Assignment 9 Written Part Student

Graded

James La Fontaine

Total Points

7 / 10 pts

Question 1

Q2

0 / 2 pts

- + 1 pt Method
- + 1 pt Answer correct
- ANSWER DOES NOT APPEAR TO BE IN THE ASSIGNMENT.

Question 2

2 / 2 pts Q3a

- ✓ + 1 pt Method: Solve G(y) = 0.
- - + 0 pts No marks could be given

Question 3

1 / 1 pt Q3b

- 🗸 + 1 pt Explain that y cannot intersect constant solutions $y=\pm \frac{\pi}{2}$
 - + 0 pts No marks could be given.

Question 4

Q3c

3 / 4 pts

- → + 2 pts Essentially correct method
 - + 1 pt Method partially correct
 - **+ 1 pt** Explain how (b) is used to justify $\arctan(\tan(y)) = y$
- + 1 pt Correct answer
 - + 0 pts No marks could be given
- Explain HOW you used part b. You ALSO need it to show that arctan(tan(y))=y. This is Important.

Notation 1 / 1 pt

→ + 1 pt No significant lapses

+ 0 pts Significant lapses

Assignment 9 Due: 6:00PM, Friday 5 June.

Name:

James La Fontaine

Student ID:

1079860

Explainer: Question 1 should be completed in WebWork by 6:00PM, Friday 5 June. WebWork should be accessed via Assignment 9 WebWork in the Assignments panel of the MAST10005 LMS Site.

You should upload a scan of neatly presented solutions to Questions 2 and 3 in **Gradescope**, which should be accessed via Assignment 9 Written Part in the Assignments section of the MAST10005 LMS Site. Please do not include your answers to Question 1 in this part.

- 1. You should complete this question in WebWork by 6:00PM, Friday 5 June. Completing this question first will make the the written part easier because you will have already found and checked the equivalent expression for $\cos^2(x)\sin^4(x)$ needed in Question 2.
- 2. Use your answer to Problem 3 in WebWork to find the antiderivative

$$\int \cos^2(x) \sin^4(x) \, \mathrm{d}x.$$

3. Consider the following separable differential equation:

$$\frac{dy}{dt} = \cos(t)\cos^2(y).$$

(a) Find all constant solutions of this differential equation (there are infinitely many).

Here
$$G(y) = \cos^2(y)$$

 $G(c) = 0 \Leftrightarrow \cos^2(c) = 0$
 $\Rightarrow \cos(c) = 0$
 $\Rightarrow C = \frac{\pi}{2} + R\pi, R \in \mathbb{Z}$
 $\Rightarrow 0 \Rightarrow y = \frac{\pi}{2} + R\pi, R \in \mathbb{Z}$

(b) Use your answer to (a) and Theorem 4.44 to explain why range $(y) \subseteq (-\frac{\pi}{2}, \frac{\pi}{2})$ for the solution of this equation satisfying the initial condition y = 0 when t = 0.

Since It kill is a constant solution, by Theorem 4.44 no other solution can take the value of multiples of II. by kill and furthermore the curves of other solutions cannot cross the lines $y = \frac{\pi}{2} + kill$ so for the IVP in which y = 0, y must be contained in the interval $(-\frac{\pi}{2}, \frac{\pi}{2})$ to not cross these lines.

(c) Solve the initial value problem with initial condition y=0 when t=0. You should explain how you use the result from (b) when solving this problem. [Hint: Review lecture slide 237.]

This assignment is worth $\frac{20}{9}\%$ of your final MAST10005 mark.

Full working should be shown in your solutions to Questions 2 and 3. There will be 1 mark overall for correct mathematical notation.

Full solutions to the assignment will be uploaded to the LMS site approximately 3 days after the assignment is due.