MIDS UC Berkeley - Machine Learning at Scale

DATSCIW261 ASSIGNMENT #1

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Week 1 Homework

References for this Assignment

- Original Assignment Instructions (https://www.dropbox.com/sh/jylzkmauxkostck/AAA2pH0cTvb0zDrbbbze3zfa/hw1 instructions.txt?dl=0)
- Wikipedia explaination of Naive Bayes document classification (https://en.wikipedia.org/wiki/Naive Bayes classifier#Document classification)
- Original paper describing the background of the Enron email corpus (http://www.aueb.gr/users/ion/docs/ceas2006_paper.pdf)
- Documentation for Scikit-Learn implementation of Naive Bayes (http://scikitlearn.org/stable/modules/naive bayes.html)
- Stanford NLP Group's explaination of Naive Bayes algorithm (http://nlp.stanford.edu/IR-book/html/htmledition/properties-of-naive-bayes-1.html)

HW 0.0 Bio

Prepare your bio and include it in this HW submission. Please limit to 100 words. Count the words in your bio and print the length of your bio (in terms of words) in a separate cell.

In [70]: bio = "Over the last five months I have worked as a data scientist in t focused on optimizing customer support experiences. Prior to that I le platform and analytics across the sales, marketing, customer support an I relocated to Austin about a year ago after residing in Seattle for 15 BS in Electrical Engineering from Union College. My goal for W261 is t experience both in theory and hands-on programming."

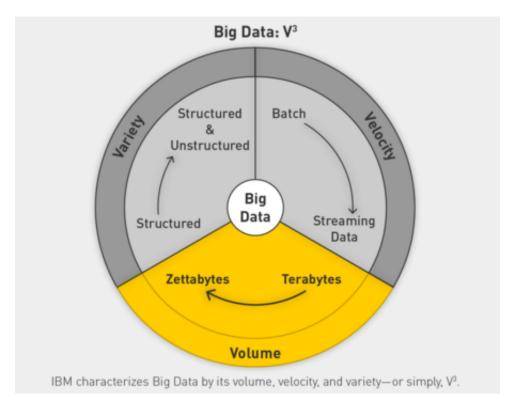
```
wordcount = len(bio.split())
print ("Bio wordcount = " + str(wordcount))
```

Bio wordcount = 97

HW1.0.0. (Graded)

Define big data. Provide an example of a big data problem in your domain of expertise.

Conceptually, Big Data is defined as data that are so large, complex and high velocity that traditional techniques are not adequate to process and deliver insights. Big Data is often described by three or four V's. Volume often distinguishes Big Data as datasets that reach the petabyte (10^15) or zettbyte (10^21) scale when compared to traditional data processing applications in the terabytes (10^12). Data these large would not fit on a typical high performance laptop with 1TB disk storage. Processing and reading even 1TB data on a laptop would take approximately 3 hours which is not satisfactory given the need to delivery timely insights. Variety includes both structured and unstructed data such as video, text, JSON, images unlike traditional systems (relational databases) that handle well-formed data in rows and columns. Velocity includes the ability of Big Data solutions to handle very fast streaming data from sources such as the social web or machine-to-machine scenarios in the Internet of Things (https://en.wikipedia.org/wiki/Internet of Things) realm. A typical laptop with even large memory would not be able to handle and persist the velocity of these data flows. Traditional data processing systems such as a data warehouses operate in batch mode that generally refresh 1-2 times a day. Veracity is the uncertainty of data and ability to manage and enforce data quality. All of these attributes make traditional data processing systems such as databases completely inadequate.



An example of a Big Data scenario at Microsoft is the collection of telemetry from hundreds of millions of Windows devices across the world on a daily basis. This results in high velocity of incoming data from user-driven actions (100's of millions of users) and application health monitoring events. A large distributed system is required to store and process the petabyte scale dataset that is collected each day.

References:

HW1.0.1. (Graded)

In 500 words (English or pseudo code or a combination) describe how to estimate the bias, the variance, the irreduciable error for a test dataset T when using polynomial regression models of degree 1,2,3,4,5 are considered. How would you select a model?

Soluion to be posted on Friday May 20th

Instructions for Spam Filter using Naive Bayes Classifier

In the remainder of this assignment you will produce a spam filter that is backed by a multinomial naive Bayes classifier b (see http://nlp.stanford.edu/IR-book/html/htmledition/properties-of-naive-bayes-1.html), which counts words in parallel via a unix, poor-man's map-reduce framework.

The data you will use is a curated subset of the Enron email corpus(whose details you may find in the file enronemail_README.txt in the directory surrounding these instructions).

In this directory you will also find starter code (pNaiveBayes.sh),(similar to the pGrepCount.sh code that was presented in this weeks lectures), which will be used as control script to a python mapper and reducer that you will supply at several stages. Doing some exploratory data analysis you will see (with this very small dataset) the following

Exploratory Data Analysis of Enron Email corpus

In [*]: ! head -n 100 enronemail_1h.txt|tail -1|less #an example SPAM email rec

0018.2003-12-18.GP 1 await your response " dear partn we are a team of government officials that belong to an eightman committee in the pres Adential cabinet as well as the senate. t the moment, we will be requiring you E assistance in a matter that involves investment of monies, which we intend to Eransfer to your account, upon clarification and a workable agreement reached in \(\sqrt{con} \) summating the project with you. based on a recommendation from an as sociate Goncerning your integrity, loyalty and understanding, we de emed it necessary to Contact you accordingly. all arrangements in r elation to this investment initiat Eve, as well as the initial capit al for its take off has been tactically set asi de to commence whate ver business you deemed fit, that will turn around profit fa Mourabl y. we request you immediately contact us if you will be favorably di spose d to act as a partner in this venture, and possibly will affor d us the opportuni Hy to discuss whatever proposal you may come up w ith. also bear in mind that th a initial capital that we shall send across will not exceed\$ 13,731, 000,00 usd [thirteen million seven hundred and thirty one thousand united states dollars) s 2 whatever areas of investment your proposal shall cover, please it should be w i Ehin the set aside capital. in this regard, the proposal you may w ish to discuss Twith us should be comprehensive enough for our bette r understanding; with speci al emphasis on the following: x obligationin your country 2. the init Mal capital base required i n your proposed investment area, as well as; 3. the ☐legal technic alities in setting up a business in your country with foreigners a s share-holders 4. the most convenient and secured mode of receivin g the funds ∏without our direct involvement. 5. your ability to pro vide a beneficiary/partn :

HW1.1.

Read through the provided control script (pNaiveBayes.sh) and all of its comments. When you are comfortable with their purpose and function, respond to the remaining homework questions below. A simple cell in the notebook with a print statement with a "done" string will suffice here.

In [9]: #Display contents of pNaiveBayes.sh (it's convenient to keep everything
!cat pNaiveBayes.sh
!echo ""
!echo "Question 1.1: DONE"

```
## pNaiveBayes.sh
## Author: Jake Ryland Williams
## Usage: pNaiveBayes.sh m wordlist
## Input:
##
         m = number of processes (maps), e.g., 4
        wordlist = a space-separated list of words in quotes, e.g.,
"the and of"
##
## Instructions: Read this script and its comments closely.
                 Do your best to understand the purpose of each comm
and,
##
                 and focus on how arguments are supplied to mapper.p
y/reducer.py,
                 as this will determine how the python scripts take
##
input.
##
                 When you are comfortable with the unix code below,
##
                 answer the questions on the LMS for HW1 about the s
tarter code.
## collect user input
m=$1 ## the number of parallel processes (maps) to run
wordlist=$2 ## if set to "*", then all words are used
## a test set data of 100 messages
data="enronemail 1h.txt"
## the full set of data (33746 messages)
# data="enronemail.txt"
## 'wc' determines the number of lines in the data
## 'perl -pe' regex strips the piped wc output to a number
linesindata=`wc -l data \mid perl -pe 's/^.*?(\d+).*?$/$1/'
## determine the lines per chunk for the desired number of processes
linesinchunk=`echo "$linesindata/$m+1" | bc`
## split the original file into chunks by line
split -l $linesinchunk $data $data.chunk.
## assign python mappers (mapper.py) to the chunks of data
## and emit their output to temporary files
for datachunk in $data.chunk.*; do
    ## feed word list to the python mapper here and redirect STDOUT
to a temporary file on disk
    ####
    ./mapper.py $datachunk "$wordlist" > $datachunk.counts &
    ####
    ####
done
## wait for the mappers to finish their work
wait
## 'ls' makes a list of the temporary count files
```

```
## 'perl -pe' regex replaces line breaks with spaces
countfiles=`\ls $data.chunk.*.counts | perl -pe 's/\n/ /'`

## feed the list of countfiles to the python reducer and redirect ST
DOUT to disk
####
####

//reducer.py $countfiles > $data.output
####
####

####

####

Clean up the data chunks and temporary count files
\rm $data.chunk.*
Ouestion 1.1: DONE
```

HW1.2.

Provide a mapper/reducer pair that, when executed by pNaiveBayes.sh will determine the number of occurrences of a single, user-specified word. Examine the word "assistance" and report your results. To do so, make sure that:

- mapper.py counts all occurrences of a single word, and
- reducer.py collates the counts of the single word.

1.2 Mapper to process Enron email corpus (100 emails)

All messages are collated to a tab-delimited format:

ID \t SPAM \t SUBJECT \t CONTENT \n.

where:

ID = string; unique message identifier SPAM = binary; with 1 indicating a spam message SUBJECT = string; title of the message CONTENT = string; content of the message

Note that either of SUBJECT or CONTENT may be "NA", and that all tab (\t) and newline (\n) characters have been removed from both of the SUBJECT and CONTENT columns.

```
In [1]: | %%writefile mapper.py
        #!/usr/bin/python
        ## mapper.py
        ## Author: James Gray
        ## Description: mapper code for HW1.2
        import sys
        import re
        count = 0
        WORD RE = re.compile(r''[\w']+")
        filename = sys.argv[1]
        findword = sys.argv[2].lower()
        with open (filename, "r") as myfile:
            # examine each line of the list of lines
            for line in myfile.readlines( ):
                 text = ""
                 # parse each line to pull out the subject and body and concaten
                enronEmail = text.join(line.split('\t')[-2:]) # take the last t
                 for word in WORD RE.findall(enronEmail):
                     if word == findword:
                         count+=1
        print count
```

Writing mapper.py

```
In [2]: # set file priveleges to execute script
!chmod a+x mapper.py
```

1.2 Reducer to total the occurences of a single word

```
In [3]: %%writefile reducer.py
#!/usr/bin/python
import sys
sum = 0
for file in sys.argv[1:]: # argument passed in is a list of chunk count
    # open each chunk count file
    with open(file, "r") as chunkfilecount:
        for line in chunkfilecount.readlines():
            tokens=line.split('\t') # the only token in this file is th
            sum+=int(tokens[0])
```

```
In [4]: # set file priveleges to execute script
!chmod a+x reducer.py
```

Writing reducer.py

1.2 Execute Unix control script

```
In [6]: # set priveleges to execute Unix script
!chmod a+x pNaiveBayes.sh

# parameter #1 -> # of mappers to run
# parameter #2 -> wordlist (the word(s) to search for and count)
!./pNaiveBayes.sh 2 assistance
```

1.2 View Output and Cross check against Grep command

This is a slight descrepency between the Unix control script and Grep command since the Grep command only evaluates the body.

HW1.3. (Graded)

Provide a mapper/reducer pair that, when executed by pNaiveBayes.sh will classify the email messages by a single, user-specified word using the multinomial Naive Bayes Formulation. Examine the word "assistance" and report your results.

To do so, make sure that:

- mapper.py and
- reducer.py

performs a single word Naive Bayes classification.

For multinomial Naive Bayes, the Pr(X = "assistance" | Y = SPAM) is calculated as follows:

the number of times "assistance" occurs in SPAM labeled documents / the number of words in documents labeled SPAM

NOTE if "assistance" occurs 5 times in all of the documents Labeled SPAM, and the length in terms of the number of words in all documents labeled as SPAM (when concatenated) is 1,000. Then Pr(X = "assistance" | Y = SPAM) = 5/1000. Note this is a multinomial

estimated of the class conditional for a Naive Bayes Classifier. No smoothing is needed in this HW.

The Naive Bayes classifier will predict the probability that an email is SPAM given the evidence of a predefined word (in this case the word "assistance"). The formula for Bayes theorem (from the book "Making Sense of Data II")

$$P(H|E) = \frac{P(E|H) * P(H)}{P(E)}$$

- P(H|E) = probability of a hypothesis(H) given some evidence(E) -> probability of SPAM given evidence of "assistance"
- P(E|H) = probability of evidence(E) given some hypothesis(H) -> probability of "assistance" given SPAM
- P(H) = probability of the hypothesis (SPAM)
- P(E) = probability of the evidence (the word "assistance")

1.3 SPAM Classifier Mapper

This mapper function will send one line for every instance of every word to the reducer. This approach, while easier to write and debug, is unlikely to be the best choice for a larger scale implementation because of the large volume of data that would have to be sent to the reducers. A potentially more-streamlined alternative would be to add a "combiner" step at the end of the mapper that would send one line for each word-email combination (E.G. Key:email-word-flag, Value:count).

In addition, if we only care about generating the conditional probabilities for each word and don't need to classify all the training emails, we could simplify the implementation even more and not send the email contents themselves to the reducer. Not only would this decrease throughput, but it would also dramatically reduce the amount of information that the reducer would need to store in memory. In this situation, our mapper could simply emit words along with their conditional class counts. I have not implemented this in this homework, but we'll want to keep this in mind for the future.

```
In [21]: | %%writefile mapper.py
         #!/usr/bin/python
         ## mapper.py
         ## Author: James Gray
         ## Description: mapper code for HW1.3
         import sys
         import re
         WORD_RE = re.compile(r"[\w']+") #Compile regex to easily parse complete
         filename = sys.argv[1]
         findwords = sys.argv[2].lower()
         with open (filename, "r") as myfile:
             for num,line in enumerate(myfile.readlines()):
                 fields=line.split('\t') #parse line into separate fields
                 subject and body=" ".join(fields[-2:]).strip()#parse the subjec
                 words=re.findall(WORD RE, subject and body) #create list of word
                 for word in words:
                     #This flag indicates to the reducer that a given word shoul
                     #by the reducer when calculating the conditional probabilit
                     flag=0
                     if word in findwords:
                         flag=1
                     #This will send one row for every word instance to the redu
                     # ID \t SPAM flag \t word \t flag for reducer
                     print fields[0]+'\t'+fields[1]+'\t'+word+'\t1\t'+str(flag)
```

Overwriting mapper.py

1.3 SPAM Classifier Reducer

The reducer maintains two associative arrays:

- The first stores information about each word, including how many times it appears in spam and ham messages, as well as if it's been flagged in the mapper.
- The second stores information about emails, including whether it is marked as spam, as well as a list of words it contains.

As described above, a more scalable solution that does not need to maintain all the contents of the emails in memory for classification could simply calculate conditional probabilities "lazily" and only store the running probability values rather than the words themselves. Once all the data has arrived from the mappers, the array containing words is updated with the calculated conditional probabilities of spam and ham. At this point, the model is "trained".

Finally, these conditional probabilities are reapplied to the word lists associated with each email to make the final spam/ham classification.

Note: I have also included (in the comments) an alternative calculation for conditional probabilities that applies a Laplace smoothing approach, since I'd already implemented it before the assignment instructions were updated. I've done the same thing with the log probability calculations.

In [22]:	

```
%%writefile reducer.py
#!/usr/bin/python
#HW 1.3 - Reducer function
from future import division #Python 3-style division syntax is much
import sys
from math import log
words={} # holds all words across the corpus
emails={}
spam email count=0 #number of emails marked as spam
spam word count=0 #number of total (not unique) words in spam emails
ham word count=0 #number of total (not unique) words in ham emails
flagged words=[]
for chunk in sys.argv[1:]: #iterate through all of the output files gen
   with open (chunk, "r") as myfile:
        for i in myfile.readlines():
            #parse the incoming line
            result=i.split("\t")
            email=result[0]
            spam=int(result[1]) # spam/ham flag
            word=result[2] # word of interest
            flag=int(result[4]) # flag from mapper denoting this is a
            #initialize storage for word/email data
            if word not in words.keys():
                words[word]={'ham count':0,'spam count':0,'flag':flag}
            if email not in emails.keys():
                emails[email]={'spam':spam,'word count':0,'words':[]}
                if spam==1:
                    spam _email_count+=1
            #store word data
            if spam==1:
                words[word]['spam count']+=1
                spam word count+=1
            else:
                words[word]['ham count']+=1
                ham word count+=1
            if flag==1 and word not in flagged words:
                flagged words.append(word)
            #store email data
            emails[email]['words'].append(word)
            emails[email]['word count']+=1
#Calculate stats for entire corpus
prior spam=spam email count/len(emails) # prior probability of SPAM
prior ham=1-prior spam # prior probability of HAM
vocab count=len(words)#number of unique words in the total vocabulary
```

for k, word in words.iteritems():

```
#These versions calculate conditional probabilities WITH Laplace sm
    #word['p spam']=(word['spam count']+1)/(spam word count+vocab count
    #word['p ham']=(word['ham count']+1)/(ham word count+vocab count)
   #Compute conditional probabilities WITHOUT Laplace smoothing
   word['p_spam']=(word['spam_count'])/(spam_word_count)
   word['p ham']=(word['ham count'])/(ham word count)
#At this point the model is now trained, and we can use it to make our
for j,email in emails.iteritems():
    #Log versions - previously used, but removed for now
    #p spam=log(prior spam)
    #p ham=log(prior ham)
   p spam=prior spam
   p ham=prior_ham
   for word in email['words']:
        if word in flagged words:
            try:
                #p spam+=log(words[word]['p spam']) #Log version - No 1
                p spam*=(words[word]['p spam'])
            except ValueError:
                continue #This means that words that do not appear in a
            try:
                #p ham+=log(words[word]['p ham']) #Log version - No lon
                p ham*=(words[word]['p ham'])
            except ValueError:
                continue
    if p spam>p_ham:
        spam pred=1
   else:
        spam pred=0
   print j+'\t'+str(email['spam'])+'\t'+str(spam pred)
```

Overwriting reducer.py

```
In [23]: # set execute priviles on mapper.py and reducer.py
!chmod a+x mapper.py reducer.py
```

1.3 Execute Naive Bayes Classifier

The output file produced by the reducer has the following structure:

ID \t SPAM \t SPAM PREDICTION

In [24]: !./pNaiveBayes.sh 5 "assistance"
!echo "HW 1.3 - Results"
!cat enronemail_1h.txt.output

HW 1.3 - Results		
0010.2003-12-18.GP 1	0	
0010.2001-06-28.SA and HP	1	1
0001.2000-01-17.beck 0	1	_
0018.1999-12-14.kaminski	0	0
0005.1999-12-12.kaminski	0	1
0011.2001-06-29.SA and HP	1	1
0008.2004-08-01.BG 1	1	1
0009.1999-12-14.farmer 0	0	
0017.2003-12-14.1aTime1 0	0	
0011.2001-06-28.SA and HP	1	1
0015.2001-00-20.SA_and_HP	1	1
0015.2001-07-03.5A_and_nr 0015.2001-02-12.kitchen 0	1	1
	1	1
0009.2001-06-26.SA_and_HP 0017.1999-12-14.kaminski		1
	0	U
0012.2000-01-17.beck 0	0	
0003.2000-01-17.beck 0	0	0
0004.2001-06-12.SA_and_HP	1	0
0008.2001-06-12.SA_and_HP	1	0
0007.2001-02-09.kitchen 0	1	
0016.2004-08-01.BG 1	0	
0015.2000-06-09.lokay 0	0	
0005.1999-12-14.farmer 0	1	
0016.1999-12-15.farmer 0	0	
0013.2004-08-01.BG 1	1	
0005.2003-12-18.GP 1	1	
0012.2001-02-09.kitchen 0	0	
0003.2001-02-08.kitchen 0	1	
0009.2001-02-09.kitchen 0	0	
0006.2001-02-08.kitchen 0	1	
0014.2003-12-19.GP 1	0	
0010.1999-12-14.farmer 0	0	
0010.2004-08-01.BG 1	0	
0014.1999-12-14.kaminski	0	0
0006.1999-12-13.kaminski	0	0
0011.1999-12-14.farmer 0	1	
0013.1999-12-14.kaminski	0	1
0001.2001-02-07.kitchen 0	1	
0008.2001-02-09.kitchen 0	0	
0007.2003-12-18.GP 1	0	
0017.2004-08-02.BG 1	1	
0014.2004-08-01.BG 1	0	
0006.2003-12-18.GP 1	0	
0016.2001-07-05.SA_and_HP	1	1
0008.2003-12-18.GP 1	0	
0014.2001-07-04.SA_and_HP	1	1
0001.2001-04-02.williams	0	0
0012.2000-06-08.lokay 0	1	
0014.1999-12-15.farmer 0	0	
0009.2000-06-07.lokay 0	0	
0001.1999-12-10.farmer 0	0	
0008.2001-06-25.SA_and_HP	1	1
0017.2001-04-03.williams	0	0
0014.2001-02-12.kitchen 0	0	

0016 2001 07 06 CA and HD	1 1
0016.2001-07-06.SA_and_HP	1 1
0015.1999-12-15.farmer 0	1
0009.1999-12-13.kaminski	0 1
0001.2000-06-06.lokay 0	1
0011.2004-08-01.BG 1	0
0004.2004-08-01.BG 1	1
0018.2003-12-18.GP 1	1
0002.1999-12-13.farmer 0	1
0016.2003-12-19.GP 1	1
0004.1999-12-14.farmer 0	0
0015.2003-12-19.GP 1	1
0006.2004-08-01.BG 1	1
0009.2003-12-18.GP 1	1
0007.1999-12-14.farmer 0	0
0005.2000-06-06.lokay 0	1
0010.1999-12-14.kaminski	0 0
0007.2000-01-17.beck 0	0
0003.1999-12-14.farmer 0	0
0003.1999-12-14.1d1me1 0	1
0017.2004-08-01.BG 1	0
0013.2001-06-30.SA_and_HP	1 0
0003.1999-12-10.kaminski	0 0
0012.1999-12-14.farmer 0	0
0004.1999-12-10.kaminski	0 1
0018.2001-07-13.SA_and_HP	1 1
0002.2001-02-07.kitchen 0	0
0007.2004-08-01.BG 1	0
0012.1999-12-14.kaminski	0 1
0005.2001-06-23.SA_and_HP	1 0
0007.1999-12-13.kaminski	0 0
0017.2000-01-17.beck 0	0
0006.2001-06-25.SA_and_HP	1 0
0006.2001-04-03.williams	0 0
0005.2001-02-08.kitchen 0	0
0002.2003-12-18.GP 1	1
0003.2003-12-18.GP 1	0
0013.2001-04-03.williams	0 0
0004.2001-04-02.williams	0 0
0010.2001-02-09.kitchen 0	0
0001.1999-12-10.kaminski	0 0
0013.1999-12-14.farmer 0	0
0015.1999-12-14.kaminski	0 0
0012.2003-12-19.GP 1	0
0016.2001-02-12.kitchen 0	0
0002.2004-08-01.BG 1	
	1 1
0002.2001-05-25.SA_and_HP	1 1
0011.2003-12-18.GP 1	0

1.3 Training Error Calculation Function

This function will be used to calculate the training error for the Naive Bayes models

1.3 Calculate Training Error for Multinomial Naive Bayes model

Interpretation of training error result: 38% of the predictions for SPAM are incorrect using the word "assistance" as an indicator for SPAM

```
In [28]: import pandas as pd

def eval_1_3():
    with open('enronemail_1h.txt.output','rb') as f:
        mr_data=pd.read_csv(f, sep='\t', header=None)
    print ("Multinomial NB Results via Poor-Man's MapReduce Implementat calculate_training_error(mr_data[1],mr_data[2])

eval_1_3()
```

```
Multinomial NB Results via Poor-Man's MapReduce Implementation using 'Assistance' only Training error: 0.38
```

HW1.4.

Provide a mapper/reducer pair that, when executed by pNaiveBayes.sh will classify the email messages by a list of one or more user-specified words.

Examine the words "assistance", "valium", and "enlargementWithATypo" and report your results (accuracy). To do so, make sure that:

- mapper.py -> counts all occurrences of a list of words
- reducer.py -> performs the multiple-word multinomial Naive Bayes classification via the chosen list. No smoothing is needed in this HW.

1.4 SPAM Classifier Mapper

This mapper function works very similarly to the implementation in 1.3. The only difference is that it enables iteration through a list of words (provided as arguments) for flagging for inclusion in the conditional probability calculation. In this example, the list of words is "assistance", "valium", and "enlargementWithATypo".

```
In [31]: %%writefile mapper.py
         #!/usr/bin/python
         #HW 1.4 - Mapper Function
         import sys
         import re
         WORD RE = re.compile(r''[\w']+")
         filename = sys.argv[1]
         findwords = sys.argv[2].lower().split()
         with open (filename, "r") as myfile:
             for num,line in enumerate(myfile.readlines()):
                 fields=line.split('\t') #parse line into separate fields
                 #parse the subject and body fields from the line, and combine i
                 subject_and_body=" ".join(fields[-2:]).strip()
                 words=re.findall(WORD RE,subject and body)
                 for word in words:
                      flag=0
                      if word in findwords:
                          flag=1
                     print fields[0]+'\t'+fields[1]+'\t'+word+'\t1\t'+str(flag)
```

Overwriting mapper.py

1.4 SPAM Classifier Reducer

This reducer is almost exactly the same as in Problem 1.3. The only difference is not in the code itself, but in the fact that it receives more than one flagged word from the mapper. Because the flagged words are tracked via a list, the reducer doesn't care how many flagged words it receives. It will incorporate all of them into the conditional probability calculation.

In [32]:	

```
%%writefile reducer.py
#!/usr/bin/python
#HW 1.4 - Reducer Function
from future import division
import sys
from math import log
emails={} #Associative array to hold email data
words={} #Associative array for word data
spam email count=0 #number of emails marked as spam
spam_word_count=0 #number of total (not unique) words in spam emails
ham word count=0 #number of total (not unique) words in ham emails
flagged words=[] #list of flagged words to include in conditional proba
for chunk in sys.argv[1:]:
   with open (chunk, "r") as myfile:
        for i in myfile.readlines():
            #parse the line
            result=i.split("\t")
            email=result[0]
            spam=int(result[1])
            word=result[2]
            flag=int(result[4])
            #initialize storage for word/email data
            if word not in words.keys():
                words[word]={'ham count':0,'spam count':0,'flag':flag}
            if email not in emails.keys():
                emails[email]={'spam':spam,'word count':0,'words':[]}
                if spam==1:
                    spam email count+=1
            #store word data
            if spam==1:
                words[word]['spam_count']+=1
                spam word count+=1
            else:
                words[word]['ham count']+=1
                ham word count+=1
            if flag==1 and word not in flagged words:
                flagged words.append(word)
            #store email data
            emails[email]['words'].append(word)
            emails[email]['word count']+=1
#Calculate stats for entire corpus
prior spam=spam email count/len(emails)
prior ham=1-prior spam
vocab count=len(words)#number of unique words in the total vocabulary
```

```
for k, word in words.iteritems():
    #These versions calculate conditional probabilities WITH Laplace sm
    #word['p_spam']=(word['spam_count']+1)/(spam_word_count+vocab_count
    #word['p_ham']=(word['ham_count']+1)/(ham_word_count+vocab_count)
    #Compute conditional probabilities WITHOUT Laplace smoothing
   word['p spam']=(word['spam count'])/(spam word count)
   word['p ham']=(word['ham count'])/(ham word count)
#At this point the model is now trained, and we can use it to make our
for j,email in emails.iteritems():
    #Log versions - no longer used
    #p spam=log(prior spam)
    #p ham=log(prior ham)
   p spam=prior spam
   p_ham=prior_ham
    for word in email['words']:
        if word in flagged words:
            try:
                #p spam+=log(words[word]['p spam']) #Log version - no 1
                p spam*=words[word]['p spam']
            except ValueError:
                pass #This means that words that do not appear in a cla
            try:
                #p ham+=log(words[word]['p ham']) #Log version - no lon
                p ham*=words[word]['p ham']
            except ValueError:
                pass
    if p spam>p ham:
        spam pred=1
   else:
        spam pred=0
    print j+'\t'+str(email['spam'])+'\t'+str(spam pred)
```

Overwriting reducer.py

```
In [33]: | # set execute priviles on mapper.py and reducer.py
         !chmod a+x mapper.py reducer.py
```

1.4 Execute Naive Bayes Classifier

In [34]: !./pNaiveBayes.sh 5 "assistance valium enlargementWithATypo"
 !echo "HW 1.4 - Results"
 !cat enronemail 1h.txt.output

HW 1.4 - Results			
0010.2003-12-18.GP	1	0	
0010.2001-06-28.SA_and_H	IP	1	1
0001.2000-01-17.beck	0	0	
0018.1999-12-14.kaminski		0	0
0005.1999-12-12.kaminski		0	1
0011.2001-06-29.SA_and_H	ΙP	1	0
0008.2004-08-01.BG	1	0	
0009.1999-12-14.farmer	0	0	
0017.2003-12-18.GP	1	0	
0011.2001-06-28.SA_and_H	ΙP	1	1
0015.2001-07-05.SA_and_H	ΙP	1	0
0015.2001-02-12.kitchen	0	0	
0009.2001-06-26.SA_and_H	IP	1	0
0017.1999-12-14.kaminski	-	0	0
0012.2000-01-17.beck	0	0	
0003.2000-01-17.beck	0	0	
0004.2001-06-12.SA and H	ΙP	1	0
0008.2001-06-12.SA and H	ΙP	1	0
0007.2001-02-09.kitchen	0	0	
0016.2004-08-01.BG	1	0	
0015.2000-06-09.lokay	0	0	
0005.1999-12-14.farmer	0	0	
0016.1999-12-15.farmer	0	0	
0013.2004-08-01.BG	1	1	
0005.2003-12-18.GP	1	0	
0012.2001-02-09.kitchen	0	0	
0003.2001-02-08.kitchen	0	0	
0009.2001-02-09.kitchen	0	0	
0006.2001-02-08.kitchen	0	0	
0014.2003-12-19.GP	1	0	
0010.1999-12-14.farmer	0	0	
0010.2004-08-01.BG	1	0	
0014.1999-12-14.kaminski	_	0	0
0006.1999-12-13.kaminski		0	0
	0	0	
0013.1999-12-14.kaminski	-	0	0
0001.2001-02-07.kitchen	0	0	
0008.2001-02-09.kitchen	0	0	
0007.2003-12-18.GP	1	0	
0017.2004-08-02.BG	1	0	
0014.2004-08-01.BG	1	0	
0006.2003-12-18.GP	1	0	
0016.2001-07-05.SA and H	_	1	0
0008.2003-12-18.GP	1	0	U
0014.2001-07-04.SA and H	_	1	0
0001.2001-07-04.SA_and_n		0	0
	_	0	U
0012.2000-06-08.lokay 0014.1999-12-15.farmer	0		
	0	0	
0009.2000-06-07.lokay	0	0	
0001.1999-12-10.farmer	0	0	^
0008.2001-06-25.SA_and_H		1	0
0017.2001-04-03.williams		0	0
0014.2001-02-12.kitchen	U	0	

0016.2001-07-06.SA and HP	1 0
	_
0015.1999-12-15.farmer 0 0009.1999-12-13.kaminski	0
	0 0
0001.2000-06-06.lokay 0	0
0011.2004-08-01.BG 1	0
0004.2004-08-01.BG 1	0
0018.2003-12-18.GP 1	1
0002.1999-12-13.farmer 0	0
0016.2003-12-19.GP 1	1
0004.1999-12-14.farmer 0	0
0015.2003-12-19.GP 1	0
0006.2004-08-01.BG 1	0
0009.2003-12-18.GP 1	1
0007.1999-12-14.farmer 0	0
0005.2000-06-06.lokay 0	0
0010.1999-12-14.kaminski	0 0
0007.2000-01-17.beck 0	0
0003.1999-12-14.farmer 0	0
0003.2004-08-01.BG 1	0
0017.2004-08-01.BG 1	1
0013.2001-06-30.SA_and_HP	1 0
0003.1999-12-10.kaminski	0 0
0012.1999-12-14.farmer 0	0
0004.1999-12-10.kaminski	0 1
0018.2001-07-13.SA and HP	1 1
0002.2001-02-07.kitchen 0	0
0007.2004-08-01.BG 1	0
0012.1999-12-14.kaminski	0 0
0005.2001-06-23.SA and HP	1 0
0007.1999-12-13.kaminski	0 0
0017.2000-01-17.beck 0	0
0006.2001-06-25.SA and HP	1 0
0006.2001-04-03.williams	0 0
0005.2001-02-08.kitchen 0	0
0002.2003-12-18.GP 1	0
0003.2003-12-18.GP 1	0
0013.2001-04-03.williams	0 0
0004.2001-04-02.williams	0 0
0010.2001-02-09.kitchen 0	0
0001.1999-12-10.kaminski	0 0
0013.1999-12-14.farmer 0	0
0015.1999-12-14.Tarmer 0	
	0 0
0012.2003-12-19.GP 1	0
0016.2001-02-12.kitchen 0	0
0002.2004-08-01.BG 1	1
0002.2001-05-25.SA_and_HP	1 0
0011.2003-12-18.GP 1	0

1.4 Calculate Training Error for Multinomial Naive Bayes model

The training error was reduced by 1% (38% to 37%) by adding a few words to identify SPAM emails.

```
In [36]: #HW 1.4 - Evaluation code

def eval_1_4():
    with open('enronemail_1h.txt.output','rb') as f:
        mr_data=pd.read_csv(f, sep='\t', header=None)
    print ("Multinomial NB Results via Poor-Man's MapReduce Implementat calculate_training_error(mr_data[1],mr_data[2])

eval_1_4()
```

Multinomial NB Results via Poor-Man's MapReduce Implementation using 'Assistance valium EnlargementWithATypo' Training error: 0.37

HW1.5.

Provide a mapper/reducer pair that, when executed by pNaiveBayes.sh will classify the email messages by all words present.

To do so, make sure that:

- mapper.py counts all occurrences of all words, and
- reducer.py performs a word-distribution-wide Naive Bayes classification.

1.5 SPAM Classifier Mapper

This mapper will need to consider all words in the email instead of specific pre-defined words. The change from the other mappers is that the check for the word and flag for the reducer was removed.

```
In [38]: | %%writefile mapper.py
         #!/usr/bin/python
         #HW 1.5 - Mapper Function
         import sys
         import re
         WORD RE = re.compile(r''[\w']+")
         filename = sys.argv[1]
         with open (filename, "r") as myfile:
             for num,line in enumerate(myfile.readlines()):
                 fields=line.split('\t') #parse line into separate fields
                 # parse the subject and body fields from the line, and combine
                 subject_and_body=" ".join(fields[-2:]).strip()
                 words=re.findall(WORD RE,subject and body)
                 for word in words:
                     # ID \t SPAM flag \t word
                     print fields[0]+'\t'+fields[1]+'\t'+word+'\t1'
```

Overwriting mapper.py

1.5 SPAM Classifier Reducer

The reducer is similar to the above reducers although the check for flagged words was removed as we need to calculate the conditional probabilities of all words

In [39]:	•	

```
%%writefile reducer.py
#!/usr/bin/python
#HW 1.5 - Reducer Function
from future__ import division
import sys
from math import log
emails={}
words={}
spam email count=0 #number of emails marked as spam
spam word count=0 #number of total (not unique) words in spam emails
ham word count=0 #number of total (not unique) words in ham emails
for chunk in sys.argv[1:]:
   with open (chunk, "r") as myfile:
        for i in myfile.readlines():
            #parse the line
            result=i.split("\t")
            email=result[0]
            spam=int(result[1])
            word=result[2]
            #initialize storage for word/email data
            if word not in words.keys():
                words[word]={'ham count':0,'spam count':0}
            if email not in emails.keys():
                emails[email]={'spam':spam,'word count':0,'words':[]}
                if spam==1:
                    spam email count+=1
            #store word data
            if spam==1:
                words[word]['spam count']+=1
                spam word count+=1
            else:
                words[word]['ham count']+=1
                ham word count+=1
            #store email data
            emails[email]['words'].append(word)
            emails[email]['word count']+=1
#Calculate stats for entire corpus
prior spam=spam email count/len(emails)
prior ham=1-prior spam
vocab count=len(words)#number of unique words in the total vocabulary
for k, word in words.iteritems():
    #These versions calculate conditional probabilities WITH Laplace sm
    #word['p spam']=(word['spam count']+1)/(spam word count+vocab count
    #word['p ham']=(word['ham count']+1)/(ham word count+vocab count)
```

```
word['p spam']=(word['spam count'])/(spam word count)
   word['p ham']=(word['ham count'])/(ham word count)
#At this point the model is now trained, and we can use it to make our
for j,email in emails.iteritems():
    #Log Version - not used
    p spam=log(prior spam)
   p ham=log(prior ham)
   p_spam=prior_spam
   p ham=prior ham
    for word in email['words']:
        try:
            #p spam+=log(words[word]['p spam']) #Log Version - not used
            p spam*=(words[word]['p spam'])
        except ValueError:
            continue #This means that words that do not appear in a cla
        try:
            #p_ham+=log(words[word]['p_ham']) #Log Version - not used
            p ham*=(words[word]['p ham'])
        except ValueError:
            continue
    if p spam>p ham:
        spam pred=1
   else:
        spam pred=0
    #print spam pred, email['spam'],p spam,p ham,j
    print j+'\t'+str(email['spam'])+'\t'+str(spam pred)
```

Overwriting reducer.py

```
In [40]: # set execute priviles on mapper.py and reducer.py
!chmod a+x mapper.py reducer.py
```

1.5 Execute Naive Bayes Classifier

In [42]: !./pNaiveBayes.sh 4 "*";
! cat enronemail_1h.txt.output

	MILDS	WZOI ZOIS IIWK WEEKOI	Gra
0010.2003-12-18.GP	1	1	
0010.2001-06-28.SA and	HP	1	0
0001.2000-01-17.beck	0	0	
0018.1999-12-14.kamins	ςi	0	0
0005.1999-12-12.kamins		0	0
0011.2001-06-29.SA and	HP	1	0
0008.2004-08-01.BG	1	0	
0009.1999-12-14.farmer	0	0	
0017.2003-12-18.GP	1	1	
0011.2001-06-28.SA and	HP	1	0
0015.2001-07-05.SA and	_	1	0
0015.2001-02-12.kitcher	_	0	
0009.2001-06-26.SA and		1	0
0017.1999-12-14.kamins	_	0	0
0012.2000-01-17.beck	0	0	·
0003.2000-01-17.beck	0	0	
0004.2001-06-12.SA and	_	1	0
0008.2001-06-12.SA and	_	1	0
0007.2001-02-09.kitcher	_	0	Ü
0016.2004-08-01.BG	1	1	
0015.2004-06-01.bg	0	0	
0005.1999-12-14.farmer	0	0	
0016.1999-12-15.farmer	_		
	0	0	
0013.2004-08-01.BG	1	0	
0005.2003-12-18.GP	1	0	
0012.2001-02-09.kitcher		0	
0003.2001-02-08.kitcher		0	
0009.2001-02-09.kitcher		0	
0006.2001-02-08.kitcher		0	
0014.2003-12-19.GP	1	1	
0010.1999-12-14.farmer	0	0	
0010.2004-08-01.BG	. 1	0	_
0014.1999-12-14.kamins		0	0
0006.1999-12-13.kamins	۲i	0	0
0011.1999-12-14.farmer	0	0	
0013.1999-12-14.kamins		0	0
0001.2001-02-07.kitcher		0	
0008.2001-02-09.kitcher	1 O	0	
0007.2003-12-18.GP	1	0	
0017.2004-08-02.BG	1	0	
0014.2004-08-01.BG	1	0	
0006.2003-12-18.GP	1	0	
0016.2001-07-05.SA_and_	HP	1	0
0008.2003-12-18.GP	1	0	
0014.2001-07-04.SA_and_	HP	1	0
0001.2001-04-02.william	ns	0	0
0012.2000-06-08.lokay	0	0	
0014.1999-12-15.farmer	0	0	
0009.2000-06-07.lokay	0	0	
0001.1999-12-10.farmer	0	0	
0008.2001-06-25.SA_and	HP	1	0
0017.2001-04-03.william	_	0	0
0014.2001-02-12.kitcher		0	
0016.2001-07-06.SA and		1	0
	- '		-

0015.1999-12-15.farmer 0	0	
0009.1999-12-13.kaminski	0	0
0001.2000-06-06.lokay 0	0	
0011.2004-08-01.BG 1	1	
0004.2004-08-01.BG 1	0	
0018.2003-12-18.GP 1	0	
0002.1999-12-13.farmer 0	0	
0016.2003-12-19.GP 1	0	
0004.1999-12-14.farmer 0	0	
0015.2003-12-19.GP 1	0	
0006.2004-08-01.BG 1	0	
0009.2003-12-18.GP 1	0	
0007.1999-12-14.farmer 0	0	
0005.2000-06-06.lokay 0	0	
0010.1999-12-14.kaminski	0	0
0007.2000-01-17.beck 0	0	
0003.1999-12-14.farmer 0	0	
0003.2004-08-01.BG 1	0	
0017.2004-08-01.BG 1	0	
0013.2001-06-30.SA and HP	1	0
0003.1999-12-10.kaminski	0	0
0012.1999-12-14.farmer 0	0	ŭ
0004.1999-12-10.kaminski	0	0
0018.2001-07-13.SA and HP	1	0
0002.2001-02-07.kitchen 0	0	O
0007.2004-08-01.BG 1	0	
0012.1999-12-14.kaminski	0	0
0005.2001-06-23.SA and HP	1	1
0007.1999-12-13.kaminski	0	0
		U
	0	1
0006.2001-06-25.SA_and_HP 0006.2001-04-03.williams	1	1
	0	0
0005.2001-02-08.kitchen 0	0	
0002.2003-12-18.GP 1	0	
0003.2003-12-18.GP 1	0	0
0013.2001-04-03.williams	0	0
0004.2001-04-02.williams	0	0
0010.2001-02-09.kitchen 0	0	•
0001.1999-12-10.kaminski	0	0
0013.1999-12-14.farmer 0	0	
0015.1999-12-14.kaminski	0	0
0012.2003-12-19.GP 1	1	
0016.2001-02-12.kitchen 0	0	
0002.2004-08-01.BG 1	0	
0002.2001-05-25.SA_and_HP	1	1
0011.2003-12-18.GP 1	1	

1.5 Calculate Training Error for Multinomial Naive Bayes model

By considering all of the words the training error was reduced an additional 3%

```
In [44]: def eval_1_5():
    with open('enronemail_1h.txt.output','rb') as f:
        mr_data=pd.read_csv(f, sep='\t', header=None)
    print ("Multinomial NB Results via Poor-Man's MapReduce Implementat calculate_training_error(mr_data[1],mr_data[2])
    eval_1_5()
```

Multinomial NB Results via Poor-Man's MapReduce Implementation Training error: 0.34

HW1.6

Benchmark your code with the Python SciKit-Learn implementation of multinomial Naive Bayes.

It always a good idea to test your solutions against publicly available libraries such as SciKit-Learn, The Machine Learning toolkit available in Python. In this exercise, we benchmark ourselves against the SciKit-Learn implementation of multinomial Naive Bayes. For more information on this implementation see: <a href="http://scikit-naive-n

learn.org/stable/modules/naive bayes.html (http://scikit-

<u>learn.org/stable/modules/naive_bayes.html</u>) more

Training error = misclassification rate with respect to a training set. It is more formally defined here:

Let DF represent the training set in the following: $Err(Model, DF) = |\{(X, c(X)) \in DF : c(X) != Model(x)\}| / |DF|$

Where \parallel denotes set cardinality; c(X) denotes the class of the tuple X in DF; and Model(X) denotes the class inferred by the Model "Model"

In this exercise, please complete the following:

- Run the Multinomial Naive Bayes algorithm (using default settings) from SciKit-Learn over the same training data used in HW1.5 and report the Training error (please note some data preparation might be needed to get the Multinomial Naive Bayes algorithm from SkiKit-Learn to run over this dataset)
- 2. Please prepare a table to present your results
- 3. Explain/justify any differences in terms of training error rates over the dataset in HW1.5 between your Multinomial Naive Bayes implementation (in Map Reduce) versus the Multinomial Naive Bayes implementation in SciKit-Learn (Hint: smoothing, which we will discuss in next lecture)
- 4. Discuss the performance differences in terms of training error rates over the dataset in HW1.5 between the Multinomial Naive Bayes implementation in SciKit-Learn with the Bernoulli Naive Bayes implementation in SciKit-Learn

```
In [52]: import re
    import numpy as np
    import pandas as pd
    from sklearn.naive_bayes import MultinomialNB, BernoulliNB
    from sklearn.feature_extraction.text import CountVectorizer
```

1.6 Data read and cleaning for SK Learn Multinomial NB Algorithm

There are some lines with "NA" as the body and these should be removed to properly train the model

				ısıana ıarger	
7	0002.2001-02- 07.kitchen	0	congrats!	contratulations on the execution of the centr	congrats! contratulations on the execution of
8	0002.2001-05- 25.SA_and_HP	1	fw: this is the solution i mentioned lsc	oo thank you, your email address was obtain	fw: this is the solution i mentioned lsc oo
9	0002.2003-12- 18.GP	1	adv: space saving computer to replace that bi	revolutionary!!! full featured!!! space savi	adv: space saving computer to replace that bi
10	0002.2004-08- 01.BG	1	advs	greetings, i am benedicta lindiwe hendricks	advs greetings, i am benedicta lindiwe hendr

1.6 Create text features using CountVectorizer

The CountVectorizer (http://scikit-

<u>learn.org/stable/modules/generated/sklearn.feature_extraction.text.CountVectorizer.html)</u> converts a collection of text documents to a matrix of token counts. Here it will process the 'subject_body' field of the DataFrame to create a vector of words and their counts. The

fit_transform method creates a document-term matrix on the number of times a specific word (feature) appears in the document. In this scenario we have 100 or less records given that we filtered out the records where an "NA" appears in the row.

In [58]: # create matrix for a single word, convert to lowercase first, filter w
 vectorizer = CountVectorizer(analyzer='word', lowercase=True)
 # create a document-term matrix
 vocabulary = vectorizer.fit_transform(dataClean['subject_body'])
 print (vocabulary)

(0, (0, (1, (1, (1, (1, (1, (1, (1, (1, (1, (1	3886) 3871) 4731) 5255) 4731) 5255) 2838) 1524) 3606) 4167) 5136) 4785) 625) 526) 4301) 3914) 619) 3552) 3448) 1581) 2910) 785) 2651) 518) 4967)	1 1 1 1 5 7 3 6 1 1 1 1 1 1 2 3 1 2 1 3 4 2 2
(93, (93, (93, (93, (93, (93, (93, (93,	3824) 3678) 607) 4633) 3840) 1652) 4717) 2081) 2633) 3553) 1261) 395) 1190) 4506) 1399) 382) 729) 1392) 103)	1 1 2 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1

1.6 Run SK Learn Multinomial Naive Bayer Classifier

The multinomial Naive Bayes (http://scikit-

<u>learn.org/stable/modules/generated/sklearn.feature_extraction.text.CountVectorizer.html</u>) algorithm uses word counts for classification.

```
In [64]: multiNB = MultinomialNB()
# fit the model to the training data using document-term matrix and cla
multiNB.fit(vocabulary, dataClean['spamflag'])
# make predictions using the training data
mnbclf_results = multiNB.predict(vocabulary)
# calculate accuracy using metrics libary
from sklearn.metrics import accuracy_score
print ("SK Learn Multinomial NB training error: " + str(1-accuracy_score)
```

SK Learn Multinomial NB training error: 0.0

1.6 Run SK Learn Bernoulli Naive Bayer Classifier

The <u>bernoulli Naives Bayes (http://nlp.stanford.edu/IR-book/html/htmledition/the-bernoulli-model-1.html)</u> algorithm generates either a 1 for the presence of the term in a document or 0 for an absence.

```
In [65]: # instantiate a bernoulli model
bernNB = BernoulliNB()
# fit the model to the training data using
bernNB.fit(vocabulary, dataClean['spamflag'])
bernclf_results = bernNB.predict(vocabulary)
# calculate accuracy using metrics libary
print ("SK Learn Bernoulli NB training error: " + str(1-accuracy_score())
```

SK Learn Bernoulli NB training error: 0.234042553191

1.6 Summary of Error Results and Conclusions

This section compares and contrasts errors produces by map-reduce and scikit-learn

Model	Training Error
Multinomial NB, Scikit-Learn Implementation	0.00
Bernoulli NB, Scikit-Learn Implementation	0.23
Multinomial NB HW1.5, MapReduce implementation	0.34

Analysis of Multinomial Naive Bayes models (MapReduce and scikit-learn)

The map-reduce Multinomial Naive Bayes model accuracy was significantly higher than the scikit-learn implementation. A few considerations come to mind why there was a difference. In the map-reduce implementation we did not design for Laplace smoothing and therefore terms that do not exist in the vocabulary produce a zero probability. Laplace smoothing is set by default in the scikit-learn implementation. Feature extraction may have also played a role. In the map-reduce implementation we used regex to parse for words while scikit-learn's countvectorizer includes digits in words while ignoring hyphenations and contractions. This can result in larger and richer vocabulary resulting in lower error.

Analysis of scikit-learn Bernoulli and Multinomial Naive Bayes models (scikit-learn)

The error of the multinomial and bernoulli naive bayes models implemented in scikit-learn differ significantly. The multinomial model error was 0 (not realistic in the real world because in this case we tested the model with training data) while the bernoulli model was 0.23. The primary reason is the multinomial model uses word counts to estimate probabilities while the bernoulli model is binary if the word appears in the document or not. This enables the multinomial model to discriminate at a deeper level and we should expect to see a lower error when compared to the Bernoulli model.

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