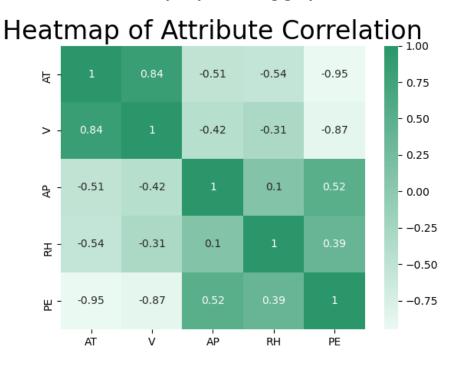
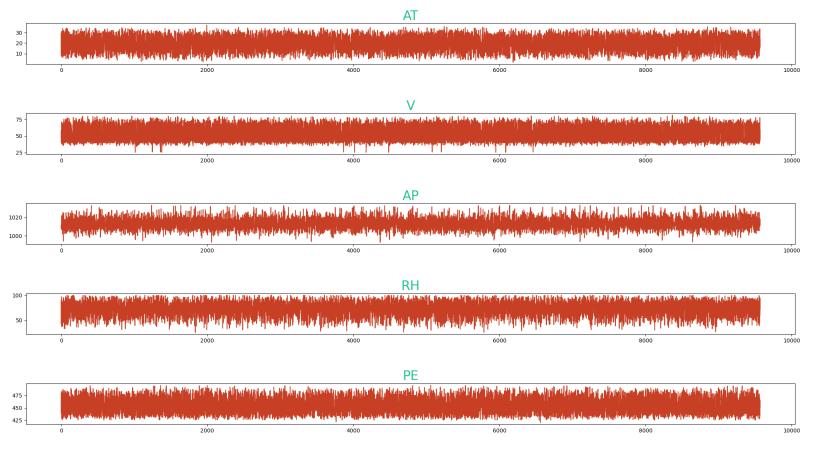
James Hooper (NETID: jah171230) Hritik Panchasara (NETID: hhp160130)

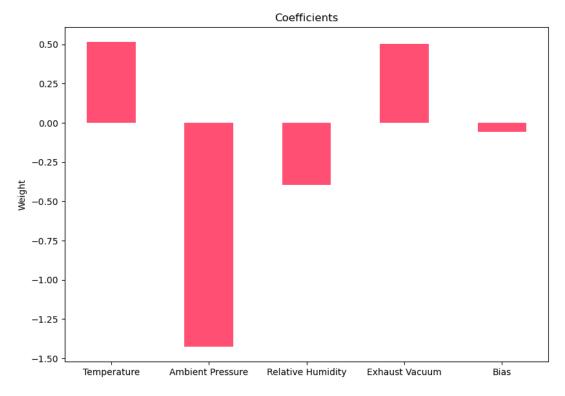
Here are the pre-processing graph results.



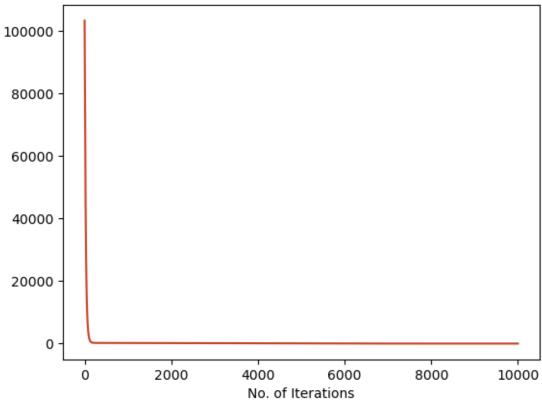


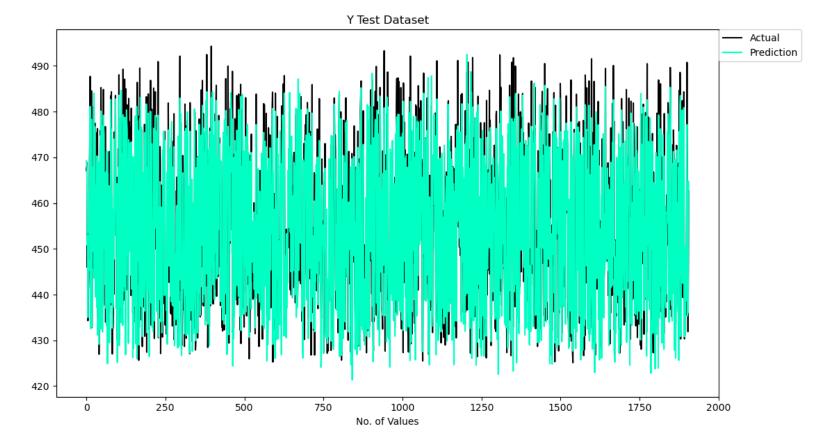
Plots of the attributes. The last plot is of the output value.

Part1 Plots for the trial with the best parameters found. State = 5.

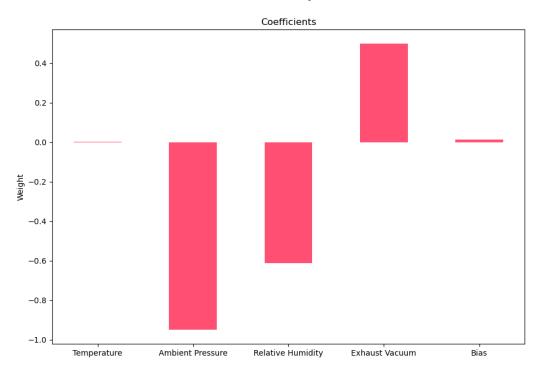


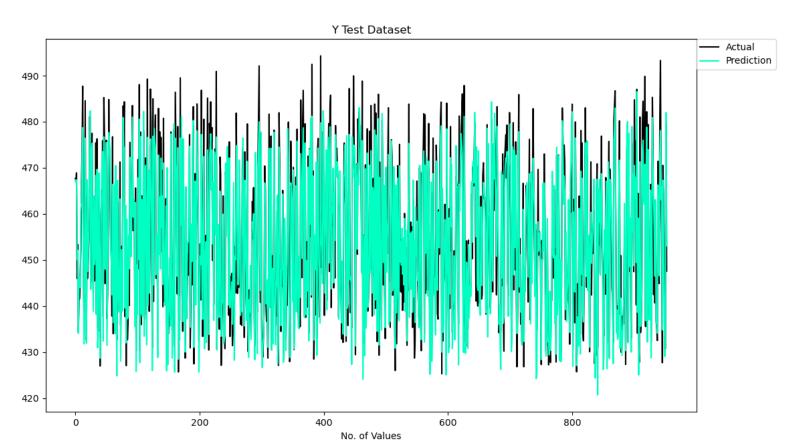






Part2 Plots for the trial with the best parameters found. State = 5.





Part 1 of Logs

Tuning the Enhanced Gradient Descent Model for Best Parameters

Part 1 of Enhanced Gradient Descent

Parameters Used:

State: 5

Alpha: .001 | Beta1: .9 | Beta2: .999 | Epsilon: 10^-8 | m = 0 | v = 0

Iterations: 5000

Train Split: 80.0 % | Test Split: 20.0 %

Coefficients:

[0.4374861331222539, -0.6123631130942228, -0.26003467414341763, 0.44559254221717787, 0.3878470184438752]

Train Accuracy:

Mean Squared Error: 81.5735800926913 R^2 Value: 0.48285457574898716

Test Accuracy:

Mean Squared Error: 80.98996701556176 R^2 Value: 0.49817895252641486

Part 1 of Enhanced Gradient Descent

Parameters Used:

State: 5

Alpha: .001 | Beta1: .9 | Beta2: .999 | Epsilon: 10^{-8} | m = 0 | v = 0

Iterations: 8000

Train Split: 80.0 % | Test Split: 20.0 %

Coefficients:

[0.48719170002575046, -1.118172756881196, -0.5029630792192917, 0.4937123219603581, 0.03896292313804325]

Train Accuracy:

Mean Squared Error: 29.51493201645292

R^2 Value: 0.8844960353362512

Test Accuracy:

Mean Squared Error: 29.646878731320733

R^2 Value: 0.8864923238960015
Part 1 of Enhanced Gradient Descent

Best one found.Parameters Used:

State: 5

Alpha: .001 | Beta1: .9 | Beta2: .999 | Epsilon: 10^-8 | m = 0 | v = 0

Iterations: 10000

Train Split: 80.0 % | Test Split: 20.0 %

Coefficients:

[0.5144726250635316, -1.423992626029842, -0.39589981822794335, 0.5009286790132073, -0.058344123852125625]

Train Accuracy:

Mean Squared Error: 26.22033816483604 R^2 Value: 0.9019748858552826

Test Accuracy:

Mean Squared Error: 26.42235572271788 R^2 Value: 0.9030012797938725

Part 1 of Enhanced Gradient Descent

Drops attribute: 'AT' (this can be verified with the heatmap showing it's correlation with 'V')

Parameters Used:

State: 5

Alpha: .001 | Beta1: .9 | Beta2: .999 | Epsilon: 10^-8 | m = 0 | v = 0

Iterations: 10000

Train Split: 80.0 % | Test Split: 20.0 %

Coefficients:

[0.4648212353511957, -1.0136507011995473, 0.4906395683339943, 0.16063057719700888]

Train Accuracy:

Mean Squared Error: 57.38900595212531

R^2 Value: 0.7500325370547691

Test Accuracy:

Mean Squared Error: 55.812871327546695

R^2 Value: 0.7628366986014008
Part 1 of Enhanced Gradient Descent

Parameters Used:

State: 5

Alpha: .001 | Beta1: .9 | Beta2: .999 | Epsilon: 10^{-8} | m = 0 | v = 0

Iterations: 10000

Train Split: 90.0 % | Test Split: 10.0 %

Coefficients:

[0.5140621380109054, -1.422759204876915, -0.39610464580669436, 0.5009524502521513, -0.05821683974215756]

Train Accuracy:

Mean Squared Error: 26.20013185328805

R^2 Value: 0.9024861152060023

Test Accuracy:

Mean Squared Error: 26.86479385463498

R^2 Value: 0.8985095209493589

Note:

A key thing to mention here is that the Adam Optimizer is recommended to have the same variable values for Alpha, Beta1, Beta2, Epsilon, initial m, and initial v. These standard values are used through most implementations of using the Adam optimization. After trying to tune the parameters for the Enhanced Gradient Descent Model here were the best parameters found: iterations = 10000, train/test split = 90/10, and keeping all attributes.

Part 2 of Logs

Comparing Gradient Descent & Sklearn Stochastic Gradient Descent Model

Part 1 of Enhanced Gradient Descent

Parameters Used:

State: 1

Alpha: .001 | Beta1: .9 | Beta2: .999 | Epsilon: 10^-8 | m = 0 | v = 0

Iterations: 10000

Train Split: 80.0 % | Test Split: 20.0 %

Coefficients:

[0.5135360955599416, -1.4129702682082277, -0.4030913398665183, 0.5012177628402052, -0.0601577196111157]

Train Accuracy:

Mean Squared Error: 25.907627020055898

R^2 Value: 0.9030119875133472

Test Accuracy:

Mean Squared Error: 28.014235643608277

R^2 Value: 0.8973077744212778
Part 2 of Enhanced Gradient Descent

Parameters Used:

State: 1

Iterations: 10000 Learning Rate: 1e-06

Coefficients:

 $[\ 6.33944060e-04-1.04579006e+00-5.69972842e-01\ 5.00032224e-01-1.42396194e-03]$

Train Accuracy:

Mean Squared Error: 29.96784033730602

R^2 Value: 0.8827791382973325

Test Accuracy:

Mean Squared Error: 35.768615316443594

R^2 Test: 0.8706809198549961
Part 1 of Enhanced Gradient Descent

Parameters Used:

State: 2

Alpha: .001 | Beta1: .9 | Beta2: .999 | Epsilon: 10^-8 | m = 0 | v = 0

Iterations: 10000

Train Split: 80.0 % | Test Split: 20.0 %

Coefficients:

[0.5146539289431077, -1.4216915288677878, -0.3944771045499932, 0.5007776345920979, -0.05787278024584849]

Train Accuracy:

Mean Squared Error: 26.35812790742656

R^2 Value: 0.9008578375693331

Test Accuracy:

Mean Squared Error: 25.894430060307297

R^2 Value: 0.9052769558060673
Part 2 of Enhanced Gradient Descent

Parameters Used:

State: 2

Iterations: 10000 Learning Rate: 1e-06

Coefficients:

 $\left[8.26639238e-04 - 1.17934925e+00 - 5.03116141e-01 \ \ 5.00811753e-01 \ \ - 2.21790217e-02 \right]$

Train Accuracy:

Mean Squared Error: 29.329251229280484

R^2 Value: 0.8865946508768744

Test Accuracy:

Mean Squared Error: 28.93303057712341

R^2 Test: 0.8899080573047872

Part 1 of Enhanced Gradient Descent

Parameters Used:

State: 3

Alpha: .001 | Beta1: .9 | Beta2: .999 | Epsilon: 10^{-8} | m = 0 | v = 0

Iterations: 10000

Train Split: 80.0 % | Test Split: 20.0 %

Coefficients:

[0.514850161615456, -1.4175520120905034, -0.4032907854138991, 0.5010969321402667, -0.05667334052436697]

Train Accuracy:

Mean Squared Error: 26.049164151569435

R^2 Value: 0.90280841347468

Test Accuracy:

Mean Squared Error: 27.403502699222685

R^2 Value: 0.9015783901380442
Part 2 of Enhanced Gradient Descent

Parameters Used:

State: 3

Iterations: 10000 Learning Rate: 1e-06

Coefficients:

 $[\ 5.79192509e-04\ -9.85495454e-01\ -5.98517524e-01\ \ 4.98454730e-01\ \ 7.34514243e-03]$

Train Accuracy:

Mean Squared Error: 31.1965394854964 R^2 Value: 0.8778546902838902

Test Accuracy:

Mean Squared Error: 32.31482406991121

R^2 Test: 0.8783472782239139

Part 1 of Enhanced Gradient Descent

Parameters Used:

State: 4

Alpha: .001 | Beta1: .9 | Beta2: .999 | Epsilon: 10^{-8} | m = 0 | v = 0

Iterations: 10000

Train Split: 80.0 % | Test Split: 20.0 %

Coefficients:

[0.5143122919765742, -1.424814866085679, -0.3971354213196689, 0.5011520085825308, -0.060557465214266824]

Train Accuracy:

Mean Squared Error: 26.236927421839752

R^2 Value: 0.9020796768035431

Test Accuracy:

Mean Squared Error: 26.35186963702148

R^2 Value: 0.9030362793154947
Part 2 of Enhanced Gradient Descent

Parameters Used:

State: 4

Iterations: 10000 Learning Rate: 1e-06 Coefficients:

[6.18053193e-04 -1.02958395e+00 -5.75053426e-01 4.99599192e-01 -1.20913344e-03]

Train Accuracy:

Mean Squared Error: 30.428115367405606

R^2 Value: 0.8811448017908418

Test Accuracy:

Mean Squared Error: 29.810869047270845

R^2 Test: 0.8834203548265686
Part 1 of Enhanced Gradient Descent

Parameters Used:

State: 5

Alpha: .001 | Beta1: .9 | Beta2: .999 | Epsilon: 10^-8 | m = 0 | v = 0

Iterations: 10000

Train Split: 80.0 % | Test Split: 20.0 %

Coefficients:

[0.5144726250635316, -1.423992626029842, -0.39589981822794335, 0.5009286790132073, -0.058344123852125625]

Train Accuracy:

Mean Squared Error: 26.22033816483604

R^2 Value: 0.9019748858552826

Test Accuracy:

Mean Squared Error: 26.42235572271788

R^2 Value: 0.9030012797938725

Part 2 of Enhanced Gradient Descent

Parameters Used:

State: 5

Iterations: 10000 Learning Rate: 1e-06

Coefficients:

[5.20305073e-04 -9.22055912e-01 -6.25737931e-01 4.97391759e-01 1.76156170e-02]

Train Accuracy:

Mean Squared Error: 33.3083715750111 R^2 Value: 0.8684416548402241

Test Accuracy:

Mean Squared Error: 33.33351926639194

R^2 Test: 0.8712252043979538

Notes:

- The chosen parameters for the SGD-Regressor kept the iterations the same as the ones
 used for the Enhanced Gradient Descent, set the learning rate to 1e-06 since it was the
 only Learning Rate that actually was optimal, set the loss function to "squared_loss",
 and did not set any penalty.
- The states here are kept the same to properly compare the models.
- The obvious conclusion to be made here is that from the chosen parameters for both models, the Enhanced Gradient Descent model that implemented the Adam optimizer performed better than the sklearn SGD-Regressor model. Lower Mean Squared Error value and a higher R^2 value.

Answers to Questions

Are you satisfied that you have found the best solution? Explain.

Overall, we are satisfied with the results we obtained from our enhanced version of vanilla Gradient Descent. The reason for this is that the accuracy achieved is something that can be interpreted as a success. Of course, there are other optimizations that can be used for the model to achieve even better results such as Normalizing or Standardizing the data before sending it through the model. There could also be other pre-processing analysis that can help modify the data to be more optimal as well. Since the accuracy seems sufficient and it is not only comparable to the SGD-Regressor model but achieves better results, we can be satisfied that we found a good solution.

Are you satisfied that the package has found the best solution? Explain.

- We feel that there is a lot more that could be done with the SGD-Regressor package that we didn't implement. There were a lot more parameters and other resources that could have helped fine tune the model. On top of Normalizing or Standardizing the data, we could have spent more time understanding all the inputs into the model that were offered. Furthermore, we are trying to compare the Adam optimizer to the SGD-Regressor model so it would be difficult to alter parameters without just having two almost incomparable models. Due to this concern we kept the SGD-Regressor model as simple as possible in order to have an easier understanding of what was directly being compared.