GOLF BALL AERODYNAMICS

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Abstract

In this project we work on golf balls and stuff.

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Acknowledgements

Chapter 1

Introduction

Stuff here about the project and aims and such.

1.1 A brief history of golf

The origins of the game of golf are difficult to trace, with suggestions that the game originated in either Scotland, France, the Netherlands, China, or even going back as far as the Roman Empire. Golf in its more modern incarnation however, is agreed to have originated in 15th century Scotland, where the first written records of the game are (somewhat humorously) related to King James II of Scotland banning the game in 1457 for fear of a decrease in archery practice in its favour.

From the 18th century onwards golf began to take form fully in Scotland, with the founding of both The Royal and Ancient Golf Club in St Andrews and The Royal Burgess Golfing Society in Edinburgh. The oldest surviving rules of golf also date from this time and these rules have been in a state of constant revision up to the modern day.

In the 19th century the popularity of golf vastly increased, seeing larger numbers of people knowing and playing the game, and the start of the first major tournaments. Additionally, the game spread out to encompass much of the British empire, to the United States and eventually to Japan, making golf into a global sport supported by a plethora of associated manufacturers, sponsors and organisations.

In the modern day, golf is potentially one of the largest sports on earth, with golf tournaments, golf manufacturing and related industries accounting for hundreds of

billions of pounds of economic activity. If successful on the golf tournament circuit, golf professionals can earn huge sums in prize money. With the players themselves and their sponsors having such a vested interest in success having a consistent and fair rule set is of paramount importance and this is dealt with jointly by The R&A (The Royal and Ancient) in most of the world and the USGA (United States Golf Association) in the Americas.

1.2   A slightly larger history of the golf ball

Golf ball technology has advanced greatly since the advent of the game. Initially, hard wooden balls were used for playing, however these were soon replaced with featherie balls which are leather pouches stuffed with feathers and then painted white.

The next major innovation in the design of golf balls came in 1848, when the gutta-percha ball was invented. This is the first ball to use a rubbery substance as continues to this day, and was easier to make into a proper sphere, unlike the previous types of ball. It was around this time that it was discovered that abrasions to the surface of the ball would improve the aerodynamic properties of the ball, making it easier to control the flight of the ball and increasing the distance at which the game could be played. This would start a series of innovations that would lead to todays dimpled balls, which we will discuss later.

After this the golf ball once again changed form with the advent of using wrapped rubber thread to help the ball to bounce better. This was coupled with the first usage of a plastic covering, in order to protect the rubber inside the ball on impact with the club. This cover also persists to this day, although the inside of the ball has seen significant development.

The modern golf ball has changed significantly from old designs. The interior of the ball is now usually a 3 piece rubber composite, with different properties in each rubber to maximize the controllability of the ball during play. The exterior is a polyurethane cover (normally white but some are in other colours) with usually between 300 to 400 dimples (though these can go as low as 200 dimples, and beyond 600 in some cases). The properties of the ball are stipulated to be within certain ranges, as set by The R&A and USGA in the rules of golf. The weight of a ball must not be greater than

(a) "Featherie" balls

(b) Pro V1 ball

Figure 1.1: In 1.1a are "Featherie" golf balls, taken from https://en.wikipedia.org/wiki/File:Featherie_golf_ball.JPG, and in 1.1b is a modern style ball, namely the Titleist Pro V1 ball.

45.93g, the diameter no less than 42.67mm and the ball must be spherically symmetric.

1.3 Aims of the project

The aim of this project is to obtain a model for how golf balls fly based on simple physical principles. Given this model we then wish to categorise individual balls based on measurements of their flight, and use this categorisation to predict trajectories for the ball

Finally, using this model, we will attempt to use a limited set of flight data (between 20 and 30 m) to predict the full flight for the ball.

Chapter 2

Preliminary Investigations and Background

In order to devise a simple model for golf ball flight we first must understand some prerequisite physics for projectiles and fluid dynamics for the airflow over the ball. Understanding how the fluid flows over the surface of the ball is crucial to understanding the difference between the flight of a golf ball and that of a standard projectile. Quantifying this effect will be a large component of this project.

There has been significant work done previously in understanding the fluid dynamics around a golf ball and how a golf ball flies. We will attempt to review some of this literature in this chapter and summarise previous work on the topic.

First though, we must understand how normal projectiles fly without taking into account fluid dynamics effects.

2.1 Projectile Motion

A projectile is a body fired into the air by an initial impulse and then allowed to fall back to ground under the action of gravity alone. This is the most naive and simplistic model of golf ball flight, completely ignoring all aerodynamic effects, however we must understand it before building up to a more complex model.

Consider motion in a 2 dimensional plane, labelled by x along the horizontal and y along the vertical A projectile is given an initial speed of the form $\vec{v}_0 = (v_x, v_y)$ at an angle α to the horizontal. We set the origin of the coordinate system to be the point

at the start of the trajectory, $(x_0, y_0) = (0,0)$. In this problem the acceleration on the projectile, after the initial impulse, is constant and of the form

$$a_x = 0, \quad a_y = -g \tag{2.1.1}$$

where g is the acceleration due to gravity. Since the acceleration is constant we can use the standard formulas for motion under constant acceleration to derive the dynamics of the projectile Young and Freedman (2008)

$$v = v_0 + at \tag{2.1.2a}$$

$$x = v_0 t + \frac{1}{2}at^2 \tag{2.1.2b}$$

$$v^2 = v_0^2 + 2ax \tag{2.1.2c}$$

$$x = \left(\frac{v_0 + v}{2}\right)t \tag{2.1.2d}$$

2.2 Basic Aerodynamics

$$\rho\frac{D\vec{q}}{Dt} = -\nabla p + \mu\nabla^2\vec{q} + f \tag{2.2.1}$$

2.3 Boundary Layers

Chapter 3

A Model of Golf Ball Flight

Chapter 4

Finding c_d and c_l

Bibliography

H. Young and R. Freedman. *University Physics*. Addison Wesley, 12 edition, 2008. ISBN 0321501306.