

Paraconsistent and Paracomplete Systems

Paraconsista

April 13 2022

Abstract

Every paraconsistent or paracomplete system invalidates one of the laws of indiscernibility or one of the laws of logical explosion.

Contents

I	General Paraqualifications	1
1	Paracomplete Systems	2
1.1	Indiscernibility of Identicals	2
1.2	Identity of Indiscernibles	2
2	Paraconsistent Systems	2
2.1	Logical Explosion	2
2.2	Contradictory Consequence	3

Part I

General Paraqualifications

1 Paracomplete Systems

A system is generally paracomplete if it invalidates one or both of the laws of indiscernibility.

1.1 Indiscernibility of Identicals

$$\frac{\exists F (Fx \oplus Fy) \vdash x \neq y}{x = y \vdash \forall F (Fx \leftrightarrow Fy)}$$

1.2 Identity of Indiscernibles

$$\frac{x \neq y \vdash \exists F (Fx \oplus Fy)}{\forall F (Fx \leftrightarrow Fy) \vdash x = y}$$

2 Paraconsistent Systems

A system is generally paraconsistent if it invalidates some number of the laws of inconsistency.

2.1 Logical Explosion

$$\frac{\neg y \vdash \neg x \vee x}{x \wedge \neg x \vdash y}$$

2.2 Contradictory Consequence

$$\frac{\neg x \vee x \vdash \neg y}{y \vdash x \wedge \neg x}$$