

# Privacy, Data Privacy and Differential Privacy

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## THE RIGHT TO PRIVACY.

“It could be done only on principles of private justice, moral fitness,  
and public convenience, which, when applied to a new subject, make



Samuel D. Warren II

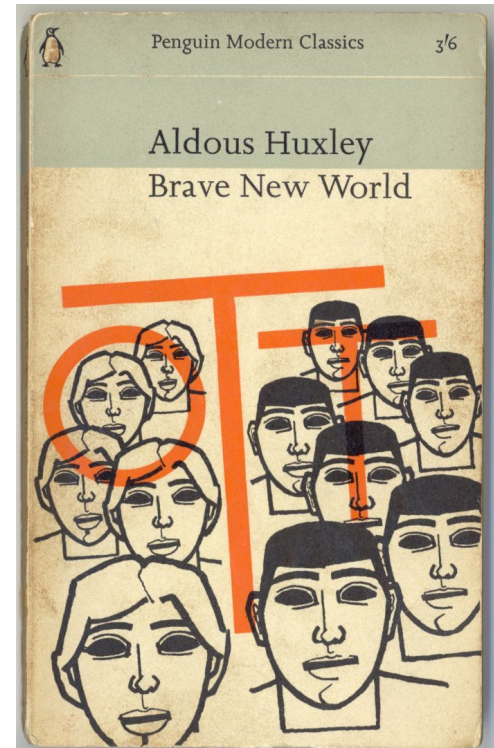


Louis Brandeis

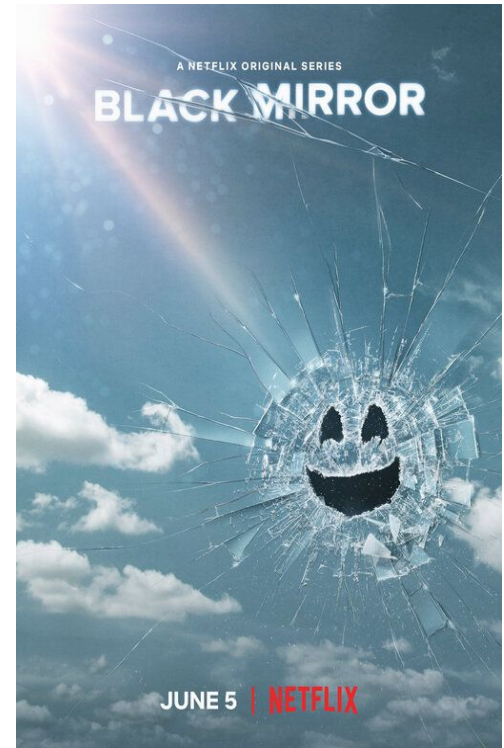
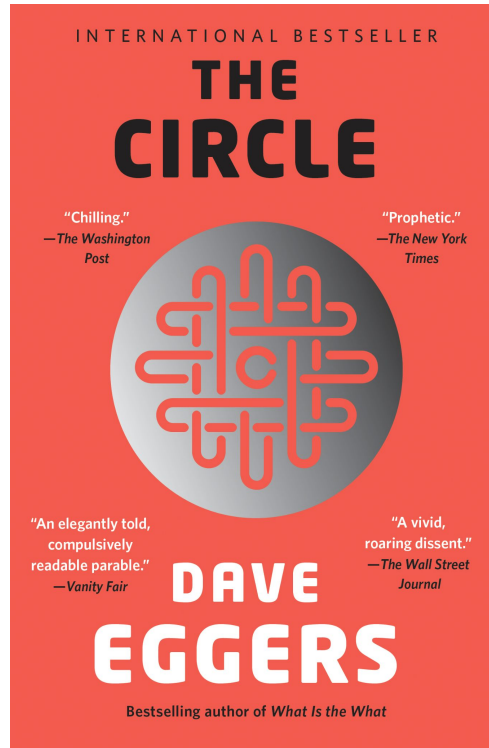
*The right to be  
let alone.*



“Nothing was your own except the few cubic centimeters in your skull.”



“I’m claiming the right to be unhappy.”



Decisional Privacy

Informational Privacy

# Decisional Privacy

*Autonomy in making  
personal decisions,  
particularly regarding their  
body or actions within their  
home*

# Informational Privacy

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*Autonomy in making  
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# Informational Privacy

*Control over one's personal  
information*

(aka **Data Privacy**)

# Differential Privacy (Dwork et al. 2006)



# Differential Privacy (Dwork et al. 2006)

Define the multiplicative distance  $\text{MULT}(P, Q)$  between two distributions  $P$  and  $Q$ :

$$\text{MULT}(P, Q) = \sup_S \left| \ln \frac{P(S)}{Q(S)} \right|,$$

where  $\frac{0}{0} := 1$ .

Let  $\Pr(\mathbf{X}|\mathbf{D})$  denote the probability distribution of the output  $\mathbf{X}$  given the observed data  $\mathbf{D}$ . For example,  $\Pr(\mathbf{X}|\mathbf{D})$  is a Normal distribution centred at the observed-data estimate  $q(\mathbf{D})$ .  $\epsilon$ -differential privacy states that

$$\text{MULT}\left(\Pr(\mathbf{X}|\mathbf{D}), \Pr(\mathbf{X}|\mathbf{D}')\right) \leq \epsilon,$$

for all neighbouring datasets  $\mathbf{D}, \mathbf{D}'$ .

# Differential Privacy (Dwork et al. 2006)

Neighbouring datasets usually mean: 1) delete/add one record/individual; 2) alter one record.

$\epsilon$  is called the ‘privacy loss budget’ but should be ‘log of the privacy loss budget’

DP is a bound on the log-likelihood ratio, where the likelihood is of publishing **X** based on **D** versus **D'**.

# Differential Privacy (Dwork et al. 2006)

Differential privacy limits the power of an  $\alpha$ -level hypothesis test of  $H_0 : D_i = s$  versus  $H_1 : D_i = t$ :

$$\text{Power} \leq \alpha e^\epsilon$$

(Wasserman & Zhou, 2010.)

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Assumes that individual records are independent.

If  $\alpha = 0.05$ , non-trivial bound only when  $\epsilon \leq \ln 20 \approx 3$ .

# Bayesian Interpretation

$\mathbf{X}$  satisfies  $\epsilon$ -differential privacy if and only if for all priors  $\pi$  on  $\mathbf{D}$ ,

$$\text{MULT}\left(\pi(D_i|\mathbf{X}, \mathbf{D}_{-i}), \pi(D_i|\mathbf{D}_{-i})\right) \leq \epsilon.$$

# Worst-Case is Not Necessarily the Worst-Case

Consider  $\mathbf{D} = \{0, 1\}^n$  and  $X = \sum_i D_i + \frac{1}{\epsilon}L$ , where  $L$  is Laplace. Let

$$\pi \left( \sum_i D_i = 0 \right) = \pi \left( \sum_i D_i = 1 \right) = 0.5.$$

Suppose that  $X = n + 1$ . Then

$$\pi(D_1 = 0|X) = \pi \left( \sum_i D_i = 0|X \right) = \frac{\exp(-[n+1]/\epsilon)}{\exp(-[n+1]/\epsilon) + \exp(-1/\epsilon)} \rightarrow 0,$$

as  $n \rightarrow \infty$ .

# Statistical Data Privacy

*How to release informative statistics **X** without compromising privacy of respondents?*

NSOs have been aware of the privacy risks of publishing aggregate information **X** for at least 50 years (Dalenius, 1977)



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So why all the talk of differential privacy?

# The Changing Privacy Landscape

ARTICLE



## Revealing information while preserving privacy

**Authors:**  [Irit Dinur](#),  [Kobbi Nissim](#) [Authors Info & Claims](#)

PODS '03: Proceedings of the twenty-second ACM SIGMOD-SIGACT-SIGART symposium on Principles of database systems • June 2003 • Pages 202–210 • <https://doi-org.ezp-prod1.hul.harvard.edu/10.1145/773153.773173>

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Authors:



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## Robust De-anonymization of Large Sparse Datasets

Arvind Narayanan and Vitaly Shmatikov

The University of Texas at Austin

### Abstract

*We present a new class of statistical de-anonymization attacks against high-dimensional micro-data, such as individual preferences, recommendations, transaction records and so on. Our techniques are robust to perturbation in the data and tolerate some mistakes in the adversary's background knowledge.*

*We apply our de-anonymization methodology to the Netflix Prize dataset, which contains anonymous movie ratings of 500,000 subscribers of Netflix, the world's largest online movie rental service. We demonstrate*

and sparsity. Each record contains many attributes (*i.e.*, columns in a database schema), which can be viewed as dimensions. Sparsity means that for the average record, there are no “similar” records in the multi-dimensional space defined by the attributes. This sparsity is empirically well-established [7, 4, 19] and related to the “fat tail” phenomenon: individual transaction and preference records tend to include statistically rare attributes.

**Our contributions.** Our first contribution is a formal model for privacy breaches in anonymized micro-data (section 3). We present two definitions, one based on the



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practice

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anonymization  
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these techniques to  
Netflix Prize  
ratings of 50  
movies online.

Article development led by ACM Queue

**These attacks on statistical databases  
are no longer a theoretical danger.**

BY SIMSON GARFINKEL, JOHN M. ABOWD,  
AND CHRISTIAN MARTINDALE

## Understanding Database Reconstruction Attacks on Public Data

IN 2020, THE U.S. Census Bureau will conduct the

DOI:10.1145/3287287

so the reconstruction no longer results  
in the original data. This has implica-  
tions for the 2020 census.

The goal of the census is to count  
every person once, and only once, and  
in the correct place. The results are  
used to fulfill the Constitutional re-  
quirement to apportion the seats in  
the U.S. House of Representatives  
among the states according to their  
respective numbers.

In addition to this primary purpose  
of the decennial census, the U.S. Con-  
gress has mandated many other uses  
for the data. For example, the U.S. De-  
partment of Justice uses block-by-  
block counts by race for enforcing the  
Voting Rights Act. More generally, the  
results of the decennial census, com-  
bined with other data, are used to  
help distribute more than \$675 bil-  
lion in federal funds to states and lo-  
cal organizations.

Beyond collecting and distributing  
data on U.S. citizens, the Census Bu-  
reau is also charged with protecting the  
privacy and confidentiality of survey re-  
sponses. All census publications must  
uphold the confidentiality standard  
specified by Title 13, Section 9 of the  
U.S. Code, which states that Census Bu-  
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Review

Authors

## LINEAR PROGRAM RECONSTRUCTION IN PRACTICE

ALONI COHEN AND KOBBI NISSIM

PODS '03

2003 •

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Online:

Department of Computer Science, Georgetown University  
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461

**ABSTRACT.** We briefly report on a successful linear program reconstruction attack performed on a production statistical queries system and using a real dataset. The attack was deployed in test environment in the course of the Aircloak Challenge bug bounty

IN 2020, THE U.S. Census Bureau will conduct the

identifying "the data furnished by any particular establishment or individual." This section prohibits the Census



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2017 4:61-84. Downloaded from www.annualreviews.org  
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Annu. Rev. Stat. Appl. 2017. 4:61-84

First published online as a Review in Advance on  
December 21, 2016

## Exposed! A Survey of Attacks on Private Data

Cynthia Dwork,<sup>1</sup> Adam Smith,<sup>2</sup> Thomas Steinke,<sup>3</sup>  
and Jonathan Ullman<sup>4</sup>

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<sup>4</sup>College of Computer and Information Science, Northeastern University, Boston,  
Massachusetts 02115; email: jullman@ccs.neu.edu

### Keywords

privacy, privacy attacks, re-identification, reconstruction attacks, tracing

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an 2019  
an 2020



• June



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# The Changing Privacy Landscape

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No. 1

PROCEEDINGS ON PRIVACY ENHANCING TECHNOLOGIES

# PoPETs

EDITED BY HASSAN JAMEEL ASGHAR AND DALI KAAFAR

 Open Access

## Averaging Attacks on Bounded Noise-based Disclosure Control Algorithms

[Hassan Jameel Asghar](#) and [Dali Kaafar](#)

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Proceedings on Privacy

2017/4  
Harvard

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But...



# But...

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# But...

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**1964:** privacy was “evaporating [and] under assault from many directions” (Packard)  
– so much so, in fact, that “we [were standing] on the threshold of what might be called the Age of the Goldfish Bowl” (Brenton)

**1890:** “Numerous mechanical devices threaten to make good the prediction that ‘what is whispered in the closet shall be proclaimed from the house-tops’” (Warren & Brandeis)

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- How do we get informed consent? How do we articulate the privacy risks while still emphasising the net positive benefit to responding to a survey?
- What data is identifying, what data is identifiable and what data constitutes an identity?
- What data is publicly available and how may this change the privacy assessment?

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