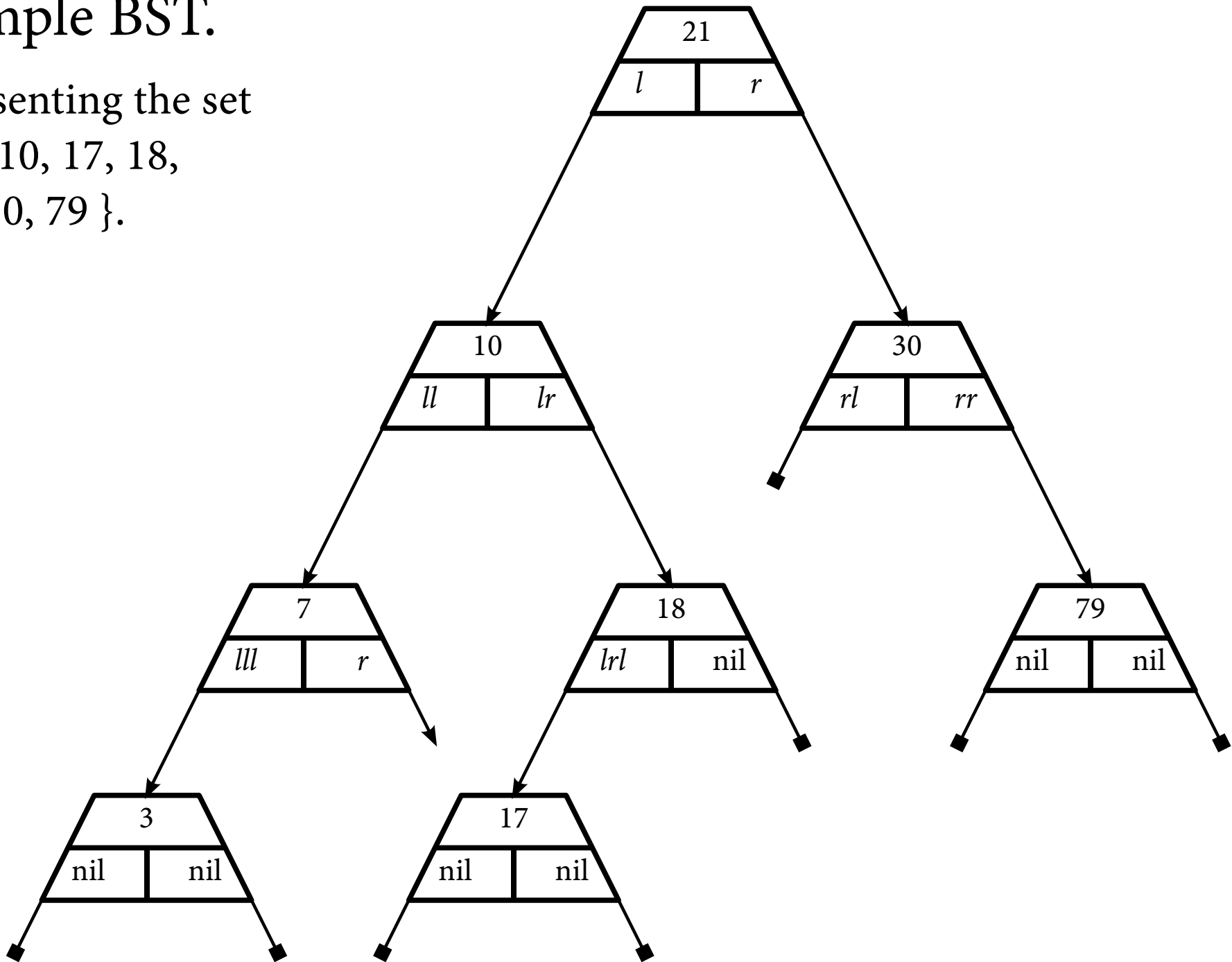


Example BST.

Representing the set
{ 3, 7, 10, 17, 18,
21, 30, 79 }.

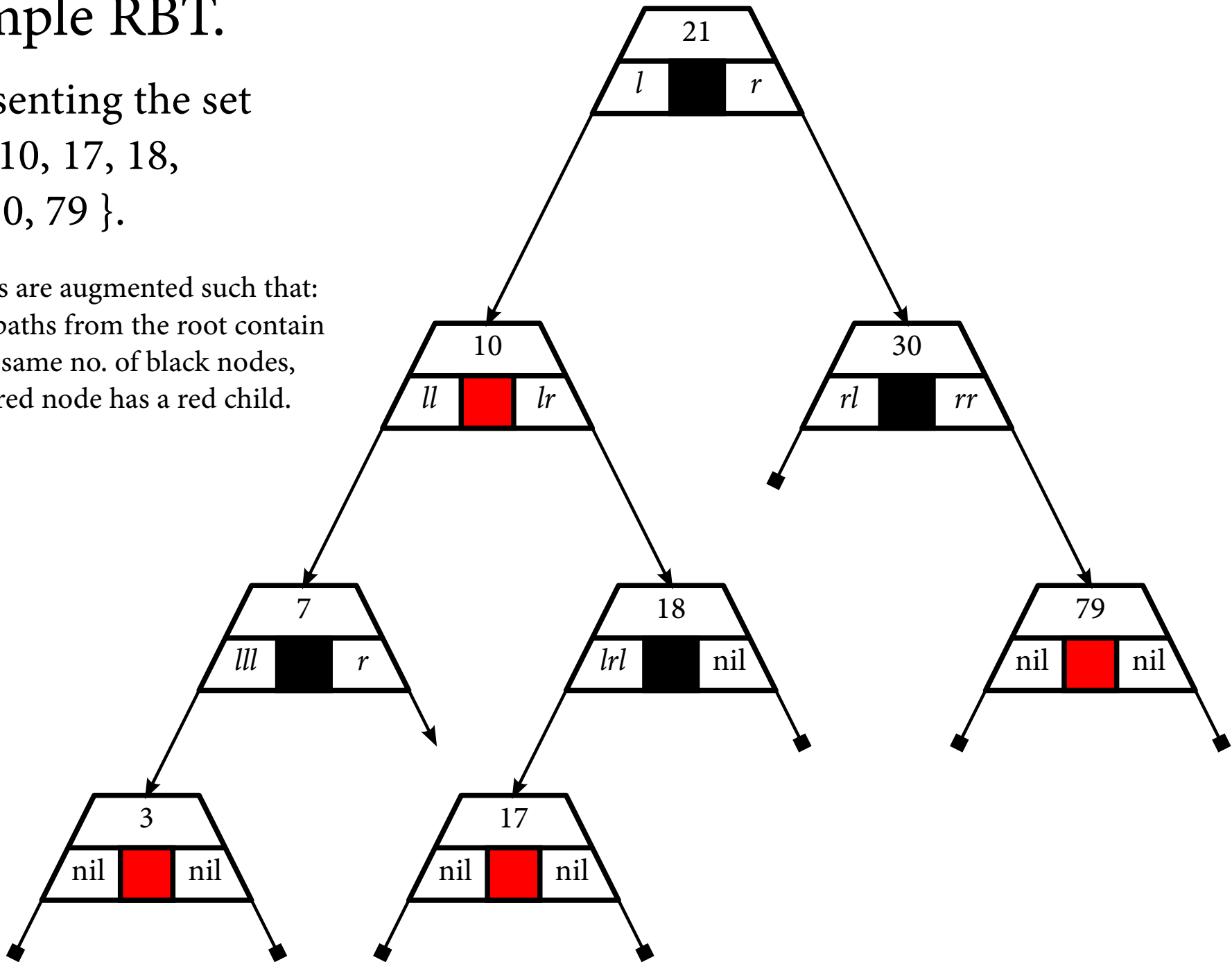


Example RBT.

Representing the set
 $\{ 3, 7, 10, 17, 18,$
 $21, 30, 79 \}$.

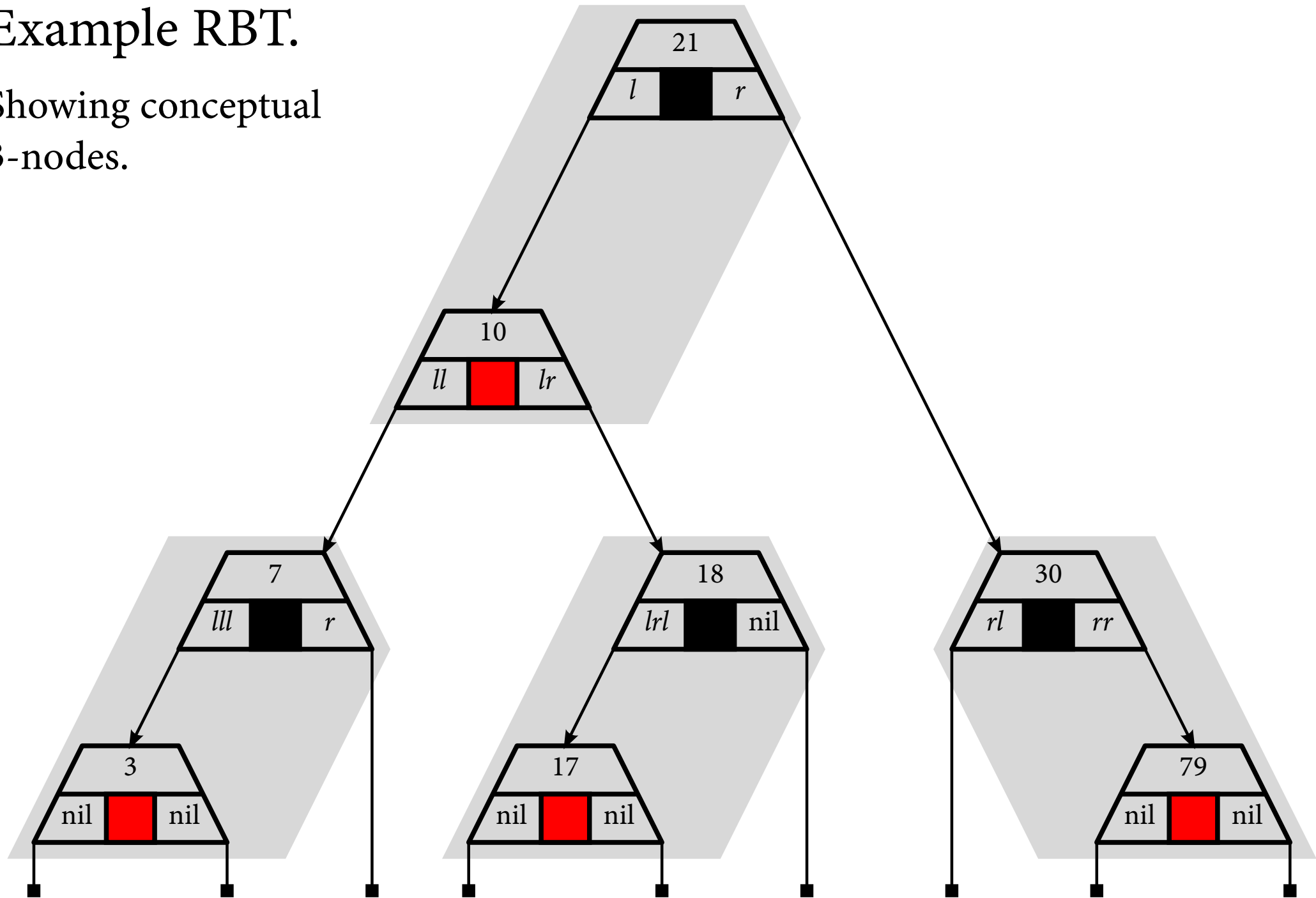
The nodes are augmented such that:

- (1) all paths from the root contain the same no. of black nodes,
- (2) no red node has a red child.



Example RBT.

Showing conceptual
3-nodes.

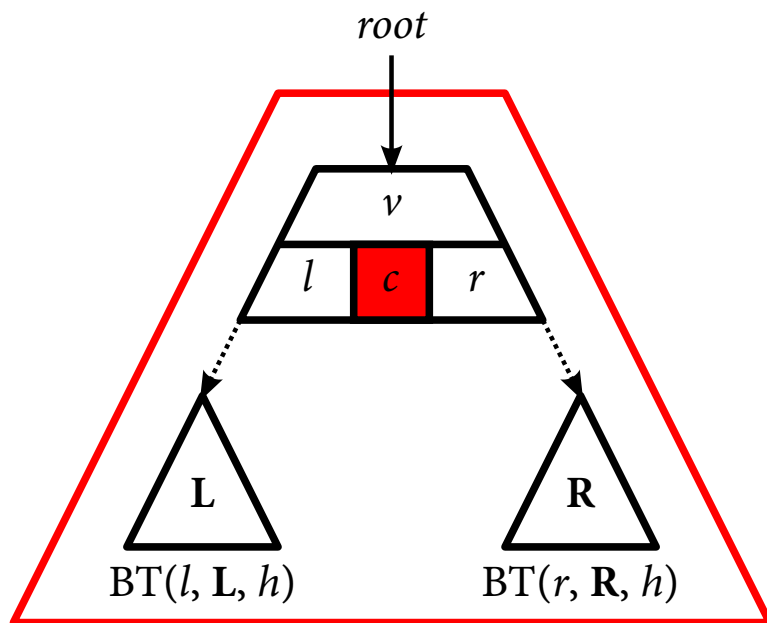


RBT predicates.

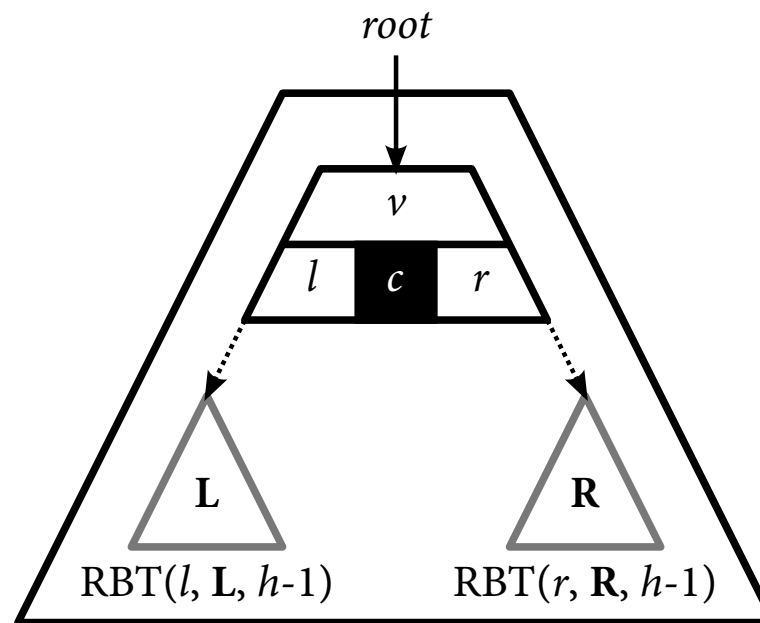
$\text{RBT}(\text{root}, \mathbf{S}, h)$



$\text{BT}(\text{root}, \mathbf{S}, h)$



$\text{RT}(\text{root}, \mathbf{S}, h)$,
where $\text{Compose}(\mathbf{L}, v, \mathbf{R}, \mathbf{S})$,
and $h \geq 0$.



$\text{NBT}(\text{root}, \mathbf{S}, h)$,
where $\text{Compose}(\mathbf{L}, v, \mathbf{R}, \mathbf{S})$,
and $h > 0$.



$\text{EBT}(\text{root}, \mathbf{S}, h)$,
where $\mathbf{S} = \emptyset$
and $h = 0$.

Compose(L, v, R, S)

$$L \cup \{v\} \cup R = S \wedge$$

$$\forall l \in L. l < v \wedge$$

$$\forall r \in R. v < r.$$

