

2a)

$$\left. \begin{aligned} T_{Ax} \vec{i} + T_{Bx} \vec{i} - R_x \vec{i} &= 0 \\ T_{Ay} \vec{j} + R_y \vec{j} - T_{By} \vec{j} &= 0 \end{aligned} \right\} \text{as the system is in equilibrium}$$

$$\Rightarrow R_x \vec{i} = T_{Ax} \vec{i} + T_{Bx} \vec{i} \quad (1)$$

$$\Rightarrow R_y \vec{j} = -T_{Ay} \vec{j} + T_{By} \vec{j} \quad (2)$$

$$(1) \quad 4000 \cos(10^\circ) = T_A \cos(15^\circ) + T_B \cos(20^\circ)$$

$$\Rightarrow 4000 \cos(10^\circ) - T_A \cos(15^\circ) = T_B \cos(20^\circ)$$

$$\Rightarrow T_B = \frac{4000 \cos(10^\circ) - T_A \cos(15^\circ)}{\cos(20^\circ)} \quad (3)$$

sub (3) into (2)

$$(2) \quad 4000 \sin(10^\circ) = -T_A \sin(15^\circ) + \left( \frac{4000 \cos(10^\circ) - T_A \cos(15^\circ)}{\cos(20^\circ)} \right) \times \sin(20^\circ)$$

~~scribbles~~

$$\Rightarrow 694.593 = -0.2588 T_A + (4192.05 - 1.0279 T_A) \times \sin(20^\circ)$$

$$\Rightarrow 694.593 = -0.2588 T_A + 1433.77 - 0.3516 T_A$$

$$\Rightarrow -739.177 = -0.6104 T_A$$

$$\Rightarrow T_A = 1210.97 \approx 1211 \text{ N}$$

sub  $T_A$  into (3)

$$\Rightarrow T_B = \frac{4000 \cos(10^\circ) - 1211 \cos(15^\circ)}{\cos(20^\circ)}$$

$$\Rightarrow T_B = 2947.23 \approx 2947 \text{ N}$$

2b) function [TA, TB] = CalcRangeOfTensions

theta = 0:0.5:20;

A = [cosd(15) cosd(20); sind(15) -sind(20)];

for i = 1:length(theta)

C = [4000\*cosd(theta(i)); -4000\*sind(theta(i))];

X = inv(A)\*C;

TA(i) = X(1);

TB(i) = X(2);

end

plot(theta, TA, 'rs', theta, TB, 'go');

grid on

xlabel("theta (degrees)");

ylabel("F(N)");

end

Yes, the tensions have an equal magnitude  
of 2097N with  $\theta = 2.5^\circ$