

Privacy, Data Privacy and Differential Privacy

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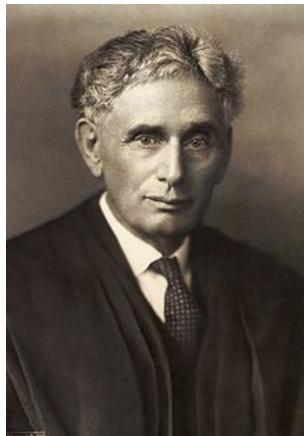
NO. 5.

THE RIGHT TO PRIVACY.

"It could be done only on principles of private justice, moral fitness, and public convenience, which, when applied to a new subject, make



Samuel D. Warren II

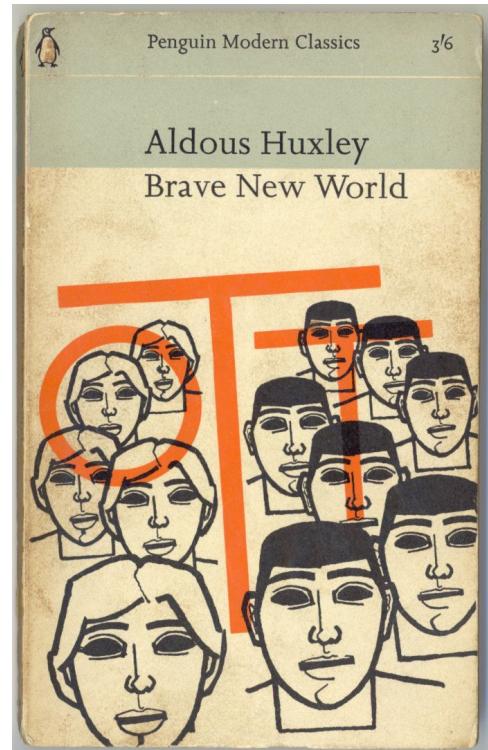


Louis Brandeis

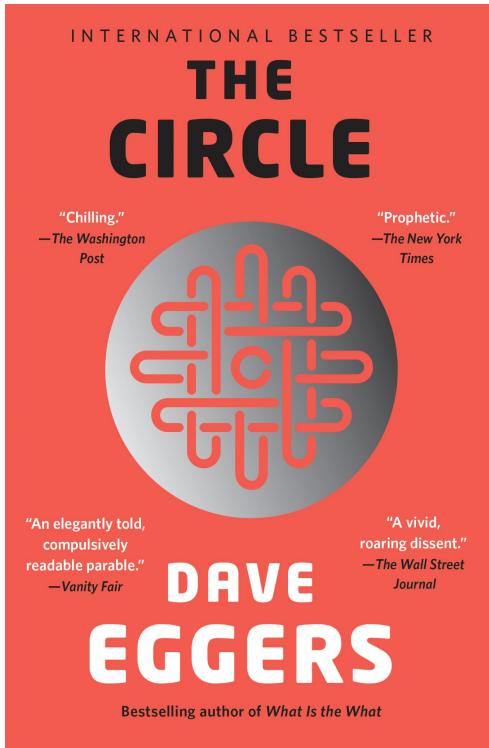
*The right to be
let alone.*



"Nothing was your own except the few cubic centimeters in your skull."



"I'm claiming the right to be unhappy."



Decisional Privacy

Informational Privacy

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Autonomy in making personal decisions, particularly regarding their body or actions within their home

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Informational Privacy

Control over one's personal information
(aka Data Privacy)

Differential Privacy (Dwork et al. 2006)

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Define the multiplicative distance $\text{MULT}(P, Q)$ between two distributions P and Q :

$$\text{MULT}(P, Q) = \sup_S \left| \ln \frac{P(S)}{Q(S)} \right|,$$

where $\frac{0}{0} := 1$.

Let $\Pr(\mathbf{X}|\mathcal{D})$ denote the probability distribution of the output \mathbf{X} given the observed data \mathcal{D} . For example, $\Pr(\mathbf{X}|\mathcal{D})$ is a Normal distribution centred at the observed-data estimate $q(\mathcal{D})$. ϵ -differential privacy states that

$$\text{MULT}\left(\Pr(\mathbf{X}|\mathcal{D}), \Pr(\mathbf{X}|\mathcal{D}')\right) \leq \epsilon,$$

for all neighbouring datasets $\mathcal{D}, \mathcal{D}'$.

Differential Privacy (Dwork et al. 2006)

Neighbouring datasets usually mean: 1) delete/add one record/individual; 2) alter one record.

ϵ is called the ‘privacy loss budget’ but should be ‘log of the privacy loss budget’

DP is a bound on the log-likelihood ratio, where the likelihood is of publishing X based on D versus D' .

Differential Privacy (Dwork et al. 2006)

Differential privacy limits the power of an α -level hypothesis test of $H_0 : D_i = s$ versus $H_1 : D_i = t$:

$$\text{Power} \leq \alpha e^\epsilon$$

(Wasserman & Zhou, 2010.)

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If $\alpha = 0.05$, non-trivial bound only when $\epsilon \leq \ln 20 \approx 3$.

Bayesian Interpretation

\mathbf{X} satisfies ϵ -differential privacy if and only if for all priors π on \mathcal{D} ,

$$\text{MULT}\left(\pi(D_i|\mathbf{X}, \mathcal{D}_{-i}), \pi(D_i|\mathcal{D}_{-i})\right) \leq \epsilon.$$

Worst-Case is Not Necessarily the Worst-Case

Consider $D = \{0, 1\}^n$ and $X = \sum_i D_i + \frac{1}{\epsilon}L$, where L is Laplace. Let

$$\pi \left(\sum_i D_i = 0 \right) = \pi \left(\sum_i D_i = 1 \right) = 0.5.$$

Suppose that $X = n + 1$. Then

$$\pi(D_1 = 0 | X) = \pi \left(\sum_i D_i = 0 | X \right) = \frac{\exp(-[n+1]/\epsilon)}{\exp(-[n+1]/\epsilon) + \exp(-1/\epsilon)} \rightarrow 0,$$

as $n \rightarrow \infty$.

Statistical Data Privacy

How to release informative statistics X without compromising privacy of respondents?

NSOs have been aware of the privacy risks of publishing aggregate information X for at least 50 years (Dalenius, 1977)

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So why all the talk of differential privacy?

The Changing Privacy Landscape

ARTICLE



Revealing information while preserving privacy

Authors: [Irit Dinur](#), [Kobbi Nissim](#) [Authors Info & Claims](#)

PODS '03: Proceedings of the twenty-second ACM SIGMOD-SIGACT-SIGART symposium on Principles of database systems • June 2003 • Pages 202–210 • <https://doi.org.ezp-prod1.hul.harvard.edu/10.1145/773153.773173>

Online: 09 June 2003 [Publication History](#)

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The Changing Privacy Landscape

ARTICLE

Reveal



Robust De-anonymization of Large Sparse Datasets

Arvind Narayanan and Vitaly Shmatikov

The University of Texas at Austin

Authors:

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2003 • Page

Online: 09 Ju

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Abstract

We present a new class of statistical de-anonymization attacks against high-dimensional micro-data, such as individual preferences, recommendations, transaction records and so on. Our techniques are robust to perturbation in the data and tolerate some mistakes in the adversary's background knowledge.

We apply our de-anonymization methodology to the Netflix Prize dataset, which contains anonymous movie ratings of 500,000 subscribers of Netflix, the world's largest online movie rental service. We demonstrate

and sparsity. Each record contains many attributes (*i.e.*, columns in a database schema), which can be viewed as dimensions. Sparsity means that for the average record, there are no "similar" records in the multi-dimensional space defined by the attributes. This sparsity is empirically well-established [7, 4, 19] and related to the "fat tail" phenomenon: individual transaction and preference records tend to include statistically rare attributes.

Our contributions. Our first contribution is a formal model for privacy breaches in anonymized micro-data (section 3). We present two definitions, one based on the

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Learned online

Article development led by queue.acm.org

DOI:10.1145/3287287

**These attacks on statistical databases
are no longer a theoretical danger.**

BY SIMON GARFINKEL, JOHN M. ABOUD,
AND CHRISTIAN MARTINDALE

Understanding Database Reconstruction Attacks on Public Data

IN 2020, THE U.S. Census Bureau will conduct the

so the reconstruction no longer results in the original data. This has implications for the 2020 census.

The goal of the census is to count every person once, and only once, and in the correct place. The results are used to fulfill the Constitutional requirement to apportion the seats in the U.S. House of Representatives among the states according to their respective numbers.

In addition to this primary purpose of the decennial census, the U.S. Congress has mandated many other uses for the data. For example, the U.S. Department of Justice uses block-by-block counts by race for enforcing the Voting Rights Act. More generally, the results of the decennial census, combined with other data, are used to help distribute more than \$675 billion in federal funds to states and local organizations.

Beyond collecting and distributing data on U.S. citizens, the Census Bureau is also charged with protecting the privacy and confidentiality of survey responses. All census publications must uphold the confidentiality standard specified by Title 13, Section 9 of the U.S. Code, which states that Census Bureau publications are prohibited from identifying "the data furnished by any particular establishment or individual." This section prohibits the Census

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| ARTICLE | Journal of Privacy and Confidentiality Vol. 10 (1) 2020 | TPDP 2018 | Submitted Published | Jan 2019 Jan 2020 |
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Review

Authors

LINEAR PROGRAM RECONSTRUCTION IN PRACTICE

ALONI COHEN AND KOBBI NISSIM

PODS '03

2003 •

Boston University

e-mail address: aloni@bu.edu

Online:

Department of Computer Science, Georgetown University

e-mail address: kobbi.nissim@georgetown.edu

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ABSTRACT. We briefly report on a successful linear program reconstruction attack performed on a production statistical queries system and using a real dataset. The attack was deployed in test environment in the course of the [Aircloak Challenge](#) bug bounty

IN 2020, THE U.S. CENSUS BUREAU WILL CONDUCT THE

identifying "the data furnished by any particular establishment or individual." This section prohibits the Census



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Journal of
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Annu. Rev. Stat. Appl. 2017. 4:61–84

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December 21, 2016

IN 2020, THE U.S. Census Bureau will conduct the

an 2019
an 2020



Exposed! A Survey of Attacks on Private Data

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and Jonathan Ullman⁴

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• June

Keywords

privacy, privacy attacks, re-identification, reconstruction attacks, tracing

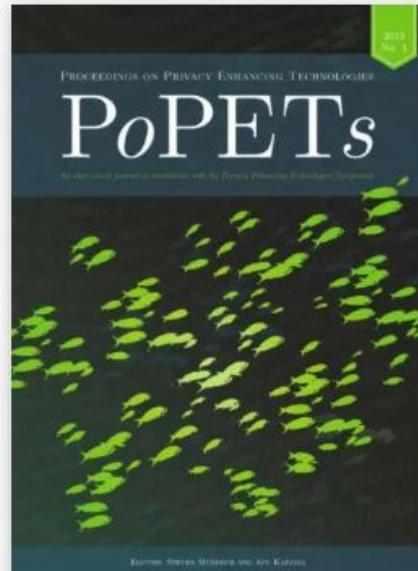
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The Changing Privacy Landscape

Journal of

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Averaging Attacks on Bounded Noise-based Disclosure Control Algorithms

[Hassan Jameel Asghar](#) and [Dali Kaafar](#)

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Proceedings on Privacy

Harvard
2017⁴

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December 21, 2016

IN 2020, THE U.S. Census Bureau will conduct the

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KEYWORDS

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– so much so, in fact, that “we [were standing] on the threshold of what might be called the Age of the Goldfish Bowl” (Brenton)

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1964: privacy was “evaporating [and] under assault from many directions” (Packard) – so much so, in fact, that “we [were standing] on the threshold of what might be called the Age of the Goldfish Bowl” (Brenton)

1890: “Numerous mechanical devices threaten to make good the prediction that ‘what is whispered in the closet shall be proclaimed from the house-tops’” (Warren & Brandeis)

Some interdisciplinary conundrums

- How do we measure an individual's valuation of their private information?

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- What data is identifying, what data is identifiable and what data constitutes an identity?
- What data is publicly available and how may this change the privacy assessment?

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