

~~P1~~ 1) Find T , N and K for plane curves

i) $\vec{r}(t) = t\hat{i} + (\ln \cos t)\hat{j}$, $-\pi/2 < t < \pi/2$

ii) $\vec{r}(t) = (2t+3)\hat{i} + (5-t^2)\hat{j}$, $-\pi/2 < t < \pi/2$

iii) $\vec{r}(t) = (\cos t + t \sin t)\hat{i} + (\sin t - t \cos t)\hat{j}$, $t > 0$.

2) Find T , N and K for the space curves

i) $\vec{r}(t) = (3 \sin t)\hat{i} + (3 \cos t)\hat{j} + 4t\hat{k}$

ii) $\vec{r}(t) = (e^t \cos t)\hat{i} + (e^t \sin t)\hat{j} + 2t\hat{k}$

3) Find the length of the curve

$$\vec{r}(t) = (\sqrt{2}t)\hat{i} + (\sqrt{2}t)\hat{j} + (1-t^2)\hat{k}$$

from $(0, 0, 1)$ to $(\sqrt{2}, \sqrt{2}, 0)$.

4) Find an equation for the circle of curvature of the curve $\vec{r}(t) = t\hat{i} + (\sin t)\hat{j}$ at the point $(\pi/2, 1)$.

* 5) Find the length of the arc of the circular helix with vector eqn:-

$$\vec{r}(t) = \langle \cos t, \sin t, t \rangle \text{ from } (1, 0, 0) \text{ to } (1, 0, 2\pi)$$