AERO-F Manual

Version 1.1

Edition 0.1/13 July 2011

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This manual was prepared with Texinfo (http://www.gnu.org/software/texinfo).

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Next: Installation

1 INTRODUCTION

AERO-F is a domain decomposition based, parallel, three-dimensional, compressible, Euler/Navier-Stokes solver based on finite volume and finite element type discretizations on unstructured meshes constructed with tetrahedra. It can model both single-phase and multi-phase flow problems where the fluid can be either a perfect gas (and

possibly going through porous media), stiffened gas, barotropic liquid governed by Tait's equation of state (EOS), or a highly explosive system describable by the Jones-Wilkins-Lee (JWL) EOS. For this purpose, it is equipped with various numerical methods and the level set technique. It can also solve multi-fluid problems whether they involve multi-phase flows or not.

AERO-F can perform steady and unsteady, inviscid (Euler) and viscous (Navier-Stokes), laminar and turbulent flow simulations. For turbulent flow computations, it offers one- and two-equation turbulence models, static and dynamic LES and Variational Multi-Scale (VMS)-LES, as well as DES methods, with or without a wall function.

AERO-F operates on unstructured body-fitted meshes, or on fixed meshes that can embed discrete representations of surfaces of obstacles around and/or within which the flow is to be computed. The body-fitted meshes and the embedded discrete surfaces can be fixed, move and/or deform in a prescribed manner (for example, as in forced oscillations), or be driven via interaction with the structural code **AERO-S**. In the case of body-fitted meshes, the governing equations of fluid motion are formulated in the arbitrary Lagrangian Eulerian (ALE) framework. In this case, large mesh motions are handled by a corotational approach which separates the rigid and deformational components of the motion of the surface of the obstacle, and robust mesh motion algorithms that are based on structural analogies. In the case of embedded surfaces, which can have complex shapes and arbitrary thicknesses, the governing equations of fluid motion are formulated in the Eulerian framework and the wall boundary or transmission conditions are treated by an embedded boundary method.

In **AERO-F**, the spatial discretization combines a second-order accurate Roe, HLLE, or HLLC upwind scheme for the advective fluxes and a Galerkin centered approximation for the viscous fluxes. This semi-discretization can also achieve a fifth-order spatial dissipation error and a sixth-order spatial dispersion error — and therefore fifth-order spatial accuracy — and possibly a sixth-order spatial accuracy. Time-integration can be performed with first- and second-order implicit, and first, second, and fourth-order explicit algorithms which, when performing in the ALE setting, satisfy their discrete geometric conservation laws (DGCLs).

AERO-F embeds **AERO-FL**, a module for solving linearized fluid equations. This module shares with **AERO-F** the semi-discretization schemes outlined above. Currently, the **AERO-FL** module can be used to compute linearized inviscid flow perturbations around an equilibrium solution, predict linearized inviscid aeroelastic (fluid-structure) responses assuming a modalized structure, compute aeroelastic snapshots in either the time or frequency domains to construct a POD (proper orthogonal decomposition) basis, generate an aeroelastic ROM (reduced-order model) in the frequency domain, and compute aeroelastic ROM solutions in the time-domain assuming a modalized structure.

AERO-F can also be used to perform flow computations past accelerating or decelerating obstacles, and steady, inviscid or viscous sensitivity analyses with respect to a set of aerodynamic and/or shape parameters. It is also equipped to communicate with a structural/thermal analyzer to perform aeroelastic, aerothermal, and aerothermoelastic analyses by state-of-the-art fluid-structure-thermal staggered solution algorithms.

AERO-F is essentially a comprehensive external flow solver. As such, it is not yet equipped with all boundary condition treatments that are characteristic of internal flow problems. Nevertheless, it can handle a class of such problems.

Next: Overview, Previous: Introduction

2 INSTALLATION

The installation of **AERO-F** on a given computing system requires the availability on that system of the following tools:

C++ compiler g++ Version 4.1.2 or higher.

Fortran compiler gfortran Version 4.1.2 or higher.

Flex utility Version 2.5 or higher. Flex is a lexical analyser required for building the parser

of AERO-F's ASCII Input Command Data file.

Bison utility Version 2.3 or higher. Bison is a parser generator required for building the

parser of AERO-F's ASCII Input Command Data file.

CMake utility Version 2.6 or higher. CMake is a cross-platform open-source build system. It is

comparable to the Unix Make program in that the build process is ultimately controlled by configuration files (CMakeLists.txt). However unlike Make, it does not directly build the final software but instead generates standard build files such as makefiles for Unix and projects/workspaces for Windows Visual C++. The CMake version 2.6 utility can be obtained from http://www.cmake.org. (Note:

a "README.cmake" file discussing details on CMake options for code

configuration and installation is available).

and following libraries:

BLAS library BLAS is a set of Basic Linear Algebra Subprograms required by various

operations performed in AERO-F.

MPI library openmpi Version 1.2.6 or higher. Open MPI is a high-performance implementation of the

Message Passing Interface (MPI) required for performing interprocessor

communication, among others. More specifically, AERO-F requires an MPI-2

implementation such as the one provided by the Open MPI project.

OpenMP API Open Multi-Processing is an Application Programming Interface (API) that

supports multi-platform shared memory multiprocessing programming in C, C++ and Fortran on many architectures, including Unix. As an option, **AERO-F** can be compiled with OpenMP to enable multi-threaded execution.

In addition, the POD (Proper Orthogonal Decomposition) and ROM (Reduced-Order Modeling) capabilities of the linearized module **AERO-FL** of **AERO-F** require the availability on the host computing system of the following libraries:

LAPACK is a high-performance Linear Algebra PACKage with advanced solvers.

ARPACK library ARPACK is the Arnoldi PACKage for the solution of large-scale symmetric,

nonsymmetric, and generalized eigenproblems.

Scalapack library Scalapack is also known as the Scalable LAPACK. This library includes a

subset of LAPACK routines redesigned for distributed memory MIMD parallel

computers.

BLACS library BLACS (Basic Linear Algebra Communication Subprograms) is a linear algebra

oriented message passing interface designed for linear algebra.

Furthermore, the embedded computational framework of **AERO-F** requires the availability on the host computing system of the following libraries:

Boost library The Boost C++ libraries are a collection of free libraries that extend the

functionality of C++.

To install **AERO-F**, follow the procedure specified below:

- From the directory containing the source code of **AERO-F**, type "cmake ." (without the ""). Note the space and the "." after the command cmake. The "." specifies the current directory.
- Watch the computer screen and verify that all invoked libraries were found and all build options were correct. A sample computer screen output of the cmake command is:

```
-- The C compiler identification is GNU
-- The CXX compiler identification is GNU
-- Check for working C compiler: /usr/bin/gcc
-- Check for working C compiler: /usr/bin/gcc -- works
-- Detecting C compiler ABI info
-- Detecting C compiler ABI info - done
-- Check for working CXX compiler: /usr/bin/c++
-- Check for working CXX compiler: /usr/bin/c++ -- works
-- Detecting CXX compiler ABI info
-- Detecting CXX compiler ABI info - done
-- The Fortran compiler identification is GNU
-- Check for working Fortran compiler: /usr/bin/gfortran
-- Check for working Fortran compiler: /usr/bin/gfortran -- works
-- Detecting Fortran compiler ABI info
-- Detecting Fortran compiler ABI info - done
-- Checking whether /usr/bin/gfortran supports Fortran 90
-- Checking whether /usr/bin/gfortran supports Fortran 90 -- yes
-- Looking for Fortran cblas_dgemm
-- Looking for Fortran cblas_dgemm - not found
-- Looking for Fortran sgemm
-- Looking for Fortran sgemm - found
-- Looking for include files CMAKE_HAVE_PTHREAD_H
-- Looking for include files CMAKE_HAVE_PTHREAD_H - found
-- Looking for pthread_create in pthreads
-- Looking for pthread_create in pthreads - not found
-- Looking for pthread_create in pthread
-- Looking for pthread_create in pthread - found
-- Found Threads: TRUE
-- A library with BLAS API found.
-- Looking for Fortran cheev
```

- -- Looking for Fortran cheev found
- -- A library with LAPACK API found.
- -- Found MPI: /usr/lib/openmpi/lib/libmpi_cxx.so
- -- Building for system type: Linux.
- -- ARPACK library /usr/lib/libarpack.so found.
- -- SCALAPACK library /usr/lib/libscalapack-openmpi.so found.
- -- BLACS library /usr/lib/libblacs-openmpi.so,/usr/lib/libblacsF77init-openmpi.so found.
- -- Boost version: 1.42.0
- -- Will compile with MPI API /usr/lib/openmpi/include/usr/lib/openmpi/include/openmpi.

Summary of build options
-----Distributed Execution: YES

Aeroelastic: YES
Embedded framework: YES
Modal capability: YES
Parallel SVD capability: YES
Build type: Release

Extra link flags:

- -- Configuring done
- -- Generating done
- -- Build files have been written to: /home/pavery/Codes/Fluid
- If necessary, edit the CMakeCache.txt file to include the file paths to all required and desired optional components that were not automatically found by cmake. Typically, the compilers, the utilities Flex and Bison, the libraries MPI, BLAS and LAPACK, and the API OpenMP will be automatically found. However, it may be necessary to specify the paths for the libraries ARPACK, Scalapack, Blacs and Boost.
- Then, also from the directory containing the source code of **AERO-F**, type make.

The successful completion of the procedure described above leads to the creation in the bin/directory of **AERO-F**'s executable aerof.

Next: Objects, Previous: Installation

3 OVERVIEW

- Object oriented input
- Syntactic rules
- Comments
- Which problems can AERO-F actually solve?

Next: Syntactic rules, Up: Overview

3.1 OBJECT ORIENTED INPUT

The structure of the text input data file follows closely the internal structure of AERO-F. As a result, this file contains a list of objects that define the problem to be solved and the numerical techniques selected for its resolution. Sample objects that are currently supported are: Problem, Input, Output, Equations, Preconditioner, ReferenceState,

BoundaryConditions, MultiPhase, Space, Time, Aeroelastic, Forced, Accelerated, MeshMotion, Linearized, and Newton. These objects can depend themselves on other lower-level objects. All are defined in Objects.

Next: <u>Comments</u>, Previous: <u>Object oriented input</u>, Up: <u>Overview</u>

3.2 SYNTACTIC RULES

Here are the rules followed in this document.

- 1. Keywords are printed like this.
- 2. Metasyntactic variables (i.e. text bits that are not part of the syntax, but stand for other text bits) are printed like *this*.
- 3. A metasyntactic variable ending by -int refers to an integer value.
- 4. A metasyntactic variable ending by *-real* refers to a real value.
- 5. A metasyntactic variable ending by -str refers to a string enclosed in double quotes ("").
- 6. A metasyntactic variable ending by -id refers to an identifier.
- 7. A metasyntactic variable ending by -obj refers to an object.
- 8. For conciseness, three dots (...) replace an object definition.

The definition of an object starts with the keyword under followed by the name of the object. The members of an object are enclosed within curly braces ({}). For example,

```
under Problem {
  Type = Steady;
  Mode = Dimensional;
}
```

is a valid syntax for the object Problem. Alternatively, it can also be written as

```
Problem.Type = Steady;
Problem.Mode = Dimensional;
```

Notes:

- 1. a semicolon (;) is required after each assignment;
- 2. the ordering of the objects as well as the ordering within an object do not matter.

Next: Which problems can AERO-F actually solve?, Previous: Syntactic rules, Up: Overview

3.3 COMMENTS

Both C and C++ style comments are supported and can be used in the input data file to comment out selected text regions:

- 1. the text region comprised between /* and */ pairs is ignored;
- 2. the remainder of a line after a double slash // is ignored.

These commands do not have the described effects inside double quotes.

Previous: Comments, Up: Overview

3.4 WHICH PROBLEMS CAN AEROF-NAME ACTUALLY SOLVE?

AERO-F can be used to perform:

- A steady or unsteady, inviscid or viscous flow computation around a fixed obstacle.
- Steady or unsteady natural convection (buoyancy) computations.
- A steady or unsteady, inviscid or viscous flow computation around a rigid or flexible obstacle set in accelerated motion.
- An unsteady, inviscid or viscous flow computation around a rigid or flexible obstacle set in a prescribed motion (forced oscillations).
- An unsteady, inviscid or viscous aeroelastic computation.
- A steady or unsteady viscous aerothermal flow computation involving a fixed obstacle.
- Steady or unsteady natural convection (buoyancy) computations coupling viscous fluid flow and heat transfer analyses.
- A steady or unsteady viscous aerothermoelastic flow computation involving a flexible obstacle.
- Any of the above computations in the presence of porous media when the fluid is modeled as a perfect gas.
- An unsteady linearized Euler flow perturbation computation in the time-domain, where the fluid is modeled as a perfect gas.
- An unsteady linearized Euler-based aeroelastic computation in which the structure is represented by a truncated set of its natural modes and the fluid is modeled as a perfect gas.
- A construction of a time- or frequency-domain POD basis when the fluid is modeled as a perfect gas and trained for obstacle vibrations.
- A construction of a time- or frequency-domain POD basis by linear interpolation between two given sets of POD basis vectors, when the fluid is modeled as a perfect gas.
- A construction of a fluid ROM trained for obstacle vibrations, when the fluid is modeled as a perfect gas.
- A time-domain ROM flow computation in which the flow is expressed in a POD basis, when the fluid is modeled as a perfect gas.
- A construction of an aeroelastic ROM in which the structure is currently represented by a truncated set of its natural modes and the fluid is modeled as a perfect gas and trained for structural vibrations.
- A time-domain aeroelastic ROM computation in which the flow is expressed in a POD basis and the structure is represented by a truncated set of its natural modes, when the fluid is modeled as a perfect gas.
- A steady or unsteady multi-fluid problem with or without a multi-phase flow component where any fluid can be modeled by the Equation Of State (EOS) of a perfect or stiffened gas, Tait's EOS for a barotropic liquid, or the JWL EOS. Viscous effects are currently implemented only for the case of multi-perfect-gas problems. The number of fluid media is arbitray. However, AERO-F can currently handle only three different fluid-fluid interfaces which furthermore must be between a same fluid referred to in this User's Reference Manual as the "primary" fluid and any one of three other fluids. In this case, the primary fluid must be identified by

fluid-id-int = 0.

• A steady, inviscid or viscous sensitivity analysis around a specified steady-state flow solution with respect to a specified set of flow and shape parameters, when the fluid is modeled as a perfect gas.

Next: Examples, Previous: Overview

4 OBJECTS

This chapter describes each object that can be inserted in the **AERO-F** input file and its syntax. The default value of each object member or parameter is given between square brackets ([]). The list of currently available objects is given below.

- Accelerated
- Aeroelastic
- Boundaries
- BoundaryConditions
- BoxFix
- ClippingDynamic
- ClippingDynamicVMS
- ConeFix
- <u>Deforming</u>
- Dynamic
- DynamicVMS
- EmbeddedFramework
- Equations
- Explicit
- Fixes
- FluidModel
- Forced
- GasModel
- Heaving
- Hydro
- Implicit
- InitialConditionsEmbedded
- <u>InitialConditionsMultiPhase</u>
- InitialState
- Inlet
- Input
- JWLModel
- LESModel

- LevelSet
- Linearized
- <u>LinearSolver</u>
- LiquidModel
- MeshMotion
- MultiPhase
- NavierStokes
- Newton
- Outlet
- Output
- Pade
- Pitching
- Plane
- Point
- PorousMedium
- Postpro
- Preconditioner
- <u>SolverPreconditioner</u>
- Problem
- ReferenceState
- Restart
- RotationAxis
- Smagorinsky
- Space
- SparseGrid
- Sphere
- <u>SphereFix</u>
- SurfaceData
- <u>Surfaces</u>
- Symmetry
- <u>Time</u>
- <u>TimeVelocity</u>
- <u>Tripping</u>
- <u>TurbulenceClosure</u>
- <u>SpaceTurbulenceModel</u>
- <u>TurbulenceModel</u>
- <u>Velocity</u>
- <u>ViscosityModel</u>
- <u>VMS</u>
- VolumeData

- VolumeInitialConditions
- Volumes
- WALE
- Wall

Next: Input, Up: Objects

4.1 DEFINING THE PROBLEM TYPE

Object: **Problem**

The Problem object sets the type, mode, and few other global parameters of the problem to be solved. Its syntax is:

```
under Problem {
  Type = type-id;
  Mode = mode-id;
  Prec = prec-id;
  Framework = framework-id;
}
```

with

type-id [Steady]:

Steady

Steady-state flow computation around a fixed obstacle (local time-step).

Unsteady

Unsteady flow computation around a fixed obstacle (global time-step).

AcceleratedUnsteady

Accelerated unsteady flow computation around a fixed obstacle (global time-step). See Accelerated.

SteadyAeroelastic

Steady-state aeroelastic computation (local time-step). See Aeroelastic.

UnsteadyAeroelastic

Unsteady aeroelastic computation (global time-step). See Aeroelastic.

AcceleratedUnsteadyAeroelastic

Accelerated unsteady aeroelastic computation (global time-step). See Aeroelastic and Accelerated.

SteadyAeroThermal

Steady-state aerothermal (thermostructure-thermofluid) flow computation around a fixed obstacle (local time-step).

UnsteadyAeroThermal

Unsteady aerothermal (thermostructure-thermofluid) flow computation around a fixed obstacle (global time-step).

SteadyAeroThermoElastic

Steady-state aerothermoelastic flow computation (local time-step). See Aeroelastic.

UnsteadyAeroThermoElastic

Unsteady aerothermoelastic flow computation (global time-step). See <u>Aeroelastic</u>.

Forced

Forced oscillations (unsteady flow) computation around a rigid or flexible obstacle (global time-step). See Forced.

UnsteadyLinearized

Unsteady flow perturbation using a linearized computational model. Currently, this option assumes that the flow is modeled by the linearized Euler equations. If the perturbation is due to a structural motion and is input as such, *mode-id* must be set to Dimensional when using this option.

UnsteadyLinearizedAeroelastic

Unsteady linearized aeroelastic computation (using a linearized computational model). Currently, this option assumes that the flow is modeled by the linearized Euler equations and the structure by a modal representation. When using this option, *mode-id* must be set to Dimensional.

PODConstruction

Construction of a POD basis from computed snapshots.

PODInterpolation

Construction of a POD basis by interpolation between two or more sets of POD basis vectors specified, together with their respective Mach numbers and angles of attack, in PODData (see Input). This file should also contain the Mach number and angle of attack at which the interpolated POD basis is desired. The size of the POD basis to be constructed must be specified in NumPOD (see Linearized). Do not forget to output the computed POD basis using the PODData command in Postpro.

ROM

Construction of a fluid ROM, given a POD basis specified in PODData (see <u>Input</u>), or time-domain ROM fluid simulation in which the flow is expressed in a POD basis specified in PODData (see <u>Input</u>). See <u>Linearized</u>.

ROMAeroelastic

Construction of an aeroelastic ROM, or time-domain ROM aeroelastic simulation in which the flow is expressed in a POD basis and the structure is represented by a truncated set of its natural modes. See Linearized.

SteadySensitivityAnalysis

Computation of the gradients, at a specified steady-state flow solution, of aerodynamic design criteria with respect to flow parameters such as the free-stream conditions (Mach number, angle of attack, and sideslip angle) and design variables such as shape design parameters (see <u>Sensitivities</u>).

SparseGridGeneration

Pre-computation and tabulation in the sparse grid format specified in <u>SparseGrid</u> of information specified in <u>MultiPhase</u>.

1D

One-dimensional computation of a spherically symmetric unsteady two-phase flow problem using the finite volume method with an exact two-phase Riemann solver (MultiPhase. Method = FiniteVolumeWithExactTwoPhaseRiemann).

mode-id [NonDimensional]:

AERO-F 1.1

NonDimensional

In this case, all input data is interpreted as being for the non-dimensionalized variables, and all solutions are outputted in non-dimensional form. AERO-F non-dimensionalizes the computational input and variables as follows:

1. coordinates in x-, y- and z-directions:

$$\overline{\underline{x}} = \frac{\underline{x}}{L_{reference}}$$

2. time:

$$\overline{t} = rac{t \; u_{reference}}{L_{reference}}$$

3. density:

$$\overline{\rho} = \frac{\rho}{\rho_{reference}}$$

4. velocity:

$$\overline{\underline{u}} = \frac{\underline{u}}{u_{reference}}$$

5. pressure:

$$\overline{P} = \frac{P}{\rho_{reference}u_{reference}^2}$$

6. temperature:

$$\overline{T} = \frac{c_u T}{u_{reference}^2}$$

where the subscript teference designates a reference value.

AERO-F computes

 $u_{teference}$ internally as follows. For a perfect gas,

$$u_{\rm reference} = M_{\rm reference} \sqrt{\gamma \frac{p_{\rm 00}}{\rho_{\rm reference}}}$$

For a barotropic liquid,

$$u_{reference} = M_{reference} \sqrt{ rac{((k_1 + k_2 p_0)(k_1 + k_2 p)^{k_2 - 1})^{rac{1}{k_2}}}{p_0}}$$

where $p_0,
ho_0, k_1$ and k_2

For a highly explosive gas modeled by the JWL equation of state,

$$u_{reference} = M_{reference}c(\rho_{reference}, p_{infty})$$

where C is the speed of sound.

are defined in LiquidModel . (see ReferenceState).

Dimensional

Input parameters and output solutions are in dimensional form. This is the default and only mode available for problems involving a structural code or a steady-state sensitivity analysis.

prec-id [NonPreconditioned]:

NonPreconditioned

The dissipation terms of the convective fluxes of the solution scheme are not preconditioned.

LowMach

The dissipation terms of the convective fluxes of the solution scheme, except when *mvp-id* is set to Exact (see Implicit), are equipped with the low-Mach Turkel preconditioner. For steady-state calculations, the inertia (or time-derivative, or temporal) terms (see Preconditioner) can also be preconditioned if desired by making the request in the Time object (see Time).

framework-id [BodyFitted]:

BodyFitted

In this case, the CFD grid must be body-fitted and the governing fluid equations are formulated in the Arbitrary Lagrangian Eulerian setting which can handle both static (fixed) and dynamic (moving and deforming) grids.

Embedded

In this case, the obstacle must be embedded in the CFD grid, and the fluid equations are formulated in the Eulerian setting and solved by an embedded boundary method for CFD.

Notes:

- 1. explicit time-integration is not recommended for low-Mach flows for computational efficiency reasons;
- 2. the Embedded framework is operational only if **AERO-F** was compiled and linked with the **PhysBAM-Lite** library.

Next: 1DGrid, Previous: Problem, Up: Objects

4.2 DEFINING THE INPUT FILES

Object: Input

The several input files that are required by AERO-F are specified within the Input object. Its syntax is:

```
under Input {
       Prefix = prefix-str;
       Connectivity = connectivity-str;
       Geometry = geometry-str;
       Decomposition = decomposition-str;
       CpuMap = cpumap-str;
       Matcher = matcher-str;
       EmbeddedSurface = embeddedsurface-str;
       WallDistance = walldistance-str;
       Solution = solution-str;
       Levelset = levelset-str;
       Position = position-str;
       StrModes = strmodes-str;
       RestartData = restartdata-str;
       Perturbed = perturbsolution-str;
       PODData = poddata-str;
       ShapeDerivative = shapederivative-str;
       under 1DRestartData { ... }
with
prefix-str [""]:
      String that is prefixed to all input file names. For example, if prefix-str is set to "data/" and connectivity-str is
      set to "wing.con", AERO-F looks for a connectivity file named "data/wing.con".
connectivity-str [""]:
      Name of the binary connectivity file produced by the SOWER program.
geometry-str [""]:
      Name of the binary geometry file produced by the SOWER program. However if Problem. Type = 1D, this
      becomes the name of the ASCII file storing a one-dimensional grid in the following format:
           number_of_nodes_in_the_grid
           distance_of_node_1_to_the_center_of_the_sphere
           distance_of_node_2_to_the_center_of_the_sphere
           distance_of_last_node_to_the_center_of_the_sphere
decomposition-str [""]:
      Name of the binary decomposition file produced by the SOWER program.
cpumap-str [""]:
      Name of the ASCII CPU map file produced by the SOWER program.
matcher-str [""]:
```

Name of the binary matcher file produced by the MATCHER program (required for simulations involving a structural code).

embeddedsurface-str [""]:

Name of the ASCII file describing in the **XPost** format a discrete representation of a surface to be embedded in the CFD grid, and around/or within which the flow is to be computed. Currently, the embedded discrete surface must be made of triangles. If it is closed, the triangles must be defined such that their normals are outward to the medium they enclose.

walldistance-str [""]:

Name of the binary distance-to-the-wall file. This file is required for turbulent flow simulations performed with the one-equation Spalart-Allmaras turbulence model or the DES method (see <u>TurbulenceModel</u>). This file contains for every mesh point its distance to the closest solid wall. This distance is used in the Spalart-Allmaras turbulence model in order to provide the correct asymptotic behavior of the turbulence variable in the near wall regions. The ASCII **XPost** version of this file is always produced when the software CD2TET is used. The conversion into binary format can be performed with the SOWER software (see Hints and tips).

solution-str [""]:

Name of the binary solution (i.e. conservative variables) file obtained from a previous simulation from which AERO-F starts. If this file is not specified, AERO-F starts from a uniform flow (see <u>Restart</u>) and in particular the variable Output.Restart.Solution).

levelset-str [""]:

This information is relevant only for multi-phase flow problems (see <u>MultiPhase</u>). The content of *levelset-str* can be the name of the binary level set solution file obtained from a previous multi-phase flow simulation from which AERO-F starts. If this file is not specified, AERO-F starts from the initial solution specified in <u>InitialConditionsMultiPhase</u>.

position-str [""]:

Name of the binary file containing the position (i.e. x,y,z node coordinates) of the mesh as outputted during a previous simulation and from which AERO-F is to start. If this file is not specified, AERO-F starts from the mesh position stored in *geometry-str* (see <u>Restart</u> and in particular the variable Output.Restart.Position).

strmodes-str [""]:

Name of the binary file containing the initial position of the fluid mesh, a set of natural structural frequencies, and the set of fluid mesh positions compatible with the corresponding set of natural structural modes. This information is required here if the computation and output of the corresponding generalized forces is

requested in the object Postpro (see Postpro).

```
restartdata-str [""]:
```

Name of the ASCII restart file obtained from a previous simulation. This file allows AERO-F to continue a simulation that was successfully completed or was for some reason interrupted (see <u>Restart</u> and in particular the variable Output.Restart.RestartData).

```
perturbsolution-str [""]:
```

Name of the binary file containing a perturbed flow solution needed for linearized flow calculations. This file can be generated, for example, by running AERO-F or AERO-S with one perturbed parameter. For full-order calculations, this parameter can be any reasonable input parameter. For reduced-order computations, only a parameter such as the displacement of the body which pertains to the sources of excitations used to construct the ROM should be considered. AERO-FL computes the initial perturbation in the flow as the difference between this flow solution and the equilibrium flow solution that must be specified in Input.Solution (see Input). If this file is not specified, the initial perturbation is set to 0.

```
poddata-str [""]:
```

Except when the problem type is PODInterpolation (see <u>Problem</u>), this is the name of the binary file containing a set of POD basis vectors that could have been generated by AERO-FL (see <u>Linearized</u>) in a previous run where the problem type was set to PODConstruction (see <u>Problem</u>). When the problem type is PODInterpolation (see <u>Problem</u>), this is the name of a text file containing the number of precomputed POD bases to be interpolated, the names of the binary files containing themselves these bases, their respective Mach numbers and angles of attack, and the Mach number and angle of attack at which interpolation is desired. The format of this text file is examplified below.

Example:

```
3
PODData.d/podVecs4.freq0.499.2_4.df5e3.30snap.100pod
PODData.d/podVecs4.freq0.520.2_6.df5e3.30snap.100pod
PODData.d/podVecs4.freq0.700.2_5.df5e3.30snap.100pod
0.499 0.520 0.700
0.550
2.4 2.6 2.5
2.45
```

The first line specifies the number of precomputed POD bases to be interpolated. Each of the following three lines specifies the path and name of the file containing a precomputed POD basis to be interpolated. The following line specifies the three Mach numbers at which the POD bases to be interpolated are precomputed, in the order in which these bases are specified. The next line specifies the interpolation Mach number. The following line specifies the three angles of attack at which the POD bases to be interpolated are precomputed, in the order in which these bases are specified. The last line specifies the interpolation angle of attack.

shapederivative-str [""]:

Name of the binary file containing essentially $\frac{d\mathbf{X}_T}{ds_j}$, the derivatives of the mesh position \mathbf{X} with respect to a number of shape design variables s_j at the fluid/structure boundary \mathbf{I} (see SensitivityAnalysis and Sensitivities). This information is generated as follows. First, an **XPost**-type ASCII file containing the following information is created. This ASCII file starts with an **XPost**-like header (see below), followed by the total number of grid points in the CFD mesh (and not the number of fluid grid points on the fluid/structure interface). Then, the information $\frac{d\mathbf{X}_T}{ds_j}$ is specified in this ASCII file for each shape design parameter s_j , one parameter at a time, in block form. First, the index j of s_j is specified on a separate line starting from j=0 (zero). Then, all grid points of the CFD mesh are considered in the same ordering as that adopted in the corresponding **XPost** geometry file. On each line corresponding to grid point s_j , the derivatives s_j , s_j , s_j , and s_j , and s_j denote the coordinates of the grid point s_j are provided. If the grid point s_j is an "interior" point, these derivatives are set to zero. An example of the ASCII file described above is given below.

Then, the ASCII file described above is converted to a distributed binary file using the **SOWER** code and generated mesh partition.

1DRestartData:

Allows the local initialization of a three-dimensional flow computation with the results of a one-dimensional spherically symmetric unsteady two-phase flow computation.

Notes:

- 1. as mentioned in the SOWER manual, there is no need to specify the ending number for the binary files;
- 2. if the name of the input files Solution, Position, RestartData, or 1DRestartData starts by a slash (/), the variable Prefix is not used for these files.
- 1DRestartData

Up: Input

4.2.1 INITIALIZING A 3D SIMULATION LOCALLY WITH 1D SPHERICALLY SYMMETRIC DATA

```
Object: 1DRestartData
```

The 1DRestartData object initializes a three-dimensional flow computation locally with the results of a one-dimensional spherically symmetric unsteady two-phase flow computation identified by a simulation tag 1Dsimulation-id-int.

The syntax of this object is:

```
under 1DRestartData[1Dsimulation-id-int] {
    File = file-str;
    X0 = x0-real;
    Y0 = y0-real;
    Z0 = z0-real;
    under FluidIDMap{ ... }
}
```

Name of the ASCII file containing the results of a previously performed one-dimensional spherically symmetric unsteady two-phase flow computation. It is subject to Input. Prefix.

x0-real [0.0]:

file-str [""]:

x-coordinate of the center of the spherical region where the flow is to be initialized by the spherically

symmetric results stored in file-str.

y0-real [0.0]:

y-coordinate of the center of the spherical region where the flow is to be initialized by the spherically symmetric results stored in *file-str*.

z0-real [0.0]:

z-coordinate of the center of the spherical region where the flow is to be initialized by the spherically symmetric results stored in *file-str*.

FluidIDMap:

This object can be used to map the fluid identification integers of a one-dimensional two-phase flow simulation to those of the three-dimensional flow computation locally initialized by the results of that one-dimensional simulation.

• FluidIDMap

Up: 1DRestartData

4.2.1.1 MAPPING A SET OF FLUID IDENTIFICATION TAGS TO ANOTHER ONE



The FluidIDMap object can be used to map the fluid identification integers of a one-dimensional two-phase flow simulation identified by its simulation tag *IDsimulation-id-int* to those of the three-dimensional flow computation locally initialized by the results of that one-dimensional simulation.

The syntax of this object is:

fluidIDreceptor [—]:

```
under FluidIDMap[FluidIDDonor-int] {
    FluidIDReceptor = fluidIDreceptor-int;
}
with
```

Integer identifying the fluid medium to be initialized using data from the fluid medium identified in the one-dimensional spherically symmetric two-phase flow simulation by the integer *FluidIDDonor-int*.

Next: Output, Previous: Input, Up: Objects

4.3 GENERATING A ONE-DIMENSIONAL SPHERICALLY SYMMETRIC GRID



The 1DGrid object allows the user to generate a uniform, one-dimensional, spherically symmetric grid within **AERO-F** instead of inputting it in <u>Input</u>.Geometry. The first point of this grid is always located at the origin of the coordinate system. However, using <u>1DRestartData</u>, the flow results obtained on this grid can be applied in a spherical region of a three-dimensional domain centered at an arbitrary point.

The syntax of this object is:

```
under 1DGrid {
  NumberOfPoints = numberofpoints-int;
  Radius = radius-real;
}
```

with

numberofpoints [0]:

Number of grid points to be generated.

radius-real [0.0]:

radius of the spherical region to be represented by a one-dimensional grid.

Next: Surfaces, Previous: 1DGrid, Up: Objects

4.4 DEFINING THE OUTPUT FILE



The Output object mainly defines the name of the files used for post-processing (see the SOWER manual) and restart purposes. Its syntax is:

```
under Output {
  under Postpro { ... }
  under Restart { ... }
}
```

Postpro:

Specifies the computational results to output.

Restart:

Specifies the data to be saved for possible restart later.

- Postpro
- Restart

Next: Restart, Up: Output

4.4.1 EXPLOITING THE COMPUTATIONAL RESULTS

Object: Postpro

The syntax of the Postpro object is:

```
under Postpro {
 Prefix = prefix-str;
 Density = density-str;
 TavDensity = tavdensity-str;
 Mach = mach-str:
 TavMach = tavmach-str;
 HWTMach = hwtmach-str;
 Pressure = pressure-str;
 TavPressure = tavpressure-str;
 DeltaPressure = deltapressure-str;
 HydroStaticPressure = hydrostaticpressure-str;
 HydrodynamicPressure = hydrodynamicpressure-str;
 Temperature = temperature-str;
 TavTemperature = tavtemperature-str;
 TemperatureNormalDerivative = tempnormder-str;
 HeatFluxPerUnitSurface = heatfluxus-str;
 HeatFlux = heatflux-str;
 TotalPressure = totalpressure-str;
 TavTotalPressure = tavtotalpressure-str;
 LiftandDrag = liftanddrag-str;
 TavLiftandDrag = tavliftanddrag-str;
 Vorticity = vorticity-str;
 TavVorticity = tavvorticity-str;
 NuTilde = nutilde-str;
 K = k-str;
 Eps = eps-str;
 EddyViscosity = eddyviscosity-str;
 DeltaPlus = deltaplus-str;
 CsDLES
          = csdles-str;
 TavCsDLES = tavcsdles-str;
          = csdvms-str;
 CsDVMS
 TavCsDVMS = tavcsdvms-str;
 MutOverMu = mutomu-str;
 SkinFriction = skinfriction-str;
 TavSkinFriction = tavskinfriction-str;
 Velocity = velocity-str;
 TavVelocity = tavvelocity-str;
 VelocityMagnitude = velocitymagnitude-str;
 HWTVelocityMagnitude = hwtvelocitymagnitude-str;
 Displacement = displacement-str;
 TavDisplacement = tavdisplacement-str;
 FlightDisplacement = fldisplacement-str;
 LocalFlightDisplacement = lfldisplacement-str;
 Force = force-str;
 GeneralizedForce = generalizedforce-str;
 TavForce = tavforce-str;
 HydroStaticForce = hydrostaticforce-str;
 HydroDynamicForce = hydrodynamicforce-str;
 Residual = residual-str;
 Frequency = frequency-int;
 TimeInterval = timeinterval-real;
 Length = length-real;
 Surface = surface-real;
```

```
XM = xm-real;
       YM = ym-real;
       ZM = zm-real;
       PODData = poddata-str;
       ROM = rom-str;
       Philevel = philevel-str;
       FluidID = fluidID-str;
       StateVector = statevector-str;
       StateVectorSensitivity
                                    = statevectorsensitivity-str;
       DensitySensitivity = densitysensitivity-str;
       MachSensitivity = machsensitivity-str;
       TemperatureSensitivity = temperatursensitivity-str;
       PressureSensitivity = pressuresensitivity-str;
       TotalPressureSensitivity = totalpressuresensitivity-str;
       VelocitySensitivity = velocitysensitivity-str;
       DisplacementSensitivity = displacementsensitivity-str;
       ForceSensitivity = forcesensitivity-str;
       SparseGrid = sparsegrid-str:
       MaterialVolumes = matvols-str;
with
prefix-str [""]:
      String that is prefixed to all post-processing file names.
density-str [""]:
      Name of the binary file that contains the sequence of nodal density values.
tavdensity-str [""]:
      Name of the binary file that contains the sequence of time-averaged nodal density values (useful particularly
      in LES simulations).
mach-str [""]:
      Name of the binary file that contains the sequence of nodal Mach number values.
hwtmach-str [""]:
      Name of the binary file that contains the sequence of nodal "hybrid wind tunnel" (see Accelerated and Figure
      HWT) Mach number values (relevant only for accelerated or decelerated flow simulations). The hybrid wind
      tunnel Mach number is defined as the Mach number based on the difference between the local velocity and
      the ALE (moving) grid velocity — that is, the relative Mach number with respect to the ALE frame.
tavmach-str [""]:
```

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Name of the binary file that contains the sequence of time-averaged nodal Mach number values (useful

particularly in LES simulations).

pressure-str [""]:

Name of the binary file that contains the sequence of nodal pressure values. If *gravity-real* and *depth-real* have nonzero values (see <u>Hydro</u>), then the pressure values are the sum of the hydrostatic and hydrodynamic pressure values.

```
pressurecoefficient-str [""]:
```

Name of the binary file that contains the sequence of nodal pressure coefficient values. These are defined in **AERO-F** only when the fluid is modeled as a perfect gas. If for some reason *gravity-real* and *depth-real* have nonzero values (see <u>Hydro</u>), then the pressure values used for this output are the sum of the hydrostatic and hydrodynamic pressure values.

```
tavpressure-str [""]:
```

Name of the binary file that contains the sequence of time-averaged nodal pressure values (useful particularly in LES simulations).

hydrostaticpressure-str [""]:

Name of the binary file that contains the sequence of nodal hydrostatic pressure (ρgh) values.

hydrodynamicpressure-str [""]:

Name of the binary file that contains the sequence of nodal hydrodynamic pressure values.

deltapressure-str [""]:

Name of the binary file that contains the sequence of pressure variations with respect to the free-stream pressure (useful particularly for Low-Mach simulations).

temperature-str [""]:

Name of the binary file that contains the sequence of nodal temperature values.

tavtemperature-str [""]:

Name of the binary file that contains the sequence of time-averaged nodal temperature values (useful particularly in LES simulations).

tempnormder-str [""]:

Name of the binary file that contains the sequence of temperature normal derivative ($\nabla T \cdot \vec{n}$) nodal values for (moving) isothermal wall boundaries and zero elsewhere.

heatfluxus-str [""]:

Name of the binary file that contains the sequence of heat flux per unit surface ($-\kappa \vec{\nabla} T \cdot \vec{n}$) nodal values

for (moving) isothermal wall boundaries and zero elsewhere.

heatflux-str [""]:

Name of the ASCII file that contains for all the time-steps:

- 1. the time-step number;
- 2. the physical time;
- 3. the subcycling factor;
- 4. the number of Newton iterations;
- 5. the heat flux exchanged through (moving) isothermal wall boundaries ($-\int_S \kappa \vec{\nabla} T \cdot \vec{n} d\sigma$).

totalpressure-str [""]:

Name of the binary file that contains the sequence of nodal total pressure values.

tavtotalpressure-str [""]:

Name of the binary file that contains the sequence of time-averaged nodal total pressure values (useful particularly in LES simulations).

liftanddrag-str [""]:

Name of the ASCII file that contains for all the time-steps:

- 1. the time-step number;
- 2. the physical time;
- 3. the subcycling factor;
- 4. the number of Newton iterations;
- 5. the drag, which is the force in the direction parallel to the free-stream velocity;
- 6. the lift, which is defined here as the force in the direction orthogonal to the vector defined by the yaw angle in the x-y plane;
- 7. the lift, which is defined here as the force in the direction orthogonal to the vector defined by the angle of attack in the x-z plane.

$tav lift and drag-str\ [""]:$

Name of the ASCII file that contains for all the time-steps:

- 1. the time-step number;
- 2. the physical time;
- 3. the subcycling factor;
- 4. the number of Newton iterations;
- 5. the time-averaged drag, which is the force in the direction parallel to the free-stream velocity;

- 6. the time-averaged lift, which is defined here as the force in the direction orthogonal to the vector defined by the yaw angle in the x-y plane;
- 7. the time-averaged lift, which is defined here as the force in the direction orthogonal to the vector defined by the angle of attack in the x-z plane.

```
vorticity-str [""]:
```

Name of the binary file that contains the sequence of nodal vorticity values.

```
tavvorticity-str [""]:
```

Name of the binary file that contains the sequence of time-averaged nodal vorticity values (useful particularly for LES simulations).

```
nutilde-str [""]:
```

Name of the binary file that contains the sequence of nodal $\tilde{\nu}_t$ (field variable in the Spalart-Allmaras turbulence model) values.

```
k-str [""]:
```

Name of the binary file that contains the sequence of nodal k (turbulent kinetic energy in the $k-\epsilon$ model) values.

```
eps-str [""]:
```

Name of the binary file that contains the sequence of nodal ϵ (turbulent kinetic energy dissipation rate in the $k-\epsilon$ model) values.

```
eddyviscosity-str [""]:
```

Name of the binary file that contains the sequence of nodal eddy viscosity values.

```
deltaplus-str [""]:
```

Name of the binary file that contains the sequence of nodal non-dimensional wall distance values (only available if a wall function is used, see <u>Wall</u>).

```
csdles-str [""]:
```

Name of the binary file that contains the sequence of nodal values of the *dynamic* Smagorinski coefficient C_s computed during a dynamic LES simulation.

```
tavcsdles-str [""]:
```

Name of the binary file that contains the sequence of time-averaged nodal values of the *dynamic* Smagorinski coefficient C_s computed during a dynamic LES simulation.

csdvms-str [""]:

Name of the binary file that contains the sequence of nodal values of the *dynamic* Smagorinski coefficient C'_s computed during a dynamic VMS-LES simulation.

tavcsdvms-str [""]:

Name of the binary file that contains the sequence of time-averaged nodal values of the *dynamic* Smagorinski coefficient C_s' computed during a dynamic VMS-LES simulation.

mutomu-str [""]:

Name of the binary file that contains the sequence of nodal values of the ratio of turbulent viscosity and molecular viscosity (available for all turbulence simulations except VMS-LES).

skinfriction-str [""]:

Name of the binary file that contains the sequence of nodal values of the skin friction coefficient.

tavskinfriction-str [""]:

Name of the binary file that contains the sequence of time-averaged nodal values of the skin friction coefficient.

velocity-str [""]:

Name of the binary file that contains the sequence of nodal velocity vectors.

tavvelocity-str [""]:

Name of the binary file that contains the sequence of time-averaged nodal velocity vectors (useful particularly for LES simulations).

velocitymagnitude-str [""]:

Name of the binary file that contains the sequence of nodal velocity magnitudes (useful particularly for low-Mach multi-phase simulations).

hwtvelocitymagnitude-str [""]:

Name of the binary file that contains the sequence of nodal "hybrid wind tunnel" (see <u>Accelerated</u> and Figure HWT) velocity magnitudes (relevant only for accelerated or decelerated flow simulations). The hybrid wind

tunnel velocity magnitude is defined as the magnitude of the difference between the velocity and the speed of the accelerating or decelerating moving grid — that is, the magnitude of the relative velocity with respect to the ALE frame.

displacement-str [""]:

Name of the binary file that contains the sequence of nodal displacement vectors.

tavdisplacement-str [""]:

Name of the binary file that contains the sequence of time-averaged nodal displacement vectors (useful particularly in LES simulations).

fldisplacement-str [""]:

Name of the binary file that contains the sequence of nodal flight displacement vectors. For accelerated flight and landing gear simulations, the flight displacement is defined as the difference between the usual mesh displacement and the product $V_{\infty}t$ where t denotes time — that is, the displacement with respect to a frame moving at the free-stream velocity.

lfldisplacement-str [""]:

Name of the binary file that contains the sequence of nodal local flight displacement vectors. For accelerated flight, the local flight displacement is defined as the difference between the usual mesh displacement and the rigid body displacement associated with the direction of acceleration — that is, the deformational component of the mesh displacement. For landing flight simulations, it is defined as the difference between the usual mesh displacement and the rigid body displacement in rolling direction.

force-str [""]:

Name of the ASCII file that contains for all the time-steps:

- 1. the time-step number;
- 2. the physical time;
- 3. the subcycling factor;
- 4. the number of Newton iterations;
- 5. the force in the x-direction;
- 6. the force in the y-direction;
- 7. the force in the z-direction;
- 8. the moment along the x-direction;
- 9. the moment along the y-direction;
- 10. the moment along the z-direction;
- 11. the energy transferred to the structure.

Note: if gravity-real and depth-real have nonzero values (see Hydro), then the force values are the sum of the

hydrostatic and hydrodynamic force values.

generalizedforce-str [""]:

Name of the ASCII file containing the generalized force(s) associated with the structural mode(s) specified under the object Input (see Input) or with the forced oscillation mode (which is not necessarily a natural structural mode) specified or implied under the object Forced (see Forced), in the following format:

- 1. the time-step number;
- 2. the physical time;
- 3. the subcycling factor;
- 4. the number of Newton iterations;
- 5. the generalized force associated with the first input mode shape;
- 6. the generalized force associated with the second input mode shape;
- 7. ...;
- 8. the generalized force associated with the last mode shape;

Note: when the simulation of a forced oscillation is specified under the object Forced (see <u>Forced</u>), a requested generalized force computation is performed with respect to the forced oscillation "mode" (which is not necessarily a natural structural mode), unless a set of natural structural modes are specified in *StrModes* under the object Input (see <u>Input</u>), in which case the generalized forces are computed with respect to these specified natural structural modes.

tavforce-str [""]:

(Useful particularly in LES simulations). Name of the ASCII file that contains for all the time-steps:

- 1. the time-step number;
- 2. the physical time;
- 3. the subcycling factor;
- 4. the number of Newton iterations;
- 5. the time-averaged force in the x-direction;
- 6. the time-averaged force in the y-direction;
- 7. the time-averaged force in the z-direction;
- 8. the time-averaged moment along the x-direction;
- 9. the time-averaged moment along the y-direction;
- 10. the time-averaged moment along the z-direction;
- 11. the time-averaged energy transferred to the structure.

hydrostaticforce-str [""]:

Name of the ASCII file that contains the components of the hydrostatic force in the x-, y-, and z-directions.

hydrodynamicforce-str [""]:

Name of the ASCII file that contains for all the time-steps:

- 1. the time-step number;
- 2. the physical time;
- 3. the subcycling factor;
- 4. the number of Newton iterations;
- 5. the hydrodynamic force in the x-direction;
- 6. the hydrodynamic force in the y-direction;
- 7. the hydrodynamic force in the z-direction;
- 8. the hydrodynamic moment along the x-direction;
- 9. the hydrodynamic moment along the y-direction;
- 10. the hydrodynamic moment along the z-direction;
- 11. the hydrodynamic energy transferred to the structure.

liftanddrag-str [""]:

Name of the ASCII file that contains for all the time-steps:

- 1. the time-step number;
- 2. the physical time;
- 3. the subcycling factor;
- 4. the number of Newton iterations;
- 5. the drag, which is the force in the direction parallel to the free-stream velocity;
- 6. the lift, which is defined here as the force in the direction orthogonal to the vector defined by the yaw angle in the x-y plane;
- 7. the lift, which is defined here as the force in the direction orthogonal to the vector defined by the angle of attack in the x-z plane.

residual-str [""]:

Name of the ASCII file that contains for all the time-steps:

- 1. the time-step number;
- 2. the elapsed time;
- 3. the relative nonlinear residual;
- 4. the CFL number.

frequency-int [0]:

The frequency (every so many time-iteration) at which the output files are written. If the frequency is set to zero, the output files are only written at the last time-iteration. When the frequency is set to a nonzero value, the output files are also written at the last time-iteration.

timeinterval-real []:

This is an alternative option to *frequency-int* for specifying when to write a result in an output file. Essentially, *timeinterval-real* is an output time-step Δt_{out} which controls the frequency at which the output files are

written as follows. Let m be a positive integer set initially to 0, and incremented by 1 after each output time-iteration is reached. Then, output is performed at each time-iteration $t^n \geq m \times \Delta t_{out}$. When timeinterval-real is specified to a strictly positive value, the output files are always written at the last

computed time-iteration. If both frequency-int and timeinterval-real are specified, frequency-int is ignored.

length-real [1.0]:

Reference length used in the computation of the moment coefficients.

surface-real [1.0]:

Reference surface used in the computation of the force and moment coefficients.

xm-real [0.0]:

x-coordinate of the point around which the moment coefficients are computed.

ym-real [0.0]:

y-coordinate of the point around which the moment coefficients are computed.

zm-real [0.0]:

z-coordinate of the point around which the moment coefficients are computed.

poddata-str [""]:

Name of the binary file to contain the computed POD basis vectors which are always output in non-dimensional form in order to be invariant with changes in altitude.

rom-str [""]:

Name of ASCII file where to output in the format described in Appendix B (see <u>ROM</u>) the matrices defining a fluid or aeroelastic ROM.

philevel-str [""]:

Name of the binary file that contains the sequence of nodal level set values.

fluidID-str [""]:

Name of the binary file that contains the sequence of nodal integer values identifying the fluid media covering these nodes (see <u>VolumeData</u> and <u>FluidModel</u>).

statevector-str [""]:

Name of the binary file that contains the sequence of nodal fluid state vector values. In particular, these

solution snapshots can be used to construct a POD basis (see **Problem**).

```
statevectorsensitivity-str [""]:
```

Name of the binary file that contains the sequence of the sensitivities of the nodal fluid state vector values with respect to the specified variables.

```
densitysensitivity-str [""]:
```

Name of the binary file that contains the sequence of sensitivities of nodal density values with respect to specified variables.

```
machsensitivity-str [""]:
```

Name of the binary file that contains the sequence of sensitivities of nodal Mach number values with respect to specified variables.

```
temperaturesensitivity-str [""]:
```

Name of the binary file that contains the sequence of sensitivities of nodal temperature values with respect to specified variables.

```
pressuresensitivity-str [""]:
```

Name of the binary file that contains the sequence of sensitivities of nodal pressure values with respect to specified variables. If *gravity-real* and *depth-real* have nonzero values (see <u>Hydro</u>), the pressure values referred to here are those corresponding to the sum of the hydrostatic and hydrodynamic pressure values.

```
totalpressuresensitivity-str [""]:
```

Name of the binary file that contains the sequence of sensitivities of nodal total pressure values with respect to specified variables.

```
velocitysensitivity-str [""]:
```

Name of the binary file that contains the sequence of sensitivities of nodal velocity vectors with respect to specified variables.

```
displacementsensitivity-str [""]:
```

Name of the binary file that contains the sequence of sensitivities of nodal displacement vectors with respect to specified variables.

```
forcesensitivity-str [""]:
```

Name of the ASCII file that contains the sequence of sensitivities of the aerodynamic forces and moments

with respect to specified variables, in the following format:

- 1. the sensitivity analysis step number;
- 2. the active specified variable: "1" for a shape parameter, "2" for the Mach number, "3" for the angle of attack, and "4" for the yaw angle (see Inlet);
- 3. the force in the x-direction;
- 4. the force in the y-direction;
- 5. the force in the z-direction;
- 6. the moment along the x-direction;
- 7. the moment along the y-direction;
- 8. the moment along the z-direction;
- 9. sonic boom (currently not supported and therefore set to zero);
- 10. the sensitivity of the force in the x-direction with respect to the specified variable;
- 11. the sensitivity of the force in the y-direction with respect to the specified variable;
- 12. the sensitivity of the force in the z-direction with respect to the specified variable;
- 13. the sensitivity of the moment along the x-direction with respect to the specified variable;
- 14. the sensitivity of the moment along the y-direction with respect to the specified variable;
- 15. the sensitivity of the moment along the z-direction with respect to the specified variable;
- 16. sensitivity of the sonic boom with respect to the specified variable (currently not supported and therefore set to zero).

sparsegrid-str [""]:

Name of the ASCII file that contains computational data tabulated in sparse grid format. If the tabulated data is to be stored across multiple files, *sparsegrid-str* is the common prefix to all these files whose names will be *sparsegrid-str*.x, with x ranging from 1 to the number of files.

matvols-str [""]:

Name of the ASCII file that contains the sequence of volumes occupied by each fluid medium during a simulation. The format of this file is as follows:

- 1. the time-step number;
- 2. the current time-instance;
- 3. the volume occupied by the fluid medium whose ID is 0;
- 4. the volume occupied by the fluid medium whose ID is 1;
- 5. ...
- 6. the volume occupied by the fluid medium whose ID is the highest;
- 7. the volume occupied by the obstacle;
- 8. the total volume of the computational domain.

Notes:

1. as mentioned in <u>Problem</u>, the output mode (non-dimensional or dimensional) is governed by the variable

Problem.Mode:

- 2. in the files containing the sensitivities of nodal flow quantities with respect to specified variables, the specific variables are identified by tags: "1" for a shape parameter, "2" for the Mach number, "3" for the main angle of attack, and "4" for the yaw angle of attack; the integer tag is placed before its corresponding result set; the results are outputted on a tag basis and for a given tag, on a node basis; the sensitivities with respect to shape parameters are outputted in the order in which these parameters are specified in the file Input.ShapeDerivative (see Input).
- 3. The binary sensitivity analysis result files can be post-processed by **SOWER** and visualized by **XPost** as all other binary output results files.

Previous: Postpro, Up: Output

4.4.2 SAVING THE COMPUTATIONAL RESULTS FOR LATER

Object: Restart

The Restart object specifies the name of the files that are written during (if the value of Output.Restart.Frequency is different from zero) and at the end of the computation. These files are only needed if one wishes to restart AERO-F (see Input). The syntax of the Restart object is:

```
under Restart {
    Prefix = prefix-str;
    Solution = solution-str;
    Position = position-str;
    LevelSet = levelset-str;
    RestartData = restartdata-str;
    Frequency = frequency-int;
    TimeInterval = timeinterval-real;
}
with

prefix-str [""]:
```

String that is prefixed to all restart file names.

```
solution-str ["DEFAULT.SOL"]:
```

Name of the binary solution (i.e. conservative variables) file.

```
position-str ["DEFAULT.POS"]:
```

Name of the binary position (i.e. x,y,z node coordinates) file. This file is written if a "ping-pong" step, "modal ping-pong" step, aeroelastic, forced vibration, or accelerated flight simulation is performed.

levelset-str ["DEFAULT.LS"]:

Name of the binary file containing the "conservative" level set variable $\rho\phi$. This file can be specified only for multi-phase flow simulations (see MultiPhase).

```
restartdata-str ["DEFAULT.RST"]:
```

Name of the ASCII restart file.

frequency-int [0]:

The frequency (every so many time-iteration) at which the restart files are re-written (each save overwrites the previous one). In the case of an aerothermal, aeroelastic, or aerothermoelastic simulation with the AERO-S code, this value must be specified in the AERO-S input file.

timeinterval-real []:

This is an alternative option to *frequency-int* for specifying when to update a restart file. Essentially, *timeinterval-real* is a restart update time-step Δt_{up} which controls the frequency at which the restart files are updated as follows. Let m be a positive integer set initially to 0, and incremented by 1 after each update time-iteration is reached. Then, the update of the restart files is performed at each time-iteration $t^n \geq m \times \Delta t_{up}$. When *timeinterval-real* is specified to a strictly positive value, the restart files are always written at the last computed time-iteration. If both *frequency-int* and *timeinterval-real* are specified,

frequency-int is ignored. This option is not recommended when performing a coupled-field simulation using also the AERO-S code.

Next: Velocity, Previous: Output, Up: Objects

4.5 SPECIFYING THE ATTRIBUTES OF THE MESH SURFACES DEFINED IN THE COMPUTER-AIDED DESIGN MODEL

Object: Surfaces

During the process of generating a fluid mesh from a computer-aided design model, several surfaces can be defined and grouped according to a user-specified id number. The Surfaces object specifies these surfaces in preparation for defining their attributes. Its syntax is:

```
under Surfaces {
    under SurfaceData[surface-id-int] { ... }
    ...
}
with
surface-id-int [None]:
```

ID number of a surface or group of surfaces.

SurfaceData:

Specifies the attributes of the mesh surfaces.

SurfaceData

Up: Surfaces

4.5.1 SPECIFYING THE ATTRIBUTES OF THE MESH SURFACES

```
Object: SurfaceData
```

The SurfaceData object defines the attributes to be assigned to the surface identified by the specified surface tag *surface-id-int*.

The syntax of this object is:

```
under SurfaceData[surface-id-int] {
  Nx = Nx-real;
  Ny = Ny-real;
  Nz = Nz-real;
  ComputeForces = computef-flag;
  SeparateForces = separatef-flag;
  ComputeHeatFlux = computehf-flag;
  SeparateHeatFlux = separatehf-flag;
  VelocityID = velocity-id-int;
  Type = type-id-;
  Temperature = temp-real;
}
```

with

Nx-real [0.0]:

This information is relevant only when the target simulation involves mesh motion. If at least one of the parameters *Nx-real* or *Ny-real* or *Nz-real* (see below) is non zero, the tagged surface (or group of surfaces) is declared a sliding plane and *Nx-real* specifies the value of the x-component of the normal to this sliding plane. In this case, the nodes in the declared sliding plane are constrained to move within this plane — that is, the component of their displacement field along the specified normal to the sliding plane is constrained to zero. If the declared sliding plane is also a symmetry plane and *type-id* of the MeshMotion object is set to *Corotational* (see MeshMotion), it is strongly recommended in this case to specify the Symmetry object within the MeshMotion object (see Symmetry).

Ny-real [0.0]:

This information is relevant only when the target simulation involves mesh motion. If at least one of the

parameters *Nx-real* or *Ny-real* or *Nz-real* (see below) is non zero, the tagged surface (or group of surfaces) is declared a sliding plane and *Ny-real* specifies the value of the y-component of the normal to this sliding plane. In this case, the nodes in the declared sliding plane are constrained to move within this plane — that is, the component of their displacement field along the specified normal to the sliding plane is constrained to zero. If the declared sliding plane is also a symmetry plane and *type-id* of the MeshMotion object is set to *Corotational* (see MeshMotion), it is strongly recommended in this case to specify the Symmetry object within the MeshMotion object (see Symmetry).

Nz-real [0.0]:

This information is relevant only when the target simulation involves mesh motion. If at least one of the parameters *Nx-real* or *Ny-real* or *Nz-real* (see below) is non zero, the tagged surface (or group of surfaces) is declared a sliding plane and *Nz-real* specifies the value of the z-component of the normal to this sliding plane. In this case, the nodes in the declared sliding plane are constrained to move within this plane — that is, the component of their displacement field along the specified normal to the sliding plane is constrained to zero. If the declared sliding plane is also a symmetry plane and *type-id* of the MeshMotion object is set to *Corotational* (see MeshMotion), it is strongly recommended in this case to specify the Symmetry object within the MeshMotion object (see Symmetry).

computef-flag []:

True

In the absence of this command, and when requested under the Output.Postpro object, AERO-F computes the total aerodynamic forces (lift, drag, forces and moments, time-averaged counterparts, etc.) generated by all "moving" surfaces except moving inlet and outlet boundaries. Setting this command to True adds to the total the contribution of the specified tagged surface (or group of surfaces).

False

In the absence of this command, and when requested under the Output.Postpro object, AERO-F computes the total aerodynamic forces (lift, drag, forces and moments, time-averaged counterparts, etc.) generated by all "moving" surfaces except moving inlet and outlet boundaries. Setting this command to False removes from the total the contribution of the specified tagged surface (or group of surfaces).

separatef-flag [False]:

True

In this case, the aerodynamic forces (lift, drag, forces and moments, time-averaged counterparts, etc.) generated by the tagged surface (or group of surfaces) are output in a separate file, assuming that such a result is requested under the Output.Postpro object. The name of each output file associated with the tagged surface (or group of surfaces) is set to the filename of the corresponding result specified under Output.Postpro with a postfix set to the surface id number.

False

In this case, the aerodynamic forces (lift, drag, forces and moments, time-averaged counterparts, etc.)

generated by the tagged surface (or group of surfaces) are not computed and output in a separate file.

computehf-flag []:

True

In the absence of this command, and when requested under the Output. Postpro object, **AERO-F** computes the total heat flux through all "moving" isothermal wall boundaries. Setting this command to True adds to the total the contribution of the specified tagged surface (or group of surfaces).

False

In the absence of this command, and when requested under the Output.Postpro object, **AERO-F** computes the total heat flux through all "moving" isothermal wall boundaries. Setting this command to False removes from the total the contribution of the specified tagged surface (or group of surfaces).

separatehf-flag [False]:

True

In this case, the heat flux values through the tagged surface (or group of surfaces) are outputted in a separate file, assuming that such a result is requested under the Output.Postpro object. The name of each output file associated with the tagged surface (or group of surfaces) is set to the filename of the corresponding result specified under Output.Postpro with a postfix set to the surface id number.

False

In this case, the heat flux values through the tagged surface (or group of surfaces) are not outputted in a separate file.

velocity-id-int [None]:

ID number of a prescribed velocity data-set including the rotation or translation axis, the center of rotation, and the angular or translational velocity (see <u>Velocity</u>, <u>RotationAxis</u>). This option can be used to prescribe the velocity field of a rotating or translating surface in a viscous flow simulation. In the case of an aeroelastic computation, if the tagged surface is at the fluid-structure interface, the prescribed velocity field is superposed to the velocity field of the transmission condition at this interface.

type-id []:

Adiabatic

In this case, the surface identified by the specified surface tag is treated as an adiabatic surface (wall).

Isotherma

In this case, the surface identified by the specified surface tag is treated as an isothermal surface (wall) where the constant temperature is specified in SurfaceData.Temperature (see below).

The default value of *type-id* is the value set in Wall. Type (see Wall).

temp-real [—]:

Temperature of the surface identified by the specified surface tag if this surface is specified as an isothermal wall in SurfaceData.Type (see above). Attention should be paid to inputting this temperature, when desired, in the same system of units as that of the ideal gas constant R (see <u>GasModel</u>) and the remainder of the input file.

Next: Volumes, Previous: Surfaces, Up: Objects

4.6 SPECIFYING ROTATIONAL AND TRANSLATIONAL VELOCITY FIELDS



Axes of rotation or translation are defined using this object to facilitate the prescription of the velocity field of the grid points lying on a rotating or translating surface (see <u>Surfaces</u>). The syntax of this object is:

```
under Velocity{
  under RotationAxis[rotation-id-int] { ... } ...
}
```

RotationAxis:

with

Specifies rotational and translational velocity fields.

rotation-id-int [None]:

ID number of a rotation or translation data-set.

RotationAxis

Up: Velocity

4.6.1 SPECIFYING ROTATIONAL AND TRANSLATION VELOCITY FIELDS (CONTINUE)

Object: RotationAxis

The RotationAxis object defines the parameters of the specified rotation/translation data-set. Its syntax is:

```
under RotationAxis[rotation-id-int] {
  Nx = Nx-real;
  Ny = Ny-real;
  Nz = Nz-real;
  X0 = X0-real;
  Y0 = Y0-real;
  Z0 = Z0-real;
  InfiniteRadius = infiniteradius-flag;
  Omega = omega-real;
```

}

with

Nx-real [0.0]:

The x-component of the normalized rotation axis or translation vector.

Ny-real [0.0]:

The y-component of the normalized rotation axis or translation vector.

Nz-real [0.0]:

The z-component of the normalized rotation axis or translation vector.

X0-real [0.0]:

The x-coordinate of the center of rotation.

Y0-real [0.0]:

The y-coordinate of the center of rotation.

Z0-real [0.0]:

The z-coordinate of the center of rotation.

infiniteradius-flag [False]:

False

When this flag is set to False, the vector specified above is interpreted as the normalized axis of rotation.

True

When this flag is set to True, the vector specified above is interpreted as the normalized direction of translation.

omega-real [0.0]:

When *infiniteradius-flag* is set to False, *omega-real* is the angular velocity. When *infiniteradius-flag* is set to True, *omega-real* becomes the magnitude of the translational velocity.

Next: ReferenceState, Previous: Velocity, Up: Objects

4.7 SPECIFYING THE ATTRIBUTES OF THE MESH VOLUMES DEFINED IN THE COMPUTER-AIDED DESIGN MODEL



During the process of generating a fluid mesh from a computer-aided design model, several volumes (sets of mesh elements) can be defined and grouped according to a user-specified id number. The Volumes object specifies these volumes in preparation for defining their attributes. Its syntax is:

```
under Volumes{
    under VolumeData[volume-id-int] { ... }
    ...
}
with
```

ID number of a volume or group of volumes.

VolumeData:

Specifies the attributes of the mesh volumes.

VolumeData

volume-id-int [None]:

Up: Volumes

Fluid

4.7.1 SPECIFYING THE ATTRIBUTES OF THE MESH VOLUMES

```
Object: VolumeData
```

The VolumeData object specifies the attributes of a region of the computational domain (subset of the mesh elements) identified by the integer *volume-id-int*. It can also be used to set the initial conditions of a multi-fluid (which includes the particular case of a single fluid with porous media) or multi-phase flow problem. The syntax of this object is:

```
under VolumeData[volume-id-int] {
    Type = type-str;
    FluidID = fluid-id-int;
    under PorousMedium { ... }
    under InitialState { ... }
}
with

type-str [Fluid]:
```

Specifies that the volume identified by *volume-id-int* is occupied by a fluid. The fluid which initially occupies this volume is identified by its integer identification number *fluid-id-int*; its material properties are set in FluidModel, and its initial state is specified in InitialState.

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Porous

Specifies that the volume identified by *volume-id-int* is occupied by a porous medium whose properties are described in the PorousMedium object.

fluid-id-int [—]:

Integer identification (ID) number of the fluid medium which initially occupies the volumic region identified by *volume-id-int*. This is the same ID used in <u>FluidModel</u> to set the material properties of this fluid medium.

PorousMedium:

Defines the properties of the porous medium occupying the volumic region of the computational domain identified by *volume-id-int* if *type-str* is set to PorousMedium.

InitialState:

Defines the initial conditions of the fluid initially occupying the volumic region of the computational domain identified by *volume-id-int* if *type-str* is set to Fluid.

- PorousMedium
- InitialState

Next: InitialState, Up: VolumeData

4.7.1.1 SPECIFYING THE PROPERTIES OF A POROUS MEDIUM

Object: PorousMedium

The PorousMedium object specifies the porosity properties of a volume that is identified by its id number and declared a porous medium. In this volume, the fluid flow is described by a generalized momentum equation based on the Brinkman-Forchheimer-Extended Darcy model. Essentially, the following sink term

$$(\alpha_i |\mathbf{u}| + \beta_i)u_i$$

is added to the i^{th} momentum equation.

The nonlinear component in the above term is called the Forchheimer term. The linear component is the usual Darcy term.

For turbulence runs, the turbulence kinetic energy k and dissipation rate ϵ of the flow through the porous media are computed as follows:

$$k = (3/2) I_{dr}^2 |{\bf u}|^2$$

$$\epsilon = \frac{C_{\mu}^{3/4} k^{3/2}}{L_{dr}}$$

where, I_{dr} and L_{dr} are user-supplied coefficients representing the average turbulence intensity and length scale respectively, and $C_{\mu}=0.09$. Using these values of k and ϵ , the eddy viscosity $\nu_t=C_{\mu}k^2/\epsilon$ is computed.

The syntax of this object is:

```
under PorousMedium {
      Ix = ix-real;
      Iy = iy-real;
      Iz = iz-real;
      Jx = jx-real;
      Jy = jy-real;
      Jz = jz-real;
      Kx = kx-real;
      Ky = ky-real;
      Kz = kz-real;
      Alphax = alphax-real;
      Alphay = alphay-real;
      Alphaz = alphaz-real;
      Betax = betax-real;
      Betay = betay-real;
      Betaz = betaz-real;
      Idr = idr-real;
      Ldr = 1dr-real;
with
```

ix-real [1.0]:

The x-component of the x-axis of the local coordinate system.

iy-real [0.0]:

The y-component of the x-axis of the local coordinate system.

iz-real [0.0]:

The z-component of the x-axis of the local coordinate system.

jx-real [0.0]:

The x-component of the y-axis of the local coordinate system.

jy-real [1.0]:

The y-component of the y-axis of the local coordinate system.

jz-real [0.0]:

The z-component of the y-axis of the local coordinate system.

kx-real [0.0]:

The x-component of the z-axis of the local coordinate system.

ky-real [0.0]:

The y-component of the z-axis of the local coordinate system.

kz-real [1.0]:

The z-component of the z-axis of the local coordinate system.

alphax-real [0.0]:

Resistance coefficient of the Forchheimer term in the local x-direction. It has S.I. units of kg/m^4.

alphay-real [0.0]:

Resistance coefficient of the Forchheimer term in the local y-direction. It has S.I. units of kg/m^4.

alphaz-real [0.0]:

Resistance coefficient of the Forchheimer term in the local z-direction. It has S.I. units of kg/m^4.

betax-real [0.0]:

Resistance coefficient of the Darcy term in the local x-direction. It has S.I. units of kg/m³/s.

betay-real [0.0]:

Resistance coefficient of the Darcy term in the local y-direction. It has S.I. units of kg/m³/s.

betaz-real [0.0]:

Resistance coefficient of the Darcy term in the local z-direction. It has S.I. units of kg/m³/s.

idr-real [0.01]:

Coefficient representing average turbulent intensity in the porous media. This is used to compute the turbulence kinetic energy k.

ldr-real [0.1]:

Coefficient representing the length scale of turbulence in the porous media (~0.1 times a characteristic passage dimension). This is used to compute the turbulence dissipation rate .

Notes:

- 1. currently, flow through a porous medium is supported only when the fluid is modeled as a perfect gas in the remainder of the computational domain;
- 2. currently, turbulence through a porous medium is supported only when a RANS turbulence model is selected for the remainder of the computational domain.

Next: ProgrammedBurn, Previous: PorousMedium, Up: VolumeData

4.7.1.2 SPECIFYING AN INITIAL STATE FOR A MULTI-FLUID COMPUTATION

```
Object: InitialState
```

In the context of a multi-fluid flow problem, this object can be used to specify the parameters of a uniform initial state in a region of the computational domain identified outside this object. Its syntax is:

```
under InitialState {
       Mach = mach-real;
       Velocity = velocity-real;
       Alpha = alpha-real;
       Beta = beta-real;
       Density = density-real;
       Pressure = pressure-real;
       Temperature = temperature-real;
with
mach-real [—]:
      Initial Mach number. To be specified only if the velocity magnitude is not specified.
velocity-real [—]:
      Initial velocity magnitude. To be specified only if the Mach number is not specified.
alpha-real [—]:
      Initial angle of attack.
beta-real [—]:
      Initial yaw angle.
density-real [—]:
```

Initial density. Needs to be specified for a perfect gas, stiffened gas, and a fluid modeled by the JWL equation of state. For a barotropic liquid, this parameter needs to be specified only if no pressure value is specified (it

is discarded if a pressure value is simultaneously specified).

```
pressure-real [—]:
```

Initial density. Needs to be specified for a perfect gas, stiffened gas, and a fluid modeled by the JWL equation of state. For a barotropic liquid, this parameter needs to be specified only if no density value is specified.

```
temperature-real [—]:
```

Initial temperature. Needs to be specified only for a barotropic liquid. It is discarded if it is specified for any other fluid.

Previous: InitialState, Up: VolumeData

4.7.1.3 SPECIFYING THE PARAMETERS OF A PROGRAMMED BURN

```
Object: ProgrammedBurn
```

The ProgrammedBurn object specifies the parameters of a programmed burn of a highly explosive material located within a region specified by a geometrical object (see <u>Box</u>, <u>Sphere</u>) of **AERO-F**. Its syntax is:

```
under ProgrammedBurn {
     IgnitionX0 = ignition-x0-real;
     IgnitionY0 = ignition-y0-real;
     IgnitionZ0 = ignition-z0-real;
     E0 = detonation-energy-real;
     ChapmanJouguetDensity = cj-density-real;
     ChapmanJouguetPressure = cj-pressure-real;
     ChapmanJouguetDetonationVelocity = cj-detonation-speed-real;
     BurnedEOS = burned-fluidID-int;
     UnburnedEOS = unburned-fluidID-int;
     IgnitionTime = ignition-time-real;
     Ignite = ignite-flag;
with
ignition-x0-real [0.0]:
      x-coordinate of the ignition point.
ignition-y0-real [0.0]:
      y-coordinate of the ignition point.
ignition-z0-real [0.0]:
      z-coordinate of the ignition point.
detonation-energy-real [—]:
```

Initial internal energy of the explosive material (prior to detonation).

cj-density-real [-1.0]:

Chapman-Jouguet density of the explosive material behind the detonation wave (just after detonation). If not provided (by default), **AERO-F** automatically computes the value of *cj-density-real*.

cj-pressure-real [-1.0]:

Chapman-Jouguet pressure of the explosive material behind the detonation wave (just after detonation). If not provided (by default), **AERO-F** automatically computes the value of *cj-pressure-real*.

cj-detonation-speed-real [-1.0]:

Chapman-Jouguet speed of the detonation wave. If not provided (by default), **AERO-F** automatically computes the value of *cj-denotation-speed-real*.

burned-fluidID-int [—]:

Integer ID of the fluid medium representing the burned explosive products.

unburned-fluidID-int [—]:

Integer ID of the fluid medium representing the unburned explosive.

ignition-time-real [0.0]:

Time at which the explosive material is ignited.

ignite-flag [True]:

True

In this case, the explosive material is ignited.

False

In this case, the explosive material is not ignited during the simulation. A typical usage of this option would be during the restarting of a three-dimensional simulation that involved a programmed burn.

Next: Equations, Previous: Volumes, Up: Objects

4.8 DEFINING THE REFERENCE STATE

Object: ReferenceState

The ReferenceState object allows to specify some of the quantities used for non-dimensionalizing the governing equations. Its syntax is:

```
under ReferenceState {
    Density = density-real;
    Temperature = temp-real;
    Reynolds = reynolds-real;
    Length = length-real;
    Mach = mach-real;
}
with density-real [—];
```

Reference density (required for simulations with variations of boundary conditions in time. See <u>BoundaryConditions</u>). If it is not specified it is set internally to the boundary value.

```
temp-real [—]:
```

Reference temperature (required for non-dimensional viscous simulations with the Sutherland viscosity model).

```
reynolds-real [—]:
```

Reynolds number (required for non-dimensional viscous simulations).

```
length-real [1.0]:
```

Reference length which is used to non-dimensionalize the mesh. The Reynolds number is based on this length.

```
Mach-real [—]:
```

Reference Mach number. Specifying a reference Mach number can be useful, for example, if the inlet Mach number is zero as in a shock-tube problem.

Note:

1. the reference state conditions that cannot be specified by this command but are perceived needed for the flow computation are set internally by the code to the corresponding boundary values.

Next: MultiPhase, Previous: ReferenceState, Up: Objects

4.9 DEFINING THE EQUATIONS TO BE SOLVED

Object: Equations

The Equations object defines the type of equations to be solved. Its syntax is:

```
under Equations {
  Type = type-id;
  GravityX = gravityx-real;
  GravityY = gravityy-real;
```

```
GravityZ = gravityz-real;
under FluidModel[fluid-id-int] { ... }
under ViscosityModel { ... }
under TurbulenceClosure { ... }
}
with
type-id [Euler]:
```

Euler

Inviscid flow simulation based on the compressible Euler equations.

NavierStokes

Viscous flow simulation based on the compressible Navier-Stokes equations.

Note that for fluids other than perfect gases, the only possible type is Euler.

```
gravityx-real [0.0]:
```

Value of the gravity field in the x-direction, if any.

```
gravityy-real [0.0]:
```

Value of the gravity field in the y-direction, if any.

```
gravityz-real [0.0]:
```

Value of the gravity field in the z-direction, if any.

FluidModel:

Defines the properties of the fluid in a single-phase flow problem. The corresponding syntax is defined in the *FluidModel* object (see <u>FluidModel</u>).

```
fluid-id-int[—]
```

Integer identifier of a fluid medium.

ViscosityModel:

Specifies the viscosity model to be used in a viscous flow problem.

TurbulenceClosure:

Specifies the turbulence model as either a RANS or LES model.

- FluidModel
- ViscosityModel
- <u>TurbulenceClosure</u>

Next: ViscosityModel, Up: Equations

4.9.1 SPECIFYING A FLUID MODEL

```
Object: FluidModel
```

The object FluidModel[fluid-int], where fluid-int is an integer identifying a fluid medium, can be used to specify an equation of state (EOS) for this medium and its parameters. The user can choose between the EOS of a perfect gas, stiffened gas, Tait's EOS which typically models a compressible barotropic liquid, and the Jones-Wilkins-Lee (JWL) EOS which typically models a highly explosive gas. Currently, viscous effects are implemented only for a perfect gas. The syntax of these objects is:

```
under FluidModel[fluid-id-int] {
  Fluid = fluidtype-id;
  PressureCutOff = pressurecutoff-real;
  under GasModel { ... }
  under LiquidModel { ... }
  under JWLModel { ... }
}
```

fluid-id-int [0]:

with

Integer number identifying a fluid medium. When the problem involves a single fluid, *fluid-id-int* must be set to 0 (which is done by default). When it involves multiple fluids, *fluid-id-int* must be assigned in a consecutive manner (no gap) starting with 0. **AERO-F** can handle a multi-fluid problem with an arbitrary number of fluid media. However, **AERO-F** can currently handle only three different fluid-fluid interfaces which furthermore must be between a same fluid — referred to in this User's Reference Manual as the "primary" fluid — and any one of three other fluids. In this case, the primary fluid must be identified by *fluid-id-int* = 0.

fluidtype-id [PerfectGas]:

PerfectGas

The fluid is modeled as a perfect gas.

StiffenedGas

The fluid is modeled as a stiffened gas.

Liquid

The fluid is modeled as a barotropic liquid governed by Tait's EOS.

JWL

The fluid is modeled as a highly explosive gas governed by the Jones-Wilkins-Lee EOS.

pressurecutoff-real [0.0]:

Lower threshold for the pressure. This limit value of the pressure can be used to avoid artificial cavitation due

to discretization error for a given EOS. Essentially, if the computed value of the pressure field becomes lower than the specified threshold value, it is set to the specified threshold value. The dimensional or non-dimensional mode of this parameter should be consistent with the mode of the simulation (see <u>Problem</u>).

GasModel:

Specifies the parameters of a perfect or stiffened gas.

LiquidModel:

Specifies the model for a compressible liquid and its parameters.

JWLModel:

Specifies the model for a highly explosive gas and its parameters.

- GasModel
- LiquidModel
- JWLModel

Next: LiquidModel, Up: FluidModel

4.9.1.1 SPECIFYING THE EQUATION OF STATE OF A PERFECT OR STIFFENED GAS

```
Object: GasModel
```

The GasModel object is currently restricted to perfect and stiffened gases. Its syntax is:

```
under GasModel {
   SpecificHeatRatio = gamma-real;
   IdealGasConstant = R-real;
   PressureConstant = psg-real;
}
```

with

gamma-real [1.4]:

Ratio of specific heats.

R-real [287.1]:

Ideal gas constant. It is used by **AERO-F** only in dimensional simulations for which temperature output is requested, in which case it must be specified in the same system of units as all other input data (in the SI system of units, its value is equal to 287.1 m²/s²/K).

psg-real [0.0]:

Stiffened gas pressure constant expressed in pressure units consistent with the system of units used by all other input data.

Notes:

- 1. if the temperature is to be outputted and/or Sutherland's viscosity model is used, pay special attention to the consistency between the units of *R-real* and those of the remainder of the input data;
- 2. the stiffened gas model is a generalization of the ideal gas model given by

$$p = (\gamma - 1)\rho\epsilon - \gamma p_{sg}$$

where p denotes pressure, γ is the ratio of specific heats, ρ is the density, ϵ is the internal energy per unit mass, and p_{sg} is a pressure constant representing, in the case of water, the molecular attraction between water molecules.

Next: JWLModel, Previous: GasModel, Up: FluidModel

4.9.1.2 SPECIFYING TAIT EQUATION OF STATE

Object: LiquidModel

The LiquidModel object is currently restricted to barotropic fluids that can be modeled with Tait's equation of state (EOS)

$$p = p_c + \alpha \rho^{\beta}$$
$$p(\rho_0) = p_0$$

which further assumes that the bulk modulus K is an affine function of the pressure

$$K = \rho \frac{dp}{d\rho} = k_1 + k_2 p$$

In the above equations, p_c and β are two constants that are determined from the knowledge of the two other constants

 $\overline{k_1}$ and $\overline{k_2}$ of the second equation as follows

$$p_c = -\frac{k_1}{k_2} \qquad \beta = k_2$$

The third constant α is determined from the additional knowledge of a reference state (ρ_0,p_0)

as follows

 $\alpha = \frac{p_0 + \frac{k_1}{k_2}}{\rho_0^{k_2}}$

The syntax of this object is:

```
under LiquidModel {
  Cv = Cv-real;
  k1 = k1-real;
  k2 = k2-real;
  Pressure = pressure-real;
  Density = density-real;
}
```

with

Cv-real [—]:

Specific heat at constant volume. If expressed in S.I. units, this constant is proportional to J/K/kg. It can be found in thermodynamic tables.

kl-real [2.07e9]:

One of the two constants defining the behaviour of the bulk modulus. If expressed in S.I. units, this constant is proportional to kg/m/s^2. For example, its value for water is 2.07e9 kg/m/s^2.

k2-real [7.15]:

Second constant defining the behaviour of the bulk modulus. This constant has no unit. For water, its value is 7.15.

pressure-real [—]:

The "reference" pressure must be chosen in agreement with the "reference" density. If expressed in S.I. units, it is proportional to kg/m/s^2. It can be found in thermodynamic tables.

density-real [—]:

The "reference" density must be chosen in agreement with the "reference" pressure. If expressed in S.I. units, it is proportional to kg/m³. It can be found in thermodynamic tables.

Notes:

- 1. the "reference" pressure, "reference" density and specific heat at constant volume are not independent and must correspond to a physical state. The user can set these constants by looking at thermodynamic tables.
- 2. it is best to set the "reference" pressure, "reference" density and specific heat at constant volume close to the values of pressure, density and specific heat at constant volume at the far-field.

Previous: LiquidModel, Up: FluidModel

4.9.1.3 SPECIFYING THE JWL EQUATION OF STATE

Object: **JWLModel**

This object can be used to specify the parameters of the Jones-Wilkins-Lee equation of state (EOS) which can be written as

$$p = \omega \rho \epsilon - A_1 \left(1 - \frac{\omega \rho}{R_1 \rho_0} \right) e^{-\frac{R_1 \rho_0}{\rho}} - A_2 \left(1 - \frac{\omega \rho}{R_2 \rho_0} \right) e^{-\frac{R_2 \rho_0}{\rho}}$$

where p denotes the pressure of the fluid medium, ρ its density, ϵ its internal energy per unit mass, ω is a non-dimensional constant, A_1 and A_2 are two constants with pressure units, R_1 and R_2 are two non-dimensional constants, and ρ_0 is a constant with a density unit.

The syntax of this object is:

```
under JWLModel {
  Omega = omega-real;
  A1 = a1-real;
  R1 = r1-real;
  A2 = a2-real;
  R2 = r2-real;
  ReferenceDensity = referencedensity-real;
}
```

with

omega-real[0.4]

First constant defining the behavior of the JWL EOS. It is non-dimensional.

a1-real[0.0]

Second constant defining the behavior of the JWL EOS. It has the dimension of a pressure. Hence, if expressed in S.I. units, it is proportional to kg/m/s^2.

r1-real[1.0]

Third constant defining the behavior of the JWL EOS. It is non-dimensional.

a2-real[0.0]

Fourth constant defining the behavior of the JWL EOS. It has the dimension of a pressure. Hence, if expressed in S.I. units, it is proportional to kg/m/s^2.

r2-real[1.0]

Fifth constant defining the behaviour of the JWL EOS. It is non-dimensional.

referencedensity-real[1.0]

Last constant defining the behaviour of the JWL EOS. It has the dimension of a density. Hence, if expressed in S.I. units, it is proportional to kg/m³.

Next: <u>TurbulenceClosure</u>, Previous: <u>FluidModel</u>, Up: <u>Equations</u>

4.9.2 SPECIFYING THE VISCOSITY MODEL

Object: ViscosityModel

The available viscosity laws are defined within the ViscosityModel object. Its syntax is:

```
under ViscosityModel {
  Type = type-id;
  SutherlandReferenceTemperature = temp-real;
  SutherlandConstant = cst-real;
}
```

with

type-id [Sutherland]:

Sutherland

Sutherland's viscosity law. For gases, a widely used formula is

$$\mu = \frac{\mu_0 \sqrt{T}}{1 + T_0/T}$$

where Sutherland's constants $\,\mu_0\,$ and $\,T_0\,$ are defined below.

Constant

Constant viscosity law:

$$\mu=\mu_{\infty}=rac{\mu_{\mathrm{D}}\sqrt{T_{\mathrm{DO}}}}{1+T_{\mathrm{D}}/T_{\mathrm{DO}}}$$

where Sutherland's constants μ_0 and T_0 are defined below. For example, when performing a dimensional simulation and using this model, these constants can be adjusted to reach a specific Reynolds number.

temp-real [110.6]:

Sutherland's reference temperature $T_{
m 0}$

Expressed in S.I. units, it is equal to 110.6 K for air.

```
cst-real [1.458e-6]:
```

Sutherland's constant μ_0 .

Expressed in S.I. units, it is equal to 1.458e-6

Kg/msK ½

for air.

Note:

1. pay special attention to the consistency of the units of *cst-real*, *R-real* (see <u>GasModel</u>), and the units of the remainder of the input files(s).

Previous: ViscosityModel, Up: Equations

4.9.3 SPECIFYING THE TURBULENCE CLOSURE

Object: TurbulenceClosure

For viscous flow simulations, the type of turbulence closure is defined within the TurbulenceClosure object. Its syntax is:

```
under TurbulenceClosure {
  Type = type-id;
  PrandtlTurbulent = coefficient-real;
  under TurbulenceModel { ... }
  under LESModel { ... }
  under Tripping{ ... }
}
```

with

type-id [None]:

None

The compressible Navier-Stokes equations are solved without any additional model.

TurbulenceModel

The averaged compressible Navier-Stokes equations are solved with an eddy viscosity turbulence model (see <u>TurbulenceModel</u>).

LESModel

The compressible Navier-Stokes equations are solved with a large eddy simulation model (see <u>LESModel</u>).

coefficient-real [0.9]:

Subgrid-scale Prandtl number which is assumed to be constant.

TurbulenceModel:

Speficies the eddy viscosity model to be used in the computation.

LESModel:

Specifies the LES model to be used in the computation.

Tripping:

Specifies the box within the computational domain in which the turbulence model is to be used.

- TurbulenceModel
- <u>LESModel</u>
- Tripping

Next: LESModel, Up: TurbulenceClosure

4.9.3.1 SPECIFYING THE EDDY VISCOSITY MODEL

```
Object: TurbulenceModel
```

For turbulent flow simulations based on the averaged Navier-Stokes equations augmented by an eddy viscosity model, the type of the turbulence model is defined within the TurbulenceModel object. Its syntax is:

```
under TurbulenceModel {
  Type = type-id;
}
```

with

type-id [SpalartAllmaras]:

SpalartAllmaras

One-equation Spalart-Allmaras turbulence model.

DES

Detached eddy simulation model based on Spalart-Allmaras' model. See Appendix C for a description of the mesh requirements (see <u>DES</u>).

KEpsilon

Two-equation $k - \epsilon$ turbulence model.

Next: Tripping, Previous: TurbulenceModel, Up: TurbulenceClosure

4.9.3.2 SPECIFYING THE LES MODEL

Object: **LESModel**

For turbulent flow simulations based on the Navier-Stokes equations augmented by a large eddy simulation model, the type of the LES model is defined within the LESModel object. Its syntax is:

```
under LESModel {
  Type = type-id;
  Delta = delta-id;
  under Smagorinsky { ... }
  under Dynamic { ... }
  under VMS { ... }
  under DynamicVMS { ... }
  under WALE { ... }
}
```

with

type-id [VMS]:

Smagorinsky

The classical filtering and Smagorinsky Eddy Viscosity model are used to separate the coarse and fine-scales and model the effect of the latter.

Dynamic

The classical filtering and variable-constant (obtained using the Germano Identity) Smagorinksy Eddy Viscosity model is used to separate the coarse and fine scales, and model the effect of the latter on the coarse scales.

VMS

The variational multiscale approach is used to separate the large and small resolved scales and to model the effect of the unresolved scales in the small resolved scales equation using a Smagorinksy Eddy Viscosity model.

DynamicVMS

The VMS method is equipped with a variational analogue of the Germano identity to compute a variable constant in the Smagorinksy Eddy Viscosity model.

WALE

The Wall-Adapting Local Eddy Viscosity (WALE) model is used for the eddy-viscosity.

delta-id [Volume]:

Volume

In this case, for a given tetrahedron T_l , the filter width Δ used to compute the eddy viscosity is set to

 $\Delta = Vol(T_l)^{1/3}$

Side

In this case, for a given tetrahedron $|\mathbf{T}_l|$, the filter width $|\Delta|$

used to compute the eddy viscosity is set to the size of the largest side of this tetrahedron.

Smagorinsky:

Specifies the classical filtering and Smagorinsky Eddy Viscosity model for separating the coarse and fine-scales and modeling the effect of the latter.

Dynamic:

Specifies the classical filtering and variable-constant (obtained using the Germano Identity) Smagorinsky Eddy Viscosity model for separating the coarse and fine-scales and modeling the effect of the latter on the coarse scales.

VMS:

Specifies the variational multiscale approach for separating the large and small resolved scales and modeling the effect of the unresolved scales in the small resolved scales equation using a Smagorinksy Eddy Viscosity model.

DynamicVMS:

Specifies the VMS method equipped with a variational analogue of the Germano identity to compute a variable constant in the Smagorinksy Eddy Viscosity model.

WALE:

Specifies the Wall-Adapting Local Eddy Viscosity (WALE) model for representing the eddy-viscosity.

- Smagorinsky
- Dynamic
- VMS
- DynamicVMS
- WALE

Next: WALE, Up: LESModel

4.9.3.2.1 SPECIFYING THE PARAMETERS OF THE SMAGORINSKY EDDY VISCOSITY MODEL

Object: Smagorinsky

The Smagorinsky object specifies the parameters of the Smagorinsky LES model. Its syntax is:

under Smagorinsky{
 Cs = coefficient-real;

}

with

coefficient-real [0.1]:

Usual Smagorinsky coefficient C_s used in computing the eddy viscosity

$$\nu_T = (C_s \Delta)^2 \sqrt{2S_{ij}S_{ij}}$$

Next: Dynamic, Previous: Smagorinsky, Up: LESModel

4.9.3.2.2 SPECIFYING THE PARAMETERS OF THE WALL-ADAPTED LOCAL EDDY VISCOSITY MODEL

Object: WALE

The WALE object specifies the parameters of the WALE LES model. Its syntax is:

```
under WALE{
  Cw = coefficient-real;
}
```

with coefficient-real [0.325]:

WALE coefficient $\left|C_w\right|$ used in computing the eddy viscosity

$$u_t = rac{\overline{
ho} (\mathcal{C}_w riangle)^2 (S^d_{ij} S^d_{ij})^{3/2}}{(S_{ij} S_{ij})^{5/2} + (S^d_{ij} S^d_{ij})^{5/4}}$$

where S_{ij}^d is the symmetric part of the square of the velocity gradient tensor and S_{ij} is the deformation tensor of the resolved field.

Next: VMS, Previous: WALE, Up: LESModel

4.9.3.2.3 SPECIFYING THE PARAMETERS OF THE DYNAMIC LES MODEL

Object: **Dynamic**

The Dynamic object specifies the parameters of Germano's dynamic LES model. Its syntax is:

```
under Dynamic{
  under Clipping { ... }
}
```

with

Clipping

The upper bound for the C_s coefficient and upper and lower bounds for the turbulent Prandtl number Pt can be specified in this object.

• ClippingDynamic

Up: **Dynamic**

4.9.3.2.3.1 SPECIFYING BOUNDS FOR THE DYNAMIC LES MODEL



The Clipping object specifies the upper bound for the C_s coefficient and the upper and lower bounds for the turbulent Prandtl number Pt in Germano's dynamic LES model.

Its syntax is:

```
under Clipping{
  CsMax = coefficient-real1;
  PtMin = coefficient-real2;
  PtMax = coefficient-real3;
}
```

with coefficient-real1 [0.4]:

This value mulitplied by the filter width Delta is used as a clipping upper bound for the dynamically evaluated $C_s\Delta$ products.

coefficient-real2 [0.5]:

This serves as a clipping lower bound for the dynamically evaluated Prandtl numbers Pt.

coefficient-real3 [1.6]:

This serves as a clipping upper bound for the dynamically evaluated Prandtl numbers Pt.

Next: DynamicVMS, Previous: Dynamic, Up: LESModel

4.9.3.2.4 SPECIFYING THE PARAMETERS OF THE VMS TURBULENCE MODEL



The VMS object specifies the parameters of the variational multiscale LES model. Its syntax is:

under VMS{

```
Csprime = coefficient-real;
AgglomerationLayer= layer-integer;
AgglomerationDepth = depth-integer;
}
with
coefficient-real [0.1]:
```

Fine-scale Smagorinsky coefficient C_s' used in computing the eddy viscosity

$$\nu_T' = (C_s' \Delta)^2 \sqrt{2S_{ij}' S_{ij}'}$$

layer-integer [1]:

Characterizes the size of a macro-cell in an agglomeration. A value of 1 results in each macro-cell containing a cell and (a subset of) its neighbors. A value of 2 results in each macro-cell containing a cell, (a subset of) its neighbors, and (a subset of) the neighbors of these neighbors, etc...

depth-integer [1]:

This is the number of recursive clustering steps to be performed for generating the agglomeration used for constructing the projector of the VMS-LES method.

Previous: VMS, Up: LESModel

4.9.3.2.5 SPECIFYING THE PARAMETERS OF THE DYNAMIC VMS LES MODEL

```
Object: DynamicVMS
```

The DynamicVMS object specifies the parameters of the dynamic variational multiscale LES model. Its syntax is:

```
under DynamicVMS{
    Type = type-id;
    Csprime = csprime-real;
    AgglomerationLayer= layer-integer;
    AgglomerationDepth1= depth-integer1;
    AgglomerationDepth2= depth-integer2;
    under Clipping { ... }
}
with

type-id [D1VMSLES]:
```

A Dynamic VMS-LES method based on the "difference" variational analogue of Germano's identity (and

therefore closest to the original version of Germano's identity). Here, the Smagorinsky subgrid-scale parameters are solved for dynamically by employing least-squares on the equations obtained by differencing the conservation equations associated with two different grid sizes.

D2VMSLES

A robust Dyamic VMS-LES method which resorts to the least-squares solution of the "stacked" conservation equations associated with two different grid sizes to compute the Smagorinsky subgrid-scale parameters dynamically.

csprime-real [0.1]:

Fall-back fine-scale Smagorinsky coefficient adopted when the computed dynamic constant falls outside the interval [0, 0.3].

layer-integer [1]:

Characterizes the size of a macro-cell in an agglomeration. A value of 1 results in each macro-cell containing a cell and (a subset of) its neighbors. A value of 2 results in each macro-cell containing a cell, (a subset of) its neighbors, and (a subset of) the neighbors of these neighbors, etc...

depth-integer 1 [1]:

This is the number of recursive clustering steps to be performed for constructing the first-level agglomeration — that is, the agglomeration used for constructing the basic projector of the dynamic VMS-LES method.

depth-integer2 [depth-integer1 + 1]:

This is the number of recursive clustering steps to be performed for constructing the second-level agglomeration — that is, the agglomeration used for constructing the projector used in the variational analogue of the Germano identity in the dynamic VMS-LES method.

Clipping

The upper bound for the C_s' coefficient and upper and lower bounds for the turbulent Prandtl number Pt' can be specified in this object.

• ClippingDynamicVMS

Up: DynamicVMS

4.9.3.2.5.1 SPECIFYING BOUNDS FOR THE DYNAMIC VMS TURBULENCE MODEL

Object:	Clipping
---------	----------

The Clipping object specifies the upper bound for the C_s^\prime coefficient and the upper and lower bounds for the

turbulent Prandtl number Pt' in the dynamic VMS turbulence model.

Its syntax is:

```
under Clipping{
  CsMax = coefficient-real1;
  PtMin = coefficient-real2;
  PtMax = coefficient-real3;
}
```

with *coefficient-real1* [0.4]:

This value mulitplied by the filter width Delta is used as a clipping upper bound for the dynamically evaluated $C_s'\Delta'$ products.

coefficient-real2 [0.5]:

This serves as a clipping lower bound for the dynamically evaluated Prandtl numbers Pt^{\prime} .

coefficient-real3 [1.6]:

This serves as a clipping upper bound for the dynamically evaluated Prandtl numbers $\left|Pt'\right|$.

4.9.3.3 TRIPPING TURBULENCE

Previous: LESModel, Up: TurbulenceClosure

Object: Tripping

Turbulence can be tripped by specifying a domain outside which the turbulent eddy viscosity is set to zero to model a laminar flow. The syntax of this command is:

```
under Tripping {
  under Box1 { ... }
}
```

Box1:

Defines a box within the computational domain (see **BoxFix**).

Next: Boundary Conditions, Previous: Equations, Up: Objects

4.10 DEFINING THE MULTI-PHASE COMPONENT OF A FLOW PROBLEM AND SPECIFYING ITS SOLUTION METHOD

Object: MultiPhase

The MultiPhase object is used to define a multi-phase flow problem or problem component and choose a multi-phase flow solver. The material interface is assumed to be well approximated by a free surface where one fluid can only apply a pressure on the other fluid, and to be initially a closed contact surface. The available multi-phase flow solvers are based either on the ghost fluid method, or on the finite volume method with exact, local, two-phase Riemann solvers. The level set technique is used for capturing the material interface.

The syntax of this object is:

```
under MultiPhase{
  LevelSetReinitializationFrequency = lsreinitfreq-int;
  PhaseChange = phasechange-str;
  Method = method-str;
  RiemannComputation = riemanncomputation-str;
  under SparseGrid{ ... }
  under InitialConditions { ... }
}
```

with

lsreinitfreq-int [0]:

Specifies the reinitialization frequency for the computation of the level set function(s). (By default, the computation of the level set function(s) is not reinitialized. Furthermore, for one-dimensional computations, it is not reinitialized either).

method-str [GhostFluidForThePoor]:

GhostFluidForThePoor

In this case, the level set method is used to capture the interface, and the multi-phase flow equations are solved by the "Ghost Fluid method for the Poor". This option can be used when running gas-gas simulations, where gas is a perfect or stiffened gas. It can also be used for solving liquid-liquid multi-phase problems if all liquids are assumed to be barotropic and are modeled by Tait's equation.

FiniteVolumeWithExactTwoPhaseRiemann

In this case, the level set method is used to capture the interface, and the multi-phase flow equations are solved by the finite volume method with exact, local, two-phase Riemann solvers. This option can be used to solve fluid-fluid problems where either fluid can be modeled as a perfect gas, stiffened gas, barotropic liquid (Tait's equation of state), or by the JWL equation of state. It is particularly useful when simulating fluid-fluid problems characterized by large contact discontinuities across the interfaces.

phasechange-str[RiemannSolution]:

This parameter is relevant only when *method-str* is set to FiniteVolumeWithExactTwoPhaseRiemann.

None

No special numerical treatment is applied to the state of a node that changes phase from one time-step to the following one.

RiemannSolution

One of the two interface states obtained by the solution of the appropriate Riemann problem is used to replace the state of a node that changes phase from one time-step to the following one.

Extrapolation

An extrapolation procedure is used to populate the state of a node that changes phase from one time-step to the following one.

riemanncomputation-str[SecondOrder]:

This parameter is relevant only when the multi-phase flow problem involves an interface between two media where at least one of them is modeled by the JWL equation of state and applies to this interface only.

FirstOrder

The Riemann invariants of the relevant Riemann problem are numerically computed using a first-order ODE integrator.

SecondOrder

The Riemann invariants of the relevant Riemann problem are numerically computed using a second-order ODE integrator.

TabulationRiemannInvariant

When Problem. Type is set to anything but SparseGridGeneration (see <u>Problem</u>), this option, which is highly recommended in this case because of its computational efficiency, requests the exploitation of a sparse grid tabulation to interpolate the values of the Riemann invariants of the relevant Riemann problem. This tabulation is specified in <u>SparseGrid</u>. On the other hand when Problem. Type is set to SparseGridGeneration (see <u>Problem</u>), this option specifies that the Riemann invariants are to be tabulated in a sparse grid according to the parameters specified in the <u>SparseGrid</u>.

TabulationRiemannProblem

When Problem. Type is set to anything but SparseGridGeneration (see <u>Problem</u>), this option requests the exploitation of a sparse grid tabulation to interpolate directly the solutions of the relevant Riemann problems. This tabulation is specified in <u>SparseGrid</u>. On the other hand when Problem. Type is set to SparseGridGeneration (see <u>Problem</u>), this option specifies that the solutions of the Riemann problems are to be tabulated in a sparse grid according to the parameters specified in the <u>SparseGrid</u>.

InitialConditions:

Defines the regions occupied by two fluids by initializing the level set function(s), and sets the initial conditions of each fluid in its region of the computational domain.

Note:

- currently, AERO-F can handle only three different fluid-fluid interfaces which furthermore must be between
 a same fluid referred to in this User's Reference Manual as the "primary" fluid and any one of three
 other fluids. In this case, the primary fluid must be identified in <u>FluidModel</u> by *fluid-id-int* = 0.
- SparseGrid
- InitialConditionsMultiPhase

Next: SparseGrid, Up: MultiPhase

4.10.1 SPECIFYING THE INITIAL CONDITIONS OF A MULTI-PHASE FLOW COMPUTATION

Object: InitialConditions

The level set function and the state of each fluid of a multi-phase flow computation are initialized using this object. The initialization of each level set function is performed by specifying the geometry of a surface that separates initially two fluids. Within the region it occupies, the state of each fluid is initialized to a uniform flow whose parameters are specified in this object.

The syntax of the InitialConditions object is:

```
under InitialConditions {
    under Sphere[sphere-id-int] { ... }
    ...
    under Plane[plane-id-int] { ... }
    ...
    under Box[box-id-int] { ... }
}
with

sphere-id-int[—]

ID number of a sphere.

plane-id-int[—]
```

ID number of a plane.

box-id-int[—]

ID number of a box.

Sphere:

Defines a geometric sphere and the initial conditions for the flow within (see **Box**).

Plane:

Defines a geometric plane and the initial conditions for the flow within the region of the computational domain it implies (see <u>Plane</u>).

^ Box:

Defines a geometric box and the initial conditions for the flow within the region of the computational domain it implies (see <u>Box</u>).

Notes:

- the <u>VolumeData</u> object offers the possibility to initialize the states of two fluids separated by rigid or flexible walls. The user is allowed to specify initial conditions using both the VolumeData object and the present object.
- 2. AERO-F initializes the solution of a multi-phase flow problem in several overwriting steps as follows: first, the states of all grid points are initialized to the values of the free-stream conditions; next, the states of all grid points belonging to a specific set of volume IDs are initialized as specified in the associated VolumeData object; next, the states of all grid points in each region of the computational domain implied by each plane specified in Plane[plane-id-int] are initialized as requested in the corresponding InitialConditions object; finally, the states of all grid points located inside each sphere specified in Box[sphere-id-int] are initialized as requested in the corresponding InitialConditions object.
- Sphere
- Plane
- Box

Next: Plane, Up: InitialConditionsMultiPhase

4.10.1.1 DEFINING A GENERIC SPHERE FOR A MULTI-PHASE FLOW COMPUTATION

```
Object: Sphere
```

The Sphere object (with an integer number appended to the last letter of this word) specifies the location and size of a spherical region, as well as the initial condition parameters for the flow inside this region. The syntax of this object is:

```
under Sphere[sphere-id-int] {
  FluidID = fluid-id-int;
  Center_x = center_x-real;
  Center_y = center_y-real;
  Center_z = center_z-real;
  Radius = radius-real;
  under InitialState{ ... }
  under ProgrammedBurn{ ... }
}
```

with *sphere-id-int*[—]

Integer identification number of the sphere defined in this object.

fluid-id-int [—]:

ID of the fluid medium for which the initial conditions specified in this sphere apply to.

 $center_x$ -real [0.0]:

Coordinate of the center of the sphere along the x axis.

```
center_y-real [0.0]:
```

Coordinate of the center of the sphere along the y axis.

```
center_z-real [0.0]:
```

Coordinate of the center of the sphere along the z axis.

```
radius-real [—]:
```

Radius of the sphere.

InitialState:

Specifies the initial state of the fluid occupying the sphere defined above.

ProgrammedBurn:

Specifies the parameters of a programmed burn of a highly explosive material located within the sphere defined above.

- InitialState
- ProgrammedBurn

Next: Box, Previous: Sphere, Up: InitialConditionsMultiPhase

4.10.1.2 DEFINING A GENERIC PLANE FOR A MULTI-PHASE FLOW COMPUTATION



The Plane object defines a plane by a point and a normal vector, and specifies the initial conditions in the region of the computational domain toward which the normal vector points to. The syntax of this object is:

```
under Plane[plane-id-int] {
    FluidID = fluid-id-int;
    Point_x = point_x-real;
    Point_y = point_y-real;
    Point_z = point_z-real;
    Normal_x = normal_x-real;
    Normal_y = normal_y-real;
    Normal_z = normal_z-real;
    under InitialState{ ... }
}
with

plane-id-int[—]
```

Integer identification number of the plane defined in this object.

```
fluid-id-int [—]:
```

ID of the fluid medium for which the initial conditions specified here apply to.

```
point_x-real [0.0]:
```

Coordinate of the point in the plane along the x axis.

```
point_y-real [0.0]:
```

Coordinate of the point in the plane along the y axis.

```
point_z-real [0.0]:
```

Coordinate of the point in the plane along the z axis.

```
normal\_x-real [0.0]:
```

Component of the normal to the plane along the x axis.

```
normal\_y-real [0.0]:
```

Component of the normal to the plane along the y axis.

```
normal_z-real [0.0]:
```

Component of the normal to the plane along the z axis.

InitialState:

Specifies the initial state of the fluid occupying the region of the computational fluid domain identified above.

• InitialState

Previous: Plane, Up: InitialConditionsMultiPhase

4.10.1.3 DEFINING A GENERIC BOX FOR A MULTI-PHASE FLOW COMPUTATION



The Box object (with an integer number appended to the last letter of this word) specifies the location and size of a boxy region, as well as the initial condition parameters for the flow inside this region. The syntax of this object is:

```
under Box[box-id-int] {
  FluidID = fluid-id-int;
  X0 = x0-real;
  Y0 = y0-real;
  Z0 = z0-real;
```

```
X1 = x1-real;
       Y1 = y1-real;
Z1 = z1-real;
        under InitialState{ ... }
       under ProgrammedBurn{ ... }
with box-id-int[—]
       Integer identification number of the box defined in this object.
fluid-id-int [—]:
      ID of the fluid medium for which the initial conditions specified in this box apply to.
x0-real [0.0]:
       x-coordinate of the lower left corner of the box.
y0-real [0.0]:
       y-coordinate of the lower left corner of the box.
z0-real [0.0]:
       z-coordinate of the lower left corner of the box.
x1-real [0.0]:
       x-coordinate of the upper right corner of the box with x1-real > x0-real.
y1-real [0.0]:
       y-coordinate of the upper right corner of the box with y1-real > y0-real.
z1-real [0.0]:
       z-coordinate of the upper right corner of the box with z1-real > z0-real.
InitialState:
       Specifies the initial state of the fluid occupying the box defined above.
```

ProgrammedBurn:

Specifies the parameters of a programmed burn of a highly explosive material located within the box defined above.

- InitialState
- ProgrammedBurn

Previous: InitialConditionsMultiPhase, Up: MultiPhase

4.10.2 TABULATING DATA IN SPARSE GRID FORMAT FOR SPEEDING UP MULTI-PHASE COMPUTATIONS

Object: SparseGrid

To accelerate the solution of flow problems involving a medium modeled by a complex and computationally intensive equation of state (EOS), the object SparseGrid offers the possibility of tabulating some data in sparse grid format (see TAB), or exploiting it when readily available. This data can be either the Riemann invariants along a characteristic curve, or the solutions of two-phase Riemann problems. When using this object to tabulate the solutions of two-phase Riemann problems, one fluid is assumed to be modeled by the JWL EOS and must be specified in FluidModel[0], and the other is assumed to be a perfect or stiffened gas and must be specified in FluidModel[1].

The syntax of this object is:

```
under SparseGrid {
       FileName = filename-str;
       NumberOfFiles = numfiles-int;
       Verbose = verbose-int;
       NumberOfInputs = numinputs-int;
       NumberOfOutputs = numoutputs-int;
       Input1Minimum = in1min-real;
       Input1Maximum = in1max-real;
       NumberOfDomains1 = numdomains1-int;
       Input6Minimum = in6min-real:
       Input6Maximum = in6max-real;
       NumberOfDomains6 = numdomains6-int;
       MinimumNumberOfPoints = minnumpts-int;
       MaximumNumberOfPoints = maxnumpts-int;
       DegreeDimAdapt = degdimadapt-real;
       RelativeAccuracy = relacc-real;
       AbsoluteAccuracy = absacc-real;
with
filename-str [""]:
```

Specifies the path and name of the file containing the tabulated data. If this data was stored across multiple files, *filename-str* is the common prefix to all names of these files.

numfiles-int [0]:

Specifies the number of files to be loaded to access the entire tabulated data.

verbose-int [0]:

This integer ranges from 0 (no output) to 9 (maximum output) and specifies the level of data reporting (on the

screen) when tabulating data in sparse grid format or exploiting it.

numinputs-int [2]:

Number of input variables of the vector function to be tabulated. For example, numinputs-int = 2 when the Riemann invariants are tabulated, and numinputs-int = 6 when the Riemann solutions are tabulated (see TAB).

numoutputs-int [2]:

Number of outputs (components of the vector function) to be tabulated (see<u>TAB</u>).

numdomains1-int [1]:

Specifies the uniform splitting of the domain of the first input variable into *numdomains1-int* subdomains. If this number is greater than 1, it automatically multiplies the number of expected sparse grids by *numdomains1-int*.

in 1 min-real [0.0]:

Specifies the lower bound of the first input variable.

in1max-real [1.0]:

Specifies the upper bound of the first input variable.

minmumpts-int [100]:

Minimum number of data points to be generated in each (see Note below) sparse grid.

maxnumpts-int [100]:

Maximum number of data points to be generated in each (see first Note below) sparse grid (however, this maximum can be slightly exceeded by **AERO-F**).

degdimadapt-real [0.75]:

This parameter, which should be given a value between 0.0 and 1.0, specifies the desired degree of dimensional adaptivity of all generated sparse grids (<u>TAB</u>).

relacc-real [1.0e-3]:

Specifies the desired level of relative accuracy to be delivered by the sparse grid tabulation.

absacc-real [1.0e-1]:

Specifies the desired level of absolute accuracy to be delivered by the sparse grid tabulation.

Note:

1. to accelerate the sparse grid tabulation of functions, the user can split the domain of each i -th input variable into an arbitrary number of subdomains parameterized above by $n_i = numdomains i$ -int. In this case, the function is tabulated in a number of sparse grids equal to $\prod_{i=1}^{N} n_i$, where N = numinputs-int.

Next: Preconditioner, Previous: MultiPhase, Up: Objects

4.11 DEFINING THE BOUNDARY CONDITIONS

```
Object: BoundaryConditions
```

The different boundary conditions are specified within the BoundaryConditions object. Its syntax is:

```
under BoundaryConditions {
  under Inlet { ... }
  under Outlet { ... }
  under Wall { ... }
  under Hydro { ... }
}
```

with

Inlet:

Defines the inflow boundary conditions.

Outlet:

Defines the outflow boundary conditions. This object can be omitted if the inflow and outflow states are the same.

Wall:

Defines the wall boundary conditions.

Hydro:

Specifies a list of additional parameters for a hydro-computation. These are used to define the far-field boundary conditions and to compute the hydrostatic and hydrodynamic pressure and force fields. Its syntax is defined by the *Hydro* object (see <u>Hydro</u>). This object can be omitted if irrelevant.

Notes:

1. if Problem.Mode is set to Dimensional, the inflow pressure and density must be specified for an aerodynamic computation and the inflow pressure and temperature for a hydro-computation;

- 2. if an outflow condition is not specified but needed for the flow computation, it is set to the inflow condition;
- 3. the boundary conditions are specified for the "run-type" variables. Hence, if Problem.Mode is set to Dimensional, the specified boundary conditions are applied "as-is" to the dimensional variables. On the other hand, if Problem.Mode is set to NonDimensional, the specified boundary conditions are applied "as-is" to the non-dimensional variables.
- Inlet
- Outlet
- Wall
- Hydro

Next: Outlet, Up: BoundaryConditions

4.11.1 DEFINING THE FAR-FIELD INLET CONDITIONS



The Inlet object defines the far-field inlet state. Its syntax is:

```
under Inlet {
  Type = type-id;
  Mach = mach-real;
  Velocity = velocity-real;
  Alpha = alpha-real;
  Beta = beta-real;
  Density = density-real;
  Pressure = pressure-real;
  Temperature = temperature-real;
  NuTilde = nutilde-real;
  K = k-real;
  Eps = eps-real;
}
```

with

type-id [External]:

External

External flow computation with free-stream conditions in all far-fields.

Internal

Designates a special class of problems in which the pressure is specified at the outlet boundary, the density and velocity vector in the case of a perfect gas and the temperature and velocity vector in the case of a barotropic liquid are specified at the inlet boundary, and both boundaries are subsonic. This class of problems arises in some internal flow applications, which explains the choice of the word "Internal". AERO-F being essentially an external flow solver, it does not offer in this case an explicit and straightforward mechanism for specifying the velocity field at the subsonic inlet boundary. However, for a perfect gas, this can be accomplished in the dimensional case by setting the Mach number and the inlet pressure, and in the

non-dimensional case by setting the Mach number only, as described below. For a barotropic liquid, it can be accomplished in both dimensional and non-dimensional cases by setting the Mach number only.

First, it is noted that because the outlet boundary is subsonic, the true pressure at the inlet is not specified but propagated numerically from the outlet boundary to the inlet boundary during the solution procedure. Hence, the inlet pressure that can be specified in the input file should be considered only as a "knob". In this case, it turns out that the free-stream Mach number is also a knob. Now, given the velocity vector to be specified at the inlet boundary, one can compute its modulus.

This modulus, v, is related to the pressure and Mach number via

$$v = M \sqrt{\frac{\gamma p}{\rho}}$$

where M , γ , p , and ρ designate the Mach number, ratio of specific heats, pressure, and density, respectively.

Hence, (after specifying the legitimate density at the inlet boundary) one begins by choosing the Mach number and the pressure at the subsonic inlet boundary so that v is equal to the modulus of the desired velocity vector.

Then, the angles of attack *alpha-real* and *beta-real* are set to obtain the desired components of this velocity vector.

Clearly, there are many (M, p) combinations that lead to the same v. Since in this case both M and p are only knobs, all combinations are in principle valid. However, those combinations with a Mach number knob that is far away from a reasonable value associated with v can lead to numerical difficulties.

In this case, AERO-F considers the inlet density to be the reference density (which is to be considered as the inlet density to be specified), the modulus of the inlet velocity vector

 v_{inlet}

to be the modulus of the reference velocity vector (which is to be considered as the modulus of the inlet velocity vector to be prescribed), the outlet pressure to be the reference pressure (which is to be considered the outlet pressure to be prescribed), and the artificial inlet pressure knob to be the reference pressure too (warning: in this context, the reference pressure is not to be confused with the non-dimensionalization pressure). It follows that AERO-F automatically sets

$$\begin{split} \bar{\rho}_{inlet} &= 1; \quad \bar{v}_{inlet} = 1 \\ \bar{p}_{inlet} &= \bar{p}_{outlet} = \frac{p_{reference}}{\rho_{reference}v_{reference}^2} = \frac{1}{\gamma M_{reference}^2} \end{split}$$

From a discussion similar to that of the dimensional case described above, it follows that in the non-dimensional case, the user needs to input only the reference Mach number and the angles of attack *alpha-real* and *beta-real*. Furthermore, from the above explanation, it also follows that the reference Mach number should be set to

$$M_{reference} = v_{inlet} \sqrt{rac{
ho_{inlet}}{\gamma p_{outlet}}}$$

Then, by default, the free-stream Mach number is set to the reference Mach number (see below).

$$BAROTROPIC\ LIQUID\ ---\ DIMENSIONAL\ CASE$$

For a barotropic fluid, the pressure and density are not independent variables. Hence, in this case, the primitive variables are the density (or pressure), velocity field, and temperature. The modulus of the inlet velocity vector is given by

$$v = M\sqrt{\frac{1}{
ho_0}((k_1 + k_2p_0)(k_1 + k_2p)^{k_2-1})^{\frac{1}{k_2}}}$$

where

$$p_0, \rho_0, k_1, k_2$$

are the "reference" pressure, "reference" density, and the two constants used for defining the barotropic equation of state of the fluid. Because the outlet boundary is subsonic, the pressure — and therefore the density — at the inlet is not specified but propagated numerically from the outlet boundary to the inlet boundary during the solution procedure. The free-stream Mach number is a knob. Given the velocity vector to be specified at the inlet boundary, one can compute its modulus.

From the above formula, it follows that, after specifying the pressure at the outlet boundary, one chooses the Mach number so that \overline{v} is equal to the modulus of the desired velocity vector. Then, one sets the angles of attack *alpha-real* and *beta-real* to obtain the desired components of this velocity vector. One also specifies the temperature at the inlet boundary.

$$BAROTROPIC\ LIQUID\ ---\ NON-DIMENSIONAL\ CASE$$

In this case, AERO-F considers the outlet density to be the reference density, and the modulus of the inlet velocity vector to be the modulus of the reference velocity vector. At the inlet, it computes the reference

temperature using the formula given in Problem. Thus AERO-F automatically sets

$$\bar{\rho}_{outlet} = 1; \ \bar{v}_{inlet} = 1$$

while the non-dimensionalized temperature is set by the user. Also, AERO-F automatically sets the artificial inlet density to

$$\bar{\rho}_{inlet} = 1$$

In addition, the user must specify the reference Mach number so that

$$M_{reference} = rac{v_{inlet}}{\sqrt{lpha k_2
ho_{outlet}^{k_2 - 1}}}$$

where
$$\alpha = \frac{1}{\rho_0^{k_2}} (p_0 + k_1/k_2)$$

In both dimensional and non-dimensional cases, for this class of flow problems, AERO-F enforces the true inlet and outlet boundary conditions in a weak sense unless it is compiled with the flag STRONG INLET BC set ON.

mach-real [—]:

Free-stream Mach number. To be specified only if a free-stream velocity (see below) is not specified. If omitted and a free-stream velocity is not specified instead, this Mach number is set to the reference Mach number. If both a free-stream Mach number and a free-stream velocity are specified, **AERO-F** chooses to run with the specified free-stream Mach number.

velocity-real [—]:

Free-stream velocity (magnitude). To be specified — whether a dimensional or non-dimensional simulation is desired — only if a free-stream Mach number (see above) is not specified. If both a free-stream Mach number and a free-stream velocity are specified, **AERO-F** chooses to run with the specified free-stream Mach number.

alpha-real [—]:

Angle of attack (in degrees) defined in the x-z plane as follows: rotate the free-stream velocity vector around the z-axis until it intersects the x-z plane. The angle of attack is then the angle between the x-axis and the rotated vector and is measured positively when rotating from x to z. It is equal to zero if the flow is parallel to the x-axis. (Think of a spherical coordinate system).

beta-real [—]:

Yaw angle (in degrees) defined in the x-y plane as follows: project the free-stream velocity vector on the x-y plane. The yaw angle is then the angle between the x-axis and the projected vector, and is measured positively when rotating from x to y. It is equal to zero if the flow is parallel to the x-axis. (Think of a spherical coordinate system).

density-real [—]:

Density. It is required if Problem. Mode is set to Dimensional and FluidModel. Fluid is set to Gas. When running a Dimensional hydro-simulation (fluid modeled as a barotropic liquid or stiffened ga or stiffened gass), the far-field density is not specified as it is set automatically using the equation of state and the far-field pressure (see LiquidModel).

pressure-real [—]:

Pressure. It is required if Problem. Mode is set to Dimensional and FluidModel. Fluid is set to Gas. When running a Dimensional hydro-simulation (fluid modeled as a barotropic liquid or stiffened gas), if the far-field pressure is not specified, it is set to the "reference" pressure specified in LiquidModel (and then the far-field density is automatically set to the "reference" density) (see <u>LiquidModel</u>).

temperature-real [—]:

Temperature. It must be specified when the fluid is modeled as a barotropic liquid (that is, when FluidModel.Fluid is set to Liquid), and only in this case. If Problem.Mode is set to Dimensional, this temperature must be specified in Kelvin (in this case, the user should verify that the ideal gas constant R (see <u>GasModel</u>) is specified in the same system of units as all other input data). If Problem.Mode is set to NonDimensional, this specified temperature is interpreted as the value of the non-dimensionalized free-stream temperature.

nutilde-real [see below]:

Field variable of the one-equation Spalart-Allmaras turbulence model whose implementation in **AERO-F** does not include the trip term which usually starts it up. The default value of this parameter in the non-dimensional case is *nutilde-real* = 0.1. Its default value in the dimensional case is *nutilde-real* = $0.1 \times \nu = 0.1 \times \mu/\rho$, where ν is the laminar kinematic viscosity of the fluid, ρ is its density, and μ is

its dynamic viscosity (see <u>ViscosityModel</u>). These default values provide fully turbulent boundary and shear layers while avoiding numerical difficulties.

k-real [—]:

Turbulent kinetic energy in the two-equation $k-\epsilon$ turbulence model (required if Problem. Mode is set to Dimensional).

eps-real [—]:

Turbulent kinetic energy dissipation rate in the two-equation $k-\epsilon$ turbulence model (required if Problem.Mode is set to Dimensional).

Note:

1. some internal flow problems are characterized by sudden time-variations of the boundary conditions. For such problems, the initial state of the flow in a certain region is uniform but not equal to the state defined by the boundary condition (an assumption that is otherwise always made by AERO-F). The problem of opening the valve of a pressurized tank is such an example. It is possible to simulate such flow problems with AERO-F in dimensional mode, using the following two-step procedure. First, the desired initial state (for example, inside the tank) is computed by setting the boundary condition artificially to the desired uniform initial state (desired inside the tank). Next, a second simulation is performed by restarting from the outcome of the first simulation. In the second simulation, the reference Mach number, reference density, and reference temperature must be set to the desired initial state because the data saved by AERO-F for re-use in a restart is always saved in non-dimensional form. If these reference values are not specified as described, AERO-F will dimensionalize the saved data by the value of the boundary condition specified in the second simulation to model the sudden variation.

Next: Wall, Previous: Inlet, Up: BoundaryConditions

4.11.2 DEFINING THE FAR-FIELD OUTLET CONDITIONS

Object: Outlet

The Outlet object defines the far-field outlet state. Its syntax is:

```
under Outlet {
    Type = type-id;
    Mach = mach-real;
    Velocity = velocity-real;
    Alpha = alpha-real;
    Beta = beta-real;
    Density = density-real;
    Pressure = pressure-real;
    Temperature = temperature-real;
    NuTilde = nutilde-real;
    K = k-real;
    Eps = eps-real;
}
with

type-id [External]:
```

External

External flow computation with free-stream conditions in all far-fields.

Internal

Designates a special class of problems in which the pressure is specified at the outlet boundary, the density and velocity vector in the case of a perfect gas and the temperature and velocity vector in the case of a barotropic liquid are specified at the inlet boundary, and both boundaries are subsonic. This class of problems arises in some internal flow applications, which explains the choice of the word "Internal". AERO-F being essentially an external flow solver, it does not offer in this case an explicit and straightforward mechanism for specifying the velocity field at the subsonic inlet boundary. However, for a perfect gas, this can be accomplished in the dimensional case by setting the Mach number and the inlet pressure, and in the non-dimensional case by setting the Mach number only, as described below. For a barotropic liquid, it can be accomplished in both dimensional and non-dimensional cases by setting the Mach number only.

First, it is noted that because the outlet boundary is subsonic, the true pressure at the inlet is not specified but propagated numerically from the outlet boundary to the inlet boundary during the solution procedure. Hence, the inlet pressure that can be specified in the input file should be considered only as a "knob". In this case, it turns out that the free-stream Mach number is also a knob. Now, given the velocity vector to be specified at the inlet boundary, one can compute its modulus.

This modulus, \overline{v} , is related to the pressure and Mach number via

$$v = M \sqrt{\frac{\gamma p}{\rho}}$$

where M , γ , p , and ρ designate the Mach number, ratio of specific heats, pressure, and density, respectively.

Hence, (after specifying the legitimate density at the inlet boundary) one begins by choosing the Mach number and the pressure at the subsonic inlet boundary so that v is equal to the modulus of the desired velocity vector.

Then, the angles of attack *alpha-real* and *beta-real* are set to obtain the desired components of this velocity vector.

Clearly, there are many (M, p) combinations that lead to the same v. Since in this case both M and P are only knobs, all combinations are in principle valid. However, those combinations with a Mach number knob that is far away from a reasonable value associated with v can lead to numerical difficulties.

In this case, AERO-F considers the inlet density to be the reference density (which is to be considered as the inlet density to be specified), the modulus of the inlet velocity vector

 v_{inlet}

to be the modulus of the reference velocity vector (which is to be considered as the modulus of the inlet velocity vector to be prescribed), the outlet pressure to be the reference pressure (which is to be considered the outlet pressure to be prescribed), and the artificial inlet pressure knob to be the reference pressure too (warning: in this context, the reference pressure is not to be confused with the non-dimensionalization pressure). It follows that AERO-F automatically sets

$$\begin{split} \bar{\rho}_{inlet} &= 1; \quad \bar{v}_{inlet} = 1 \\ \bar{p}_{inlet} &= \bar{p}_{outlet} = \frac{p_{reference}}{\rho_{reference} v_{reference}^2} = \frac{1}{\gamma M_{reference}^2} \end{split}$$

From a discussion similar to that of the dimensional case described above, it follows that in the non-dimensional case, the user needs to input only the reference Mach number and the angles of attack *alpha-real* and *beta-real*. Furthermore, from the above explanation, it also follows that the reference Mach number should be set to

$$M_{reference} = v_{inlet} \sqrt{rac{
ho_{inlet}}{\gamma p_{outlet}}}$$

Then, by default, the free-stream Mach number is set to the reference Mach number (see below).

$$BAROTROPIC\ LIQUID\ ---\ DIMENSIONAL\ CASE$$

For a barotropic fluid, the pressure and density are not independent variables. Hence, in this case, the primitive variables are the density (or pressure), velocity field, and temperature. The modulus of the inlet velocity vector is given by

$$v = M\sqrt{\frac{1}{
ho_0}((k_1 + k_2p_0)(k_1 + k_2p)^{k_2-1})^{\frac{1}{k_2}}}$$

where

$$p_0, \rho_0, k_1, k_2$$

are the "reference" pressure, "reference" density, and the two constants used for defining the barotropic equation of state of the fluid. Because the outlet boundary is subsonic, the pressure — and therefore the density — at the inlet is not specified but propagated numerically from the outlet boundary to the inlet boundary during the solution procedure. The free-stream Mach number is a knob. Given the velocity vector to be specified at the inlet boundary, one can compute its modulus.

From the above formula, it follows that, after specifying the pressure at the outlet boundary, one chooses the Mach number so that v is equal to the modulus of the desired velocity vector. Then, one sets the angles of

attack *alpha-real* and *beta-real* to obtain the desired components of this velocity vector. One also specifies the temperature at the inlet boundary.

$$BAROTROPIC\ LIQUID\ ---\ NON-DIMENSIONAL\ CASE$$

In this case, AERO-F considers the outlet density to be the reference density, and the modulus of the inlet velocity vector to be the modulus of the reference velocity vector. At the inlet, it computes the reference temperature using the formula given in Problem. Thus AERO-F automatically sets

$$\bar{\rho}_{outlet} = 1; \ \bar{v}_{inlet} = 1$$

while the non-dimensionalized temperature is set by the user. Also, AERO-F automatically sets the artificial inlet density to

$$\bar{\rho}_{inlet} = 1$$

In addition, the user must specify the reference Mach number so that

$$M_{reference} = rac{v_{inlet}}{\sqrt{\alpha k_2 \rho_{outlet}^{k_2 - 1}}}$$

where
$$\alpha=rac{1}{
ho_0^{k_2}}(p_0+k_1/k_2)$$

In both dimensional and non-dimensional cases, for this class of flow problems, AERO-F enforces the true inlet and outlet boundary conditions in a weak sense unless it is compiled with the flag STRONG_INLET_BC set ON.

mach-real [—]:

Free-stream Mach number. To be specified only if a free-stream velocity (see below) is not specified. If omitted and a free-stream velocity is not specified instead, this Mach number is set to the reference Mach number. If both a free-stream Mach number and a free-stream velocity are specified, **AERO-F** chooses to run with the specified free-stream Mach number.

velocity-real [—]:

Free-stream velocity (magnitude). To be specified — whether a dimensional or non-dimensional simulation is desired — only if a free-stream Mach number (see above) is not specified. If both a free-stream Mach number and a free-stream velocity are specified, **AERO-F** chooses to run with the specified free-stream Mach number.

alpha-real [—]:

Angle of attack (in degrees) defined in the x-z plane as follows: rotate the free-stream velocity vector around the z-axis until it intersects the x-z plane. The angle of attack is then the angle between the x-axis and the rotated vector and is measured positively when rotating from x to z. It is equal to zero if the flow is parallel to the x-axis. (Think of a spherical coordinate system).

beta-real [—]:

Yaw angle (in degrees) defined in the x-y plane as follows: project the free-stream velocity vector on the x-y plane. The yaw angle is then the angle between the x-axis and the projected vector, and is measured positively when rotating from x to y. It is equal to zero if the flow is parallel to the x-axis. (Think of a spherical coordinate system).

density-real [—]:

Density. It is required if Problem. Mode is set to Dimensional and FluidModel. Fluid is set to Gas. When running a Dimensional hydro-simulation (fluid modeled as a barotropic liquid or stiffened ga or stiffened gass), the far-field density is not specified as it is set automatically using the equation of state and the far-field pressure (see LiquidModel).

pressure-real [—]:

Pressure. It is required if Problem. Mode is set to Dimensional and FluidModel. Fluid is set to Gas. When running a Dimensional hydro-simulation (fluid modeled as a barotropic liquid or stiffened gas), if the far-field pressure is not specified, it is set to the "reference" pressure specified in LiquidModel (and then the far-field density is automatically set to the "reference" density) (see LiquidModel).

temperature-real [—]:

Temperature. It must be specified when the fluid is modeled as a barotropic liquid (that is, when FluidModel.Fluid is set to Liquid), and only in this case. If Problem.Mode is set to Dimensional, this temperature must be specified in Kelvin (in this case, the user should verify that the ideal gas constant R (see <u>GasModel</u>) is specified in the same system of units as all other input data). If Problem.Mode is set to NonDimensional, this specified temperature is interpreted as the value of the non-dimensionalized free-stream temperature.

nutilde-real [—]:

Field variable of the one-equation Spalart-Allmaras turbulence model whose implementation in **AERO-F** does not include the trip term which usually starts it up. The default value of this parameter in the non-dimensional case is *nutilde-real* = 0.1. Its default value in the dimensional case is *nutilde-real* = \$0.1\times \nu = 0.1\times \nu\chanklet \times \nu\times \nu\times \times \

k-real [—]:

Turbulent kinetic energy in the two-equation $k-\epsilon$ turbulence model (required if Problem. Mode is set to Dimensional).

eps-real [—]:

Turbulent kinetic energy dissipation rate in the two-equation $k - \epsilon$ turbulence model (required if Problem. Mode is set to Dimensional).

Note:

1. some internal flow problems are characterized by sudden time-variations of the boundary conditions. For such problems, the initial state of the flow in a certain region is uniform but not equal to the state defined by the boundary condition (an assumption that is otherwise always made by AERO-F). The problem of opening the valve of a pressurized tank is such an example. It is possible to simulate such flow problems with AERO-F in dimensional mode, using the following two-step procedure. First, the desired initial state (for example, inside the tank) is computed by setting the boundary condition artificially to the desired uniform initial state (desired inside the tank). Next, a second simulation is performed by restarting from the outcome of the first simulation. In the second simulation, the reference Mach number, reference density, and reference temperature must be set to the desired initial state because the data saved by AERO-F for re-use in a restart is always saved in non-dimensional form. If these reference values are not specified as described, AERO-F will dimensionalize the saved data by the value of the boundary condition specified in the second simulation to model the sudden variation.

Next: Hydro, Previous: Outlet, Up: BoundaryConditions

4.11.3 DEFINING THE WALL CONDITIONS



For viscous simulations, three different types of solid wall are currently supported and defined within the Wall object whose syntax is:

```
under Wall {
    Type = type-id;
    Integration = integration-id;
    Temperature = temp-real;
    Delta = delta-real;
}
with

type-id [Adiabatic]:
Adiabatic
```

Adiabatic wall.

Isothermal

Isothermal wall with temperature set to Wall. Temperature.

integration-id []:

WallFunction

Modeling by the discretized governing equations up to a distance Wall.Delta from the wall. The region of the boundary layer that is not resolved by the mesh is modeled by Reichardt's nonlinear wall function (available for all Navier-Stokes simulations with or without turbulence models).

Full

Modeling by the discretized governing equations up to the wall (not available for Navier-Stokes simulations with the $k-\epsilon$ turbulence model). In this case, it is strongly recommended to have the first layer of elements above the wall located at $y^+ \approx 1$.

If *integration-id* is not specified, AERO-F sets *integration-id* to Full for Navier-Stokes simulations without turbulence modeling and to WallFunction for Navier-Stokes simulations with turbulence modeling (including LES).

temp-real [—]:

Wall temperature (required for an isothermal wall).

delta-real [—]:

Distance of the fictitious computational domain to solid walls (required for a modelisation with the wall function). This global parameter is kept constant during the computation and can be set and verified using the following guidelines:

* In principle, the suitability of a specific value of *delta-real* can be assessed only a posteriori, by checking the values of the y^+ of the corresponding solution as explained below. Hence, one begins with a trial value

of delta-real then adjusts it after one or more additional runs.

* A good first trial value of *delta-real* can be obtained as follows. Typically, the non-dimensional value of the friction velocity is of the order of 1/20, and the non-dimensional value of the dynamic viscosity coefficient is of the order of 1. Using these typical values, the formula relating the y^+ to y, the non-dimensional friction

velocity and the non-dimensional dynamic viscosity becomes

$$y^+ = Re^{\frac{\bar{y}}{20}}$$

where Re denotes the Reynolds number and \bar{y} denotes y after non-dimensionalization by the reference length (used for the definition of the Reynolds number). Hence, a first trial value of delta-real can be chosen so that $\bar{y} = delta$ -real produces a value of y^+ that is within the acceptable limits of the wall function.

AERO-F uses Reichardt's law which is valid within all three zones of the boundary layer: the viscous

sublayer ($0 \le y^+ \le 5$) where the non-dimensional velocity u^+ is a linear function of y^+ , the buffer

layer where the relationship is log-linear, and the logarithmic layer where the relationship is logarithmic. However, because of the reasons explained below, the user is advised to verify that *delta-real* is chosen so that

$$30 \le y^+ \le 100$$

(see below).

* Check the lower limit of y^+ . In the commonly used applications of wall functions, the meshing should be arranged so that the values of y^+ at all the wall-adjacent mesh points is only slightly above the recommended lower limit between 20 and 30. The real reason is not that the form usually assumed for the wall functions is

not valid much below these values (given that Reichardt's law is valid), but the fact that if *delta-real* is positioned too low, the CFD computation will start too close to the wall and its accuracy will depend on the specifics of the chosen turbulence model. If this model does not reproduce correctly the asymptotic behavior of the solution near the wall (for example, the standard LES model or the standard $k - \epsilon$ model), a flawed

computation can be expected even though the connection with the wall function is performed at a valid point. On the other hand, the computation may be safe if the dynamic LES model is used instead. In any case, the lower limit given above offers the best chances to correctly resolve the turbulent portion of the boundary layer. It should be noted however that this limit may be impossible to satisfy close to separation or reattachment zones unless y^+ is based upon y^* .

- * Check the upper limit on y^+ . In the case of moderate Reynolds numbers, where the boundary layer only extends to y^+ of 300 to 500, there is no chance of accurately resolving the boundary layer if the first mesh point is placed at a location with the value of y^+ of 100 or higher.
- * Check the resolution of the boundary layer. If boundary layer effects are important, it is recommended that the resolution of the boundary layer is checked after the computation. This can be achieved by a plot of the ratio between the turbulent to the molecular viscosity, which is high inside the boundary layer. Adequate boundary layer resolution requires at least 8-10 points in the layer. An attempt to address this requirement can be performed a priori by estimating the thickness of the boundary layer assuming the obstacle is locally a flat plate, and using the experiment-based formulae

$$\delta = \frac{5.2x}{\sqrt{R}\epsilon_x}$$
 (laminar)

and

$$\delta = \frac{0.37x}{Re_x^{0.2}}$$
 (turbulent)

where δ denotes the thickness of the boundary layer at the distance x from the leading edge of the plate, and Re_x denotes the Reynolds number based on a length equal to x for this specific purpose.

- * For robustness, the mesh spacing and *delta-real* should be such that the distance to the wall is equal to the average value of the wall normal mesh spacing. For some complex flow configurations, the robustness of the solver can be further increased by choosing a larger value of Wall.Delta during the first few time iterations, performing a run with this larger value, then restarting from the result of this run and using the suitable value of Wall.Delta.
- * In any case, the chosen value of the distance to the wall should be validated a posteriori by inspecting the resulting values of the y^+ field as discussed above. This can be done by requesting one restart iteration after setting Postpro.DeltaPlus to output the values of y^+ .

Previous: Wall, Up: BoundaryConditions

4.11.4 DEFINING A LIST OF ADDITIONAL PARAMETERS FOR HYDRO-SIMULATION

Object: **Hydro**

When performing a hydro-computation, a list of additional parameters is needed for computing the far-field pressure and the hydrostatic and hydrodynamic pressure and force fields. This list is currently defined within the Hydro object. Its syntax is:

```
under Hydro{
    Depth = depth-real;
}
with
depth-real [0.0]:
```

Depth of the origin of the mesh coordinate system.

Next: Space, Previous: Boundary Conditions, Up: Objects

4.12 SETTING THE PARAMETERS OF THE CHOSEN LOW-MACH PRECONDITIONER



The Preconditioner object specifies the parameters of the low-Mach Turkel preconditioner for the artificial viscosity as well as inertia (or time-derivative, or temporal) terms of the equations to be solved. The preconditioner is local,

i.e. its value changes at each node and during the simulation. Its key variable is

$$\beta = \min(1.0, \max(Mach, kM_{local}))$$

where M_{local} is the value of the local mach number.

The syntax of the Preconditioner object is:

```
under Preconditioner{
  Mach = Mach-real;
  k = k-real;
}
```

with

Mach-real [1.0]:

Minimal value of the preconditioner for the low-Mach Turkel preconditioner. The recommended value is of the order of the characteristic Mach number of the simulation being run. In general, a good choice is a value slightly smaller than the inlet Mach number. However, it can be necessary to set it to a higher value for flows with pockets of very small velocities.

k-real [1.0]:

This parameter characterizes the low-Mach preconditioner for both gas and liquid flows. The recommended value is of the order of unity. However, it can be necessary to set it to a higher value for flows with pockets of very small velocities.

Notes:

- 1. the user can check that at values of the Mach number in the compressible flow regime, β becomes equal to 1 if the above parameters are reasonably well chosen in which case the preconditioner becomes inactive and therefore does not bother compressible flow computations even when turned on;
- 2. explicit time-integration is not recommended for low-Mach flows for computational efficiency reasons.

Next: Time, Previous: Preconditioner, Up: Objects

4.13 DEFINING THE SPACE DISCRETIZATION



The finite I volume discretization of the governing equations is defined within the Space object. Its syntax is:

```
under Space {
  under NavierStokes { ... }
  under TurbulenceModel { ... }
```

```
under LevelSet { ... }
under Boundaries { ... }
under Fixes { ... }
}
```

with

NavierStokes:

Defines the spatial discretization of the inviscid part of the Euler or averaged Navier-Stokes equations. Its syntax is defined in the *space-obj* object.

TurbulenceModel:

Defines the spatial discretization of the inviscid part of the turbulence model equation(s). Its syntax is defined by the *space-obj* object.

LevelSet:

Defines the spatial discretization of the generalized level set equation(s). Its syntax is defined by the *space-obj* object.

Boundaries:

Defines the options available for the numerical treatment of the far-field boundary conditions.

Fixes:

Defines the few modifications that can be applied to the spatial discretization of the governing equations in order to improve its robustness.

Note:

- 1. the discretization of the viscous and source terms of the governing equations is always performed by a Galerkin finite element technique.
- NavierStokes
- SpaceTurbulenceModel
- LevelSet
- Boundaries
- Fixes

Next: SpaceTurbulenceModel, Up: Space

4.13.1 NAVIERSTOKES

Object: NavierStokes

The NavierStokes object defines the finite volume discretization of the governing Euler or Navier-Stokes equations. Its syntax is:

```
under NavierStokes {
   Flux = flux-id;
   Reconstruction = reconstruction-id;
   AdvectiveOperator = advectiveOperator-id;
   Limiter = limiter-id;
   Gradient = gradient-id;
   Dissipation = dissipation-id;
   Beta = beta-real;
   Gamma = gamma-real;
   Eps = eps-real;
}
```

Roe

with

flux-id [Roe]:

Specifies Roe's numerical flux.

HLLE

Specifies the HLLE (Harten-Lax-van Leer-Einfeldt) numerical flux, which enables the intermediate state to satisfy the so-called entropy and positivity conditions but is more diffusive than Roe's flux. This choice for the numerical flux is available however only when the specified equation of state (EOS) is that of a perfect gas (see FluidModel). If any other EOS is specified in FluidModel, flux-id is automatically reset to Roe by AERO-F.

HLLE

Specifies the HLLC (devised by Toro, HLL for Harten-Lax-van Leer and C for "contact") numerical flux, which can remain positively conservative and is computationally more efficient than Roe's flux. This choice for the numerical flux is available however only when the specified equation of state (EOS) is that of a perfect gas (see FluidModel). If any other EOS is specified in FluidModel, flux-id is automatically reset to Roe by AERO-F.

reconstruction-id [Linear]:

Constant

A constant variation of the solution is assumed within each control volume. This leads to a first-order space-accurate scheme.

Linear

A linear variation of the solution is assumed within each control volume. This leads to at least a second-order space-accurate scheme.

advectiveoperator-id [FiniteVolume]:

FiniteVolume

This option is relevant only if *reconstruction-id* is set to Linear. In this case, the flux function is computed using the reconstructed values of the primitive variables.

Galerkin

This option is relevant only if *reconstruction-id* is set to Linear. Because they are obtained by extrapolation, the reconstructed values of the primitive variables may occasionally be non-physical. In such a case, they may lead to the appearance of a NaN when used for computing the flux function. To avoid this pitfall and the expensive "if"-type of testing that can prevent it, this option requests that the reconstructed values of the primitive variables be used only in the (Wi - Wj) term of the numerical flux function and that the constant values be used in the centered flux component of this flux function as well as in its associated matrix. This is justified by the two following observations about the upwinded flux: a) its centered flux term is by construction second-order space-accurate and therefore does not need to be evaluated at the reconstructed values of the primitive variables in order to be second-order space-accurate, and b) the evaluation of the (Wi-Wj) term does not incur the computation of any quantity that can generate a NaN (such as for example, the speed of sound which involves a square root).

limiter-id [None]:

None

No limiter is used.

VanAlbada

The one-dimensional limiter developed by van Albada is used.

Barth

The multi-dimensional limiter developed by Barth is used.

Venkatakrishnan

The multi-dimensional limiter developed by Venkatakrishnan (smooth version of Barth's limiter) is used.

PressureSensor

A sensor is used to switch to a constant reconstruction in regions where the flow exhibits large pressure gradients.

gradient-id [LeastSquares]:

LeastSquares

A least squares technique is used to compute the nodal gradients for second-order reconstruction. This option is the most robust one, particularly for turbulent flows.

Galerkin

A weighted Galerkin technique is used to compute the nodal gradients for second-order reconstruction.

NonNodal

A "geometrical upwind", non-nodal technique is used to compute the gradients for second-order reconstruction. This option is the least dissipative one.

dissipation-id [SecondOrder]:

SecondOrder

This is a misnomer as in this case, the resulting scheme is the standard *beta-real gamma-real* scheme which in the general case has a second-order dispersion error, a third-order dissipation error and therefore is spatially second-order accurate.

SixthOrder

beta-real [1/3]:

gamma-real [1.0]:

Parameter that controls the spatial numerical viscosity introduced by the chosen numerical flux. A value of one recovers the original flux, while a value less than one decreases the added numerical viscosity. For a fixed value of *beta-real* (see above), this parameter controls the third-order spatial dissipation of the scheme. When *gamma-real* is set to 0, the third-order spatial dissipation error is eliminated and the leading spatial dissipation error becomes fifth-order. In this case, if *dissipation-id* is set to SecondOrder, the scheme becomes fourth-order space-accurate at best when *beta-real* is set to 1/3.

eps-real [0.1]:

Parameter used in Venkatakrishnan's limiter and in the pressure sensor. The limiter becomes more active if this value is reduced.

Note:

1. for the level set equation(s), only the SecondOrder option of dissipation-id is currently supported.

Next: LevelSet, Previous: NavierStokes, Up: Space

4.13.2 TURBULENCEMODEL

```
Object: TurbulenceModel
```

The TurbulenceModel object defines the finite volume discretization of the turbulence model equations. Its syntax is:

```
under TurbulenceModel {
   Reconstruction = reconstruction-id;
   AdvectiveOperator = advectiveOperator-id;
   Limiter = limiter-id;
   Gradient = gradient-id;
   Dissipation = dissipation-id;
   Beta = beta-real;
   Gamma = gamma-real;
   Eps = eps-real;
}
```

reconstruction-id [Constant]:

Constant

with

A constant variation of the solution is assumed within each control volume. This leads to a first-order space-accurate scheme.

Linear

A linear variation of the solution is assumed within each control volume. This leads to at least a second-order space-accurate scheme.

advectiveoperator-id [FiniteVolume]:

FiniteVolume

This option is relevant only if *reconstruction-id* is set to Linear. In this case, the flux function is computed using the reconstructed values of the primitive variables.

Galerkin

This option is relevant only if *reconstruction-id* is set to Linear. Because they are obtained by extrapolation, the reconstructed values of the primitive variables may occasionally be non-physical. In such a case, they may lead to the appearance of a NaN when used for computing the flux function. To avoid this pitfall and the expensive "if"-type of testing that can prevent it, this option requests that the reconstructed values of the primitive variables be used only in the (Wi - Wj) term of the numerical flux function and that the constant values be used in the centered flux component of this flux function as well as in its associated matrix. This is justified by the two following observations about the upwinded flux: a) its centered flux term is by construction second-order space-accurate and therefore does not need to be evaluated at the reconstructed values of the primitive variables in order to be second-order space-accurate, and b) the evaluation of the (Wi - Wj) term does not incur the computation of any quantity that can generate a NaN (such as for example, the speed of sound which involves a square root).

limiter-id [None]:

None

No limiter is used.

VanAlbada

The one-dimensional limiter developed by van Albada is used.

Barth

The multi-dimensional limiter developed by Barth is used.

Venkatakrishnan

The multi-dimensional limiter developed by Venkatakrishnan (smooth version of Barth's limiter) is used.

PressureSensor

A sensor is used to switch to a constant reconstruction in regions where the flow exhibits large pressure gradients.

gradient-id [LeastSquares]:

LeastSquares

A least squares technique is used to compute the nodal gradients for second-order reconstruction. This option is the most robust one, particularly for turbulent flows.

Galerkin

NonNodal

A weighted Galerkin technique is used to compute the nodal gradients for second-order reconstruction.

A "geometrical upwind", non-nodal technique is used to compute the gradients for second-order reconstruction. This option is the least dissipative and therefore the preferred one. However, it can slow down convergence.

dissipation-id [SecondOrder]:

SecondOrder

This is a misnomer as in this case, the resulting scheme is the standard *beta-real gamma-real* scheme which in the general case has a second-order dispersion error, a third-order dissipation error and therefore is spatially second-order accurate.

SixthOrder

beta-real [1/3]:

```
gamma-real [1.0]:
```

Parameter that controls the spatial numerical viscosity introduced by the chosen numerical flux. A value of one recovers the original flux, while a value less than one decreases the added numerical viscosity. For a fixed value of *beta-real* (see above), this parameter controls the third-order spatial dissipation of the scheme. When *gamma-real* is set to 0, the third-order spatial dissipation error is eliminated and the leading spatial dissipation error becomes fifth-order. In this case, if *dissipation-id* is set to SecondOrder, the scheme becomes fourth-order space-accurate at best when *beta-real* is set to 1/3.

```
eps-real [0.1]:
```

Parameter used in Venkatakrishnan's limiter and in the pressure sensor. The limiter becomes more active if this value is reduced.

Note:

1. for the level set equation(s), only the SecondOrder option of dissipation-id is currently supported.

Next: Boundaries, Previous: SpaceTurbulenceModel, Up: Space

4.13.3 LEVELSET

```
Object: LevelSet
```

The LevelSet object defines the finite volume discretization of the level set equation(s). Its syntax is:

```
under LevelSet {
    Reconstruction = reconstruction-id;
    AdvectiveOperator = advectiveOperator-id;
    Limiter = limiter-id;
    Gradient = gradient-id;
    Dissipation = dissipation-id;
    Beta = beta-real;
    Gamma = gamma-real;
    Eps = eps-real;
}
with

reconstruction-id [Constant]:
```

Constant

A constant variation of the solution is assumed within each control volume. This leads to a first-order space-accurate scheme.

Linear

A linear variation of the solution is assumed within each control volume. This leads to at least a second-order space-accurate scheme.

advectiveoperator-id [FiniteVolume]:

FiniteVolume

This option is relevant only if *reconstruction-id* is set to Linear. In this case, the flux function is computed using the reconstructed values of the primitive variables.

Galerkin

This option is relevant only if *reconstruction-id* is set to Linear. Because they are obtained by extrapolation, the reconstructed values of the primitive variables may occasionally be non-physical. In such a case, they may lead to the appearance of a NaN when used for computing the flux function. To avoid this pitfall and the expensive "if"-type of testing that can prevent it, this option requests that the reconstructed values of the primitive variables be used only in the (Wi - Wj) term of the numerical flux function and that the constant values be used in the centered flux component of this flux function as well as in its associated matrix. This is justified by the two following observations about the upwinded flux: a) its centered flux term is by construction second-order space-accurate and therefore does not need to be evaluated at the reconstructed values of the primitive variables in order to be second-order space-accurate, and b) the evaluation of the (Wi - Wj) term does not incur the computation of any quantity that can generate a NaN (such as for example, the speed of sound which involves a square root).

limiter-id [None]:

None

No limiter is used.

VanAlbada

The one-dimensional limiter developed by van Albada is used.

Barth

The multi-dimensional limiter developed by Barth is used.

Venkatakrishnan

The multi-dimensional limiter developed by Venkatakrishnan (smooth version of Barth's limiter) is used.

PressureSensor

A sensor is used to switch to a constant reconstruction in regions where the flow exhibits large pressure gradients.

gradient-id [LeastSquares]:

LeastSquares

A least squares technique is used to compute the nodal gradients for second-order reconstruction. This option

is the most robust one, particularly for turbulent flows.

Galerkin

A weighted Galerkin technique is used to compute the nodal gradients for second-order reconstruction.

NonNodal

A "geometrical upwind", non-nodal technique is used to compute the gradients for second-order reconstruction. This option is the least dissipative one.

dissipation-id [SecondOrder]:

SecondOrder

This is a misnomer as in this case, the resulting scheme is the standard *beta-real gamma-real* scheme which in the general case has a second-order dispersion error, a third-order dissipation error and therefore is spatially second-order accurate.

SixthOrder

beta-real [1/3]:

gamma-real [1.0]:

Parameter that controls the spatial numerical viscosity introduced by the chosen numerical flux. A value of one recovers the original flux, while a value less than one decreases the added numerical viscosity. For a fixed value of *beta-real* (see above), this parameter controls the third-order spatial dissipation of the scheme. When *gamma-real* is set to 0, the third-order spatial dissipation error is eliminated and the leading spatial dissipation error becomes fifth-order. In this case, if *dissipation-id* is set to SecondOrder, the scheme becomes fourth-order space-accurate at best when *beta-real* is set to 1/3.

eps-real [0.1]:

Parameter used in Venkatakrishnan's limiter and in the pressure sensor. The limiter becomes more active if

this value is reduced.

Note:

1. for the level set equation(s), only the SecondOrder option of dissipation-id is currently supported.

Next: Fixes, Previous: LevelSet, Up: Space

4.13.4 SPECIFYING THE NUMERICAL TREATMENT OF THE FAR-FIELD BOUNDARY CONDITIONS



The Boundaries object defines the options available for the numerical treatment of the far-field boundary conditions.

Its syntax is:

```
under Boundaries {
  Type = type-id
}
```

with

type-id [StegerWarming];

StegerWarming

The fluxes at the far-field boundaries are computed using the StegerWarming scheme. This option is only available when the fluid in the far-field is a perfect gas.

Ghidaglia

The fluxes at the far-field boundaries are computed using Ghidaglia's approach which does not assume that the flux is a homogeneous function of degree one and therefore is applicable to all equations of state supported by **AERO-F**.

ConstantExtrapolation

A constant extrapolation procedure is applied for outgoing variables. This option is recommended when the low-Mach preconditioner (see <u>Problem</u>) is employed (and the Mach number is below 0.01).

Previous: Boundaries, Up: Space

4.13.5 FINE TUNING THE SPATIAL DISCRETIZATION



The Fixes object defines the few modifications that can be applied to the spatial discretization of the governing equations in order to improve its robustness. Its syntax is:

```
under Fixes {
  under Sphere1 { ... }
  under Box1 { ... }
  under Cone1 { ... }
  Symmetry = symmetry-id;
}
```

with

Sphere1:

Defines a sphere in which the value of Reconstruction (see NavierStokes) is set to Constant.

Box1:

Defines a box in which the value of Reconstruction (see NavierStokes) is set to Constant.

Cone1:

Defines a conical frustrum in which the value of Reconstruction (see NavierStokes) is set to Constant.

symmetry-id [None]:

None

No symmetry of the spheres, boxes and cones is performed.

X

An additional sphere, box or cone is generated by symmetry with respect to the plane orthogonal to the x-axis and containing the origin.

Y

An additional sphere, box or cone is generated by symmetry with respect to the plane orthogonal to the y-axis and containing the origin.

Z

An additional sphere, box or cone is generated by symmetry with respect to the plane orthogonal to the z-axis and containing the origin.

Note:

- 1. currently the user can specify 10 spheres (Sphere1 to Sphere10), 10 boxes (Box1 to Box10), and 10 cones (Cone1 to Cone10).
- SphereFix
- BoxFix
- ConeFix

Next: BoxFix, Up: Fixes

4.13.5.1 DEFINING A GENERIC SPHERE

Object: Sphere

The syntax of the Sphere (with an integer appended to the last letter of this word) object is:

```
under Sphere {
    X0 = x0-real;
    Y0 = y0-real;
    Z0 = z0-real;
    Radius = radius-real;
}

with

x0-real [0.0]:
    x-coordinate of the center of the sphere.

y0-real [0.0]:
    y-coordinate of the center of the sphere.

z0-real [0.0]:
    z-coordinate of the center of the sphere.

radius-real [0.0]:
    Radius of the sphere.
```

Next: ConeFix, Previous: SphereFix, Up: Fixes

4.13.5.2 DEFINING A GENERIC BOX

Object: Box

The syntax of the Box (with an integer appended to the last letter of this word) object is:

```
under Box {
    X0 = x0-real;
    Y0 = y0-real;
    Z0 = z0-real;
    X1 = x1-real;
    Y1 = y1-real;
    Z1 = z1-real;
}
with

x0-real [0.0]:
```

x-coordinate of the lower left corner of the box.

```
y0-real [0.0]:
```

y-coordinate of the lower left corner of the box.

z0-real [0.0]:

z-coordinate of the lower left corner of the box.

x1-real [0.0]:

x-coordinate of the upper right corner of the box with x1-real > x0-real.

y1-real [0.0]:

y-coordinate of the upper right corner of the box with y1-real > y0-real.

z1-real [0.0]:

z-coordinate of the upper right corner of the box with z1-real > z0-real.

Previous: BoxFix, Up: Fixes

4.13.5.3 DEFINING A GENERIC CONICAL FRUSTRUM



The syntax of the Cone (with an integer appended to the last letter of this word) object is:

```
under cone-obj {
    X0 = x0-real;
    Y0 = y0-real;
    Z0 = z0-real;
    Radius0 = radius0-real;
    X1 = x1-real;
    Y1 = y1-real;
    Z1 = z1-real;
    Radius1 = radius1-real;
}
with

x0-real [0.0]:
```

x-coordinate of the center of the first circle delimiting the first end of the conical frustrum.

y0-real [0.0]:

y-coordinate of the center of the first circle delimiting the first end of the conical frustrum.

z0-real [0.0]:

z-coordinate of the center of the first circle delimiting the first end of the conical frustrum.

radius0-real [0.0]:

Radius of the first circle delimiting the first end of the conical frustrum.

x1-real [0.0]:

x-coordinate of the center of the second circle delimiting the second end of the conical frustrum.

y1-real [0.0]:

y-coordinate of the center of the second circle delimiting the second end of the conical frustrum.

z1-real [0.0]:

z-coordinate of the center of the second circle delimiting the second end of the conical frustrum.

radius 1-real [0.0]:

Radius of the second circle delimiting the second end of the conical frustrum.

Next: Newton, Previous: Space, Up: Objects

4.14 DEFINING THE TIME-INTEGRATION



The Time object characterizes how the governing equations are integrated in time (even steady-state flows are obtained through a pseudo-time integration). Its syntax is:

```
under Time {
  Type = type-id;
  Prec = prec-id;
  MaxIts = maxits-int;
  Eps = eps-real;
  TimeStep = timestep-real;
  MaxTime = maxtime-real;
  Cfl0 = cfl0-real;
  Cfl1 = cfl1-real;
  Cfl2 = cfl2-real;
  CflMax = cflmax-real;
  Ser = ser-real;
  under Implicit { . . . }
  under Explicit { . . . }
}
```

```
with
```

```
type-id [Implicit];
```

Implicit

Implicit time-integration is used.

Explicit

Explicit time-integration is used.

prec-id [NonPreconditioned]:

NonPreconditioned

For steady-state calculations, the inertia (or time-derivative, or temporal) terms of the solution scheme are not low-Mach preconditioned.

LowMach

For **steady-state single phase flow calculations only**, the inertia (or time-derivative, or temporal) terms of the solution scheme are equipped with the low-Mach Turkel preconditioner whose parameters are set by the Preconditioner object (see <u>Preconditioner</u>), as long as an explicit scheme (see <u>Explicit</u>) or the backward Euler implicit scheme (see <u>Implicit</u>) is chosen for advancing in pseudo-time the iterative solution. This option can be combined with the low-Mach preconditioning of the dissipation terms of the convective fluxes of the solution scheme than can be specified in the Problem object (see <u>Problem</u>). Note that when the fluid is modeled as a barotropic liquid governed by Tait's equation of state, this preconditioner does not seem to be effective.

maxits-int [100]:

Maximum number of time-steps (or half the number of snapshots per modal impulse — see Running AERO-FL).

```
eps-real [1.e-6]:
```

Relative decrease of the spatial nonlinear residual (only for steady-state flow simulations).

```
timestep-real [—]:
```

Time-step (only for unsteady flow simulations). If this variable is set to a positive value, the CFL strategy is not used for the time-step computation.

```
maxtime-real [1.e99]:
```

Maximum physical time (only for unsteady flow simulations that do not invlove a structural code). The simulation terminates when either the maximum number of iterations or the maximum time is reached.

```
cfl0-real [5.0]:
cfl1-real [0.0]:
cfl2-real [0.0]:
```

```
cflmax-real [1000.0]: 
ser-real [0.7]:
```

Parameters that define the CFL strategy (and in turn the time-step) expressed as CFL = min(max(Cfl1, Cfl2*it), Cfl0/ $\|R\|$ ^ser), CflMax), with it and R denoting respectively the time-iteration index and the spatial residual.

Note:

- 1. for one-dimensional two-phase flow computations (<u>Problem</u>.Type = 1D), only explicit time-integration is currently available.
- Implicit
- Explicit

Next: Explicit, Up: Time

4.14.1 DEFINING THE IMPLICIT TIME-INTEGRATION

Object: Implicit

The Implicit object defines how the system of nonlinear equations is solved at every time-step. Its syntax is:

```
under Implicit {
   Type = type-id;
   MatrixVectorProduct = mvp-id;
   FiniteDifferenceOrder = fdorder-id;
   TurbulenceModelCoupling = tmcoupling-id;
   under Newton { ... }
}
```

with

type-id [BackwardEuler]:

BackwardEuler

First-order time-integration based on the backward Euler scheme. This is the default and only time-integrator available for steady-state computations.

ThreePointBackwardDifference

Second-order time-integration based on the three-point backward difference scheme.

mvp-id [Approximate]:

Approximate

Relevant only for the case where second-order accuracy in space is specified. In this case, matrix-vector products are based on an approximate Jacobian matrix obtained by linearizing the first-order approximation of

the convective flux and the second-order approximation of the diffusive one.

Exact

Matrix-vector products are based on the exact Jacobian matrix. Currently, this option is available only for flow simulations using the perfect gas Equation of State (EOS), Roe's numerical flux, and without low-Mach preconditioning. For flow simulations using any other EOS or numerical flux, or with low-Mach preconditioning, and for the generalized level set equation(s), this option reverts to the finite difference option with *fdorder-id* = FirstOrder.

FiniteDifference

Matrix-vector products are based on a finite-difference formula of the combined convective and viscous fluxes. This allows to capture the effect of the exact Jacobian matrix without having to compute and to store it.

fdorder-id [FirstOrder]:

This option is available only when *mvp-id* (MatrixVectorProduct) is set to FiniteDifference. It specifies the order of the finite difference approximation of the product of the Jacobian matrix of the implicit scheme with a vector, independently from the order of the spatial discretization of the problem.

FirstOrder

In this case, the finite differencing scheme is a first-order finite-difference formula that requires only one residual evaluation per computation.

SecondOrder

In this case, the finite differencing scheme is a more accurate (at least in principle) second-order finitedifference formula that requires however two residual evaluations per computation.

tmcoupling-id [Weak]:

This object member is relevant only for simulations with turbulence modeling. The following description of the usage of this parameter refers to a two-by-two block partitioning of the Jacobian of the coupled Navier-Stokes and turbulence model equations, according to the flow and turbulence model unknowns.

Weak

In this case, the Jacobian of the implicit problem is approximated by a blog diagonal matrix. Therefore, the linearized flow and turbulence model equations are decoupled at each step of the Newton method. This also implies that the parameters of the linear equation solver can be adjusted separately for the flow equations using LinearSolver.NavierStokes, and the turbulence model equations using LinearSolver.TurbulenceModel (see <u>LinearSolver</u>).

Strong

In this case, the Jacobian of the implicit problem accounts for the coupling of the flow and turbulence model equations. Consequently, the fully coupled linearized flow and turbulence model equations are solved at each step of the Newton method. In this case also, the parameters of the linear equation solver must be specified under LinearSolver.NavierStokes only, and any input to the object LinearSolver.TurbulenceModel is ignored by **AERO-F** (see <u>LinearSolver</u>).

Note:

- for LES, dynamic LES, VMS-LES, and dynamic VMS-LES computations, the source terms associated with turbulence modeling are explicitized and therefore do not contribute to the Jacobian matrix of the implicit scheme.
- Newton

Previous: Implicit, Up: Time

4.14.2 DEFINING THE EXPLICIT TIME-INTEGRATION



The Explicit object defines how the system of nonlinear equations is advanced at every time-step using an explicit scheme.

Currently, explicit time-integration is not supported for usage with the AERO-FL module. Hence, the UnsteadyLinearized, UnsteadyLinearizedAeroelastic, PODConstruction, PODInterpolation, ROM and ROMAeroelastic options in the Problem object cannot be specified together with explicit time-integration.

The syntax of Explicit is:

```
under Explicit {
  Type = type-id;
}
```

with

type-id [RungeKutta4];

RungeKutta4

Fourth-order time-accurate, four-stage, Runge-Kutta scheme.

RungeKutta2

Second-order time-accurate, two-stage, Runge-Kutta scheme.

Next: Forced, Previous: Time, Up: Objects

4.15 SOLVING A SYSTEM OF NONLINEAR EQUATIONS



The use of a Newton method to solve a system of nonlinear equations occurs in the Implicit (see Implicit) and MeshMotion (see MeshMotion) objects. The syntax of the Newton object is:

```
under Newton {
  MaxIts = maxits-int;
```

```
FailSafe = failsafe-str;
       EpsRelRes = epsrelres-real; (or Eps = eps-real;)
       EpsAbsRes = epsabsres-real;
       EpsAbsInc = epsabsinc-real;
       under LinearSolver { ... }
maxits-int [1]:
```

Maximum number of nonlinear iterations.

failsafe-str [0ff]:

0n

with

This command is relevant only if reconstruction-id is set to Linear — that is, for second-order space discretization (see NavierStokes). In this case, when a negative pressure and/or density is encountered during a Newton iteration, the Newton iteration is repeated with the nodal gradients set to zero at the points where the pressure and/or density are negative. The calculation of the nodal gradients is re-activated however at these points at the next iteration.

Always0n

This command is relevant only if reconstruction-id is set to Linear — that is, for second-order space discretization (see NavierStokes). When the fails afe-str is set to Always on and a negative pressure and/or density is encountered during a Newton iteration, the Newton iteration is repeated with the nodal gradients set to zero at the points where the pressure and/or density are negative. In this case, this treatment is maintained at these points in all subsequent Newton iterations.

0ff

This command is relevant only if reconstruction-id is set to Linear — that is, for second-order space discretization (see NavierStokes). In this case, when a negative pressure and/or density is encountered during a Newton iteration, AERO-F is stopped and an error message is output on the screen.

epsrelres-real (or eps-real) [0.01]:

Tolerance for monitoring at each k -th Newton iteration the convergence of the Eucledian norm of the relative value of the nonlinear residual r^k . Convergence of the Newton process is declared whenever either of the following criteria is satisfied

$$\|r^k\|_2=0$$
 or $\|r^k\|_2\leq epsrel res-real$ $\|r^0\|_2$

or

$$k>0$$
 and $\|r^k\|_2 \leq epsabsres-real$ and $\|x^k-x^{k-1}\|_2 \leq epsabsinc-real$

where r^0 is the initial value of the nonlinear residual, x^k and r^k are the iterate solution at the k -th Newton

iteration and its corresponding residual, respectively, and *epsabsres-real* and *epsabsinc-real* are defined below.

epsabsres-real [MachinePrecision]:

Tolerance for monitoring at each k -th Newton iteration the convergence of the Eucledian norm of the (absolute) value of the nonlinear residual r^k . Convergence of the Newton process is declared whenever either of the following criteria is satisfied

$$\|r^k\|_2=0$$
 or $\|r^k\|_2\leq epsrelres ext{-real}\ \|r^0\|_2$

or

$$k>0$$
 and $\|r^k\|_2 \leq epsabsres-real$ and $\|x^k-x^{k-1}\|_2 \leq epsabsinc-real$

where r^0 is the initial nonlinear residual, x^k and r^k are the iterate solution at the k-th Newton iteration and its corresponding residual, respectively, *epsrelres-real* is defined above, and *epsabsinc-real* is defined below. The default value for *epsabsres-real* is the machine precision for double precision arithmetics (the difference between 1 and the smallest representable value that is greater than 1) which is typically of the order of 1e-16. Hence, it is sufficiently small so that by default, the convergence criterion of the Newton process is in principle based on the Eucledian norm of the relative value of the nonlinear residual r^k .

epsabsinc-real [MachinePrecision]:

Tolerance for monitoring at each k -th Newton iteration the Eucledian norm of the incremental solution of the nonlinear problem being solved. Convergence of the Newton process is declared whenever either of the following criteria is satisfied

$$\|r^k\|_2=0$$
 or $\|r^k\|_2\leq epsrelres{-real}\|r^0\|_2$

or

$$k>0$$
 and $\|r^k\|_2 \leq epsabsres-real$ and $\|x^k-x^{k-1}\|_2 \leq epsabsinc-real$

where r^0 is the initial nonlinear residual, and r^k and r^k are the iterate solution at the r^k -th Newton iteration and its corresponding residual, respectively, and *epsrelres-real* and *epsabsres-real* are defined above. The default value of *epsabsinc-real* is the machine precision for double precision arithmetics (the difference between 1 and the smallest representable value that is greater than 1) which is typically of the order of 1e-16. Hence, it is sufficiently small so that by default, the convergence criterion of the Newton process is in principle based on the Eucledian norm of the relative value of the nonlinear residual r^k .

LinearSolver:

Specifies the linear equation solver (and its parameters) to be used at each Newton iteration.

Note:

- 1. when *failsafe-str* is set to 0n or Always0n and a negative pressure and/or density is encountered during a Newton iteration, no information is recorded in the restart file about the whereabout of that negative pressure and/or density. As a result, the first residual obtained after a restart operation may differ from the last residual computed in the previous run.
- LinearSolver

Up: Newton

4.15.1 SOLVING A SYSTEM OF LINEAR EQUATIONS

```
Object: LinearSolver
```

The object LinearSolver specifies how a linearized system of equations is solved at each Newton iteration, or during a sensitivity analysis (see <u>SensitivityAnalysis</u> and <u>Sensitivities</u>). Its syntax is:

```
under LinearSolver {
    under NavierStokes (or TurbulenceModel or LevelSet){
    Type = type-id;
    Output = output-str;
    MaxIts = maxits-int;
    KrylovVectors = krylov-int;
    Eps = eps-real;
    under Preconditioner { ... }
    }
}
with
```

Gmres

Generalized minimum residual algorithm.

Richardson

Richardson's algorithm.

Cg

Conjugate gradient algorithm. This linear equation solver is applicable only to the system of equations associated with mesh motion (see <u>MeshMotion</u>).

Gcr

Generalized conjugate residual algorithm.

```
output-str [""]:
```

Name of the ASCII file that contains the sequence of linear residuals. If *output-str* is set to "stdout" ("stderr") the linear residuals are printed on the standard I/O stream stdout (stderr).

maxits-int [30]:

Maximum number of linear iterations.

krylov-int [30]:

Number of search directions (only for the GMRES algorithm).

eps-real [0.01]:

Relative decrease of the linear residual.

Preconditioner:

Specifies the preconditioner to be used with the linear equation solver.

Notes:

when Implicit.TurbulenceModelCoupling is set to Weak — that is, the contributions of the linearizations of the mean flow and turbulence model equations to the Jacobian of the implicit problem are decoupled (see Implicit) — or the "ghost fluid method of the poor" for which the level set and flow equations are also decoupled is specified (see MultiPhase) for the solution of a multi-phase problem, the parameters of the linear equation solver should be specified separately for each independent system of equations. In such cases, the definition of the LinearSolver object within the Newton object (see Newton) becomes

```
under LinearSolver {
  under NavierStokes { ... }
  under TurbulenceModel { ... }
  under LevelSet { ... }
}
```

with

NavierStokes:

Specifies the linear solver for the Euler or averaged Navier-Stokes equations by specifying all parameters described at the beginning of this section under this object.

TurbulenceModel:

Specifies the linear solver for the turbulence model equation(s) by specifying all parameters described at the beginning of this section under this object.

LevelSet:

Specifies the linear solver for the level set equation(s) by specifying all parameters described at the beginning of this section under this object.

2. when Implicit.TurbulenceModelCoupling is set to Strong — that is, the contributions of the linearizations of the mean flow and turbulence model equations to the Jacobian of the implicit problem are coupled (see Implicit) — the parameters of the linear equation solver should be specified for the NavierStokes object only because a single set of coupled equations is solved in terms of both the flow and turbulence model variables. In this case, the definition of the object LinearSolver within the object Newton (see Newton) becomes

```
under LinearSolver {
 under NavierStokes { ... }
```

SolverPreconditioner

Up: LinearSolver

4.15.1.1 ACCELERATING A LINEAR SOLVER

Object: **Preconditioner**

To increase the efficiency of the linear solver, it can be preconditioned. The preconditioners currently available are described within the Preconditioner object. Its syntax is:

```
under Preconditioner {
       Type = type-id;
       Fill = fill-int;
with
type-id [Ras]:
Identity
      No preconditioner.
Jacobi
      Jacobi preconditioner.
Ras
      Restricted additive Schwarz algorithm.
```

fill-int [0]:

Level of fill for the incomplete LU factorization used in the restricted additive Schwarz algorithm.

Next: Accelerated, Previous: Newton, Up: Objects

4.16 IMPOSING FORCED OSCILLATIONS

Object:	Forced
---------	--------

The Forced object enables the simulation of flow problems on dynamic meshes set in a prescribed oscillatory motion, if the problem type (type-id) is set to Forced (see Problem). This motion can be associated with the prescribed heaving or pitching of a rigid obstacle, or the prescribed deformation of a flexible obstacle. The syntax of the Forced object is:

```
under Forced {
       Type = type-str;
       Frequency = frequency-real;
      TimeStep = timestep-real;
      under Heaving{ ... }
       under Pitching{ ... }
       under Deforming{ ... }
with
```

type-str [Deforming]:

Specifies a heaving, pitching, or deforming type of forced oscillations of the obstacle.

frequency-int [—]:

Frequency of the prescribed oscillatory motion.

timestep-real [—]:

Computational time-step for sampling the prescribed oscillatory motion.

Heaving:

Prescribes a rigid heaving motion.

Pitching:

Prescribes a rigid pitching motion.

Deforming:

Prescribes a motion associated with a flexible obstacle.

- Heaving
- Pitching
- Deforming

Next: Pitching, Up: Forced

4.16.1 DESCRIBING A PRESCRIBED HEAVING MOTION

Object: Heaving

This object can be used to specify the following heaving motion of a rigid obstacle

$$x = x_0 + a(1 - \cos(2\pi f t))$$

and move the fluid mesh accordingly. In the above equation, x_0 denotes the initial position of the fluid mesh (or its surfacic component), a denotes the vector amplitude of the displacement of the fluid mesh (or the obstacle), f its frequency specified in *frequency-int* of object Forced (see Forced), and x denotes either the position of the entire fluid mesh or that of the surfacic fluid mesh. In the latter case, the motion of the remaining fluid grid points is computed using a mesh updating algorithm to be specified (see MeshMotion). The syntax of the Heaving object is:

```
under Heaving{
  Domain = domain-id;
  AX = ax-real;
  AY = ay-real;
  AZ = az-real;
}
```

with

domain-id [Volume];

Volume

In this case, the entire fluid mesh is set into the specified heaving motion.

Surface

In this case, only the surfacic mesh is set into the specified heaving motion and the position of the remaining fluid grid points is computed by one of AERO-F's mesh motion algorithms to be specified (see MeshMotion).

ax-real [0.0]:

x component of the vector amplitude of the motion.

ay-real [0.0]:

y component of the vector amplitude of the motion.

az-real [0.0]:

z component of the vector amplitude of the motion.

Next: Deforming, Previous: Heaving, Up: Forced

4.16.2 DESCRIBING A PRESCRIBED PITCHING MOTION

Object: Pitching

This object can be used to specify the following pitching motion of a rigid obstacle

$$x = x_0 + \left[\mathbf{R}(\alpha_0 + \alpha_{max}\sin(2\pi ft)) - \mathbf{I}\right]x_0$$

where x_0 denotes the initial position of the fluid mesh (or its surfacic component), \mathbf{R} denotes the rotation matrix around a specified pitching axis, α_0 denotes the desired initial pitch angle of the obstacle, α_{max} the desired final pitch angle of the obstacle, f the frequency of the oscillations specified in *frequency-int* of the object Forced, f denotes the identity matrix, and f denotes either the position of the entire fluid mesh or that of the surfacic fluid mesh. In the latter case, the motion of the remaining fluid grid points is computed using a mesh updating algorithm to be specified (see MeshMotion).

The syntax of the Pitching object is:

```
under Pitching{
   Domain = domain-id;
   Alpha0 = alpha0-real;
   AlphaMax = alphamax-real;
   X1 = x1-real;
   Y1 = y1-real;
   Z1 = z1-real;
   X2 = x2-real;
   Y2 = y2-real;
   Z2 = z2-real;
}
```

with

domain-id [Volume];

Volume

In this case, the entire fluid mesh is set into the specified pitching motion.

Surface

In this case, only the surfacic mesh is set into the specified pitching motion and the position of the remaining fluid grid points is computed by one of AERO-F's mesh motion algorithms to be specified (see MeshMotion).

alpha0-real [0.0]:

Desired initial pitch angle of the obstacle. A positive value rotates the obstacle around the axis of rotation specified below in the clockwise direction. If *alpha0-real* is non zero, AERO-F will first get the obstacle and

surrounding mesh to the position implied by this rotation.

alphamax-real [0.0]:

Desired final pitch angle of the obstacle. A positive value rotates the obstacle around the axis of rotation specified below in the clockwise direction.

x1-real [0.0]:

x-component of the first point defining the axis of pitching.

y1-real [-1.0]:

y-component of the first point defining the axis of pitching.

z1-real [0.0]:

z-component of the first point defining the axis of pitching.

x2-real [0.0]:

x-component of the second point defining the axis of pitching.

y2-real [1.0]:

y-component of the second point defining the axis of pitching.

z2-real [0.0]:

z-component of the second point defining the axis of pitching.

Previous: Pitching, Up: Forced

4.16.3 DESCRIBING A PRESCRIBED MOTION ASSOCIATED WITH A FLEXIBLE OBSTACLE

Object: **Deforming**

This object can be used to specify the following motion associated with a flexible obstacle

$$x = x_0 + \alpha(x_f - x_0)\sin(2\pi ft)$$

where

 x_0 and x_f denote the initial and final mesh positions, α is an amplification factor, and f is the frequency of the oscillations.

The syntax of the Deforming object is:

```
under Deforming {
    Domain = domain-id;
    Position = position-str;
    Amplification = amplification-real;
}
with

domain-id [Volume];
```

Volume

In this case, the entire fluid mesh is set into the specified deforming motion.

Surface

In this case, only the surfacic mesh is set into the specified deforming motion and the position of the remaining fluid grid points is computed by one of AERO-F's mesh motion algorithms to be specified (see MeshMotion).

position-str [""]:

Name of the binary file containing the final mesh position. See <u>Hints and tips</u> for an explanation regarding how to obtain that file.

amplification-real [1.0]:

Amplification factor.

Next: Aeroelastic, Previous: Forced, Up: Objects

4.17 ACCELERATING THE MESH

Object: Accelerated

AERO-F can be used to compute a flow around a rigid or flexible obstacle set in accelerated motion. In this case, the "hybrid wind tunnel" framework of computation (see Figure HWT) is adopted — that is, an increase of the free-stream velocity associated with an acceleration of the obstacle is accounted for by accelerating accordingly the ALE mesh. In other words, the motion of the obstacle, which is initially at the free-stream velocity then accelerated, is represented in a frame moving at the free-stream velocity with respect to the ground. The accelerated motion can be characterized either by a constant acceleration field, or deduced from a piecewise linear velocity time-profile that is specified in the TimeVelocity object. For an obstacle moving with a piecewise linear velocity, a set of time-velocity pairs are specified. In this case, the velocity is linearly interpolated and the acceleration is approximated by a corresponding piecewise constant field.

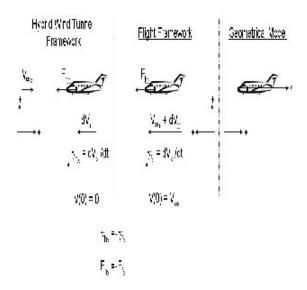


Figure HWT: the hybrid wind tunnel computational framework

The syntax of the Accelerated object is:

```
under Accelerated {
   Tag = tag-id;
   LawType = lawtype-id;
   AccelerationX = acc-x-real;
   AccelerationZ = acc-y-real;
   AccelerationZ = acc-z-real;
   TimeStep = timestep-real;
   under TimeVelocity1 { ... }
}
```

tag-id [Mach]:

Mach

The value associated with the sequence of outputed nodal values (see <u>Postpro</u>) is the free-stream Mach number.

Velocity

The value associated with the sequence of outputed nodal values (see <u>Postpro</u>) is the free-stream velocity magnitude.

Time

The value associated with the sequence of outputed nodal values (see Postpro) is the time.

lawtype-id [ConstantAcceleration]:

ConstantAcceleration

The obstacle has a constant acceleration given by AccelerationX, AccelerationY, and AccelerationZ. The sign convention is that of the hybrid wind tunnel computational framework graphically depicted in Figure HWT. For example, a positive acceleration in the x direction corresponds to a physical deceleration.

VelocityLaw

The obstacle has a piecewise linear in time velocity specified by the TimeVelocity objects.

acc-x-real [0.0]:

Constant acceleration of the obstacle in the x-direction. The sign convention is that of the hybrid wind tunnel computational framework graphically depicted in Figure HWT.

acc-y-real [0.0]:

Constant acceleration of the obstacle in the y-direction. The sign convention is that of the hybrid wind tunnel computational framework graphically depicted in Figure HWT.

acc-z-real [0.0]:

Constant acceleration of the obstacle in the z-direction. The sign convention is that of the hybrid wind tunnel computational framework graphically depicted in Figure HWT.

timestep-real [—]:

Time-step. If this specified time-step is larger than the specified or CFL-induced time-step of the flow-solver, the flow-solver will subcycle.

TimeVelocity1:

Defines the velocity at a specified time. Its syntax is defined by the object TimeVelocity.

Note:

1. acceleration can affect the angle of attack. For example, the acceleration along the x-axis shown in Figure Acceleration causes the angle of attack to decrease in time. On the other hand, for this example, an acceleration along both x- and z-axes with the ratio *acc-z-reallacc-x-real* equal to the tangent of the angle of attack will maintain the angle of attack constant in time.

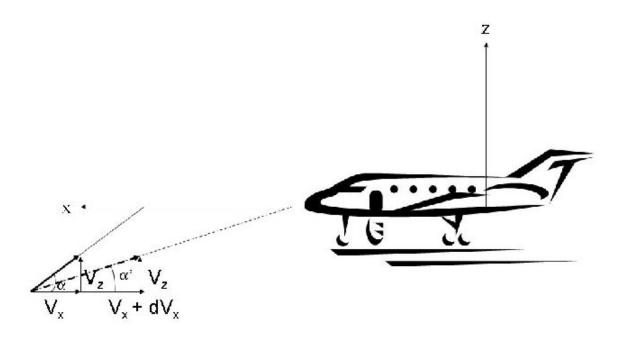


Figure Acceleration: example of the effect of acceleration on the angle of attack

• <u>TimeVelocity</u>

Up: Accelerated

4.17.1 SPECIFYING A VELOCITY AT A GIVEN TIME

Object: TimeVelocity

The TimeVelocity object specifies the velocity of an obstacle at a certain time.

```
under TimeVelocity1 {
   Time = time-real;
   VelocityX = v-x-real;
   VelocityY = v-y-real;
   VelocityZ = v-z-real;
}
```

with

time-real [—]

Specified time.

```
v-x-real [0.0]
```

Velocity of the obstacle in the x-direction at the specified time.

```
v-y-real [0.0]
```

Velocity of the obstacle in the y-direction at the specified time.

```
v-z-real [0.0]
```

Velocity of the obstacle in the z-direction at the specified time.

Notes:

- 1. currently, only 10 time-velocity pairs can be specified.
- it is implied that the first time-velocity pair is not specified by any TimeVelocity object. It is rather
 automatically generated using zero for the initial time and the free-stream flow conditions for the initial
 velocity (Mach number and angles of attack). It is also assumed that the TimeVelocity objects are ordered with
 increasing time;
- 3. from the above, it follows that the first specified time must be different from zero;
- 4. when the time is greater than the time specified in the last TimeVelocity object, the velocity is assumed to be constant and set to the value specified by the last TimeVelocity object.

Next: MeshMotion, Previous: Accelerated, Up: Objects

4.18 SPECIFYING AEROELASTIC PARAMETERS

Object: Aeroelastic

Aeroelastic parameters are specified within the Aeroelastic object. Its syntax is:

```
under Aeroelastic {
    Force = force-id;
    InternalPressure = pressure-real;
}

force-id [Last]:
```

Last

The local aerodynamic forces exchanged with the structure code are based on the last computed pressure field within a cycle of the staggered solution procedure.

Averaged

The local aerodynamic forces exchanged with the structure code are based on the time-averaged pressure field within a cycle of the staggered solution procedure.

pressure-real [0.0]:

When computing the generalized local aerodynamic forces exerted on the surface of an obstacle, **AERO-F** always assumes the presence of a uniform pressure field within (or from the dry side of) the obstacle; therefore, it computes the net generalized forces due to both the external and internal (or dry side) pressure fields. The *pressure-real* parameter specifies the value of the uniform pressure field within (or from the dry side of) the obstacle (the default value is 0). The reader should note that for an obstacle with a closed surface, this feature, which is very convenient for aeroelastic computations, has no effect on the values of the global generalized aerodynamic forces. It affects however the resulting displacements and stresses of the obstacle.

Next: EmbeddedFramework, Previous: Aeroelastic, Up: Objects

4.19 MOVING THE MESH



For a simulation on a moving grid, the MeshMotion object constructs a strategy and specifies an algorithm for updating the position of the grid points of the CFD mesh. In general, the motion of the interior grid points is driven by that of the points lying on the surfaces of the CFD mesh (see the **CD2TET** user manual for the mesh motion attributes of the various types of surfaces recognized by **AERO-F**). Therefore, the mesh motion conventions of three important types of surfaces are first discussed below.

The mesh motion of the nodes on a moving wall can be either prescribed (see <u>Forced</u>), or obtained via communication with **AERO-S** during a fluid-structure simulation.

The nodes on a sliding plane (see <u>SurfaceData</u>) slide in this plane — that is, the component of their displacement field along the specified normal to the sliding plane is constrained to zero.

By default, the nodes of a symmetry plane are fully restrained — that is, their motion is set to zero. However, there is one exception to this rule. If *type-id* of this MeshMotion object is set to *Corotational*, **AERO-F** does not necessarily fully restrain (set to zero) the motion of the nodes of a symmetry plane (see Symmetry). Furthermore, if desired — for example, to prevent mesh crossovers near a moving wall — the nodes of a symmetry plane can be forced to slide within this plane if it is also explicitly declared as a sliding plane (see SurfaceData). In this case, if *type-id* of the MeshMotion object is set to *Corotational* (see MeshMotion object (see Symmetry).

The syntax of the MeshMotion is:

```
under MeshMotion {
  Type = type-id;
  Element = element-id;
  VolumeStiffness = stiffness-factor;
  Mode = mode;
  NumIncrements = numincrements;
  FeedBack = feedback-frequency;
```

```
under Symmetry { ... }
under Newton { ... }
}
with

type-id [Basic]:
```

Basic

In this case, no special treatment is applied to potentially large displacements and/or deformations.

Corotational

In this case, potentially large displacements and/or deformations are handled by the corotational method, which is applied in addition to the chosen mesh motion algorithm. The corotational method separates the motion of the moving walls into two components: a rigid one that is trivially transmitted to the interior mesh points, and a deformational one that is treated by the chosen mesh motion algorithm.

element-id [BallVertexSprings]:

FiniteElement

Specifies the mesh motion method based on the linear finite element structural analogy.

NonLinearFiniteElement

Specifies the mesh motion method based on the nonlinear finite element structural analogy. This method can be equipped with a safeguard against mesh instabilities (not to be confused with mesh crossovers, see *stiffness-factor* below). It does not suffer from the hysterisis phenomenon and therefore is suitable for long cyclic problems.

TorsionalSprings

Specifies the mesh motion method based on the linear torsional springs analogy. This method can also be equipped with a safequard against mesh instabilities (not to be confused with mesh crossovers, see *stiffness-factor* below). It is a good candidate for problems with large-amplitude mesh deformations.

BallVertexSprings

Specifies the mesh motion method based on the linear ball vertex springs analogy. This method can also be equipped with a safeguard against mesh instabilities (not to be confused with mesh crossovers, see *stiffness-factor* below). It is a good candidate for problems with large-amplitude mesh deformations and is more economical than the torsional springs method.

${\tt NonlinearBallVertexSprings}$

Specifies the nonlinear version of the ball vertex springs method. This method can also be equipped with a safeguard against mesh instabilities (not to be confused with mesh crossovers, see *stiffness-factor* below). It does not suffer from the hysterisis phenomenon and therefore is a good candidate for long cyclic problems with large-amplitude mesh deformations.

```
stiffness-factor [0.0]:
```

This parameter is active for all mesh motion algorithms except that based on the linear finite element method (*element-id* = FiniteElement). When **positive**, it adds to the basic pseudo-stiffness of an element — which is usually

inversely proportional to its volume in order to prevent mesh crossovers — a positive term that is proportional to its volume and multiplied by *stiffness-factor*, thereby preventing this element from becoming increasingly flexible when stretched and causing a mesh instability. By default, the value of this parameter is zero, which does not provide additional stiffening during stretching. The higher the value of this parameter is, the stiffer the pseudo-structure becomes when stretched and the less likely to induce a mesh instability. However, as the value of this parameter is increased, the conditioning of the corresponding pseudo-stiffness matrix becomes worse, and more iterations may become necessary for updating the position of the mesh.

mode [NonRecursive]:

The prescribed boundary displacement field can be applied in multiple increments (or fractions) to minimize the likelyhood of crossovers during the mesh motion. The number of increments can be specified is *numincrements* (see below).

NonRecursive

If *mode* is set to NonRecursive (which is the default value), then the prescribed boundary displacement field is applied in *numincrements* equal increments and the stiffness of the mesh is updated at each step.

Recursive

If *mode* is set to Recursive, the prescribed boundary displacement field is recursively applied in fractions computed so that, in principle, the motion of the moving surface does not exceed, for a given fraction (except possibly the last one), the thickness of the first layer of elements above this surface. In this case, the stiffness of the mesh is also updated at each step and *numincrements* defines the maximum number of allowable increments.

numincrements [1]:

This parameter defines either the number of increments in which to apply the prescribed boundary displacement field when *mode* is set to NonRecursive, or the maximum number of allowable fractions of this displacement when *mode* is set to Recursive. The default value is 1.

feedback-frequency [0]:

Feedback on the performance of the choice made in *mode* is available in the form of output to the screen of the minimum and maximum applied fractions of a prescribed wall-boundary displacement. The feedback is printed every *feedback-frequency* iterations/time-steps of a steady/unsteady computation. It is useful for checking, when *mode* is set to Recursive, whether a large discrepancy occurs between the minimum and maximum applied fractions of the prescribed wall-boundary displacement, in which case setting *mode* to NonRecursive would produce a better performance of the chosen mesh motion algorithm. Setting *feedback-frequency* to zero (default) results in turning off this option.

Newton:

Specifies the parameters of the Newton method for solving the nonlinear system of discrete equations.

Symmetry:

Acknowledges the presence of a symmetry plane in the mesh so that the mesh motion solver can constrain the solution of the mesh motion equations appropriately.

Note:

- the default value for Newton.LinearSolver.Type is Cg while the default value for Newton.LinearSolver.Preconditioner.Type is Jacobi;
- BoundaryLayer
- Symmetry
- Newton

Up: MeshMotion

4.19.1 MESH MOTION IN THE PRESENCE OF A PLANE OF SYMMETRY



For a simulation on a moving grid, this object should be specified within the mesh motion object (see MeshMotion) when *type-id* of the MeshMotion object is set to *Corotational* (see MeshMotion), the computational domain contains a symmetry plane, and it is desired to fully restrain the nodes of this symmetry plane or constrain their motion to sliding within the symmetry plane.

The syntax of the Symmetry object is:

```
under Symmetry {
  Nx = Nx-real;
  Ny = Ny-real;
  Nz = Nz-real;
}
```

with

Nx-real [0.0]:

The x-component of the normal to the symmetry plane.

Ny-real [0.0]:

The y-component of the normal to the symmetry plane.

Nz-real [0.0]:

The z-component of the normal to the symmetry plane.

Notes:

- 1. currently, **AERO-F** allows only one plane of symmetry if the simulation involves a moving grid and requires this plane of symmetry to be parallel to one of the three canonical planes;
- 2. if *type-id* of the MeshMotion object is set to *Corotational* (see MeshMotion) and the Symmetry object is specified, the nodes of a symmetry plane will "rigidly" slide within this plane. To have them slide while allowing deformation of the elements they are attached to, the user must also declare the symmetry plane a sliding plane (see SurfaceData).

Next: Linearized, Previous: MeshMotion, Up: Objects

4.20 SPECIFYING THE EMBEDDED BOUNDARY METHOD FOR CFD

```
Object: EmbeddedFramework
```

The object EmbeddedFramework is primarily used to specify **AERO-F**'s embedded boundary method for CFD. This method is activated however only if Problem. Type is set to Embedded (see Problem). Its parameters are: (a) the specific intersector which tracks the position (and shape) of an embedded discrete surface (which can be the union of multiple disconnected embedded surfaces) representing the wet surface of an obstacle (which can be the union of multiple disconnected obstacles); and (b) the specific energy conserving algorithm for computing the flow-induced forces and moments on this embedded surface and enforcing the equilibrium transmission condition in the case of a fluid-structure simulation.

In the case of a closed embedded discrete surface, the object EmbeddedFramework is also used to specify the initial state of the fluid medium occupying the region of the computational domain enclosed by this surface.

The syntax of this object is:

```
under EmbeddedFramework {
   Intersector = intersector-id;
   SurrogateSurface = surrogatesurface-id;
   under InitialConditions { ... }
}
```

with

intersector-id [FRG]:

Specifies a computational approach for computing the intersection of an embedded discrete surface with the embedding CFD grid in order to track in time the position and shape of this embedded surface.

FRG

In this case, a fast, projection-based approach is used for tracking the fluid-structure interface. This approach requires that the embedded surface be closed and remain closed throughout the entire simulation.

Furthermore, it is accurate only if the region enclosed by the embedded surface is resolved by the embedding

CFD grid.

PhysBAM

In this case, a slower but more general geometric-based approach is used for tracking the fluid-structure interface. This approach is equally applicable to open and closed embedded surfaces. Furthermore, it is accurate even when the embedded discrete surface is closed and the region enclosed by this surface is not resolved by the embedding CFD grid.

surrogatesurface-id [ReconstructedSurface]:

Specifies a surrogate surface on which to compute the flow-induced forces and moments and a corresponding conservative algorithm for performing this computation and that of the load transferred to the real structure in the case of a fluid-structure simulation.

ReconstructedSurface

In this case, the surrogate surface is reconstructed within **AERO-F** based on the computed intersection between the embedded discrete surface and embedding fluid mesh.

ControlVolumeFace

In this case, the surrogate surface is defined as the assembly of the control volume faces that are the closest to the computed intersection between the embedded discrete surface and embedding fluid mesh.

InitialConditions:

In the case of a closed embedded discrete surface, this object allows a convenient initialization of the state (or states) of the fluid medium (or media) occupying the region (or regions) enclosed by this surface.

InitialConditionsEmbedded

Up: EmbeddedFramework

4.20.1 SPECIFYING THE INITIAL CONDITIONS OF A MULTI-FLUID PROBLEM



This object provides a convenient way for initializing to a uniform condition the state of a fluid medium in a region of the computational fluid domain delimited by a closed embedded discrete surface. Because a closed surface can consist of multiple disconnected closed surfaces, the aforementioned region of interest is identified here by specifying a point it contains (this point does not need to be a CFD grid point). Because the initialization procedure depends on the EOS of the fluid medium of interest, the integer identification number of this fluid medium is also specified in Point. Finally, the initial state itself is specified in InitialState.

The syntax of this object is:

```
under InitialConditions {
  under Point[point-id-int] { ... }
...
```

```
}
```

with

point-id-int[—]

Integer identification number of a point located in a region of the computational fluid domain delimited by a closed embedded discrete surface. This point does not need to be a CFD grid point.

Point:

Specifies the coordinates of a point in space identified by *point-id-int* and the integer identification number of the fluid medium that contains it.

Point

Up: InitialConditionsEmbedded

4.20.1.1 SPECIFYING A POINT AND THE FLUID MEDIUM CONTAINING IT



This object specifies the coordinates of a point (which is not necessarily a CFD grid point) identified by *point-id-int* for the purpose of identifying the region of the computational fluid domain containing this point and delimited by an embedded discrete and closed surface. It also identifies the fluid medium occupying this region by specifying its integer identification number, and initializes its state to that of a uniform condition specified in <u>InitialState</u>.

The syntax of this object is:

```
under Point {
    FluidID = fluid-id-int;
    X = x-real;
    Y = y-real;
    Z = z-real;
    under InitialState{ ... }
}
```

fluid-id-int [—]:

Integer number identifying the fluid medium containing the point identified by point-id-int.

x-real [0.0]:

Coordinate of the point identified by *point-id-int* along the x axis.

y-real [0.0]:

Coordinate of the point identified by *point-id-int* along the y axis.

z-real [0.0]:

Coordinate of the point identified by *point-id-int* along the z axis.

InitialState:

Specified the initial conditions to be applied in the region of the computational fluid domain containing the point identified by *point-id-int* and delimited by an embedded discrete and closed surface.

• InitialState

Next: SensitivityAnalysis, Previous: EmbeddedFramework, Up: Objects

4.21 DEFINING THE PARAMETERS OF THE LINEARIZED MODULE AERO-FL

Object: Linearized

AERO-F can also be used to solve a set of linearized flow equations around a given (equilibrium) configuration when the considered fluid is a perfect gas. The module within AERO-F that performs this task is referred to as AERO-FL. This module also offers a dimensional POD-based ROM capability trained for obstacle vibrations. Currently, AERO-FL supports only the linearized Euler equations for a perfect gas, and implicit time-integration. It can be used to perform (see Problem):

- 1. an unsteady linearized Euler flow perturbation computation in the time-domain;
- 2. an unsteady linearized Euler-based aeroelastic computation in which the structure is represented by a truncated set of its natural modes (dimensional);
- 3. a construction of a time- or frequency-domain POD basis (dimensional);
- 4. a construction of a time- or frequency-domain POD basis by linear interpolation between several sets of POD basis vectors (dimensional);
- 5. a construction of a fluid ROM trained for obstacle vibrations (dimensional);
- 6. a construction of an aeroelastic ROM trained for structural vibrations (dimensional);
- 7. a time-domain ROM fluid computation (dimensional);
- 8. a time-domain ROM aeroelastic computation in which the flow is expressed in a POD basis and the structure is represented by a truncated set of its natural modes (dimensional).

The linearized Euler flow simulations are initialized by a perturbation of the steady-state flow solution around which the linearized flow was computed. This is performed by: a) perturbing a flow parameter such as the angle of attack, Mach number, altitude, or shape of the obstacle and computing a new steady-state solution, then b) specifying the obtained perturbed flow solution in Input.Perturbed (see Input). A noteworthy initialization is that in which the perturbed flow corresponds to a shape perturbation induced by a modal displacement of the structure (communicated to the fluid by a ping-pong step). In this case, and in the event of a linearized aeroelastic

computation, the structure can be conveniently initialized by the same modal displacement using Linearized. ExcMode as explained below.

Currently, a linearized Euler-based aeroelastic simulation can be driven only by a modal source term associated with the structure. For this reason, such a simulation can be performed only in dimensional mode. See <u>Problem.</u>

The syntax of the Linearized object is:

```
under Linearized{
      StrModes = strmodes-str;
      NumStrModes = numberstructuralmodes-int;
      ExcMode
                = idmodetobeexcited-int;
      Domain = domain-id;
      InitialConditions = ic-id:
      Amplification = amplitude-real;
                 = frequencystep-real;
      FreqStep
                    = finitedifferenceepsilon-real;
      Eps
      Eps2
                 = timestepepsilon-real;
      Tolerance = eigensolvertolerance-real;
              = numberPODmodes-int;
      NumPOD
      under Pade { ... }
with
strmodes-str [""]:
```

Name of the binary file containing the initial mesh position, a set of natural structural frequencies, and the set of fluid mesh positions that are compatible with the corresponding set of natural structural modes. This information is needed to construct a fluid POD basis, a fluid ROM, or an aeroelastic ROM. It can also be used to create a source term to drive a (full-order or reduced-order) linearized unsteady flow simulation. Even when specified, this file is not exploited unless the corresponding entry NumStrModes is set to a non-zero positive value.

numberstructuralmodes-int [0]:

Specifies the first so-many structural modes to be exploited among those specified in StrModes. If this parameter is set to 0, the StrMode file is not exploited even if specified.

idmodetobeexcited-int [1]:

This information is processed only when performing a linearized Euler-based aeroelastic simulation to be driven by a source term constructed from a modal input to the underlying structure. It identifies the structural mode to be excited by its relative position in the StrModes file. Again, this parameter has no effect if NumStrModes is set to 0.

domain-id [Time]:

Time

Specifies time-domain integration of the linearized fluid equations when generating snapshots — that is, when

Problem. Type is set to PODConstruction (see Problem).

Frequency

Specifies the solution of the linearized Euler equations in the frequency-domain.

ic-id [Displacement]:

Displacement

Specifies that the initial disturbance (excitation) originates from a structural displacement mode. Not needed when *type-id* is set to PODConstruction or to PODInterpolation. See <u>Problem</u>.

Velocity

Specifies that the initial disturbance (excitation) originates from a structural velocity mode. Not needed when *type-id* is set to PODConstruction or to PODInterpolation. See <u>Problem</u>.

amplitude-real [1.0]:

Amplification factor for the time-domain initial excitation specified by ExcMode.

frequencystep-real [0]:

This variable specifies the reduced frequency stepping for the snapshots when constructing a POD basis in the frequency-domain. The first considered reduced frequency is always set to zero. The total number of considered reduced frequencies is given by MaxIts of the Time object (see <u>Time</u>).

finitedifferenceepsilon-real [1e-4]:

Perturbation parameter used for generating by finite-differencing some of the terms governing the linearized fluid equations.

timestepepsilon-real [5]:

This variable should be specified when performing a linearized simulation in order to provide a reference time for the computation of the fluid-structure coupling matrices involved in the POD construction.

eigensolvertolerance-real [1e-8]:

Tolerance for convergence criterion used in the solution of eigen problems associated with the generation of a POD basis.

numberPODmodes-int [0]:

When constructing a POD basis directly or by interpolation, this parameter specifies the number of POD modes to be constructed or interpolated between two POD basis vectors. See Problem. In direct mode, NumPOD must be smaller than StrModes*(2*MaxIts + 1). In interpolation mode, NumPOD must be smaller or equal to the common size of the two existing POD basis vectors input in PODData (see Input). When constructing a ROM, this parameter specifies the first so-many POD basis vectors to use among those specified in PODData (see

Input).

Pade:

Sets the parameters of the Pade-based reconstruction strategy for accelerating the computation of the snapshots during the construction of a POD basis in the frequency domain.

Notes:

- 1. currently, AERO-FL performs space-discretization using only the second-order MUSCL scheme;
- 2. currently, AERO-FL computes the gradient of the flux vector with respect to the fluid state vector using only the exact method, and all gradients with respect to mesh motion using finite differencing;
- 3. currently, AERO-FL performs time-discretization using only the three-point backward difference scheme for the fluid, the midpoint rule for the structure, the A6 staggered procedure for their coupling (see the AERO-S user manual), and a constant global time-step. However, the three-point backward difference scheme for the fluid is initialized in this case using a forward Euler scheme with a time-step equal to the square of the specified time-step in order to maintain "practical" second-order time-accuracy and avoid the pitfalls associated with trivial starting procedures for this multi-step scheme. As far as time-stepping is concerned, only TimeStep and MaxIts need be set in the Time object (see Time) when running AERO-FL. In this case, the first parameter specifies the time-step which in this case is held constant because the system is linear and the second one specifies the number of steps to be performed or half the number of snapshots per modal impulse to be generated. However, all other commands such as the Newton command which contains the LinearSolver object (see Newton, see LinearSolver) must be specified by the user;
- 4. AERO-FL initializes the three-point backward difference scheme for the fluid using a two-point explicit scheme (forward Euler) and a time-step equal to the square of the specified time-step;
- 5. currently, AERO-FL saves a constructed POD but not a constructed ROM. The reason is that constructing a POD is computationally far more expensive than constructing a ROM. Starting from a saved POD basis, AERO-FL builds a ROM on the fly and uses it to perform a time-domain simulation. However, if the user is interested in outputting a ROM for usage by another code such as, for example, MATLAB, the user can request a ROM simulation, set MaxIts to zero, and specify a filename in Postpro.ROM. In this case, the ROM is built but no time-domain simulation is performed, and the ROM is outputted in the specified output file.
- AERO-FL's POD construction capability can also be used to construct a POD basis from snapshots collected during previous dimensional or non-dimensional nonlinear simulations and saved in Postpro. StateVector (see <u>Postpro</u>).
- Pade

Up: Linearized

4.21.1 PADE-BASED RECONSTRUCTION OF SNAPSHOTS

Object:	Pade
---------	------

When constructing a POD basis in the frequency domain, snapshots are computed by sweeping over a set of reduced frequencies and solving for each one of them a system of equations with multiple right-sides (one right-side per applied structural vibration mode). These frequencies, which are determined by the parameters

Linearized.FreqStep and Time.MaxIts, are referred to here as the "fine reduced frequency points" by analogy with a "fine grid". The snapshot computation can be expedited by a reconstruction strategy that can be described as follows. The user can specify up to 11 coarse reduced frequency points referred to here as the "coarse reduced frequency points", by analogy with a "coarse grid". Then, the snapshots and their successive reduced frequency derivatives are computed at these coarse reduced frequency points only, for all specified structural vibration modes, and reconstructed on the fine reduced frequency points using a multi-point Pade approximation scheme. For each coarse reduced frequency point, the successive reduced frequency derivatives of the snapshots can be obtained by solving the same system of equations governing the snapshot itself but with a different right-side. Hence, the reconstruction strategy described here is most effective when the chosen iterative solver is tailored for systems of equations with multiple right-sides. For this reason, this Pade-based frequency sweep strategy can be activated only when the linear, Krylov-based, iterative solver is Gcr (see LinearSolver).

Furthermore, the polynomial degrees L and M of the numerator and denominator of the Pade approximation, respectively, must be chosen so that L+M+1 is a multiple of the number of coarse reduced frequency points used at one-time, in order to have a constant number of right-sides per coarse reduced frequency point.

The syntax of the Pade object is:

```
under Pade {
  Freq1 = freq1-real;
  Freq2 = freq2-real;
  Freq3 = freq3-real;
  Freq4 = freq4-real;
    .;
    .;
    .;
    Freq11 = freq11-real;
    L = numeratordegree-int;
    M = denominatordegree-int;
    NumPoints = nptspade-int;
}
with

freq1-real [-1]:
```

Value for the first coarse reduced frequency point.

numeratordegree-int [3]:

Degree of the polynomial in the numerator of the Pade approximation.

denominatordegree-int [4]:

Degree of the polynomial in the denominator of the Pade approximation.

nptspade-int [0]:

Number of coarse frequency points exploited at one-time in each Pade approximation.

Note:

1. the coarse reduced frequency points must be specified in ascending order.

Previous: Linearized, Up: Objects

4.22 SENSITIVITY ANALYSIS

Object: SensitivityAnalysis

When Problem. Type is set to SteadySensitivityAnalysis, the user can request in the object Postpro the computation and output of sensitivities (gradients) of aerodynamic-related quantities q_i with respect to a speficied set of flow and shape parameters s_j , at a steady-state fluid solution specified in Input. Solution (see Sensitivities). The object SensitivityAnalysis is used to set the parameters of the underlying sensitivity analysis.

The aerodynamic quantities q_i for which **AERO-F** can evaluate sensitivities $\frac{dq_i}{ds_i}$ at a specified steady-state flow

solution are (see <u>Postpro</u>):

- 1. The aerodynamic forces and moments.
- 2. The nodal density values.
- 3. The nodal velocity values.
- 4. The nodal Mach number values.
- 5. The nodal temperature values.
- 6. The nodal pressure values.
- 7. The nodal total pressure values.
- 8. The nodal fluid state-vector (conservative variables) values.
- 9. The nodal mesh displacement values.

The parameters s_j with respect to which **AERO-F** can compute sensitivities $\frac{dq_i}{ds_j}$ at a specified steady-state flow

solution are:

- 1. The free-stream Mach number.
- 2. The free-stream angle of attack.
- 3. The free-stream sideslip angle.
- 4. One or several shape parameters (of the obstacle).

Notes:

- 1. currently, sensitivities can be computed only when the computational fluid domain is discretized by a tetrahedral mesh, the fluid is modeled as a perfect gas, and turbulence modeling if any is performed using the modified form of the Spalart-Allmaras turbulence model, the Detached Eddy Simulation (DES) model, or the $k \epsilon$ turbulence model (see TurbulenceModel);
- 2. performing a sensitivity analysis requires specifying a mesh motion algorithm in <u>MeshMotion</u> in order to determine the interior components of the mesh shape gradients (see <u>Sensitivities</u>);
- 3. for a sensitivity analysis, <u>Problem</u>. Type must be set to SteadySensitivityAnalysis, <u>Problem</u>. Mode must be set to Dimensional, <u>FarField</u>. Type must be set to StegerWarming, and <u>MeshMotion</u>. Type must be set to Basic;
- 4. also for a sensitivity analysis, the linearized fluid system of equations and the mesh motion equation must be solved very precisely (see <u>Sensitivities</u>);
- 5. in the presence of a low-mach preconditioner, **AERO-F** automatically sets <u>Implicit</u>.MatrixVectorProduct and <u>Implicit</u>.FiniteDifferenceOrder to FiniteDifference and 2, respectively, for the purpose of sensitivity analysis;
- 6. when turbulence is modeled using the modified form of the Spalart-Allmaras model (see <u>TurbulenceModel</u>), AERO-F automatically sets <u>Implicit</u>.TurbulenceModelCoupling to Strong for the purpose of sensitivity analysis; in this case however, the sensitivity analysis with respect to a shape parameter may not be accurate because currently, AERO-F does not account for the variation of the distance to the wall with a shape parameter;
- 7. when <u>Implicit</u>.MatrixVectorProduct is set to Approximate, **AERO-F** automatically changes this setting to FiniteDifference and sets FiniteDifferenceOrder to 2, for the purpose of sensitivity analysis.

The syntax of the object SensitivityAnalysis is:

```
under SensitivityAnalysis{
    SensitivityComputation = sensitivitycomputation-id;
    SensitivityMesh = sensitivitymesh-flag;
    SensitivityMach = sensitivityMach-flag;
    SensitivityAlpha = sensitivityalpha-falg;
    SensitivityBeta = sensitivitybeta-flag;
    EpsFD = epsfd-real;
    under LinearSolver{ ... }
}
```

sensitivitycomputation-flag [Analytical]

Analytical

Requests the analytical computation of the derivatives appearing in the right-hand side of the linearized fluid system of equations and of the gradients of the aerodynamic forces and moments with respect to the specified flow and shape parameters (see <u>Sensitivities</u>). However, if the flow is viscous and turbulence is modeled using the DES model (see <u>TurbulenceModel</u>), **AERO-F** automatically resets *sensitivitycomputation-flag* to FiniteDifference. If the flow is viscous and modeled using the k - ϵ turbulence model instead (see

TurbulenceModel), AERO-F automatically resets sensitivitycomputation-flag to SemiAnalytical.

SemiAnalytical

Requests the approximation by the second-order central finite difference method of the derivatives appearing in the right-hand side of the linearized fluid system of equations, and the analytical computation of the gradients of the aerodynamic forces and moments with respect to the specified flow and shape parameters (see <u>Sensitivities</u>). However, if the flow is viscous and turbulence is modeled using the DES model (see <u>TurbulenceModel</u>), **AERO-F** automatically resets *sensitivitycomputation-flag* to FiniteDifference.

FiniteDifference

Requests the approximation by the second-order central finite difference method of the derivatives appearing in the right-hand side of the linearized fluid system of equations and of the gradients of the aerodynamic forces and moments with respect to the specified flow and shape parameters (see Sensitivities).

sensitivitymesh-flag [0ff]

0n

This flag setting specifies that the computation of the sensitivities requested in <u>Postpro</u> be (also) performed with respect to shape parameters \mathbf{s}_{j} . The user does not need to specify these shape parameters directly.

Instead, the user should specify in this case the wall boundary components of the mesh shape gradients in the binary file inputted in <u>Input</u>. ShapeDerivative (see <u>Sensitivities</u>). Failure to input this binary file results in skipping the computation of the sensitivities requested in <u>Postpro</u> with respect to any shape parameter.

Off

In this case, no sensitivity requested in **Postpro** is computed with respect to a shape parameter.

sensitivityMach-flag [0ff]

0n

This flag setting specifies that the computation of the sensitivities requested in <u>Postpro</u> be (also) performed with respect to the free-stream Mach number.

Off

In this case, no sensitivity requested in <u>Postpro</u> is computed with respect to the free-stream Mach number.

sensitivityalpha-flag [0ff]

0n

This flag setting specifies that the computation of the sensitivities requested in <u>Postpro</u> be (also) performed with respect to the free-stream angle of attack.

0ff

In this case, no sensitivity requested in <u>Postpro</u> is computed with respect to the free-stream angle of attack.

sensitivitybeta-flag [0ff]

0n

This flag setting specifies that the computation of the sensitivities requested in <u>Postpro</u> be (also) performed

with respect to the free-stream sideslip angle.

Off

In this case, no sensitivity requested in **Postpro** is computed with respect to the free-stream sideslip angle.

```
epsfd-real [1e-5]
```

Scalar defining the magnitude of the perturbation performed when approximating a derivative by the second-order central finite difference method.

LinearSolver:

Specifies the linear equation solver (and its parameters) to be used for solving the

• LinearSolver

Next: Running Aero-F, Previous: Objects

5 EXAMPLES

- Steady flow computation
- Unsteady aeroelastic computation
- Full order linearized
- POD basis
- ROM simulation

Next: Unsteady aeroelastic computation, Up: Examples

5.1 STEADY FLOW COMPUTATION

First, the computation of a steady-state inviscid flow around a three-dimensional wing is examplified.

```
File ``wing.steady''
------*
File ``wing.steady''
-----*

under Problem {
   Type = Steady;
   Mode = NonDimensional;
}

under Input {
   Prefix = "data/";
   Connectivity = "wing.con";
   Geometry = "wing.msh";
   Decomposition = "wing.dec";
   CpuMap = "wing.4cpu";
}

under Output {
```

```
under Postpro {
    Prefix = "result/";
    Residual = "wing.res";
   Force = "wing.lift";
Mach = "wing.mach";
    Frequency = 0;
  under Restart {
    Prefix = "result/";
    Solution = "wing.sol";
    RestartData = "wing.rst";
    Frequency = 0;
Equations.Type = Euler;
under BoundaryConditions {
  under Inlet {
    Mach = 0.5;
    Alpha = 0.0;
    Beta = 0.0;
  }
}
under Space {
  under NavierStokes {
    Reconstruction = Linear;
    Gradient = Galerkin;
  }
under Time {
  MaxIts = 10;
  Eps = 1.e-6;
  Cf10 = 10.0;
  CflMax = 1.e99;
  Ser = 1.0;
  under Implicit {
    MatrixVectorProduct = FiniteDifference;
    under Newton {
      MaxIts = 1;
      under LinearSolver {
        under NavierStokes {
          Type = Gmres;
          MaxIts = 30;
          KrylovVectors = 30;
          Eps = 0.05;
          Preconditioner.Type = Ras;
    }
 }
```

Next: Full order linearized, Previous: Steady flow computation, Up: Examples

5.2 UNSTEADY AEROELASTIC COMPUTATION

Next, the aeroelastic computation of an inviscid flow around a three-dimensional wing is examplified.

```
File ``wing.aero''
Problem.Type = UnsteadyAeroelastic;
under Input {
  Prefix = "data/";
  Connectivity = "wing.con";
Geometry = "wing.msh";
  Decomposition = "wing.dec";
  CpuMap = "wing.4cpu";
  Matcher = "wing.match";
Solution = "pingpong/wing.sol";
  Position = "pingpong/wing.pos";
under Output {
  under Postpro {
    Prefix = "result/";
    Force = "wing.lift";
    Mach = "wing.mach";
    Displacement = "wing.disp";
    Frequency = 10;
  under Restart {
    Prefix = "result/";
    Solution = "wing.sol";
Position = "wing.pos";
    RestartData = "wing.rst";
  }
Equations.Type = Euler;
under BoundaryConditions {
  under Inlet {
    Mach = 0.901;
    Alpha = 0.0;
    Beta = 0.0;
    Density = 1.117e-7;
    Pressure = 11.0;
}
under Space {
  under NavierStokes {
    Reconstruction = Linear;
    Limiter = VanAlbada;
    Gradient = Galerkin;
    Beta = 0.33333333;
under Time {
  Cf10 = 1.e5;
  CflMax = 1.e5;
  under Implicit {
    Type = ThreePointBackwardDifference;
    MatrixVectorProduct = Approximate;
    under Newton {
      MaxIts = 2;
      Eps = 0.01;
      under LinearSolver {
        under NavierStokes {
```

```
Type = Gmres;
          MaxIts = 30;
          KrylovVectors = 30;
          Eps = 0.01;
          Preconditioner.Type = Ras;
   }
 }
under MeshMotion {
 Type = Basic;
 Element = TorsionalSprings;
 under Newton {
   MaxIts = 1;
   under LinearSolver {
      Type = Cg;
     MaxIts = 50;
      Eps = 0.001;
     Preconditioner.Type = Jacobi;
 }
```

Next: POD basis, Previous: Unsteady aeroelastic computation, Up: Examples

5.3 FULL-ORDER LINEARIZED AEROELASTIC COMPUTATION

Next, the full-order linearized aeroelastic computation of an inviscid flow around a three-dimensional wing is examplified.

```
File ``wing.full''
under Problem {
  Type = UnsteadyLinearized;
  Mode = Dimensional;
under Input {
  Prefix = "InputFiles.d/";
 Connectivity = "pp.con";
Geometry = "pp.msh";
Decomposition = "pp.dec";
  CpuMap = "pp.4cpu";
  Perturbed = "agard.m0.678.deformed.lsq.steady.sol";
  Solution = "agard.m0.678.nodisp.lsq.steady.sol";
  Position = "agard.undisp.pp.pos";
under Output {
  under Postpro {
  Prefix = "";
    Force = "liftfull4.m0.678.p34_5";
    Frequency = 1;
}
```

```
under Linearized{
  StrModes = "modes1.pp";
  NumStrModes = 4;
 ExcMode = 1;
  Domain = Time;
  Amplification = 0.1;
  Eps = 1e-4;
under Equations {
  Type = Euler;
under BoundaryConditions {
  under Inlet {
   Mach = 0.678;
   Density = 2.338e-7;
   Pressure = 34.5;
    Alpha = 0.0;
    Beta = 0.0;
 }
under Space {
  under NavierStokes {
    Reconstruction = Linear;
   Limiter = VanAlbada;
   Gradient = LeastSquares;
    }
under Time {
  Type = Implicit;
  TypeTimeStep = Global;
  TimeStep = .001;
  MaxIts = 200;
  Eps = 1.e-8;
 under Implicit {
   MatrixVectorProduct = Exact;
    under Newton {
     MaxIts = 1;
      Eps = 0.0001;
      under LinearSolver {
        under NavierStokes {
          Type = Gmres;
         MaxIts = 100;
         KrylovVectors = 100;
          Eps = 0.0001;
      Output = "stdout";
      under Preconditioner { Type = Ras; Fill = 0; }
     }
   }
 }
```

Next: ROM simulation, Previous: Full order linearized, Up: Examples

5.4 CONSTRUCTING A POD BASIS

Next, the construction of a POD basis in the frequency-domain for a three-dimensional wing operating at M = 0.901 is examplified.

```
File ``wing.pod''
under Problem {
  Type = PODConstruction;
  Mode = Dimensional;
under Input {
 Prefix = "InputFiles.d/";
Connectivity = "pp.con";
Geometry = "pp.msh";
Decomposition = "pp.dec";
  CpuMap = "pp.4cpu";
  Solution = "agard.m0.901.nodisp.lsq.steady.sol";
  Position = "agard.undisp.pp.pos";
under Output {
  under Postpro {
    Prefix = "";
    Frequency = 0;
    PodData = "PodData.d/podVecs4.freq0.901.df5e3.150snap.400pod";
  }
}
under Linearized{
  StrModes = "modes1.pp";
  NumStrModes = 4;
  Domain = Frequency;
  FreqStep = 0.005;
  Eps = 1e-5;
  NumPOD = 400;
under Equations {
  Type = Euler;
under BoundaryConditions {
  under Inlet {
    Mach = 0.901;
    Density = 1.117e-7;
    Pressure = 5.0;
    Alpha = 0.0;
    Beta = 0.0;
  }
}
under Space {
  under NavierStokes {
    Reconstruction = Linear;
    Gradient = LeastSquares;
    Beta = 0.333333333;
}
under Time {
  Type = Implicit;
  TypeTimeStep = Global;
```

```
TimeStep = 4.0e-5;
MaxIts = 151;
Eps = 1.e-8;
under Implicit {
  MatrixVectorProduct = Exact;
  under Newton {
    MaxIts = 1;
    Eps = 1e-8;
    under LinearSolver {
      under NavierStokes {
        Type = Gmres;
        MaxIts = 100;
        KrylovVectors = 100;
        Eps = 0.0001;
     Output = "stdout";
    under Preconditioner { Type = Ras; Fill = 0; }
  }
}
```

Previous: POD basis, Up: Examples

5.5 REDUCED-ORDER AEROELASTIC COMPUTATION

Next, a ROM aeroelastic computation of a wing operating at M = 0.800 is examplified.

```
File ``wing.rom''
under Problem {
  Type = ROMAeroelastic;
  Mode = Dimensional;
under Input {
  Prefix = "InputFiles.d/";
  Connectivity = "pp.con";
  Geometry = "pp.msh";
  Decomposition = "pp.dec";
  CpuMap = "pp.4cpu";
  Perturbed = "agard.m0.800.deformed.lsq.steady.sol";
  Solution = "agard.m0.800.nodisp.lsq.steady.sol";
  Position = "agard.undisp.pp.pos";
  PodData = "../PodData.d/podVecs4.m0.800.dt4e5.225snap.300pod";
under Output {
  under Postpro {
   Prefix = "";
   Force = "liftrom.freq800.30snap.50of100pod.p7";
    Frequency = 1;
  }
under Linearized{
```

```
StrModes = "modes1.pp";
 NumStrModes = 4;
 ExcMode = 1;
 Amplification = 0.1;
 Eps = 1e-4;
 NumPOD = 300;
under Equations {
 Type = Euler;
under BoundaryConditions {
 under Inlet {
   Mach = 0.800;
   Density = 1.117e-7;
   Pressure = 10.0;
   Alpha = 0.0;
   Beta = 0.0;
}
under Space {
 under NavierStokes {
   Flux = Roe;
    Reconstruction = Linear;
   Gradient = LeastSquares;
   }
}
under Time {
 Type = Implicit;
 TypeTimeStep = Global;
 TimeStep = .001;
 MaxIts = 500;
 Eps = 1.e-8;
 under Implicit {
   MatrixVectorProduct = Exact;
    under Newton {
     MaxIts = 1;
     Eps = 1e-8;
     under LinearSolver {
       under NavierStokes {
         Type = Gmres;
         MaxIts = 100;
         KrylovVectors = 100;
         Eps = 0.0001;
      under Preconditioner { Type = Ras; Fill = 0; }
     }
   }
 }
```

Next: Running AERO-FL, Previous: Examples

6 RUNNING AEROF

AERO-F has no graphical interface. It is a command-line driven program that reads a problem definition file once at the beginning of the processing. This problem definition file is a regular ASCII text file (see <u>Object oriented input</u>).

Calls for simulations involving only AERO-F look like

```
mpirun [host_name] nb_cpus aerof filename
```

where *host_name* is the (optional) name of the computer on which the job is executed, *number_cpus* is the number of processes allocated for the job, and *filename* is the ASCII file containing the problem definition.

Aeroelastic and aerothermal simulations require the interaction of AERO-F with a structural code. If AERO-S or AERO-H is used for that purpose, aeroelastic and aerothermal calls look like

```
mpirun [fluid_host_name] fluid_nb_cpus aerof fluid_filename :
[struct_host_name] struct_nb_cpus aeros struct_filename
```

If the above syntax is not supported by your MPI implementation, the same simulation can be started with

```
mpirun [host_name] total_nb_cpus loader fluid_nb_cpus aerof.so fluid_filename ,
struct_nb_cpus aeros.so struct_filename
```

Aerothermoelastic simulations require the interaction of AERO-F with a structural code and a heat transfer code. If AERO-S and AERO-H are used for that purpose, aerothermoelastic calls look like

```
mpirun [fluid_host_name] fluid_nb_cpus aerof fluid_filename :
[struct_host_name] struct_nb_cpus aeros struct_filename :
[heat_host_name] heat_nb_cpus aeros heat_filename
```

If the above syntax is not supported by your MPI implementation, the same simulation can be started with

```
mpirun [host_name] total_nb_cpus loader fluid_nb_cpus aerof.so fluid_filename ,
struct_nb_cpus aeros.so struct_filename , heat_nb_cpus aeros.so heat_filename
```

- ExampleSteadyFlowComputation
- ExampleUnsteadyFlowComputation
- ExampleForcedOscillationsComputation
- ExampleUnsteadyAeroelasticComputation

Next: ExampleUnsteadyFlowComputation, Up: Running Aero-F

6.1 STEADY FLOW COMPUTATION

A steady-state flow computation is selected by setting Problem.Type = Steady. By default, the computation starts from a uniform flowfield around the undeformed configuration. To modify this behavior, Input.Solution and Input.Position must be set to some appropriate values. The other critical variables to watch for are the total number of time-steps (Time.MaxIts), the spatial residual relative decrease (Time.Eps), and the inital and maximum CFL numbers (Time.Cf10 and Time.Cf1Max). As a first-order time-integrator is always selected for steady-state computations, only one Newton iteration (Time.Implicit.Newton.MaxIts) should be performed at every time-step.

Next: ExampleForcedOscillationsComputation, Previous: ExampleSteadyFlowComputation, Up: Running Aero-F

6.2 UNSTEADY FLOW COMPUTATION

An unsteady flow computation is selected by setting Problem. Type = Unsteady. By default, the computation starts from a uniform flowfield around the undeformed configuration. To modify this behavior, Input. Solution and Input. Position must be set to some appropriate values. The other critical variables to watch for are the time-step (Time. TimeStep) or alternatively the CFL strategy, the maximum number of time-steps and the maximum time (Time. MaxIts and Time. MaxItme), and the type of time-integrator (Time. Implicit. Type). At least two Newton iterations (Time. Implicit. Newton. MaxIts) should be performed at every time-step to preserve the accuracy of the time-integrator.

Next: <u>ExampleUnsteadyAeroelasticComputation</u>, Previous: <u>ExampleUnsteadyFlowComputation</u>, Up: <u>Running Aero-F</u>

6.3 FORCED OSCILLATIONS COMPUTATION

A forced oscillations computation is selected by setting Problem. Type = Forced. In addition to what applies to an unsteady flow computation (see ExampleUnsteadyFlowComputation), the critical variables to watch for are the forced oscillations parameters (Forced) and the mesh motion algorithm (MeshMotion). During such a flow computation, the shape of the obstacle shape is varied between the final shape (Forced.Position) and its symmetric position with respect to the original shape. Note that the computation starts from the original shape. The latter that can be generated by a "ping-pong" step (see ExampleUnsteadyAeroelasticComputation).

Previous: ExampleForcedOscillationsComputation, Up: Running Aero-F

6.4 UNSTEADY AEROELASTIC COMPUTATION

Aeroelastic computations using AERO-F require the additional usage of a structure solver that is equipped to communicate with this flow solver, and a fluid-structure preprocessor that is capable of generating the data structures necessary for exchanging aeroelastic data between the fluid and structural codes. If AERO-S and MATCHER are used for that purpose, an aeroelastic simulation is usually (but not necessarily) carried out in the following three steps:

- a "ping-pong" step to transmit to AERO-F the initial deformation of the flexible obstacle. This step is
 performed like a true aeroelastic computation (see below) and is requested by setting the AERO command in
 the AERO-S input file to PP. The critical variables to watch for are the mesh motion algorithm (MeshMotion)
 and the position of the deformed obstacle (Output.Restart.Position) that will be needed for the next two
 steps;
- 2. a steady-state flow computation around the deformed obstacle configuration (see <u>ExampleSteadyFlowComputation</u>). This is a recommended but not mandatory step of an aeroelastic

simulation:

3. an unsteady flow computation around the moving and deforming obstacle. Such a computation is performed by setting Problem. Type to UnsteadyAeroelastic. The critical variables to watch for are the initial flow solution and node position (Input.Solution and Input.Position) obtained from the two previous steps, the time-step (Time.TimeStep) or alternatively the CFL strategy, the type of time-integrator (Time.Implicit.Type), and the mesh motion algorithm (MeshMotion). Note that to avoid subcycling (i.e. performing several fluid time-steps during one structural time-step), the CFL number (Time.Cfl0 and Time.CflMax) needs to be set to a large value (e.g. 1.e5);

Next: Restarting AERO-F, Previous: Running Aero-F

7 RUNNING AEROFL

The linearized fluid code may be used for a variety of purposes including the following:

- 1. conducting a time-domain linearized flow simulation possibly coupled to a (currently modalized) vibrating structure;
- 2. constructing a time- or frequency-domain POD basis;
- 3. interpolating a POD basis from previously computed ones;
- 4. constructing an aeroelastic ROM in the frequency domain;
- 5. conducting a time-domain aeroelastic ROM simulation in which the structure is modalized;

All of the above running modes require performing first one or several simulations aimed at generating a reference equilibrium solution. Next, in order to perform any of the computations listed above, the following parameters must be specified under Problem (see <u>Problem</u>) and <u>Linearized</u> (see <u>Linearized</u>).

- 1. To conduct full-order linearized simulations, set Type in Problem to UnsteadyLinearized or UnsteadyLinearizedAeroelastic. In the latter case, represent the structure by a set of modes (currently) by setting appropriately Linearized.StrModes and Linearized.NumStrModes, and excite it by setting appropriately Linearized.ExcMode and Linearized.Amplification. Do not forget to input the information needed for initializing the flow perturbation by specifying Input.Perturbed.
- 2. To construct a POD basis, set Type in Problem to PODConstruction. The construction process requires sources of excitation. Currently, these sources are modal impulses of the structure. For this reason, set appropriately Linearized.StrModes, Linearized.NumStrModes, Linearized.Amplification, and Time.MaxIts. The latter parameter specifies half the number of snapshots per modal impulse. The POD basis may be constructed in either the time- or frequency-domain; this is specified in Domain (see <u>Linearized</u>). To accelerate the construction of a POD basis in the frequency-domain, consider the Pade reconstruction strategy defined under the Pade object. Do not forget to specify in NumPOD, the number of desired POD basis vectors. To interpolate a POD basis, set Type in Problem to PODInterpolation. Use Input.PODData to specify the two sets of POD basis vectors and their respective Mach numbers to be used in the interpolation process (see <u>Input</u>); also, input the desired Mach interpolation point. Specify the desired POD output file in Postpro.PODData.

- 3. To construct a fluid ROM, set Type in Problem to ROM and Domain in Linearized to Time, and set Input.PODData and Linearized.NumPOD appropriately. Set Time.MaxIts to zero if you want AERO-FL to exit after constructing the ROM, or to a non zero value if you desire a time-domain simulation using this ROM. Do not forget to specify the desired output file in Postpro.ROM.
- 4. To construct an aeroelastic ROM, set Type in Problem to ROMAeroelastic and Domain in Linearized to Time, and set Input.PODData and Linearized.NumPOD appropriately. Represent the structure by a set of modes by specifying also appropriately Linearized.StrModes and Linearized.NumStrModes. Set Time.MaxIts to zero if you want AERO-FL to exit after constructing the aeroelastic ROM, or to a non zero value if you desire a time-domain simulation using this aeroelastic ROM. Do not forget to specify the desired output file in Postpro.ROM.
- 5. To conduct a fluid ROM simulation, set Type in Problem to ROM. Also, specify the POD basis using Input.PODData and Linearized.NumPOD. Do not forget to input the information needed for initializing the flow perturbation by specifying Input.Perturbed.
- 6. To conduct aeroelastic ROM simulations, set Type in Problem to ROMAeroelastic. Specify the POD basis using Input.PODData and Linearized.NumPOD. Do not forget to input the information needed for initializing the flow perturbation by specifying Input.Perturbed. Represent the structure by a set of modes (currently) by setting appropriately Linearized.StrModes and Linearized.NumStrModes, and excite it by setting appropriately Linearized.ExcMode and Linearized.Amplification.

Next: Restarting Aero-FL, Previous: Running AERO-FL

8 RESTARTING AEROF

For all flow simulations, AERO-F can restart from a previous run that was successfully completed. AERO-F can also restart from a previous run that was for some reason interrupted (i.e. computer crash) if the value of Output.Restart.Frequency was different from zero. In both cases, in order to restart AERO-F, the variables Input.Solution, Input.Position (if applicable) and Input.RestartData need to be set to their appropriate values (i.e. the ones used in the object Output.Restart of the previously completed or interrupted run). For example, an initial input file used for an aeroelastic simulation should contain

```
under Output {
  under Restart {
    Solution = "wing.sol";
    Position = "wing.pos";
    RestartData = "wing.rst";
  }
}
```

To restart the aeroelastic simulation, the second input file should contain

```
under Input {
   Solution = "wing.sol";
   Position = "wing.pos";
   RestartData = "wing.rst";
```

}

and can also contain in Output. Restart the information necessary to save future restart data.

Notes:

- 1. there is no need to copy any of the output files (specified in Output.Postpro) since the restart appends the data to the original (ASCII and binary) files;
- 2. it is currently not allowed to change the output frequency Output.Postpro.Frequency nor to change the name of the output files nor to add other output files (in Output.Postpro) when restarting a simulation. This restriction does not exist if the variable Input.RestartData is not set. In that case, the run restarts from a previous solution Input.Solution and a previous position Input.Position (if applicable) but the time-step number and the physical time are reset to zero;
- 3. as mentioned in <u>Restart</u>, the value of the restart frequency Output.Restart.Frequency must be specified in the AERO-S input file in the case of an aerothermal, aeroelastic, or aerothermoelastic simulation with the AERO-S code;
- 4. the variable Input.RestartData should not be used when starting an aeroelastic simulation from a pre-computed steady-state of the flow-field because it de-synchronizes in this case AERO-F and the structural solver.

Next: Hints and tips, Previous: Restarting AERO-F

9 RESTARTING AEROFL

Currently, AERO-FL cannot run in restart mode.

Next: <u>ROM</u>, Previous: <u>Restarting Aero-FL</u>

Appendix A HINTS AND TIPS

- Decompose the mesh in many subdomains to be able to run a simulation with the same input files but with a different number of processors.
- Terminate the execution of AERO-F with

```
kill -USR1 pid
```

where *pid* is the process identification number of one of the AERO-F processes. Once the kill signal is sent to AERO-F, it exits at the next time-iteration.

• Create binary files from ASCII **XPost** files by using the SOWER program:

```
sower -fluid -split -con <connectivity file>
-mesh <mesh file prefix> -result <ASCII file> -ascii
```

-output

dile prefix>

• Install the info version of this user's guide. On your (Unix) system, this can be achieved by 1) copying the aerof.info file to the place where your info files live (usually /usr/local/info), and 2) issuing the command install-info /usr/local/info/aerof.info /usr/local/info/dir. You will then be able to access the documentation with the command info aerof. Note that particular sections ("nodes") can be accessed directly. For example, info aerof Problem will take you directly to the definition of the Problem object.

Next: <u>DES</u>, Previous: <u>Hints and tips</u>

Appendix B ROM OUTPUT FORMAT

AERO-FL can output in ASCII format either a fluid ROM, or an aeroelastic ROM. This appendix characterizes the ROM in each case and describes the format of the corresponding output.

- Fluid ROM
- Aeroelastic ROM

Next: Aeroelastic ROM, Up: ROM

B.1 FLUID ROM

In this case, the outputted ROM matrix is an $n_f \times n_f$ POD-based, real, full matrix $\tilde{\mathbf{H}}$ whose exploitation may require first its dimensionalization as follows

$$\mathbf{H}(p_{\infty}, \rho_{\infty}) = \sqrt{\frac{p_{\infty}}{\rho_{\infty}}} \ \tilde{\mathbf{H}}$$

where p_{∞} and p_{∞} denote the free-stream pressure and density, respectively. In other words, $\tilde{\mathbf{H}}$ does not contain information about the altitude whereas $\tilde{\mathbf{H}}$ does.

The adjusted ROM matrix **H** governs the perturbed equations of equilibrium

$$(\mathbf{w})_{,t} + \mathbf{H}\mathbf{w} = 0$$

where \mathbf{w} denotes the perturbation of the reduced-order fluid state vector about a steady-state operating point and \mathbf{H} denotes a time-derivative. The matrices \mathbf{H} and \mathbf{H} can be exploited at least in the following ways:

• In principle, H can be used for a time-domain simulation assuming that an appropriate initial condition is specified. However, providing an initial condition for the above equation is not an intuitive task (unlike a modal coordinate system in the case of a structure). A straightforward approach for constructing a meaningful initial condition consists of gaining access to the POD basis that was used for computing H and projecting a meaningful full order initial condition onto this reduced basis.

• Alternatively, $\tilde{\mathbf{H}}$ can be used to investigate the stability of the fluid system. If all the real parts of its eigenvalues are positive, the fluid system is stable for all free-stream densities and pressures.

The output format of $\tilde{\mathbf{H}}$ is as follows:

- $n_f \mid 0 \text{ (line 1)}$
- Row 1 of $\tilde{\mathbf{H}}$ (line 2)
- Row 2 of **H** (line 3)
- [
- Row n_f of $\tilde{\mathbf{H}}$ (line $n_f + 1$)

For example, the following MATLAB code can read in this case the ROM output file:

```
M=readRom('filename');
function [N] = readRom(fn)
line1 = dlmread(fn,' ',[0 0 0 1]);
N=dlmread(fn, ' ', [1 0 line1(1)+2*line1(2) line1(1)+2*line1(2)-1]);
```

Previous: Fluid ROM, Up: ROM

B.2 AEROELASTIC ROM

In this case, the outputted ROM consists of the following 3 imes 3 block, real matrix $ilde{\mathbf{N}}$





 $-\mathbf{B_m}$

 $-\tilde{\mathbf{C}}_{\mathbf{m}}$

I

 $\tilde{\mathbf{N}} =$



-0

 $-\Omega^2$

0

 \mathbf{I}_{s}

-0

which does not depend on the free-stream pressure and density — and therefore on altitude — and whose exploitation may first require its dimensionalization as follows





 $-\mathbf{B_m}$

 $-\sqrt{\frac{p_{\infty}}{\rho_{\infty}}} \; \tilde{\mathbf{C}}_{\mathbf{m}}$



 $\mathbf{N}(p_{\infty}, \rho_{\infty}) =$



0

 $-\Omega^2$

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where p_{∞} and p_{∞} denote the free-stream pressure and density at the desired altitude, respectively,

$$\mathbf{P_m} = p_{\infty} \tilde{\mathbf{P}}_{\mathbf{m}} = \mathbf{X^T} (\partial \mathbf{f^{ext}}/\partial \mathbf{w})$$

and

- ullet $ilde{\mathbf{H}}$ is as in the previous case the $n_f imes n_f$, real fluid ROM matrix
- $\mathbf{H}(p_{\infty},\rho_{\infty})=\sqrt{p_{\infty}/\rho_{\infty}}\tilde{\mathbf{H}}$ is the corresponding $n_f\times n_f$, real, dimensional, adjusted fluid ROM

matrix

- ullet ${f B_m}$ and ${f C_m}=\sqrt{p_\infty/
 ho_\infty} {f ilde C}_m$ are two $n_f imes n_s$ fluid/structure coupling matrices
- **X** is the matrix of natural mode shapes of the dry structure (in this case, without the rotational degrees of freedom), **f**^{ext} is the vector of aerodynamic loads and **W** is the state vector of the fluid system
- ullet $\mathbf{P_m} = p_{\infty} \tilde{\mathbf{P}_m}$ is an $n_s \times n_f$ load transfer matrix
- ullet Ω^2 is an $n_s imes n_s$ diagonal matrix storing the squares of the structural natural circular frequencies
- ullet $oxed{\mathbf{I}_s}$ is the $egin{aligned} n_s imes n_s \end{aligned}$ identity matrix

The adjusted ROM matrix ${f N}$ governs the perturbed equations of equilibrium

$$\dot{\mathbf{q}} = \mathbf{N}\mathbf{q}$$

where

 $\mathbf{q} = [$ \mathbf{w} $\dot{\mathbf{u}}_{\mathbf{m}}$ $\mathbf{u}_{\mathbf{m}}$ $]^T$

is the aeroelastic state vector consisting of the perturbation of the reduced-order fluid state vector about an operating point, the structural modal displacements, and structural modal velocities.

The blocks of **N** govern the following system of coupled, fluid/structure equations

$$(\mathbf{w})_{,t} + \mathbf{H}\mathbf{w} + \mathbf{B}_{\mathbf{m}}\dot{\mathbf{u}}_{\mathbf{m}} + \mathbf{C}_{\mathbf{m}}\mathbf{u}_{\mathbf{m}} = 0$$
$$\mathbf{I}_{s}\ddot{\mathbf{u}}_{\mathbf{m}} + \Omega^{2}\mathbf{u}_{\mathbf{m}} = \mathbf{P}_{\mathbf{m}}\mathbf{w}$$

where the dot and the yt represent both a derivative with respect to time.

The matrix N can be exploited at least in the following ways:

- The eigenvalue analysis of \mathbb{N} determines the stability of the aeroelastic system for the flight conditions defined by p_{∞} and p_{∞} . Altitude sweeps are simply performed by changing appropriately the values of the free-stream pressure and density in \mathbb{N} .
- The matrix blocks of N may be used to form the above system of equations. The aeroelastic ROM can then be used for time-domain simulations provided that initial conditions are specified for um and w (see related comment in section describing the fluid ROM output).

The output format of $\tilde{\mathbf{N}}$ is as follows:

```
• n_f n_s (line 1)

• Row 1 of \tilde{\mathbf{N}} (line 2)

• Row 2 of \tilde{\mathbf{N}} (line 3)

• :

• Row n_f of \tilde{\mathbf{N}} (line n_f + 2n_s + 1)
```

For example, the following MATLAB code can read in this case the ROM output file — that is, the matrix $\tilde{\mathbf{N}}$:

```
[N,nf,ns]=readRom('filename');
function [N,nf,ns] = readRom(fn)
line1 = dlmread(fn,' ',[0 0 0 1]);
endOfN = line1(1)+2*line1(2);
endCol = line1(1)+2*line1(2)-1;
N=dlmread(fn, ' ', [1 0 endOfN endCol]);
nf = line1(1);
ns = line1(2);
```

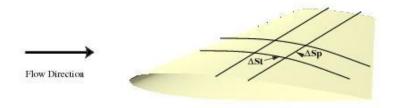
Furthermore, the following MATLAB code can read the ROM output file and output the dimensionalized matrix \mathbf{N} for specified values of p_{∞} and p_{∞} :

```
[N,nf,ns] = readRom('filename',p_inf,rho_inf)
function [N,nf,ns] = readRom(fn,p_inf,rho_inf)
line1 = dlmread(fn,' ',[0 0 0 1]);
endOfN = line1(1)+2*line1(2);
endCol = line1(1)+2*line1(2)-1;
Ntilde = dlmread(fn, ' ', [1 0 endOfN endCol]);
nf = line1(1);
ns = line1(2);
N(1:nf,1:nf) = sqrt(p_inf/rho_inf) ...
*Ntilde(1:nf,1:nf);
```

Next: TAB, Previous: ROM

Appendix C DETACHED EDDY SIMULATIONS (DES): MESH REQUIREMENTS

Detached Eddy Simulation (DES) is a hybrid (zonal) turbulence model that employs a RANS type closure close to the wall (in the boundary-layer) and a LES type closure in the detached shear layer. This approach surmounts the expensive problem of having to resolve the thin boundary-layer by traditional LES means. Hence, DES aims at achieving best of both worlds, by making use of the reliability of the RANS model in predicting boundary-layer separation points and by resolving the effect of the separated shear layers using a subgrid scale LES model.



In AERO-F, a DES procedure based on the the Spalart-Allmaras (SA) one-equation model is implemented. DES uses a mesh dependent length scale to switch between the RANS and LES domains. More specifically, the length scale (l_{DES}) of the DES model is computed in each tetrahedron T_I as

$$l_{DES}(T_I) = \min (d_{wall}(T_I), C_{DES}\Delta(T_I))$$

with

$$\Delta = \max_{e \in T_I} (meas(e))$$

where, d_{wall} is the shortest distance to the wall from the centroid of tetrahedron T_I , C_{DES} is the DES model constant and e is an edge of tetrahedron T_I . The value of the model constant is set to $C_{DES}=0.65$ after calibration with homogeneous isotropic turbulence. If $l_{DES}=d_{wall}$ then the RANS model is active and if $l_{DES}=C_{DES}\Delta$ then the LES model is active.

Hence, when creating a mesh for DES simulations, one has to adhere to the following details:

- 1. Create a surface mesh such that its streamwise (ΔSt) and spanwise (ΔSp) lengths are of the order of the boundary-layer thickness so that l_{DES} always switches to d_{wall} in the boundary-layer. For unstructured meshes, this means that one has to choose a surface mesh size of at least the boundary-layer thickness. For the leading edge, one has usually to choose a smaller mesh size to capture the geometry accurately but this size has to be at least the boundary-layer thickness at the leading edge. Again, this would ensure that $l_{DES} = d_{wall}$ in the leading edge boundary-layer. At the trailing edge, one again has to use smaller mesh sizes to correctly capture the geometry, but in this case one does not need to worry about the mesh requirements of DES. This is because, once the flow has separated, the RANS model does not help in modeling the physics of the detached boundary layer any longer.
- 2. Introduce (extrude) prism layers to fill up the boundary-layer thickness. The vertical spacing of each prism layer can be based on any mesh growth scheme chosen by the user. This is because the vertical spacing of each prism layer is always smaller than the boundary-layer thickness and hence the switch always selects $l_{DES} = d_{wall}$ in the boundary-layer.
- 3. Outside the prism layers, in the expected shear layers, create isotropic LES meshes with characteristic mesh sizes of the order of the Taylor microscale $\lambda_T \approx \sqrt{15}Re_L^{-1/2}L$, where, L is the integral length scale (usually the body length) and Re_L is the Reynolds number based on L. It is a good practice to use a mesh size of around $5\lambda_T$ near the wall and gradually increase the size to about $10\lambda_T$ in the far-field.

Next: Sensitivities, Previous: DES

Appendix D SPARSE GRID TABULATION OF RIEMANN INVARIANTS AND SOLUTIONS

Sparse grid tabulations are used in **AERO-F** to accelerate the solution of multi-phase flow problems involving a medium modeled by a complex and computationally intensive Equation Of State (EOS), such as the JWL EOS,

using the FiniteVolumeWithExactTwoPhaseRiemann method which requires the computation of the solutions of local, one-dimensional two-phase Riemann problems (see MultiPhase). The tabulation of certain quantities related to this computation allows to bypass some of the more costly computational steps. While such tabulations may not be readily available to the user, they can be generated in a sparse grid format using AERO-F. This appendix provides instructions to set up the input file needed by AERO-F to generate these tabulations, as well as guidelines for how to choose their appropriate parameters.

General Settings

In order to tabulate some data in sparse grid format, the user must specify

```
Problem.Type = SparseGridGeneration;
```

as well as the name *filename-str* of the output file(s) that will contain the tabulated data

```
Output.PostPro.SparseGrid = filename-str;
```

(see Problem and PostPro).

Data to Tabulate

Currently, **AERO-F** can tabulate quantities related to the computation of the solution of a one-dimensional two-phase Riemann problem between a JWL EOS and a perfect or stiffened gas EOS only. These quantities are the Riemann invariants of the JWL EOS, and the solutions of one-dimensional, two-phase Riemann problems. The first option (Riemann invariants) is recommended because it is fast, easy, and has demonstrated superior potential for accelerating the computation of two-phase flow problems involving the JWL EOS using the numerical method FiniteVolumeWithExactTwoPhaseRiemann.

In order to tabulate the Riemann invariants of the JWL EOS, the user must specify in the **AERO-F** ASCII input file:

```
under Equations {
  under FluidModel[0] {
    Fluid = JWL;
    under JWLModel { ... }
  }
}
under MultiPhase{
  RiemannComputation = TabulationRiemannInvariant;
}
```

where JWLModel specifies the parameters of the considered JWL EOS.

In order to tabulate the solutions of one-dimensional two-phase Riemann problems between a JWL EOS and a perfect or stiffened gas EOS, the user must specify in the **AERO-F** ASCII input file:

```
under Equations {
  under FluidModel[0] {
   Fluid = StiffenedGas;
  under GasModel { ... }
```

```
}
under FluidModel[1] {
  Fluid = JWL;
  under JWLModel { ... }
}

under MultiPhase{
  RiemannComputation = TabulationRiemannProblem;
}
```

where **GasModel** and **JWLModel** specify the parameters of the two considered EOSs.

How to Tabulate Riemann Invariants of the JWL EOS

The Riemann invariant of the JWL EOS is the scalar quantity

$$I(\rho, s) = \int \frac{c(\rho, s)}{\rho} d\rho$$

which depends on two variables:

the density ρ , and the mathematical entropy

$$s = \frac{p - A_1 e^{-\frac{R_1 \rho_0}{\rho}} - A_2 e^{-\frac{R_2 \rho_0}{\rho}}}{\rho^{\omega + 1}}$$

where P is pressure and the other parameters of the JWL EOS are user-specified in FluidModel[0].

Therefore, in this case the user must specify in the object <u>SparseGrid</u>: (a) that the sparse grid will have two input variables and one output variable, and (b) the lower and upper bounds of each input variable as follows:

```
\begin{array}{lll} \mbox{NumberOfInputs} &=& 2; \\ \mbox{NumberOfOutputs} &=& 1; \\ \mbox{Input1Minimum} &=& in1min-real; \\ \mbox{Input1Maximum} &=& in1max-real; \\ \mbox{Input2Minimum} &=& in2min-real; \\ \mbox{Input2Maximum} &=& in2max-real; \\ \end{array}
```

The first input variable is the density and the second one is the entropy. Determining the optimal choices of the bounds of the input variables requires predicting accurately the ranges of these variables spanned during the exploitation of the tabulation and therefore is a difficult task. For this reason, these bounds can be only estimated. The density of a highly explosive gas modeled by the JWL EOS usually has a maximum value given by the initial conditions of the application problems and a minimum value that is several orders of magnitude lower. For example, in SI units, the density can easily vary between 1 and 1630 $Kg.m^{-3}$. Estimates of the bounds for entropy are not

straightforward to obtain. With pressure values varying in a typical application problem between an initial value often of the order of several $10^9 Pa$ s and a value that is several orders of magnitude lower than that of the surrounding fluid, the computed entropies associated with such density and pressure values can span several orders of magnitude. Instead, it is easier to compute the value of the entropy corresponding to the values of the density and

pressure of the JWL fluid associated with typical initial conditions of application problems of interest and tabulate around this value. This is generally sufficient as a highly explosive gas usually undergoes an expansion during which the entropy does not vary significantly.

The choice of the numerical parameters for the construction of a sparse grid depends on several factors such as the data to be tabulated, the user-desired accuracy, and the maximum size of the grid (which can determine how long it takes to generate and exploit a sparse grid). As such, several tabulation iterations may be needed to obtain the desired result.

AERO-F refines a sparse grid tabulation until one of three stopping criteria is reached: the desired relative accuracy is satisfied, the desired absolute accuracy is satisfied, or the maximum number of points in the tabulation is exceeded. For the tabulation of Riemann invariants of the JWL EOS, the user can start with

```
MaximumNumberOfPoints = 10000;
RelativeAccuracy = 1.0e-3;
AbsoluteAccuracy = 0.1;
```

The errors are estimated a posteriori at the last created points of the sparse grid. The relative errors are computed with respect to the difference between the largest and smallest computed values of the data to be tabulated. A minimum number of points for the tabulation can also be specified. For example,

```
MinimumNumberOfPoints = 100:
```

Since the data to be tabulated may not exhibit the same variations for different input variables, the user is given the possibility to refine the sparse grid along the input variable for which the errors decrease the most. This is done by specifying the degree of dimensional adaptivity which can take any real value between 0 and 1. A degree of 0 corresponds to a uniform refinement in each input variable, while a degree of 1 corresponds to a refinement based solely on the errors. For the tabulation of Riemann invariants of the JWL EOS, the user is advised to use values above 0.7 but below 1.0:

```
DegreeDimAdapt = 0.7;
```

To enable parallel processing during the tabulation and accelerate the exploitation of this tabulation during subsequent **AERO-F** computations, the user can request the tabulation of a single domain in several complementary sparse grids characterized by the same numerical parameters. For this purpose, the user can specify a uniform splitting of the domain of each input variable in a number of subdomains that depends directly on its range (the larger is the range, the more attractive it becomes to decompose it). For example, the user can specify:

```
NumberOfDomains1 = 3;
NumberOfDomains2 = 2;
```

which leads to six complementary sparse grids characterized by the same numerical parameters.

How to Tabulate Solutions of One-Dimensional Two-Thase JWL-Gas Riemann Problems

The solution of a one-dimensional, two-phase Riemann problem at the interface between two initial states depends on the initial values of the density and pressure, and the jump in the initial velocities. This solution can be

reconstructed from the knowledge of the constant density states on both sides of the material interface. Therefore, in this case the user must specify in the object SparseGrid: (a) that the sparse grid will have five input and two output variables (which are the constant density states at the left and right of the material interface), and (b) the lower and upper bounds of each input variable as follows:

```
NumberOfInputs = 5;
NumberOfOutputs = 2;
Input1Minimum = in1min-real;
Input2Minimum = in2min-real;
Input2Maximum = in2max-real;
Input3Minimum = in3min-real;
Input3Maximum = in3max-real;
Input4Minimum = in4min-real;
Input4Maximum = in4min-real;
Input5Minimum = in5min-real;
Input5Maximum = in5min-real;
Input5Maximum = in5max-real;
```

The first and second input variables are the density and pressure in the perfect or stiffened gas, the third and fourth are the density and pressure in the medium modeled by the JWL EOS, and the fifth input variable is the difference between the velocity of the perfect/stiffened gas and that of the JWL medium. Specifying the bounds of each input variable is not easy, especially since some initial states lead to vacuum state solutions. For this purpose, the user needs to estimate a priori these bounds. To this effect, it is useful to note that the velocity jump at the material interface can be either positive or negative, and that in general it is not very large unless the jump of the initial velocities is large, or a strong shock wave interacts with the material interface.

The choice of the numerical parameters characterizing the sparse grid are specified in the same manner as in the previous case. In particular, the same values as before can be used for the minimum number of points and desired accuracies:

```
MinimumNumberOfPoints = 100;
RelativeAccuracy = 1.0e-3;
AbsoluteAccuracy = 0.1;
```

It is recommended to choose a maximum number of points of at least 100,000 and a degree of dimensional adaptivity of 0.9. It is also particularly useful to consider splitting the domain of each input variable. It is strongly advised to split the domain of the velocity difference input variable so that a sparse grid avoids as much as possible tabulating both vacuum state and non-vacuum state solutions. Therefore, even if the values of the velocity difference do not span several orders of magnitude, it is still recommended to split the domain of this input variable.

Previous: TAB

Appendix E COMPUTATION OF SENSITIVITIES

The derivative at a fluid equilibrium point — that is, a steady-state fluid sate vector \mathbf{W}_o — of an aerodynamic-related quantity $q_i = q_i(\mathbf{W}(s_j))$ with respect to a flow or shape parameter s_j can be written as

$$\frac{dq_i}{ds_j}|_{\mathbf{W}_o} = \frac{dq_i}{d\mathbf{W}}|_{\mathbf{W}_o} \frac{d\mathbf{W}}{ds_j}|_{\mathbf{W}_o}$$

where:

• $\frac{dq_i}{d\mathbf{W}}|_{\mathbf{W}_{\sigma}}$ can be computed analytically or by finite differencing, depending on the complexity of the

dependence of q_i on \mathbf{W} .

• $\frac{d\mathbf{W}}{ds_i}|_{\mathbf{W}_o}$ can be determined from the stationarity at \mathbf{W}_o of the equation of dynamic equilibrium of the fluid

$$\mathbf{F}\left(\mathbf{W}(s_i), \mathbf{X}(s_i), s_i\right) = 0$$

where ${\bf F}$ denotes the system of nonlinear equations governing the steady-state fluid sate vector ${\bf W}_{\sigma}$, and ${\bf X}$ denotes the vector of nodal positions of the fluid mesh. The differentiation of the above equation at ${\bf W}_{\sigma}$ leads to the characterization of the gradient $\frac{d{\bf W}}{ds_i}|_{{\bf W}_{\sigma}}$ as the solution of the linearized system of equations

$$\left[\frac{\partial \mathbf{F}}{\partial \mathbf{W}}|\mathbf{w}_{o}\right]\frac{d\mathbf{W}}{ds_{j}}|\mathbf{w}_{o} = -\frac{\partial \mathbf{F}}{\partial s_{j}}|\mathbf{w}_{o} - \frac{\partial \mathbf{F}}{\partial \mathbf{X}}|\mathbf{w}_{o}\frac{d\mathbf{X}}{ds_{j}}$$

where:

- o $\frac{\partial \mathbf{F}}{\partial s_i}|_{\mathbf{W}_p}$ can be computed analytically or by finite differencing.
- o $\frac{d\mathbf{X}}{ds_j}$ is non zero only when s_j is a shape parameter; for this reason, $\frac{d\mathbf{X}}{ds_j}$ is referred to here as the

"shape gradient" of the fluid mesh position vector, or simply as the mesh shape gradient.

The mesh shape gradient can be divided into two components:

ullet The wall boundary component $\dfrac{d\mathbf{X}_{\Gamma}}{ds_{j}}$ which is associated with the grid points of the CFD mesh lying on the

wall boundary \square . This component is *user-specified* in <u>Input</u>. ShapeDerivative as it pertains directly to the shape of the obstacle around/within which a flow is computed.

• The interior component $\frac{d\mathbf{X}_{\Omega}}{ds_{j}}$ which is associated with the grid points located in the interior Ω of the

computational fluid domain. Using for the CFD mesh a deformation model based on a structural analogy (see <u>MeshMotion</u>), this component is determined by solving the usual boundary-driven mesh deformation problem to obtain

$$\frac{d\mathbf{X}_{\Omega}}{ds_{j}} = -\left[\tilde{\mathbf{K}}_{\Omega\Omega}^{-1}\tilde{\mathbf{K}}_{\Omega\Gamma}\right]\frac{d\mathbf{X}_{\Gamma}}{ds_{j}}$$

where $\tilde{\mathbf{K}}$ is the pseudo stiffness matrix of the CFD mesh generated by the chosen of **AERO-F** mesh motion algorithm (see <u>MeshMotion</u>).

In summary, given a *user-specified* wall-boundary shape derivative $\frac{d\mathbf{X}_{\Gamma}}{ds_i}$, **AERO-F** computes the gradient at a

fluid equilibrium point \mathbf{W}_o of an aerodynamic-related quantity q_i with respect to a flow or shape parameter s_j as follows

$$\frac{dq_i}{ds_j}|_{\mathbf{W}_o} = -\frac{dq_i}{d\mathbf{W}}|_{\mathbf{W}_o} \left[\frac{\partial \mathbf{F}}{\partial \mathbf{W}}|_{\mathbf{W}_o} \right]^{-1} \left(\frac{\partial \mathbf{F}}{\partial s_j}|_{\mathbf{W}_o} + \left[\begin{array}{cc} \frac{\partial \mathbf{F}}{\partial \mathbf{X}_{\Omega}}|_{\mathbf{W}_o} & \frac{\partial \mathbf{F}}{\partial \mathbf{X}_{\Gamma}}|_{\mathbf{W}_o} \end{array} \right] \left[\begin{array}{cc} -\tilde{\mathbf{K}}_{\Omega\Omega}^{-1}\tilde{\mathbf{K}}_{\Omega\Gamma} \\ \tilde{\mathbf{I}} \end{array} \right] \frac{d\mathbf{X}_{\Gamma}}{ds_j} \right)$$