

Taylor Rule	$i^* = r_{\text{neutral}} + \pi_e + 0.5(\hat{Y}_e - \hat{Y}_{\text{trend}}) + 0.5(\pi_e - \pi_{\text{target}})$
Nominal policy rate:	$Y_e$ real GDP growth = nominal – inflation $\pi_e$
Real target rate	Nominal policy rate – Expected inflation ( $\pi_e$ )
Trade surplus: ~ current account	$(X - M) = (S - I) + (T - G)$ .
Grinold-Kroner	$E(R_e) \approx \frac{D}{P} + (\%ΔE - \%ΔS) + \%ΔP/E$
Equity beta, asset i:	$\beta_{i,M} = \frac{\text{Cov}(R_i, R_M)}{\text{Var}(R_M)} = \rho_{i,M} \left( \frac{\sigma_i}{\sigma_M} \right)$
Global risk premium:	$RP_i^G = \beta_{i,GM} RP_{GM} = \rho_{i,GM} \sigma_i \left( \frac{RP_{GM}}{\sigma_{GM}} \right)$
Segmented risk prem: beta = 1	$RP_i^S = 1 \times RP_i^G = 1 \times \sigma_i \left( \frac{RP_i^S}{\sigma_i} \right)$
Singer-Terhaar	$RP_i = \varphi RP_i^G + (1 - \varphi) RP_i^S$
Real estate growth rate:	$E(R_{re}) = \text{Cap rate} + \text{NOI growth rate} - \%Δ\text{Cap rate}$ $\sim \text{cap rate} = \text{value}/\text{NOI}$ ~finite horizons
Surplus Optimizer:	$U_m = E(R_m) - 0.005\lambda \sigma_m^2$ m = $(\Delta A - \Delta L)/A_0$
Prob. above threshold:	$[E(R_p) - R_{\text{Threshold}}]/\sigma_p$ . ~ derive from percentage
Risk parity weight:	$w_i \times \text{Cov}(r_i, r_P) = \frac{1}{n} \sigma_P^2$
Marginal CTRisk	$\beta_{i,P} * \sigma_P$ optimal AA when SR = RP/MCTR
Absolute CTRisk	$\text{ACTR}_i = (\text{Weight}_i)(\text{MCTR}_i)$
Fundamental law:	$E(R_A) = IC \sqrt{B_R} \sigma_{R_A} TC$ IC forecast ~ actual TC translate /1
Eff. number of stocks:	$= \frac{1}{\sum_{i=1}^n w_i^2} = 1/\text{HHI}$
Macaulay duration:	weighted average time of receipt all payments
Modified duration:	Mac D * (1+yield) <sup>-1</sup> ~ % change in price for a change in ytm
Money duration:	Port mod duration × Port market value BPV: multiply by 0.0001 ~ used for futures
Duration BPV <sub>Exposure</sub> : immunize = 0	$= (\text{BPV}_{\text{Liability}} - \text{BPV}_{\text{Asset}}) + (\text{N}_{\text{Futures}} \times \text{BPV}_{\text{Fut}})$ ~ BPV <sub>Fut</sub> = BPV <sub>CTD</sub> /ConvFact <sub>CTD</sub>
Effective duration:	$= \frac{(\text{PV}_-) - (\text{PV}_+)}{2(\Delta\text{Curve})(\text{PV}_0)} = \sum_{k=1}^n \text{KeyRateDur}_k$
Effective convexity	$= \frac{(\text{PV}_-) + (\text{PV}_+) - 2(\text{PV}_0)}{(\Delta\text{Curve})^2(\text{PV}_0)}$ .
Rolling yield	= Coupon income + Rolldown return
Rolldown return:	$= \frac{(\text{Bond price}_{\text{End-of-horizon period}} - \text{Bond price}_{\text{Beginning-of-horizon period}})}{\text{Bond price}_{\text{Beginning-of-horizon period}}}$
Δ price views yield	$= (-\text{ModDur} \times \Delta\text{Yield}) + [\frac{1}{2} \times \text{Convexity} \times (\Delta\text{Yield})^2]$
Δ price views spread	$= (-\text{ModSpreadDur} \times \Delta\text{Spread}) + [\frac{1}{2} \times \text{Convexity} \times (\Delta\text{Spread})^2]$
Leveraged return:	$r_P = \frac{r_I \times (V_E + V_B) - (V_B \times r_E)}{V_E}$
Butterfly spread	$2 \times \text{Yield}_{\text{Medium}} - \text{Yield}_{\text{Short}} - \text{Yield}_{\text{Long}}$ ~ positive view: decrease in spread
Quantifying credit spread changes:	Close to par: one period spread = LGD × POD ~ spread combination of credit + liquidity risk Distressed = 1 – LGD i.e. recovery rate
Excess Spread	$= (\text{Spread}_0/\text{periods}) - (\text{EffSpreadDur} \times \Delta\text{Spread})$ ~ POD × LDG for E[Excess Spread Return]
CDS protection cost % of notional amount	$= (\text{CDS Spread} - \text{Protect Pmt}) * \text{EffSpreadDur}$ ~ exchanged upfront, MTM using new spread
Select effect:	$W_B (R_P - R_B)$
BHB alloc:	$(W_P - W_B) R_B$ does not penalize cost of not being in mkt
BF alloc:	$(W_P - W_B) (R_B - R_{Bmk \text{ Total}})$ same total effect as above
Type I error: false pos – incorrectly pass test hired manager underperforms	

Yield spread:	Nearest gov bond: slope bias, mat. mismatch
G-Spread:	Bond YTM and linear interpolation treasury
I-Spread:	Short term swaps across all maturities MRR
ASW	Bond's coupon – interpolated swap rate
Z-Spread	Derived constant spread over gov spot curve
CDS-Spread	Issuer CDS – Z-Spread = pos/neg basis
OAS-Spread	Derived as Z-spread using arb-free rate options
Spread factor:	%Δ spread * DTS = %Δ spread
Eff Spread Tran Cost:	$= \text{Trade size} \times \text{Trade price} - \left( \frac{\text{Bid} + \text{Ask}}{2} \right)$
Eff Spread	$= 2 \times \left( \frac{\text{Bid} + \text{Ask}}{2} \right) - \text{Trade price}$
Implementation Shortfall	$= \text{Paper return} - \text{Actual return (includes fees)}$ $= \text{Execution Cost} + \text{Opportunity Cost} + \text{Fee}$
Execution cost	$= \sum s_j p_j - \sum s_j p_d : \text{executed} - \text{executed @ dec}$ $\underbrace{(\sum s_j) p_0}_{\text{Delay cost}} - \underbrace{(\sum s_j) p_d}_{\text{Trading cost}} + \underbrace{\sum s_j p_j - (\sum s_j) p_0}_{\text{Trading cost}}$
Opportunity cost	$= (S - \sum s_j) (P_n - P_d) : \text{unexecuted * (now - dec)}$
Trade costs:	$\frac{(P - P^*)}{P^*} \times 10,000 \text{ bps}$ where $P^*$ = arrival, VWAP...
Index cost	$= \frac{(\text{Index VWAP} - \text{Index arrival price})}{\text{Index arrival price}} \times 10^4$
Market-adjusted cost	= Arrival cost (bps) – $\beta \times \text{Index cost (bps)}$
Sortino ratio: ~ above a target ~ capital preservation	$\widehat{SR}_D = \frac{\bar{r}_p - \bar{r}_T}{\widehat{\sigma}_D}$
Treynor ratio: ~ systematic risk	$T_A = \frac{\bar{R}_A - \bar{r}_f}{\widehat{\sigma}_A}$
Upside capture	Geometric $R_{\text{Port}}/R_{\text{Bmk}}$ when $R_{\text{Bmk}} > 0$
Carhart (factor based)	$R_p - R_f = a_p + b_p \text{RMRF} + b_p \text{SMB} + b_p \text{HML} + b_p \text{WML} + E_p$ pos sensitivities indicate small value momentum SS = Active rtn - net port sensitivity * factor rtn
Call-put parity	$S_0 + p_0 = c_0 + X/(1+r)^T$ $F_0(T)/(1+r)^T + p_0 = c_0 + X/(1+r)^T$
	Protective puts/calls limit downside at the expense of option premium. Covered puts/calls limit upside for receipt of option premium.
	Bull/bear spreads: long & short the same instrument, different strike prices > initial net outflow always negative, calls with lower X expensive > Put bear spread breakeven such that $-S_T + X_H - P_H + P_L = 0$
	A collar is a protective put financed by writing a call at a higher strike price > assumes stock already held, all payoffs positive if appreciated
	Long calendar spread: buy distant-dated call option, short near-dated call > capture time value if price change is not imminent, after early expiry > also if IV is to increase
	Volatility Skew: IV increases for OTM puts & decreases for OTM calls > Risk reversal buy relatively undervalued OTM call & sell put
	Contango: volatility higher on long-term options decreases to spot at expiry > negative roll-down losses on futures, buy puts/write calls > Swap payoff = Notional × (Realized Variance – Implied Variance)
Min var. hedge ratio:	$h = \rho \left( \frac{\sigma_{R_D; R}}{F_{FX}} \right) \times \begin{cases} \sigma(R_{DC}) \\ \sigma(F_{FX}) \end{cases}$ h% short foreign long forward / $R_D$
Cash equitization:	$N_f \beta_f F_{\text{Contract Size}} = \text{Desired exposure} \times \beta_{\text{Target}}$
Target portfolio duration	= $\text{ModD}_{\text{Target}} * \text{MV}_{\text{Port}} = \sum \text{ModD}_i * \text{MV}_i$
Variance Notional:	$= \frac{\text{Vega notional}}{2 \times \text{Strike price}}$
Var Swap <sub>t</sub>	$= \text{notional} \times P V_t(T) \times \left\{ \frac{1}{T} \times [\text{RealizedVol}(0, t)]^2 + \frac{T-t}{T} \times [\text{ImpliedVol}(t, T)]^2 - \text{Strike}^2 \right\}$
Prob rate change:	Effective federal funds rate implied by futures contract – Current federal funds rate Federal funds rate assuming a rate hike – Current federal funds rate
Immunized convexity:	$\frac{\text{MacDur}^2 + \text{MacDur} + \text{Dispersion}}{(1 + \text{Cash flow yield})^2}$