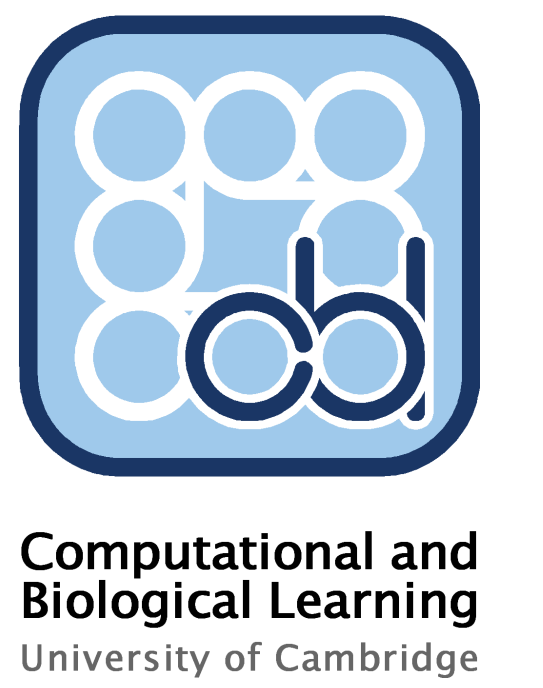
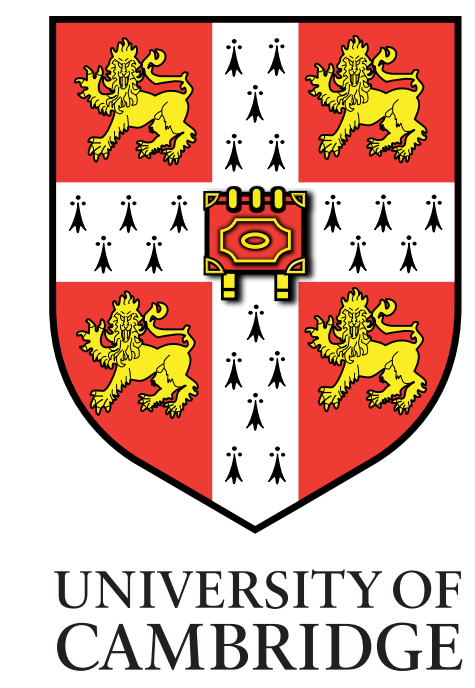




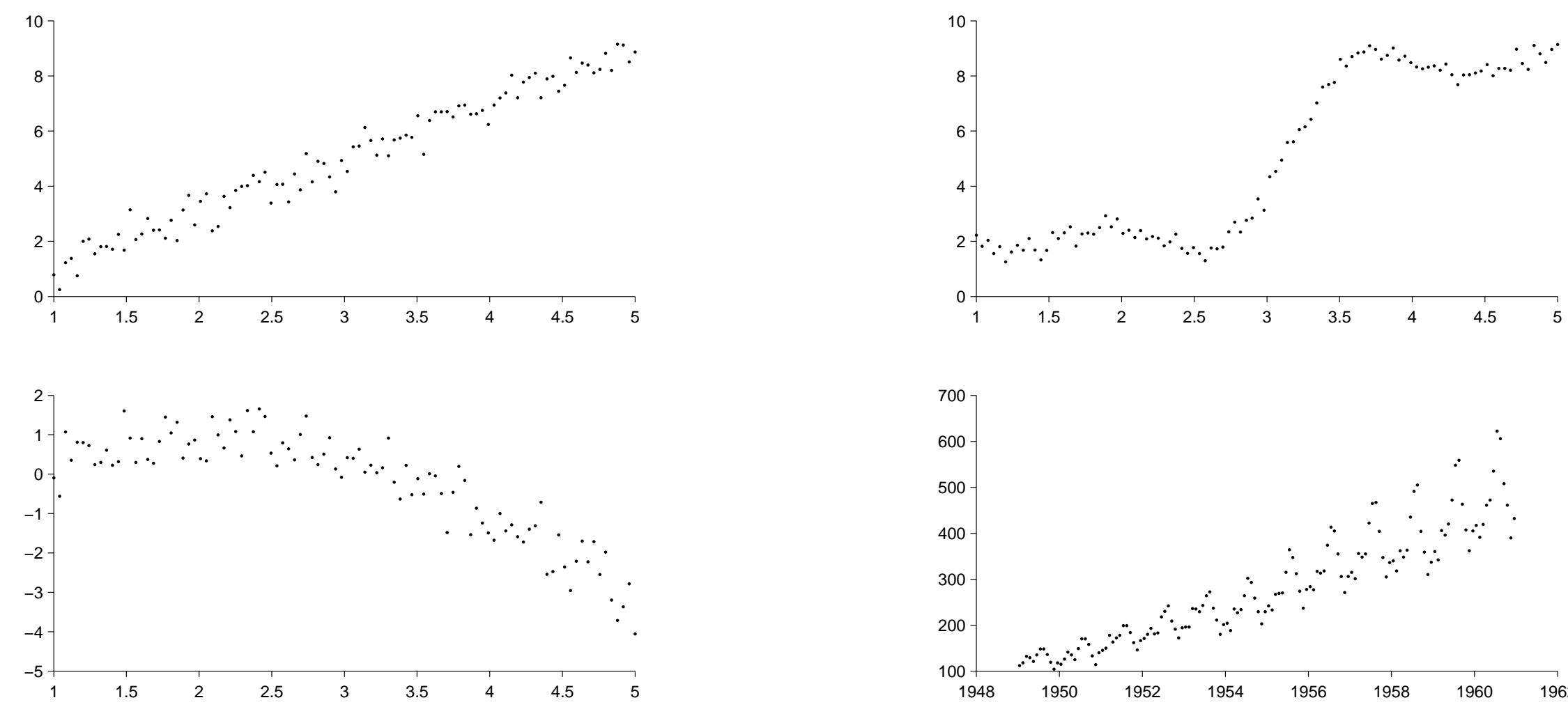
Automating pattern discovery and the statistical process for regression

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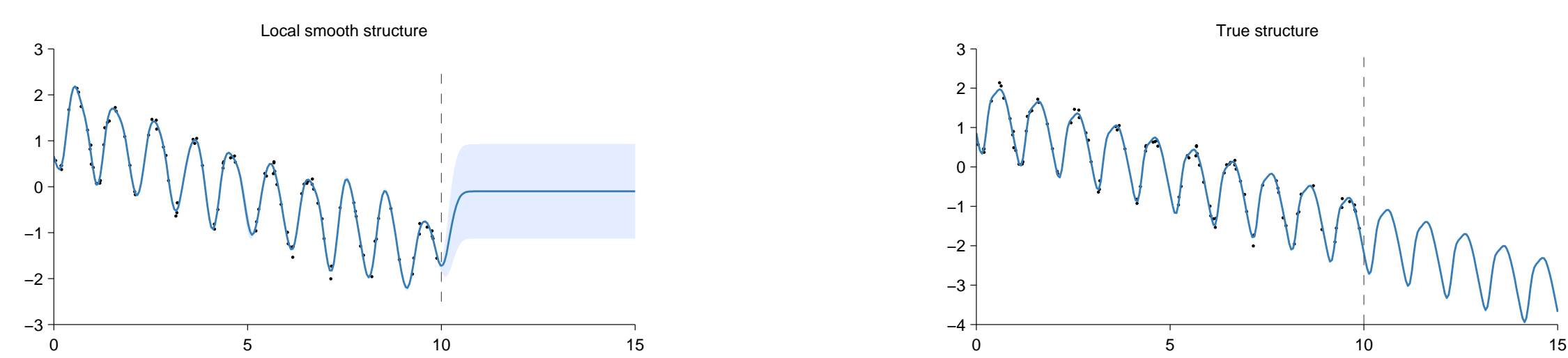
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Data often exhibits high level structure or patterns



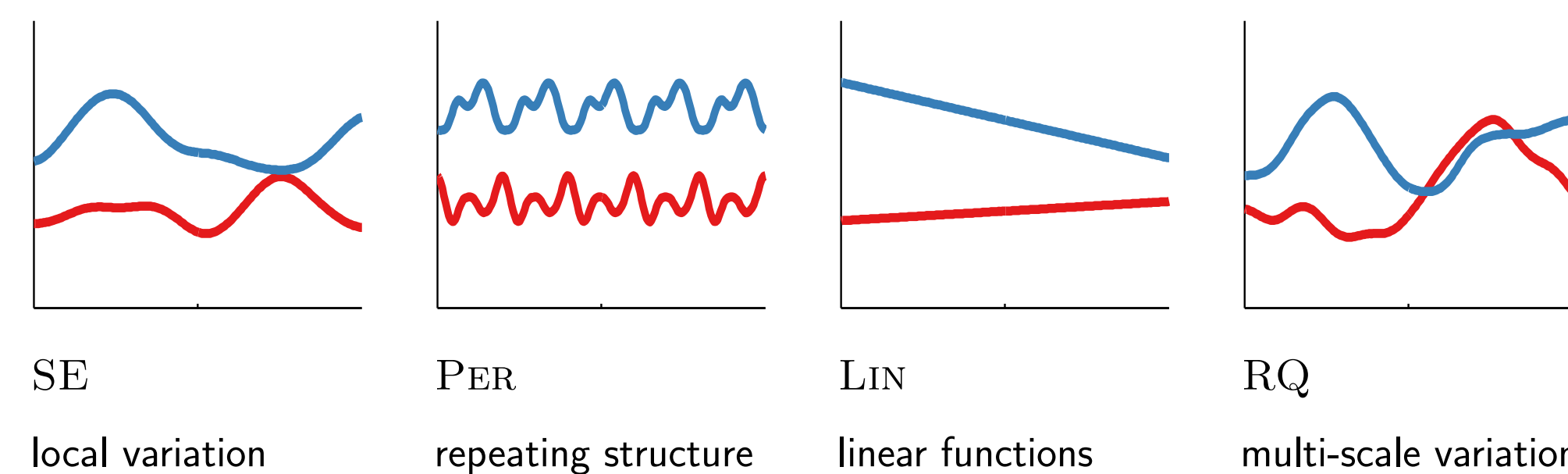
Identifying this structure is crucial for extrapolation



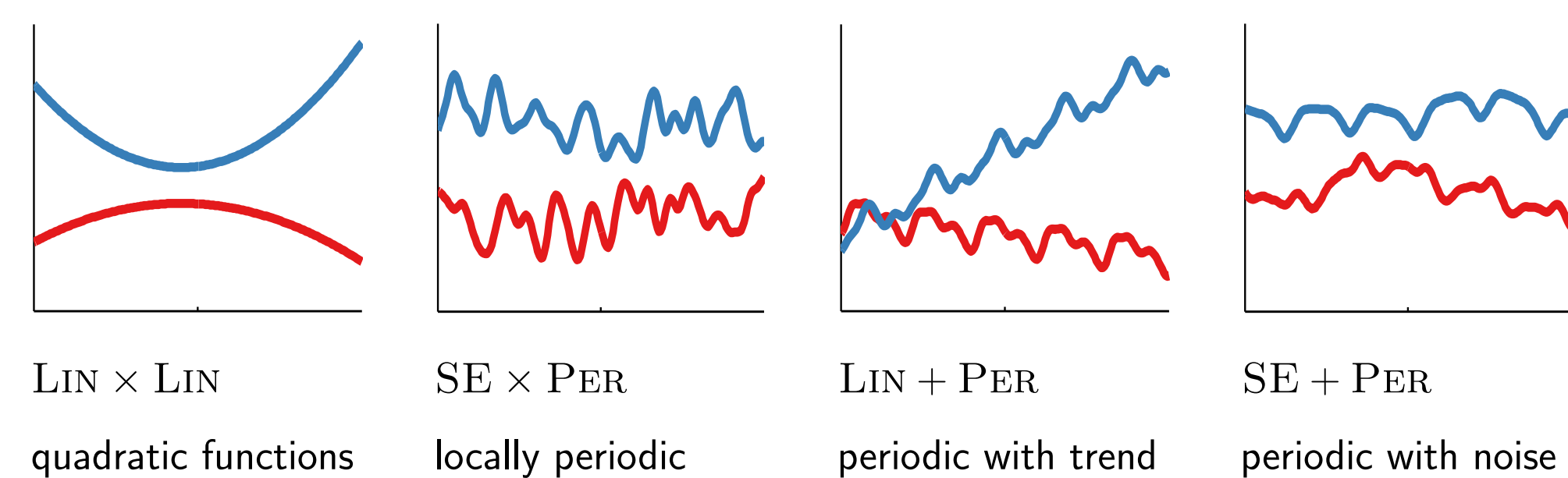
- Traditionally, a researcher / scientist / statistician would select an appropriate model for the type of structures present
- Automatic model selection techniques already exist, typically choosing between a finite or restricted set of models
- Instead, we automate statistical model *construction*

Gaussian process regression can model many structures with an appropriately chosen kernel

- The kernel encodes the inductive bias of the model i.e. the types of functions the model 'believes in'
- Below we list standard base kernels, and examples of functions the model believes in (samples from the prior)



- Base kernels can be combined to create more complicated structural assumptions



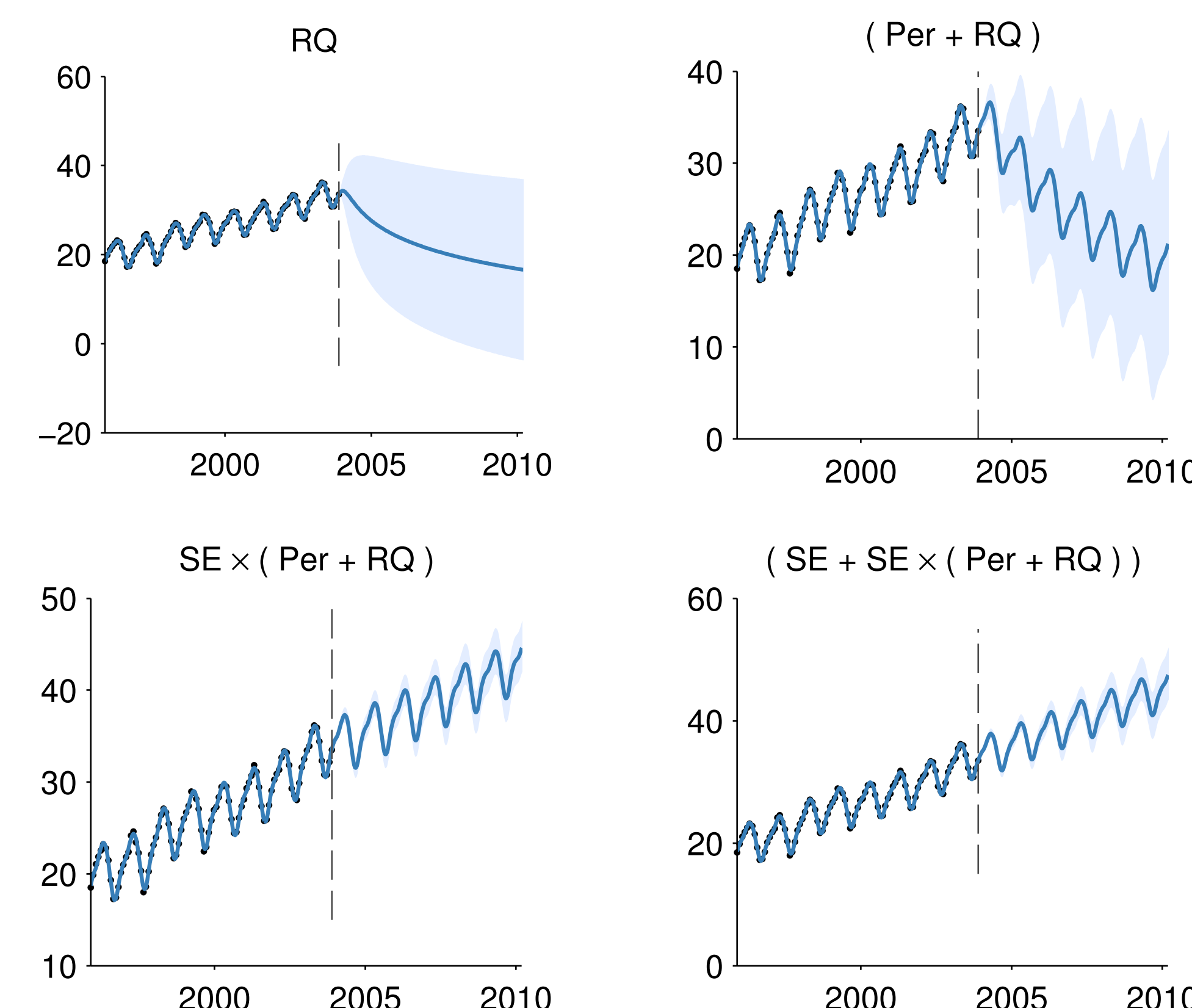
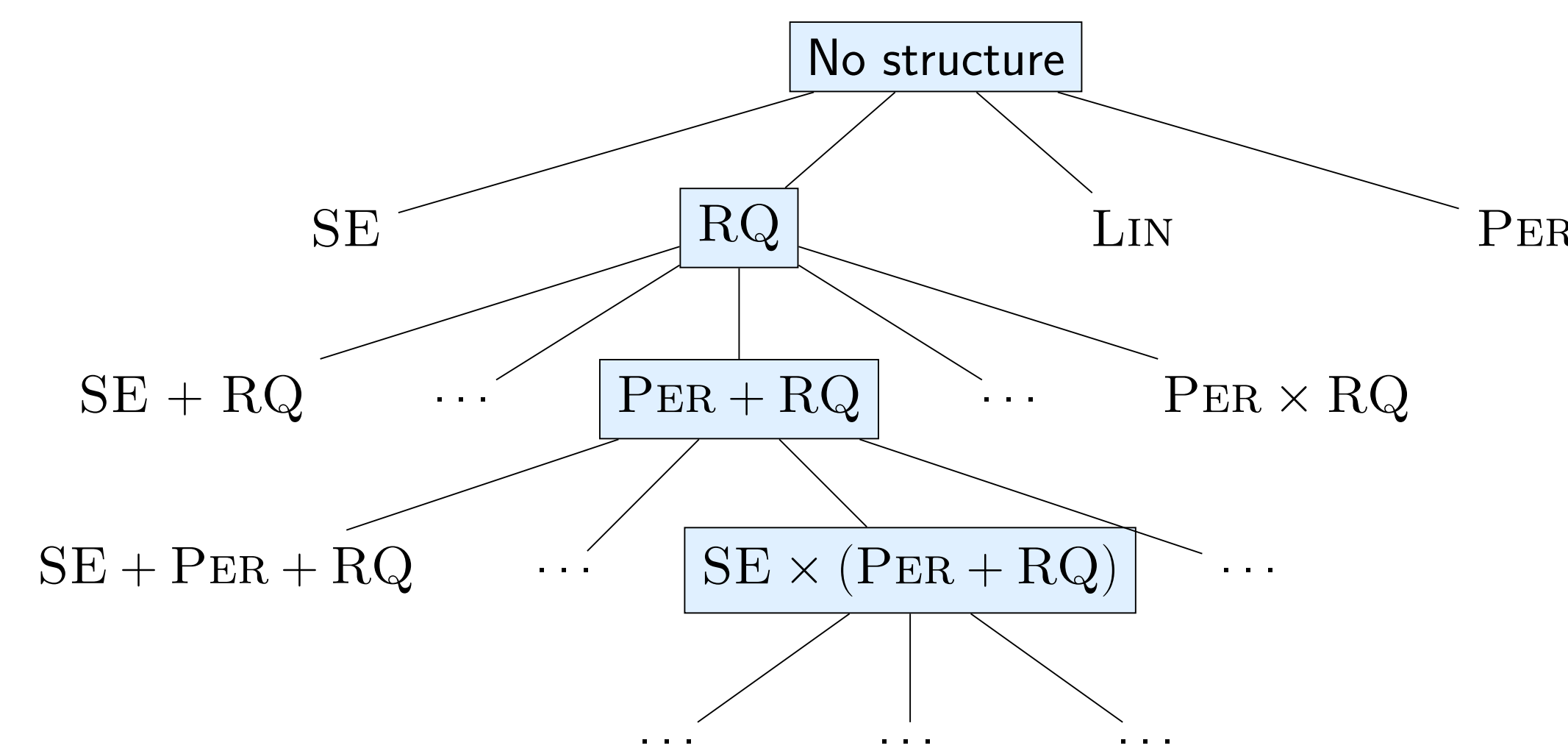
We consider all kernel expressions derived from a generative grammar...

- Constructing appropriate composite kernels has previously been the domain of Gaussian process experts
- We consider all algebraic expressions involving a small number of base kernels and the operations '+' and 'x', including e.g.

Bayesian linear regression	LIN
Bayesian polynomial regression	$LIN \times LIN \times \dots$
Generalized Fourier decomposition	$PER + PER + \dots$
Generalized additive models	$\sum_{d=1}^D SE_d$
Automatic relevance determination	$\prod_{d=1}^D SE_d$
Linear trend with deviations	$LIN + SE$
Linearly growing amplitude	$LIN \times SE$

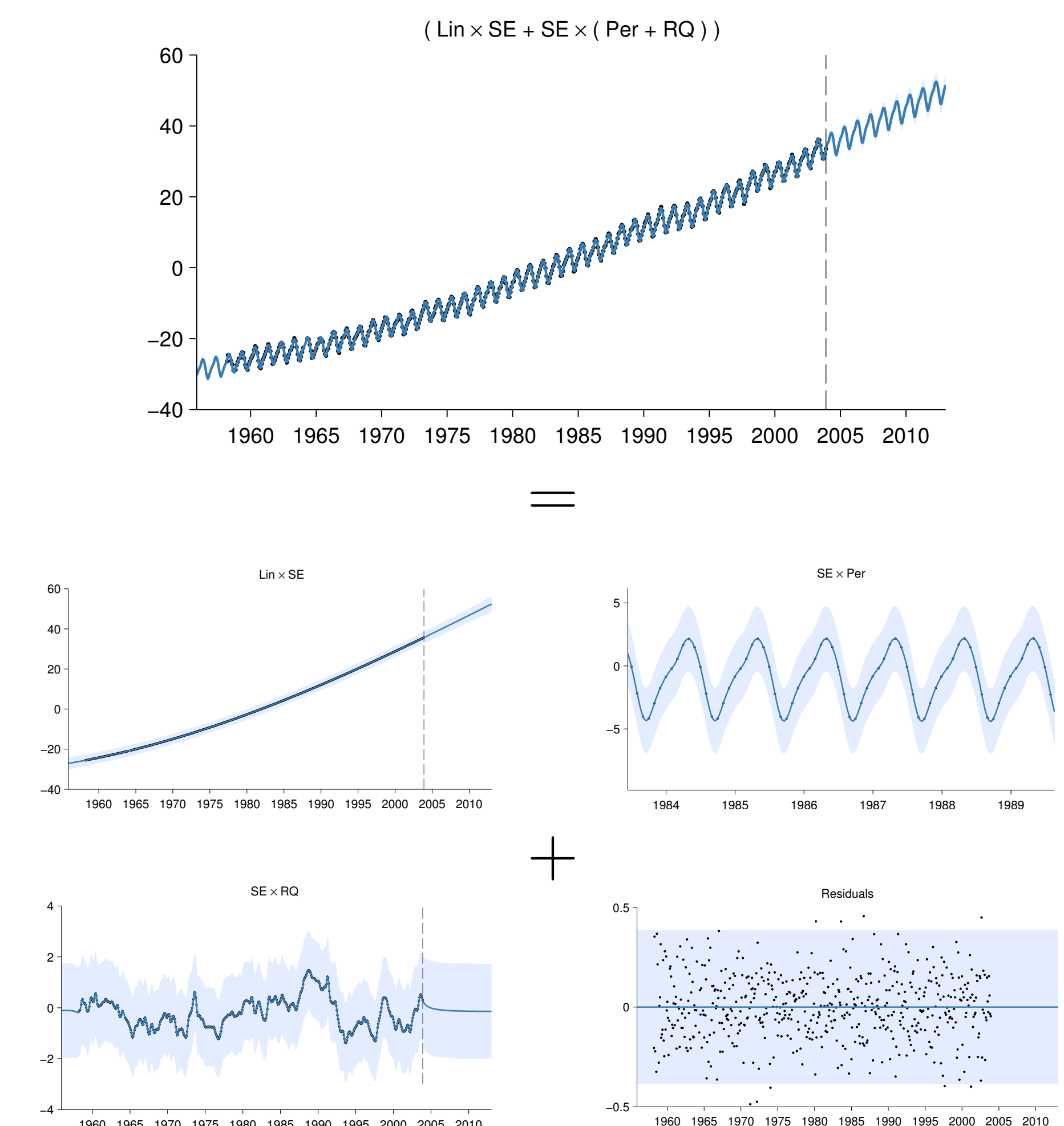
... which we search greedily, producing progressively better statistical models

- We try all base kernels, selecting the one with the highest (approximate) marginal likelihood which balances data fit and model complexity
- The search continues by adding an extra term to the current best kernel, stopping when marginal likelihood no longer improves



Example: Mauna Loa CO₂ concentration

- By automatically inferring an appropriate kernel, we can also automatically decompose functions into additive components (additive components of the kernel correspond to independent additive functions)



Example: International airline passengers

