Titanic Survivors

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October 23, 2015

Overview

The following is an attempt to predict survival of passengers on the Titanic. The data available for use is as follows:

```
891 obs. of 12 variables:
## 'data.frame':
   $ PassengerId: int 1 2 3 4 5 6 7 8 9 10 ...
                : int 0 1 1 1 0 0 0 0 1 1 ...
   $ Survived
##
                : int 3 1 3 1 3 3 1 3 3 2 ...
##
   $ Pclass
##
   $ Name
                : Factor w/ 891 levels "Abbing, Mr. Anthony",...: 109 191 358 277 16 559 520 629 417 58
##
   $ Sex
                 : Factor w/ 2 levels "female", "male": 2 1 1 1 2 2 2 2 1 1 ...
##
   $ Age
                       22 38 26 35 35 NA 54 2 27 14 ...
##
   $ SibSp
                 : int
                      1 1 0 1 0 0 0 3 0 1 ...
##
   $ Parch
                 : int 000000120 ...
                 : Factor w/ 681 levels "110152", "110413",...: 524 597 670 50 473 276 86 396 345 133 ...
##
   $ Ticket
##
   $ Fare
                 : num 7.25 71.28 7.92 53.1 8.05 ...
                 : Factor w/ 148 levels "", "A10", "A14",..: 1 83 1 57 1 1 131 1 1 1 ...
  $ Cabin
                 : Factor w/ 4 levels "", "C", "Q", "S": 4 2 4 4 4 3 4 4 4 2 ...
   $ Embarked
```

SPECIAL NOTES:

Pclass is a proxy for socio-economic status: 1st ~ Upper; 2nd ~ Middle; 3rd ~ Lower

SibSp refers to the number of siblings or spouses

Parch refers to the number of parents or children

Since age was not available for all passengers, missing age values were projected using a linear model composed of number of siblings/spouses, number of parents/children, and class. For the rest of the paper, any mention of Age is actually referring to the projected age.

Primary predictors - Sex and Class

Starting from nothing, correlations with survival will give us a rough sense of the relative importance of variables.

```
## Sex Pclass Fare Embarked Parch Age
## -0.53882559 -0.35965268 0.26818862 -0.18997851 0.09331701 -0.07722109
## projAge SibSp
## -0.07722109 -0.01735836
```

Sex, Pclass, and Fare jump out as the three likely predictors. Attempting to model survival using Sex, Pclass, and Fare in a logistic regression shows that both Sex and Pclass improve model fit, but Fare does not.

```
## Analysis of Deviance Table
##
## Model 1: Survived ~ Sex
## Model 2: Survived ~ Sex + Pclass
## Model 3: Survived ~ Sex + Pclass + Fare
##
     Resid. Df Resid. Dev Df Deviance Pr(>Chi)
## 1
           889
                   917.80
## 2
           888
                                90.608
                   827.20
                           1
                                         <2e-16 ***
## 3
           887
                   826.67
                                 0.521
                                         0.4704
                           1
## Signif. codes:
                   0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
```

A likely explanation of this is the high correlation between Pclass and Fare. Fare doesn't ostensibly provide any insight not provided by Pclass.

[1] -0.5494996

Low correlation across the entire sample does not necessarily mean a variable will not add value to the model. As shown below, there are several more terms that add significant value to the model.

```
## Analysis of Deviance Table
##
## Model 1: Survived ~ Sex
## Model 2: Survived ~ Sex + Pclass
## Model 3: Survived ~ Sex + Pclass + projAge
## Model 4: Survived ~ Sex + Pclass + projAge + SibSp
## Model 5: Survived ~ Sex + Pclass + projAge + SibSp + Sex:Pclass
     Resid. Df Resid. Dev Df Deviance Pr(>Chi)
##
## 1
           889
                   917.80
## 2
           888
                   827.20
                           1
                                90.608 < 2.2e-16 ***
## 3
           887
                   808.96
                                18.239 1.949e-05 ***
                           1
## 4
           886
                   787.47
                                21.487 3.563e-06 ***
## 5
           885
                   764.48
                                22.990 1.628e-06 ***
## ---
                   0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
## Signif. codes:
```

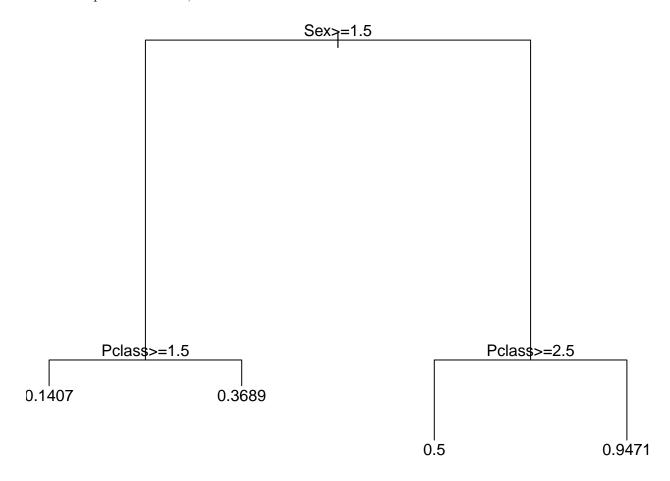
Secondary Predictors - Age and Siblings

How can we explain the effect of Age and SibSp on the model? Why is the interaction term between Sex and Pclass important?

To answer these questions, let's look at a decision tree that takes Sex and Pclass into account.

Here, we see that 94.7% of 1st and 2nd class women survived versus 50% of 3rd class women. Additionally, 14% of 2nd and 3rd class men survived versus 36.9% of 1st class men. Two things are clear from this tree:

- Pclass matters much more for women than for men, explaining the importance of the interaction term
- To improve the model, our focus should be on 3rd class women and 1st class men.

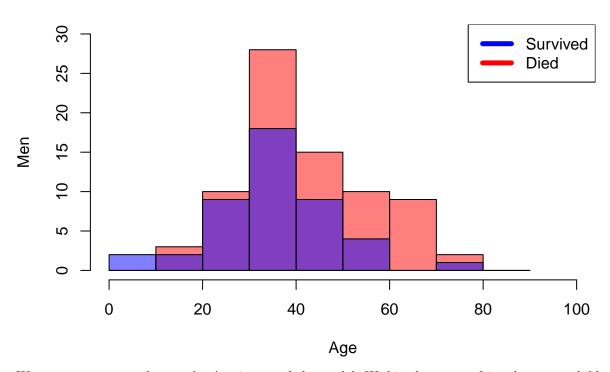


Let's subset the data into our new groups of interest and re-correlate with survival.

1st class men

Age projAge Fare SibSp Embarked Parch ## -0.27056553 -0.27056553 0.09124571 0.06835598 -0.06544025 0.01529884

Age of 1st Class Men, Split by Survival

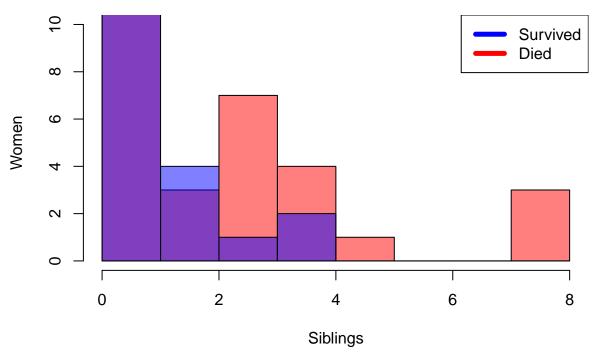


We can now more easily see why Age improved the model. Within the group of 1st class men, children are more likely to survive and older men are more likely to die.

3rd class women

```
## Fare Embarked SibSp Age projAge Parch ## -0.3019067 -0.2017206 -0.1906067 -0.1766173 -0.1766173 -0.1700098
```

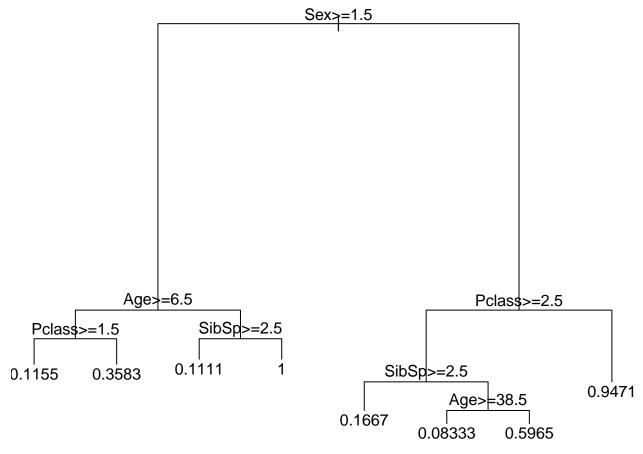
Siblings for 3rd Class Women, Split by Survival



We can now more easily see why SibSp improved the model. Within the group of 3rd class women, those with fewer siblings are more likely to survive. There also does appear to be an effect from Fare and Embarked emerge in this subset. However, this investigation will not be pursued in this paper.

A (More) Complete Decision Tree

Let's add our secondary predictors to our decision tree:



Here, we can see the effect of Age on 1st class men and SibSp on 3rd class women. We can also see that in fact, both Age and SibSp have an effect on our other groups as well.

The large groups still with room for improvement at this point are shown below along with the group survival correlations.

• 1st class men over the age of 6.5

```
## SibSp Embarked Fare Parch
## 0.08748861 -0.06464291 0.06056810 -0.02093851
```

• 3rd class women under the age of 38.5 with 2 or fewer siblings

```
## Embarked Fare Parch
## -0.19870102 -0.05232360 -0.01619802
```

There is no obvious improvement to be made for 1st class men over the age of 6.5.

It is possible that accounting for embarkment could improve predictions for 3rd class women under the age of 38.5 with 2 or fewer siblings. However, this investigation will not be pursued in this paper.

Logistic Regression, Decision Tree, or Random Forest?

Now that we know which variables we want to include, let's compare the relative success of these techniques on the train and test data sets.

Logistic Regression

Below is the proportion of correct responses in the train set using logistic regression on Sex+Pclass+SibSp+projAge+Sex:Pclass.

[1] 0.8125701

On the test data, this performs at about .77 correct.

Logistic Model Tree

Below is the proportion of correct responses in the train set using a logistic model tree partitioned on Sex+Pclass+projAge and leaves modeled with Parch+SibSp+Embarked.

[1] 0.8282828

On the test data, this performs at about .78 correct.

Conditional Tree

Below is the proportion of correct responses in the train set using a conditional inference tree on Sex+Pclass+SibSp+projAge.

[1] 0.8395062

On the test data, this performs at about .75 correct.

Random forest

Below is the proportion of correct responses in the train set using a random forest on Sex+Pclass+SibSp+projAge.

[1] 0.8204265

On the test data, this performs at about .75 correct.

Naive Bayes

Below is the proportion of correct responses in the train set using a Naive Bayesian classifier on Sex+Pclass+Embarked

[1] 0.7777778

On the test data, this performs at about .68

${\bf Adaboost}$

 $Below\ is\ the\ proportion\ of\ correct\ responses\ in\ the\ train\ set\ using\ Adaboost\ on\ Sex+Pclass+SibSp+projAge+Parch+Fare+Embaron and the set of the proportion of\ correct\ responses\ in\ the\ train\ set\ using\ Adaboost\ on\ Sex+Pclass+SibSp+projAge+Parch+Fare+Embaron and the proportion of\ correct\ responses\ in\ the\ train\ set\ using\ Adaboost\ on\ Sex+Pclass+SibSp+projAge+Parch+Fare+Embaron and the proportion\ of\ correct\ responses\ in\ the\ train\ set\ using\ Adaboost\ on\ Sex+Pclass+SibSp+projAge+Parch+Fare+Embaron and the proportion\ of\ correct\ responses\ in\ the\ train\ set\ using\ Adaboost\ on\ Sex+Pclass+SibSp+projAge+Parch+Fare+Embaron and the proportion\ of\ correct\ responses\ in\ the\ train\ set\ using\ Adaboost\ on\ Sex+Pclass+SibSp+projAge+Parch+Fare+Embaron and the proportion\ of\ correct\ responses\ in\ the\ train\ set\ using\ Adaboost\ on\ Sex+Pclass+SibSp+projAge+Parch+Fare+Embaron\ on\ sex+Pclass+SibSp+projAge+Parch+Far$

[1] 0.8765432

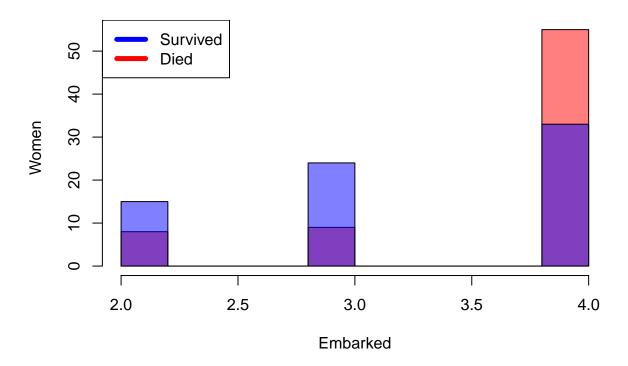
On the test data, this performs at about .73684.

Room for further improvement

Embarkment's role in survival was not explored in this analysis. It had a weak, but statistically significant correlation with Survival across the entire population, as well as with 3rd class women.

```
##
           Sex
                    Pclass
                                          Embarked
                                  Fare
                                                          Parch
## -0.53882559 -0.35965268
                           0.26818862 -0.18997851 0.09331701 -0.07722109
       projAge
                     SibSp
## -0.07722109 -0.01735836
##
         Fare
                Embarked
                              SibSp
                                                                Parch
                                           Age
                                                   projAge
## -0.3019067 -0.2017206 -0.1906067 -0.1766173 -0.1766173 -0.1700098
```

Embarkments for 3rd Class Women, Split by Survival



Embarkment also potentially improves upon the regression model and can't be explained away as redundant because it is not as strongly correlated with Pclass as Fare was.

```
## Analysis of Deviance Table
##
## Model 1: Survived ~ Sex
## Model 2: Survived ~ Sex + Pclass
## Model 3: Survived ~ Sex + Pclass + projAge
## Model 4: Survived ~ Sex + Pclass + projAge + SibSp
## Model 5: Survived ~ Sex + Pclass + projAge + SibSp + Sex:Pclass
## Model 6: Survived ~ Sex + Pclass + projAge + SibSp + Embarked + Sex:Pclass
     Resid. Df Resid. Dev Df Deviance Pr(>Chi)
##
## 1
           889
                   917.80
## 2
           888
                   827.20 1
                               90.608 < 2.2e-16 ***
## 3
           887
                   808.96 1
                               18.239 1.949e-05 ***
## 4
           886
                   787.47
                           1
                               21.487 3.563e-06 ***
                               22.990 1.628e-06 ***
## 5
           885
                   764.48
                           1
## 6
           884
                   758.76 1
                                5.718
                                        0.01679 *
                   0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
## Signif. codes:
          Fare
                    Pclass
                              Survived
                                                Sex
                                                            Age
                                                                    projAge
               0.25329050 -0.18997851 0.11984079 -0.04483030 -0.04483030
## -0.28679953
##
         SibSp
                     Parch
   0.03762860
               0.01627835
```

Besides embarkment, certain variables were removed from the start. The marginal benefits of Name, Ticket, and Cabin were deemed too small to warrant a thoughtful translation of those fields for use in modeling. It is however always possible these fields do contain useful information which could improve the model.