Assignment 3 • Graded

## Student

James La Fontaine

## **Total Points**

11 / 12 pts

## Question 1

Question 1 11 / 12 pts

1.1 L Question 1

- **11** / 12 pts
- ✓ + 1 pt 1a) M: Demonstrated understanding of the difference between a partial sum and a term of a series
- ✓ + 1 pt 1a) A: partial sums are: 1, 0, 0.5, 0.333, 0.375, 0.367, 0.368, 0.368, 0.368, 0.368, 0.368
- → + 1 pt 1a) M: Sketching points
- → + 1 pt 1a) A: Axes labelled and points identifiable
- → + 1 pt 1a) A: Guess of convergence or divergence matches graph
- **→ + 1 pt** 1b) A: Correct reason why  $\sum_{n=0}^{\infty} \frac{(-1)^n}{n!}$  fails the div. test, ratio test, or comparison test from lectures.
- → 1 pt 1c) A: The ratio test is the test used from Wikipedia
  - **+ 1 pt** 1c) A: States a correct version of: If  $\lim_{n \to \infty} \left| \frac{a_{n+1}}{a_n} \right| < 1$  then  $\sum_{n=0}^{\infty} a_n$  converges, or another applicable version of the ratio test.
- → 1 pt 1c) M: Simplifying factorials (or another appropriate method if incorrect test is used)
- $\checkmark$  + 1 pt 1c) J: Has shown  $\lim_{n\to\infty}\left|\frac{a_{n+1}}{a_n}\right|<1$  to justify convergence. (or correctly checked test condition if another test is used)
- $\checkmark$  + 1 pt 1c) A: Limit is 0, AND, series converges, AND justification of limit laws AND standard limit  $\frac{1}{n} \to 0$  included when needed. (or correct conclusion and justification if another test is used)
- → + 1 pt N: Notation correct throughout question 1
  - + 0 pts Scored zero
- clearly define the test, refer to solutions
- 2 Good

Question assigned to the following page: 1.1

Ealculus 2 Written Assignment 3  $a) S_0 = \frac{(-1)^0}{0!} = 1$ 5,=0 S3 ≈ 0.333  $S_2 = 0.5$ S<sub>5</sub> ≈ 0.367 5, = 0.375 5, 2 0.368 Se ≈0.368 5,20.368 5820.368 5 ≈ 0.368 The series appears to converge to approximately 0.368 b) I would like to apply the ratio fest but the series does not satisfy the condition that it must be a positive term series. Question assigned to the following page: 1.1

c) Ratio test from Wikipedia:  $\left(\times \frac{1}{n}\right)$ Standard limits and limit laws the series is convergent by the ratio test 50



No questions assigned to the following page.				

a) 
$$y$$
-intercept  
 $x=0$ 

$$f(x) = \frac{(e^{\circ} - e^{\circ})^{2}}{(e^{\circ} + e^{\circ})^{2}} = \frac{5}{\frac{1}{2}(e^{\circ} + e^{\circ})}$$

$$= 0 - \frac{5}{2 \cdot 2} = -5$$

$$f(x) = \sin h^{2}(x) - \frac{5}{\cosh^{2}(x)} = C$$

$$\frac{5}{\cosh^{2}(x)} = \cos h(x) = C$$

$$sin h^{2}(x) - 5cosh(x) = 0$$
 $cosh^{2}(x) - 1 - 5cosh(x) = 0$ 

let 
$$\cosh(x) = 2 \Rightarrow 2^2 - 52 - 1 = 0$$

$$Z = 5 \pm \sqrt{25 - 4 \cdot 1 \cdot - 1} = 5 \pm \sqrt{29}$$

: 
$$x = \pm \operatorname{arcCosh}\left(\frac{5+\sqrt{29}}{2}\right)$$
 as  $\cosh(x) > 1$ 

and 
$$\tanh^2(x) = \tanh^2(-x)$$
  
and  $\operatorname{sech}(x) = \operatorname{sech}(-x)$ 

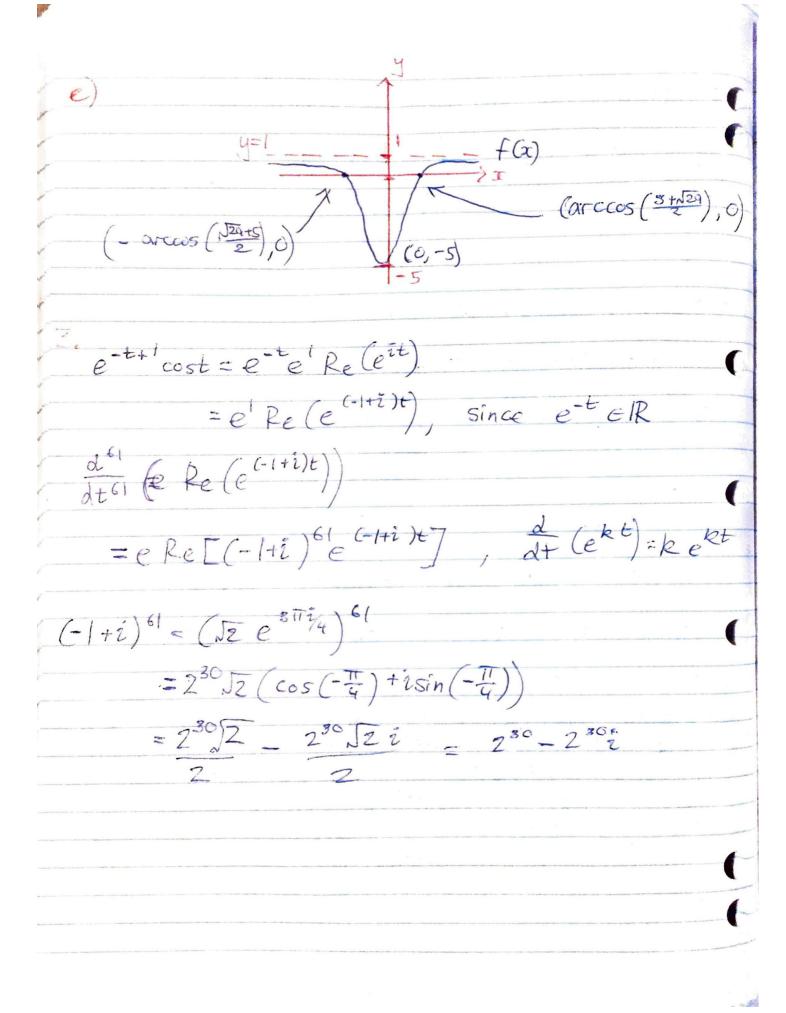


No questions assigned to the following page.				

(b) stationary point(s) occur when f'(x)=0  $\frac{d}{dx}\left(\tanh^{2}(x)\right) - \frac{d}{dx}\left(5\operatorname{sech}(x)\right)$  $= \frac{d}{dx} \left( \cosh^2(x) \right) - 5 \frac{d}{dx} \left( \cosh(x) \right) - \frac{d}{dx} \left( 1 \right)$ = 2 coshocsinhoc - 5 sinhoc 7 sinh(2x) = 5 sinhx =0 51mh (2a) = 55inh(x) => Sinh(x)(2 coshx -5) =0 sinh (x) = 0 x = 0Stationary point at (0, -5) c) f(x) is an even function as  $10 + \tanh^2(x) - 5\operatorname{sech}(x) = \tanh^2(-x) - 5\operatorname{sech}(-x)$ 1) The function is continuous for all xCER.

according to continuity theorems I and 3 which
state that the addition of two continuous
functions will give a continuous function and
that hyperbolic functions including tanh 2(x)
(preserves continuity by theorem 4 feg) and
sech(x) are continuous. (

No questions assigned to the following page.				



No questions assigned to the following page.				

Hence  $\frac{d^{61}}{dt^{61}} \left( e^{-t+1} \cos t \right) = e \operatorname{Re} \left[ \left( 2^{30} - 2^{30} i \right) \right]$   $= \operatorname{eRe} \left[ \left( 2^{30} - 2^{30} i \right) e^{-t} \left( \cos t + i \sin t \right) \right]$   $= \operatorname{eRe} \left[ \left( 2^{30} e^{-t} - 2^{30} i e^{-t} \right) \left( \cos t + i \sin t \right) \right]$   $= e \left( 2^{30} e^{-t} \cos t + 2^{30} e^{-t} \sin t \right)$   $= 2^{30} e^{-t+1} \cos t + 2^{30} e^{-t+1} \sin t$ 

£		And the control of th		