# **Entropic Forces in Brownian Motion**

Phys 160 Journal Article Report James Saslow

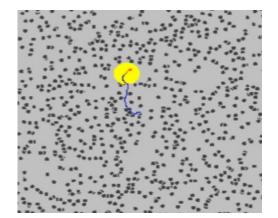
Link to video presentation:

https://www.youtube.com/watch?v=hjmek4pmBJ4&list=PLITM2LUMMTGrnFzYMk5mpvfbSER\_krg7l&index=2

## **Random Walks**

**Brownian Motion** 

(Drift, continuous process)

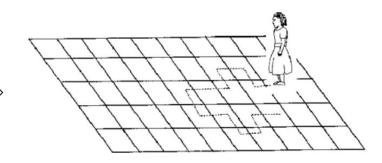


Yellow particle submerged in a fluid

#### **Random Walks**

Simplification

(No drift, discrete process)

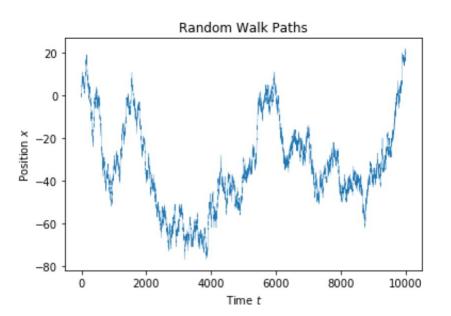


A drunk person making equal steps in random directions

## Random Walks In 1D

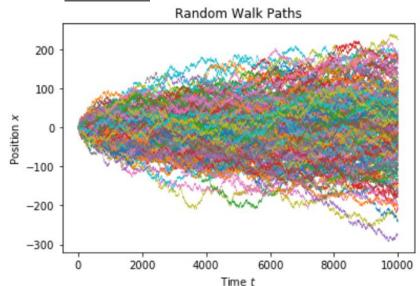
#### A Single Random Walk

- Not very interesting



#### **Several Random Walks**

Very Interesting behavior... <u>Normal</u>
<u>Distribution</u>

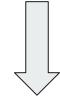


## Time Evolution of Random Walk Distribution



**Diffusion Equation** 

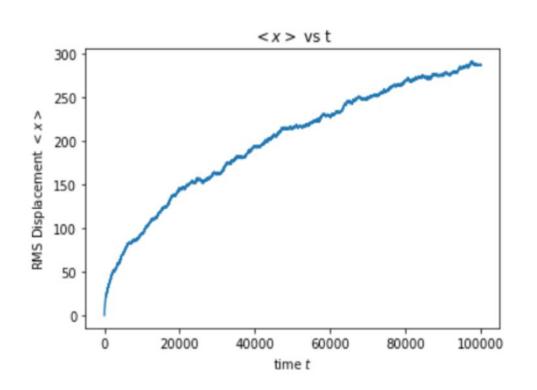
$$\frac{\partial f(\mathbf{r},t)}{\partial t} = D\nabla^2 f(\mathbf{r},t)$$



**Probability Distribution** 

$$f(x,t) = \frac{1}{\sqrt{2\pi[\sigma(t)]^2}} e^{-\frac{x^2}{2[\sigma(t)]^2}}$$

# RMS Displacement as Function of Time



$$< x > \propto t^{1/2}$$

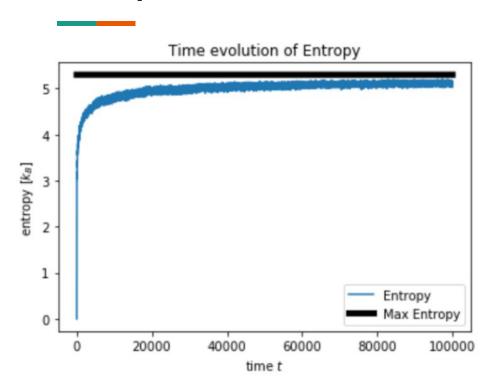
- Concavity in x(t) implies non-zero acceleration
- F=ma ... there must be a force

 It's as if there is a macroscopic force pulling the random walkers away from the starting point

**Entropic Force** 

$$< F > = -mD^2/ < x^3 >$$

# **Entropic Forces**



 The entropic force pulls drunkards away from the origin in order to maximize entropy (Diffusive equilibrium)

#### Conclusion

- Use entropic force/entropy maximization approach to solve other Brownian motion problems
- We don't need the Central Limit Theorem anymore!

Figure 6: Entropy as a function of time for 200 Random Walks