Assignment 6 Written Part Graded Student James La Fontaine **Total Points** 10 / 10 pts Question 1 Q2a 1 / 1 pt → + 1 pt Correct + 0 pts Incomplete + 0 pts Click here to replace this description. Question 2 Q2b 4 / 4 pts → + 1 pt Solve for points + 1 pt Answers partially correct. + 0 pts Blank page found **Question 3** Q₂c 2 / 2 pts + 0 pts No marks Question 4 **2** / 2 pts Q2d → 1 pt Labelled Tangent Points + 0 pts No marks Write out the coordinates at each point.

Question 5 Challenge ✓ +0 pts No marks will be given. GOOD Question 6 Notation 1/1 pt

+ 0 pts zero

→ + 1 pt Notation

Assignment 6 Due: 6:00PM, Friday 15 May.

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Explainer: Question 1 should be completed in **WebWork** by 6:00PM, Friday 15 May. WebWork should be accessed via Assignment 6 WebWork in the Assignments panel of the MAST10005 LMS Site.

You should upload a scan of neatly presented solutions to Question 2 in **Gradescope**, which should be accessed via Assignment 6 Written Part in the Assignments section of the MAST10005 LMS Site. Please do not include your answers to Question 1 in your solutions to the written part.

- 1. You should complete this question in WebWork by 6:00PM, Friday 15 May. It will test your ability to calculate implicit derivatives. Completing Question 1 before you attempt Question 2 will make Question 2 easier because you will have already checked that your formula for the implicit derivative of the curve $C = \{(x,y) \in \mathbb{R}^2 \mid x^4 + y^2 = 4x^2 + 3y\}$ correct.
- 2. Consider the curve

$$C = \{(x, y) \in \mathbb{R}^2 \mid x^4 + y^2 = 4x^2 + 3y\}$$

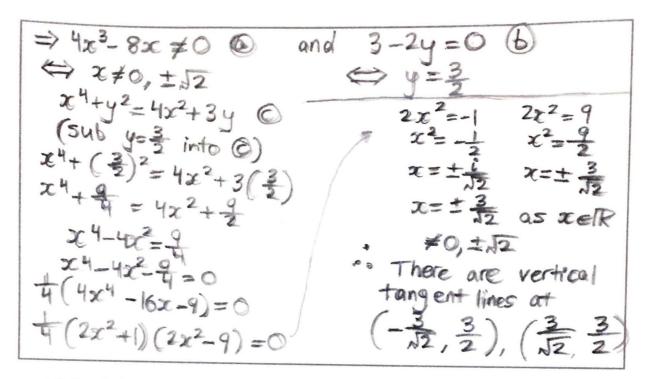
(a) Find all intercepts of C.

$$x^{1}+y^{2}=4x^{2}+3y$$
 $dy = 4x^{3}-8x$
 $x^{2}-intercepts$ where $y=0$:

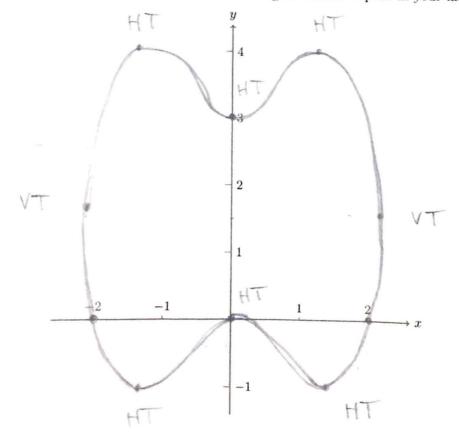
 $x^{2}=4x^{2}+3y$
 $x^{2}=4x^{2}+3y$
 $x^{2}=4x^{2}+3y$
 $x^{2}=3y$
 $x^{2}-3y=0$
 $x^{2}-3y=0$
 $x^{2}=0$
 $x^{2}-4=0$
 $x^{2}=0$
 $x^{2}=0$

(b) Find the points in C where the tangent line is *horizontal*. Be careful to check the conditions given in Theorem 3.34. [Hint: there are 6 points in total.]

(c) Find the points in C where the tangent line is vertical. Be careful to check the conditions given in Theorem 3.34.



(d) Sketch C on the axes. Label all the points you found in (b) and (c). Abbreviations HT for Horizontal tangent and VT for Vertical tangent will save space in your labelling.



Extra challenge problem [No marks]:

Find a > 0 and formulas for functions $f_1 : [-a, a] \longrightarrow \mathbb{R}$ and $f_2 : [-a, a] \longrightarrow \mathbb{R}$ such that Cis the union of the graphs of f_1 and f_2 .

Important Note: If you decide not to do the challenge problem, you should still include this page in your solutions. If you don't do this, Gradescope will not allow you to submit.

$$a = \frac{3}{\sqrt{12}}$$
 as this is where the vertical tangents are and therefore where the curve must be splittinto functions.

$$y = y(x)$$

$$y^{2} - 3y + x^{4} - 4x^{2} = 0$$

$$y = 3 \pm \sqrt{9 - 4(x^{4} - 4x^{2})}$$

$$y = 3 \pm \sqrt{9 - 4(x^{4} - 4x^{2})}$$

$$y = 3 \pm \sqrt{9 - 4x^{4} + 16x^{2}}$$

$$f_{1}(x) = 3 + \sqrt{-4x^{4} + 16x^{2} + 9}$$

$$f_{2}(x) = 3 - \sqrt{-4x^{4} + 16x^{2} + 9}$$

Assignment Information

This assignment is worth $\frac{20}{9}\%$ of your final MAST10005 mark.

Full working should be shown in your solutions to Question 2. There will be 1 mark overall for correct mathematical notation.

Full solutions to the assignment will be uploaded to the LMS site approximately 3 days after the assignment is due.