odl)
```

5.6.1.16 fbp_op_odl

```
lgd.fbp_op_odl
```

Initial value:

```
1 = odl.tomo.fbp_op(  
2     fwd_op_odl, filter_type="Ram-Lak", frequency_scaling=0.6  
3 )
```

5.6.1.17 fig

```
lgd.fig
```

5.6.1.18 figsize

```
lgd.figsize
```


5.6.1.19 fwd_op_odl

```
lgd.fwd_op_odl = odl.tomo.RayTransform(reco_space, geometry)
```

5.6.1.20 g

```
lgd.g = odl.solvers.SeparableSum(data_fit, reg_func)
```

5.6.1.21 geometry

```
lgd.geometry = odl.tomo.parallel_beam_geometry(reco_space, num_angles=num_angles)
```

5.6.1.22 grad

```
lgd.grad = odl.Gradient(reco_space)
```

5.6.1.23 ground_truth

```
tuple lgd.ground_truth
```

Initial value:

```
1 = (  
2     torch.from_numpy(phantom_np).to(device).unsqueeze(0)  
3 )
```

5.6.1.24 gt

```
lgd.gt
```

5.6.1.25 img_size

```
int lgd.img_size = 256
```

5.6.1.26 L

```
lgd.L = odl.BroadcastOperator(fwd_op_odl, grad)
```

5.6.1.27 lam

```
float lgd.lam = 0.015
```

5.6.1.28 lgd_net

```
lgd.lgd_net = LGD_net().to(device)
```

5.6.1.29 lgd_recon_np

```
tuple lgd.lgd_recon_np
```

Initial value:

```
1 = (  
2     recon.detach().cpu().numpy().squeeze()  
3 )
```

5.6.1.30 loss

```
lgd.loss = mse_loss(recon, ground_truth)
```

5.6.1.31 losses

```
list lgd.losses = ckpt["losses"]
```

5.6.1.32 mse_loss

```
lgd.mse_loss = torch.nn.MSELoss()
```

5.6.1.33 niter

```
lgd.niter = 200
```

5.6.1.34 num_angles

```
int lgd.num_angles = 30
```

5.6.1.35 num_epochs

```
int lgd.num_epochs = 2000
```

5.6.1.36 num_learnable_params

```
lgd.num_learnable_params
```

Initial value:

```
1 = sum(  
2     p.numel() for p in lgd_net.parameters() if p.requires_grad  
3 )
```

5.6.1.37 op_norm

```
float lgd.op_norm = 1.1 * odl.power_method_opnorm(L, maxiter=20)
```

5.6.1.38 optimizer

```
lgd.optimizer = torch.optim.Adam(lgd_net.parameters(), lr=1e-4)
```

5.6.1.39 parser

```
lgd.parser = argparse.ArgumentParser()
```

5.6.1.40 phantom_np

```
lgd.phantom_np = phantom_odl.__array__()
```

5.6.1.41 phantom_odl

```
lgd.phantom_odl = odl.phantom.shepp_logan(reco\_space, modified=True)
```

5.6.1.42 reco_space

```
lgd.reco_space
```

Initial value:

```
1 = odl.uniform_discr(  
2     min_pt=[-20, -20],  
3     max_pt=[20, 20],  
4     shape=[img_size, img_size],  
5     dtype="float32",  
6 )
```

5.6.1.43 recon

```
lgd.recon = lgd\_net(y, x_init)
```

5.6.1.44 reg_func

```
float lgd.reg_func = lam * odl.solvers.L1Norm(grad.range)
```

5.6.1.45 required

```
lgd.required
```

5.6.1.46 save_interval

```
int lgd.save_interval = 1
```

5.6.1.47 sigma

```
lgd.sigma = 2.0
```

5.6.1.48 start_idx

```
int lgd.start_idx = 1989
```

5.6.1.49 step_size

```
int lgd.step_size = 1 / op_norm
```

5.6.1.50 str

```
lgd.str
```

5.6.1.51 tau

```
lgd.tau = sigma / op_norm**2
```

5.6.1.52 type

```
lgd.type
```

5.6.1.53 verbose_interval

```
int lgd.verbose_interval = 1
```

5.6.1.54 x_admm_np

```
lgd.x_admm_np = x_admm_odl.__array__()
```

5.6.1.55 x_admm_odl

```
lgd.x_admm_odl = L.domain.zero()
```

5.6.1.56 x_init

```
tuple lgd.x_init
```

Initial value:

```
1 = (
2     torch.from_numpy(
3         fbp_op_odl(y.detach().cpu().numpy().squeeze()).__array__()
4     )
5     .to(device)
6     .unsqueeze(0)
7 )
```

5.6.1.57 y

```
tuple lgd.y
```

Initial value:

```
1 = (
2     torch.from_numpy(data_np).to(device).unsqueeze(0)
3 )
```

5.7 segment Namespace Reference

Variables

- [fig](#)
- [ax](#)
- [figsize](#)
- [ct_img](#) = `skimage.io.imread("data/CT.png")`
- [ct_threshold](#) = `threshold_otsu(ct_img)`
- [ct_segmented](#) = `ct_img > ct_threshold`
- [se](#) = `disk(4)`
- [ct_mask](#) = `remove_small_objects(binary_opening(ct_segmented, se))`
- [ct_labelled](#) = `label(ct_mask == 0)`
- [ct_props](#) = `regionprops(ct_labelled)`
- [lung_idx](#) = `sorted(list(range(3)), key=lambda i: ct_props[i].area)[:2]`
- [cmap](#)
- [coins_img](#) = `skimage.io.imread("data/coins.png")`
- [coins_marked](#) = `coins_img.copy()`
- [coins_pre](#) = `rank.median(coins_img, np.ones((1, 7)))`
- `int` [coins_segmented](#) = `1 - chan_vese(coins_pre, mu=0.1)`
- [coins_labelled](#) = `label(coins_segmented)`
- `list` [desired_coins_idx](#)
- [flowers_img](#) = `skimage.io.imread("data/noisy_flower.jpg")`
- [flowers_pre](#) = `denoise_tv_bregman(flowers_img, weight=0.5)`
- [km](#) = `KMeans_Custom(K=6)`
- [flowers_data](#) = `flowers_pre[:, :8, :].reshape(-1, 3)`
- [verbose](#)
- [flowers_flat](#) = `flowers_pre.reshape(-1, 3)`
- [flowers_segmented](#) = `km.predict_cluster(flowers_flat)`
- `int` [flowers_purple](#) = 0

5.7.1 Variable Documentation

5.7.1.1 ax

```
segment.ax
```

5.7.1.2 cmap

```
segment.cmap
```

5.7.1.3 coins_img

```
tuple segment.coins_img = skimage.io.imread("data/coins.png")
```

5.7.1.4 coins_labelled

```
segment.coins_labelled = label(coins_segmented)
```

5.7.1.5 coins_marked

```
segment.coins_marked = coins_img.copy()
```

5.7.1.6 coins_pre

```
segment.coins_pre = rank.median(coins_img, np.ones((1, 7)))
```

5.7.1.7 coins_segmented

```
segment.coins_segmented = 1 - chan_vese(coins_pre, mu=0.1)
```

5.7.1.8 ct_img

```
segment.ct_img = skimage.io.imread("data/CT.png")
```

5.7.1.9 ct_labelled

```
float segment.ct_labelled = label(ct_mask == 0)
```

5.7.1.10 ct_mask

```
segment.ct_mask = remove_small_objects(binary_opening(ct_segmented, se))
```

5.7.1.11 ct_props

```
segment.ct_props = regionprops(ct_labelled)
```

5.7.1.12 ct_segmented

```
segment.ct_segmented = ct_img > ct_threshold
```

5.7.1.13 ct_threshold

```
segment.ct_threshold = threshold_otsu(ct_img)
```

5.7.1.14 desired_coins_idx

```
list segment.desired_coins_idx
```

Initial value:

```
1 = [  
2     coins_labelled[50, 40],  
3     coins_labelled[125, 100],  
4     coins_labelled[200, 160],  
5     coins_labelled[275, 240],  
6 ]
```


5.7.1.15 fig

```
segment.fig
```

5.7.1.16 figsize

```
segment.figsize
```

5.7.1.17 flowers_data

```
segment.flowers_data = flowers_pre[:, ::8, ::8, :].reshape(-1, 3)
```

5.7.1.18 flowers_flat

```
segment.flowers_flat = flowers_pre.reshape(-1, 3)
```

5.7.1.19 flowers_img

```
segment.flowers_img = skimage.io.imread("data/noisy_flower.jpg")
```

5.7.1.20 flowers_pre

```
segment.flowers_pre = denoise_tv_bregman(flowers_img, weight=0.5)
```

5.7.1.21 flowers_purple

```
segment.flowers_purple = 0
```

5.7.1.22 flowers_segmented

```
segment.flowers_segmented = km.predict_cluster(flowers_flat)
```

5.7.1.23 km

```
segment.km = KMeans_Custom(K=6)
```

5.7.1.24 lung_idx

```
segment.lung_idx = sorted(list(range(3)), key=lambda i: ct_props[i].area)[:2]
```

5.7.1.25 se

```
segment.se = disk(4)
```

5.7.1.26 verbose

```
segment.verbose
```

Chapter 6

Class Documentation

6.1 imagetools.ml.KMeans_Custom Class Reference

Implements a class that handles KMeans Clustering.

Public Member Functions

- `def __init__ (self, K)`
- `def assignment (self, data)`
Assigns a matrix where each row represents the assigned centroid.
- `def fit (self, data, verbose=10, limit=1e5)`
Fits the KMeans clusters.
- `def predict (self, data)`
Returns an array whose rows are the closest centroid to each datum.
- `def predict_cluster (self, data)`
Returns an array whose entries are the closest centroid to each datum, mapped to a single identifying integer.

Public Attributes

- [K](#)
- [centroids](#)

6.1.1 Detailed Description

Implements a class that handles KMeans Clustering.

6.1.2 Constructor & Destructor Documentation

6.1.2.1 `__init__()`

```
def imagetools.ml.KMeans_Custom.__init__ (
    self,
    K )
```

6.1.3 Member Function Documentation

6.1.3.1 `assignment()`

```
def imagetools.ml.KMeans_Custom.assignment (
    self,
    data )
```

Assigns a matrix where each row represents the assigned centroid.

Parameters

| | |
|-------------|--|
| <i>data</i> | The data to assign labels to. Must be an (N, P) array. |
|-------------|--|

Returns

labels

6.1.3.2 `fit()`

```
def imagetools.ml.KMeans_Custom.fit (
    self,
    data,
    verbose = 10,
    limit = 1e5 )
```

Fits the KMeans clusters.

@details Uses the KMeans++ algorithm to initialise centroids, and then iteratively updates them using Lloyd's algorithm.

@param data The data to assign labels to. Must be an (N, P) array.

@param verbose How often to print out number of reassigned labels.

@param limit Maximum number of iterations before stopping. Prevents an indefinite loop.

6.1.3.3 `predict()`

```
def imagetools.ml.KMeans_Custom.predict (
    self,
    data )
```

Returns an array whose rows are the closest centroid to each datum.

Parameters

| | |
|-------------|--|
| <i>data</i> | The data to assign labels to. Must be an (N, P) array. |
|-------------|--|

Returns

predictions (N, P) array of centroids

6.1.3.4 predict_cluster()

```
def imagetools.ml.KMeans_Custom.predict_cluster (
    self,
    data )
```

Returns an array whose entries are the closest centroid to each datum, mapped to a single identifying integer.

Parameters

| | |
|-------------|--|
| <i>data</i> | The data to assign labels to. Must be an (N, P) array. |
|-------------|--|

Returns

predictions (N, 1) array of predicted clusters

6.1.4 Member Data Documentation**6.1.4.1 centroids**

```
imagetools.ml.KMeans_Custom.centroids
```

6.1.4.2 K

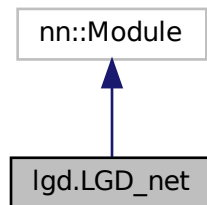
```
imagetools.ml.KMeans_Custom.K
```

The documentation for this class was generated from the following file:

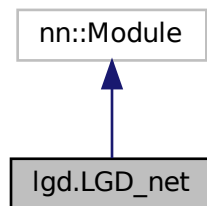
- /home/jhughes2712/projects/image_analysis/jh2284/src/imagetools/[ml.py](#)

6.2 lgd.LGD_net Class Reference

Inheritance diagram for lgd.LGD_net:



Collaboration diagram for lgd.LGD_net:



Public Member Functions

- def `__init__` (self, `niter`=5, `step_size`=`step_size`)
- def `forward` (self, `y`, `x_init`)

Public Attributes

- `niter`
- `prox`
- `step_size`
- `fwd_op_torch`
- `adj_op_torch`

6.2.1 Constructor & Destructor Documentation

6.2.1.1 `__init__()`

```
def lgd.LGD_net.__init__ (
    self,
    niter = 5,
    step_size = step_size )
```

6.2.2 Member Function Documentation

6.2.2.1 `forward()`

```
def lgd.LGD_net.forward (
    self,
    y,
    x_init )
```

6.2.3 Member Data Documentation

6.2.3.1 `adj_op_torch`

`lgd.LGD_net.adj_op_torch`

6.2.3.2 `fwd_op_torch`

`lgd.LGD_net.fwd_op_torch`

6.2.3.3 `niter`

`lgd.LGD_net.niter`

6.2.3.4 `prox`

`lgd.LGD_net.prox`

6.2.3.5 step_size

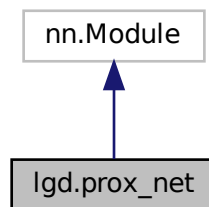
`lgd.LGD_net.step_size`

The documentation for this class was generated from the following file:

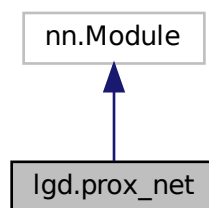
- /home/jhughes2712/projects/image_analysis/jh2284/src/lgd.py

6.3 lgd.prox_net Class Reference

Inheritance diagram for `lgd.prox_net`:



Collaboration diagram for `lgd.prox_net`:



Public Member Functions

- `def __init__ (self, n_in_channels=2, n_out_channels=1, n_filters=32, kernel_size=3)`
- `def forward (self, x, u)`

Public Attributes

- [pad](#)
- [conv1](#)
- [conv2](#)
- [conv3](#)
- [act1](#)
- [act2](#)

6.3.1 Constructor & Destructor Documentation

6.3.1.1 `__init__()`

```
def lgd.prox_net.__init__ (
    self,
    n_in_channels = 2,
    n_out_channels = 1,
    n_filters = 32,
    kernel_size = 3 )
```

6.3.2 Member Function Documentation

6.3.2.1 `forward()`

```
def lgd.prox_net.forward (
    self,
    x,
    u )
```

YOUR CODE HERE

6.3.3 Member Data Documentation

6.3.3.1 `act1`

```
lgd.prox_net.act1
```

6.3.3.2 act2

`lgd.prox_net.act2`

6.3.3.3 conv1

`lgd.prox_net.conv1`

6.3.3.4 conv2

`lgd.prox_net.conv2`

6.3.3.5 conv3

`lgd.prox_net.conv3`

6.3.3.6 pad

`lgd.prox_net.pad`

The documentation for this class was generated from the following file:

- /home/jhughes2712/projects/image_analysis/jh2284/src/lgd.py

Chapter 7

File Documentation

7.1 `/home/jhughes2712/projects/image_analysis/jh2284/src/imagetools/__init__.py` File Reference

Namespaces

- [imagetools](#)

7.2 `/home/jhughes2712/projects/image_analysis/jh2284/src/imagetools/ml.py` File Reference

Module containing implementations of machine learning algorithms.

Classes

- class [imagetools.ml.KMeans_Custom](#)
Implements a class that handles KMeans Clustering.

Namespaces

- [imagetools.ml](#)

Functions

- def [imagetools.ml.gradient_descent](#) (obj, grad, x0, obj_min, eps, lr, max_iters, filename)
Implements vanilla gradient descent for scalar functions on R^2 , where the true global minimum is known.

7.2.1 Detailed Description

Module containing implementations of machine learning algorithms.

Uses numpy to implement KMeans and Gradient Descent, in a way which is not as optimised as, say, scikit-learn, but is readable.

Author

Created by J. Hughes on 8th June 2024.

7.3 `/home/jhughes2712/projects/image_analysis/jh2284/src/imagetools/plotting.py` File Reference

Module building on matplotlib to provide image-specific plotting functions.

Namespaces

- [imagetools.plotting](#)

Functions

- `def imagetools.plotting.plot_image (ax_sp, img, title, cmap, gt=None)`
Plots an image and compares to GT.

7.3.1 Detailed Description

Module building on matplotlib to provide image-specific plotting functions.

Author

Created by J. Hughes on 8th June 2024.

7.4 `/home/jhughes2712/projects/image_analysis/jh2284/src/imagetools/signals.py` File Reference

Module providing useful functions for image processing when employing Fourier and Wavelet transforms.

Namespaces

- [imagetools.signals](#)

Functions

- def [imagetools.signals.iterative_soft_thresholding](#) (data_sampled, lam, n_iters, gt=None)
Implements ISTA in 1D.
- def [imagetools.signals.fft1c](#) (x)
- def [imagetools.signals.ifft1c](#) (y)
- def [imagetools.signals.ComplexSoftThresh](#) (y, lam)
- def [imagetools.signals.coefts2img](#) (LL, coefts)
- def [imagetools.signals.img2coefts](#) (Wim, levels=4)
- def [imagetools.signals.unstack_coefts](#) (Wim)
- def [imagetools.signals.dwt2](#) (im)
- def [imagetools.signals.idwt2](#) (Wim)

7.4.1 Detailed Description

Module providing useful functions for image processing when employing Fourier and Wavelet transforms.

Many of the functions are taken from the 'helper' module provided on the Image Analysis course GitLab page.

Author

Created by J. Hughes on 8th June 2024.

7.5 /home/jhughes2712/projects/image_analysis/jh2284/src/inverse_problems.py File Reference

Script running code for questions 2.1, 2.2, 2.3, and 3.1.

Namespaces

- [inverse_problems](#)

Variables

- [inverse_problems.file_list](#) = f.read().split("\n")[:-1]
- [inverse_problems.y_noisy](#) = np.array([float(x) for x in file_list])
- [inverse_problems.y_outlier](#) = np.array([float(x) for x in file_list])
- [inverse_problems.x](#) = np.arange(len(y_noisy))
- [inverse_problems.a_noisy_l2](#) = np.sum(x * y_noisy) / np.sum(x * x)
- [inverse_problems.b_noisy_l2](#) = np.mean(y_noisy) - a_noisy_l2 * np.mean(x)
- [inverse_problems.a_outlier_l2](#) = np.sum(x * y_outlier) / np.sum(x * x)
- [inverse_problems.b_outlier_l2](#) = np.mean(y_outlier) - a_outlier_l2 * np.mean(x)
- [inverse_problems.fig](#)
- [inverse_problems.ax](#)
- [inverse_problems.figsize](#)
- list [inverse_problems.B_coefts](#) = []
- [inverse_problems.obj_l1](#) = lambda B: np.sum(np.abs(B[0] * x + B[1] - y))
- [inverse_problems.grad_l1](#)
- [inverse_problems.B0](#) = np.array([0.1, 0.1])

- float `inverse_problems.lr` = 0.0001
- `inverse_problems.B` = `gradient_descent(obj_l1, grad_l1, B0, 0, 0.01, lr, 100, "gd_l1")`
- `inverse_problems.rng` = `np.random.default_rng(seed=42)`
- `inverse_problems.signal` = `np.zeros(100)`
- `inverse_problems.data` = `fft1c(signal)`
- int `inverse_problems.sample_freq` = 4
- `inverse_problems.mask_random` = `rng.uniform(0, 1, 100)`
- `inverse_problems.mask_unif` = `np.zeros(100)`
- `inverse_problems.start_index` = `rng.integers(0, sample_freq)`
- `inverse_problems.sample_random` = `mask_random * data`
- `inverse_problems.sample_unif` = `mask_unif * data`
- int `inverse_problems.signal_random` = `ifft1c(sample_random) * sample_freq`
- int `inverse_problems.signal_unif` = `ifft1c(sample_unif) * sample_freq`
- `inverse_problems.data_random_recon`
- `inverse_problems.mse_random`
- `inverse_problems.lam`
- `inverse_problems.n_iters` = 1000
- `inverse_problems.gt`
- `inverse_problems.data_unif_recon`
- `inverse_problems.mse_unif`
- int `inverse_problems.signal_random_recon` = `ifft1c(data_random_recon) * sample_freq`
- int `inverse_problems.signal_unif_recon` = `ifft1c(data_unif_recon) * sample_freq`
- `inverse_problems.label`
- `inverse_problems.title`
- `inverse_problems.xlabel`
- `inverse_problems.ylabel`
- `inverse_problems.river_img` = `skimage.io.imread("data/river_side.jpeg")`
- `inverse_problems.river_img_dw` = `dwt2(river_img)`
- `inverse_problems.river_img_recon` = `idwt2(river_img_dw)`
- `inverse_problems.th` = `np.quantile(abs(river_img_dw), 0.85)`
- `inverse_problems.river_img_dw_th` = `abs(river_img_dw) > th`
- tuple `inverse_problems.plotrange`
- `inverse_problems.aximg0` = `ax[0].imshow(abs(river_img_dw), vmin=plotrange[0], vmax=plotrange[1])`
- `inverse_problems.aximg1` = `ax[1].imshow(abs(river_img_dw_th), cmap="grey")`
- float `inverse_problems.obj` = `lambda x: 0.5 * (x[0] ** 2) + (x[1] ** 2)`
- `inverse_problems.grad` = `lambda x: np.array([x[0], 2.0 * x[1]])`
- `inverse_problems.x0` = `np.array([1.0, 1.0])`
- float `inverse_problems.eps` = 0.01
- float `inverse_problems.obj_min` = 0.0

7.5.1 Detailed Description

Script running code for questions 2.1, 2.2, 2.3, and 3.1.

This script solves various inverse problems related to signal and image processing, employing various iterative strategies and signal transforms.

Author

Created by J. Hughes on 8th June 2024.

7.6 /home/jhughes2712/projects/image_analysis/jh2284/src/lgd.py File Reference

Script for training LGD.

Classes

- class [lgd.prox_net](#)
- class [lgd.LGD_net](#)

Namespaces

- [lgd](#)

Variables

- [lgd.parser](#) = argparse.ArgumentParser()
- [lgd.type](#)
- [lgd.str](#)
- [lgd.choices](#)
- [lgd.required](#)
- [lgd.args](#) = parser.parse_args()
- [int lgd.img_size](#) = 256
- [lgd.reco_space](#)
- [int lgd.num_angles](#) = 30
- [lgd.geometry](#) = odl.tomo.parallel_beam_geometry(reco_space, num_angles=num_angles)
- [lgd.fwd_op_odl](#) = odl.tomo.RayTransform(reco_space, geometry)
- [lgd.fbp_op_odl](#)
- [lgd.adj_op_odl](#) = fwd_op_odl.adjoint
- [lgd.phantom_odl](#) = odl.phantom.shepp_logan(reco_space, modified=True)
- [lgd.data_odl](#) = fwd_op_odl(phantom_odl)
- [lgd.fbp_odl](#) = fbp_op_odl(data_odl)
- [lgd.phantom_np](#) = phantom_odl.__array__()
- [lgd.fbp_np](#) = fbp_odl.__array__()
- [lgd.data_np](#) = data_odl.__array__()
- [lgd.fig](#)
- [lgd.ax](#)
- [lgd.figsize](#)
- [lgd.gt](#)
- [lgd.grad](#) = odl.Gradient(reco_space)
- [lgd.L](#) = odl.BroadcastOperator(fwd_op_odl, grad)
- [lgd.data_fit](#) = odl.solvers.L2NormSquared(fwd_op_odl.range).translated(data_odl)
- [float lgd.lam](#) = 0.015
- [float lgd.reg_func](#) = lam * odl.solvers.L1Norm(grad.range)
- [lgd.g](#) = odl.solvers.SeparableSum(data_fit, reg_func)
- [lgd.f](#) = odl.solvers.ZeroFunctional(L.domain)
- [float lgd.op_norm](#) = 1.1 * odl.power_method_opnorm(L, maxiter=20)
- [int lgd.niter](#) = 200
- [float lgd.sigma](#) = 2.0
- [float lgd.tau](#) = sigma / op_norm**2

- `lgd.callback`
- `lgd.x_admm_odl = L.domain.zero()`
- `lgd.x_admm_np = x_admm_odl.__array__()`
- tuple `lgd.device`
- `int lgd.step_size = 1 / op_norm`
- `lgd.lgd_net = LGD_net().to(device)`
- `lgd.num_learnable_params`
- tuple `lgd.y`
- tuple `lgd.x_init`
- tuple `lgd.ground_truth`
- `lgd.mse_loss = torch.nn.MSELoss()`
- `lgd.optimizer = torch.optim.Adam(lgd_net.parameters(), lr=1e-4)`
- `int lgd.num_epochs = 2000`
- `lgd.ckpt = torch.load("outputs/weights_1990.pth", map_location=device)`
- `int lgd.start_idx = 1989`
- `lgd.losses = ckpt["losses"]`
- `int lgd.save_interval = 1`
- `int lgd.verbose_interval = 1`
- `lgd.recon = lgd_net(y, x_init)`
- `lgd.loss = mse_loss(recon, ground_truth)`
- dictionary `lgd.checkpoint`
- string `lgd.checkpoint_filepath = f"outputs/weights_{epoch+1:03d}.pth"`
- tuple `lgd.lgd_recon_np`

7.6.1 Detailed Description

Script for training LGD.

Reconstructs CT images using FBP and ADMM, and compares to a data-driven LGD algorithm. Can be run in 'demo' mode, just performing the last 10 epochs of training from a checkpoint, or 'full' mode which runs all 2000 training epochs.

Author

Created by J. Hughes on 8th June 2024.

7.7 `/home/jhughes2712/projects/image_analysis/jh2284/src/segment.py` File Reference

Script running code for segmentation problems.

Namespaces

- `segment`

Variables

- `segment.fig`
- `segment.ax`
- `segment.figsize`
- `segment.ct_img = skimage.io.imread("data/CT.png")`
- `segment.ct_threshold = threshold_otsu(ct_img)`
- `segment.ct_segmented = ct_img > ct_threshold`
- `segment.se = disk(4)`
- `segment.ct_mask = remove_small_objects(binary_opening(ct_segmented, se))`
- `segment.ct_labelled = label(ct_mask == 0)`
- `segment.ct_props = regionprops(ct_labelled)`
- `segment.lung_idx = sorted(list(range(3)), key=lambda i: ct_props[i].area)[:2]`
- `segment.cmap`
- `segment.coins_img = skimage.io.imread("data/coins.png")`
- `segment.coins_marked = coins_img.copy()`
- `segment.coins_pre = rank.median(coins_img, np.ones((1, 7)))`
- `int segment.coins_segmented = 1 - chan_vede(coins_pre, mu=0.1)`
- `segment.coins_labelled = label(coins_segmented)`
- `list segment.desired_coins_idx`
- `segment.flowers_img = skimage.io.imread("data/noisy_flower.jpg")`
- `segment.flowers_pre = denoise_tv_bregman(flowers_img, weight=0.5)`
- `segment.km = KMeans_Custom(K=6)`
- `segment.flowers_data = flowers_pre[:, :8, :].reshape(-1, 3)`
- `segment.verbose`
- `segment.flowers_flat = flowers_pre.reshape(-1, 3)`
- `segment.flowers_segmented = km.predict_cluster(flowers_flat)`
- `int segment.flowers_purple = 0`

7.7.1 Detailed Description

Script running code for segmentation problems.

This script segments the three images given on the question sheet using three different segmentation algorithms.

Author

Created by J. Hughes on 8th June 2024.

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