

Taylor Rule	$i^* = r_{\text{neutral}} + \pi_e + 0.5(\hat{Y}_e - \hat{Y}_{\text{trend}}) + 0.5(\pi_e - \pi_{\text{target}})$		
Nominal policy rate:	Y_e real GDP growth = nominal – inflation π_e		
Real target rate	Nominal policy rate – Expected inflation (π_e)		
Trade surplus: ~ current account	$(X - M) = (S - I) + (T - G)$.		
Grinold-Kroner	$E(R_e) \approx \frac{D}{P} + (\% \Delta E - \% \Delta S) + \% \Delta P / E$		
Equity beta, asset i:	$\beta_{i,M} = \frac{\text{Cov}(R_i, R_M)}{\text{Var}(R_M)} = \rho_{i,M} \left(\frac{\sigma_i}{\sigma_M} \right)$		
Global risk premium:	$RP_i^G = \beta_{i,GM} RP_{GM} = \rho_{i,GM} \sigma_i \left(\frac{RP_{GM}}{\sigma_{GM}} \right)$		
Segmented risk prem: beta = 1	$RP_i^S = 1 \times RP_i^S = 1 \times \sigma_i \left(\frac{RP_i^S}{\sigma_i} \right)$		
Singer-Terhaar	$RP_i = \varphi RP_i^G + (1 - \varphi) RP_i^S$		
Real estate growth rate:	$E(R_{re}) = \text{Cap rate} + \text{NOI growth rate} - \% \Delta \text{Cap rate}$ ~ cap rate = value/NOI ~finite horizons		
Surplus Optimizer:	$U_m = E(R_m) - 0.005 \lambda \sigma_m^2$ m = $(\Delta A - \Delta L) / A_0$		
Prob. above threshold:	$[E(R_p) - R_{\text{Threshold}}] / \sigma_p$. ~ derive from percentage		
Risk parity weight:	$w_i \times \text{Cov}(r_i, r_P) = \frac{1}{n} \sigma_P^2$		
Marginal CTRisk	$\beta_{i,P} * \sigma_P$ optimal AA when SR = RP/MCTR		
Absolute CTRisk	$\text{ACTR}_i = (\text{Weight}_i)(\text{MCTR}_i)$		
Fundamental law:	$E(R_A) = IC \sqrt{BR} \sigma_{R_A} TC$	IC forecast ~ actual TC translate /1	
Eff. number of stocks:	$= \frac{1}{\sum_{i=1}^n w_i^2} = 1/\text{HHL}$		
Macaulay duration:	weighted average time of receipt all payments		
Modified duration:	Mac D * (1+yield) ⁻¹ ~ % change in price for a change in ytm		
Money duration:	Port mod duration × Port market value BPV: multiply by 0.0001 ~ used for futures		
Duration BPV _{Exposure} : immunize = 0	$= (\text{BPV}_{\text{Liability}} - \text{BPV}_{\text{Asset}}) + (N_{\text{Futures}} \times \text{BPV}_{\text{Fut}})$ ~ $\text{BPV}_{\text{Fut}} = \text{BPV}_{\text{CTD}} / \text{ConvFact}_{\text{CTD}}$		
Effective duration:	$= \frac{(\text{PV}_-) - (\text{PV}_+)}{2(\Delta \text{Curve})(\text{PV}_0)} = \sum_{k=1}^n \text{KeyRateDur}_k$		
Effective convexity	$= \frac{(\text{PV}_-) + (\text{PV}_+) - 2(\text{PV}_0)}{(\Delta \text{Curve})^2 (\text{PV}_0)}$		
Rolling yield	= Coupon income + Rolldown return		
Rolldown return:	$= \frac{(\text{Bond price}_{\text{End-of-horizonperiod}} - \text{Bond price}_{\text{Beginning-of-horizonperiod}})}{\text{Bond price}_{\text{Beginning-of-horizonperiod}}}$		
Δ price views <u>yield</u>	$= (-\text{ModDur} \times \Delta \text{Yield}) + [\frac{1}{2} \times \text{Convexity} \times (\Delta \text{Yield})^2]$		
Δ price views <u>spread</u>	$= (-\text{ModSpreadDur} \times \Delta \text{Spread}) + [\frac{1}{2} \times \text{Convexity} \times (\Delta \text{Spread})^2]$		
Leveraged return:	$r_P = \frac{r_I \times (V_E + V_B) - (V_B \times r_B)}{V_E}$		
Butterfly spread	$2 \times \text{Yield}_{\text{Medium}} - \text{Yield}_{\text{Short}} - \text{Yield}_{\text{Long}}$ ~ positive view: decrease in spread		
Quantifying <u>credit spread</u> changes:	Close to par: one period spread = LGD × POD ~ spread combination of credit + liquidity risk Distressed = 1 – LGD i.e. recovery rate		
Excess Spread	$= (\text{Spread}_0 / \text{periods}) - (\text{EffSpreadDur} \times \Delta \text{Spread})$ ~ – POD × LDG for $E[\text{Excess Spread Return}]$		
CDS protection cost % of notional amount	$= (\text{CDS Spread} - \text{Protect Pmt}) * \text{EffSpreadDur}$ ~ exchanged upfront, MTM using new spread		
Select effect:	$W_B (R_P - R_B)$	Interact effect	$(W_P - W_B) (R_P - R_B)$
BHB alloc:	$(W_P - W_B) R_B$ does not penalize cost of not being in mkt		
BF alloc:	$(W_P - W_B) (R_B - R_{\text{Bmk Total}})$ same total effect as above		
Type I error: false pos – incorrectly pass test hired manager underperforms			

Yield spread:	Nearest gov bond: slope bias, mat. mismatch
G-Spread:	Bond YTM and linear interpolation treasury
I-Spread:	Short term swaps across all maturities MRR
ASW	Bond's <u>coupon</u> – interpolated swap rate
Z-Spread	Derived constant spread over gov spot curve
CDS-Spread	Issuer CDS – Z-Spread = pos/neg basis
OAS-Spread	Derived as Z-spread using arb-free rate options
Spread factor:	%Δ spread * DTS = %Δ spread
Eff Spread <u>Tran Cost</u> :	= Trade size × Trade price – $\left(\frac{\text{Bid} + \text{Ask}}{2}\right)$
Eff Spread	= $2 \times \left(\frac{\text{Bid} + \text{Ask}}{2}\right)$ – Trade price
Implementation Shortfall	= Paper return – Actual return (<i>includes fees</i>) = Execution Cost + Opportunity Cost +Fee
Execution cost	= $\sum s_j p_j - \sum s_j p_d$: <i>executed – executed @ dec</i> $\underbrace{\left(\sum s_j\right) p_0 - \left(\sum s_j\right) p_d}_{\text{Delay cost}} + \underbrace{\sum s_j p_j - \left(\sum s_j\right) p_0}_{\text{Trading cost}}$
Opportunity cost	= $\left(S - \sum s_j\right) \left(P_n - P_d\right)$: <i>unexecuted * (now – dec)</i>
Trade costs:	$\frac{(P - P^*)}{P^*} \times 10,000$ bps where P^* = arrival, VWAP...
Index cost	= $\frac{(\text{Index VWAP} - \text{Index arrival price})}{\text{Index arrival price}} \times 10^4$
Market- <u>adjusted</u> cost	= Arrival cost (bps) – β × Index cost (bps)
Sortino ratio: ~ above a target ~ capital preservation	$\widehat{\text{SR}}_D = \frac{\bar{r}_P - \bar{r}_T}{\hat{\sigma}_D}$
Treynor ratio: ~ systematic risk	$T_A = \frac{R_A - \bar{r}_f}{\hat{\beta}_A}$
Upside capture	Geometric R_{Port} / R_{Bmk} when $R_{Bmk} > 0$
Carhart (<i>factor based</i>)	$R_p - R_f = a_p + b_{p1}\text{RMRF} + b_{p2}\text{SMB} + b_{p3}\text{HML} + b_{p4}\text{WML} + E_p$ <i>pos sensitivities indicate small value momentum</i> $SS = \text{Active rtn} - \sum \text{net port sensitivity} * \text{factor rtn}$
Call-put parity	$S_0 + p_0 = c_0 + X / (1 + r)^T$ $F_0(T) / (1 + r)^T + p_0 = c_0 + X / (1 + r)^T$.
Protective puts/calls <i>limit downside</i> at the <i>expense</i> of option premium. Covered puts/calls <i>limit upside</i> for <i>receipt</i> of option premium.	
Bull/bear spreads: long & short the same instrument, different strike prices > initial <u>net</u> outflow always negative, calls with lower X expensive > Put bear spread breakeven such that $-S_T + X_H - P_H + P_L = 0$	
A collar is a protective put financed by writing a call at a higher strike price > assumes stock already held, all payoffs positive if appreciated	
Long calendar spread: buy distant-dated call option, short near-dated call > capture time value if price change is not imminent, after early expiry > also if IV is to increase	
Volatility Skew: IV increases for OTM puts & decreases for OTM calls > Risk reversal buy relatively undervalued OTM call & sell put	
Contango: volatility higher on long-term options decreases to spot at expiry > negative roll-down losses on futures, buy puts/write calls > Swap payoff = Notional × (Realized Variance – Implied Variance)	
Min var. hedge ratio:	$h = \rho \left(\frac{\rho R_D; R}{F_{FX}} \right) \times \left[\frac{\sigma(R_{DC})}{\sigma(R_{FX})} \right]$ $h\%$ short foreign long forward / R_D
Cash equitization:	$N_f \beta_f F_{\text{Contract Size}} = \text{Desired exposure} \times \beta_{\text{Target}}$
Target portfolio duration = $\text{ModD}_{\text{Target}} * \text{MV}_{\text{Port}} = \sum \text{ModD}_i * \text{MV}_i$	
Variance Notional:	= $\frac{\text{Vega notional}}{2 \times \text{Strike price}}$
$\text{Var Swap}_t = \text{notional} \times P V_T(T) \times \left\{ \frac{t}{T} \times \left[\text{RealizedVol}(0, t) \right]^2 + \frac{T-t}{T} \times \left[\text{ImpliedVol}(t, T) \right]^2 - \text{Strike}^2 \right\}$	
<u>Effective federal funds rate implied by futures contract – Current federal funds rate</u> Prob rate change: <u>Federal funds rate assuming a rate hike – Current federal funds rate</u>	
Immunized convexity:	$\frac{\text{MacDur}^2 + \text{MacDur} + \text{Dispersion}}{(1 + \text{Cash flow yield})^2}$