

GPG: A KEY SIGNING PARTY

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OUTLINE



1 SECTION 1

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SECTION 1



$$\begin{aligned} -\varepsilon \Delta u + b \cdot \nabla u &= f && \text{in } \Omega \subset \mathbb{R}^d \\ u &= 0 && \text{on } \partial\Omega \end{aligned}$$

Look at these equations...

THEOREM

A Theorem

$$-\frac{1}{2} \nabla \cdot b \geq \rho \geq 0.$$

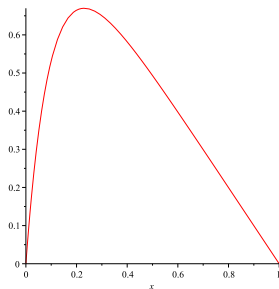
PROOF.

A Proof

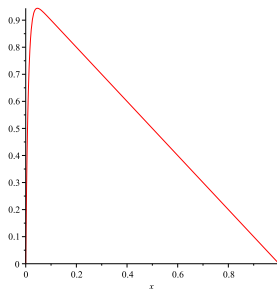




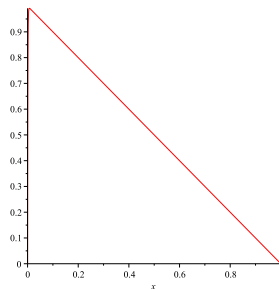
There are some pictures below...



(a) $\varepsilon = 0.1$



(b) $\varepsilon = 0.01$

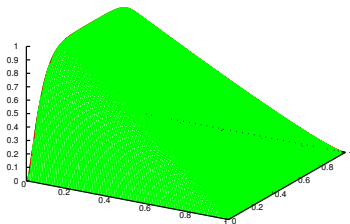


(c) $\varepsilon = 0.001$

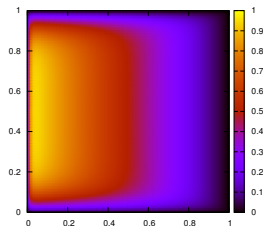
ANOTHER FRAME

Some equations and pictures...

$$\begin{aligned} -0.01\Delta u + (-1, 0)^\top \cdot \nabla u &= 1 \quad \text{in } \Omega \subset \mathbb{R}^d \\ u &= 0 \quad \text{on } \partial\Omega \end{aligned}$$



(a) Standard plot



(b) Temperature map



SECTION 2



A definition...

DEFINITION (SOMETHING TO DEFINE)

Some text...

$$B_\varepsilon(u_h, v) := \varepsilon(\nabla u_h, \nabla v) + (b \cdot \nabla u_h, v) = (f, v) \quad \forall v \in V_h.$$

MORE?





SECTION 3



- Γ the union of boundary faces (those in $\partial\Omega$).
- For $e \in \mathcal{E}_h^o$, T^+ is the downwind cell, T^- the upwind cell as determined by $b \cdot n$ on the face from each cell, n being the outward pointing normal.
- For $e \in \mathcal{E}_h^o$ the jump $[[\cdot]]$ and average $\{\{\cdot\}\}$ are defined by

$$[[\nu]] = \nu^+ n^+ + \nu^- n^-, \quad [[\tau]] = \tau^+ \cdot n^+ + \tau^- \cdot n^-$$

$$\{\{\nu\}\} = \frac{1}{2}(\nu^+ + \nu^-), \quad \{\{\tau\}\} = \frac{1}{2}(\tau^+ + \tau^-).$$

- On the boundary these become

$$[[\nu]] = \nu n, \quad \{\{\nu\}\} = \nu, \quad \{\{\tau\}\} = \tau.$$

- A very useful identity

$$\sum_{T \in \mathcal{T}_h} \int_{\partial T} \nu \tau \cdot n = \int_{e \in \mathcal{E}_h} [[\nu]] \cdot \{\{\tau\}\} + \int_{e \in \mathcal{E}_h^o} \{\{\nu\}\} [[\tau]]$$



SECTION 4

FUTURE WORK ON...



- Idea 1.
- Idea 2.
- Idea 3.

Extra info...

REFERENCES

