



THE UNIVERSITY OF
MELBOURNE

v1.0

Sensors and Signal Processing

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Mobile Computing | 13-Aug-2018

COMP90018 - Mobile Computing Systems Programming

“The materials on LMS for tutorials are confusing. I heard they're mixed with last year/semester's.”

Microblog: Feedback

“For some complex mobile devices, maybe it's difficult to determine a single goal or it is multi-functional, in this case, the execution and evaluation should be separated for each goal or integrate them together? And how?”

Microblog: Question

1. Technology inevitably alters our perception of reality.

SpiderSense, 2013



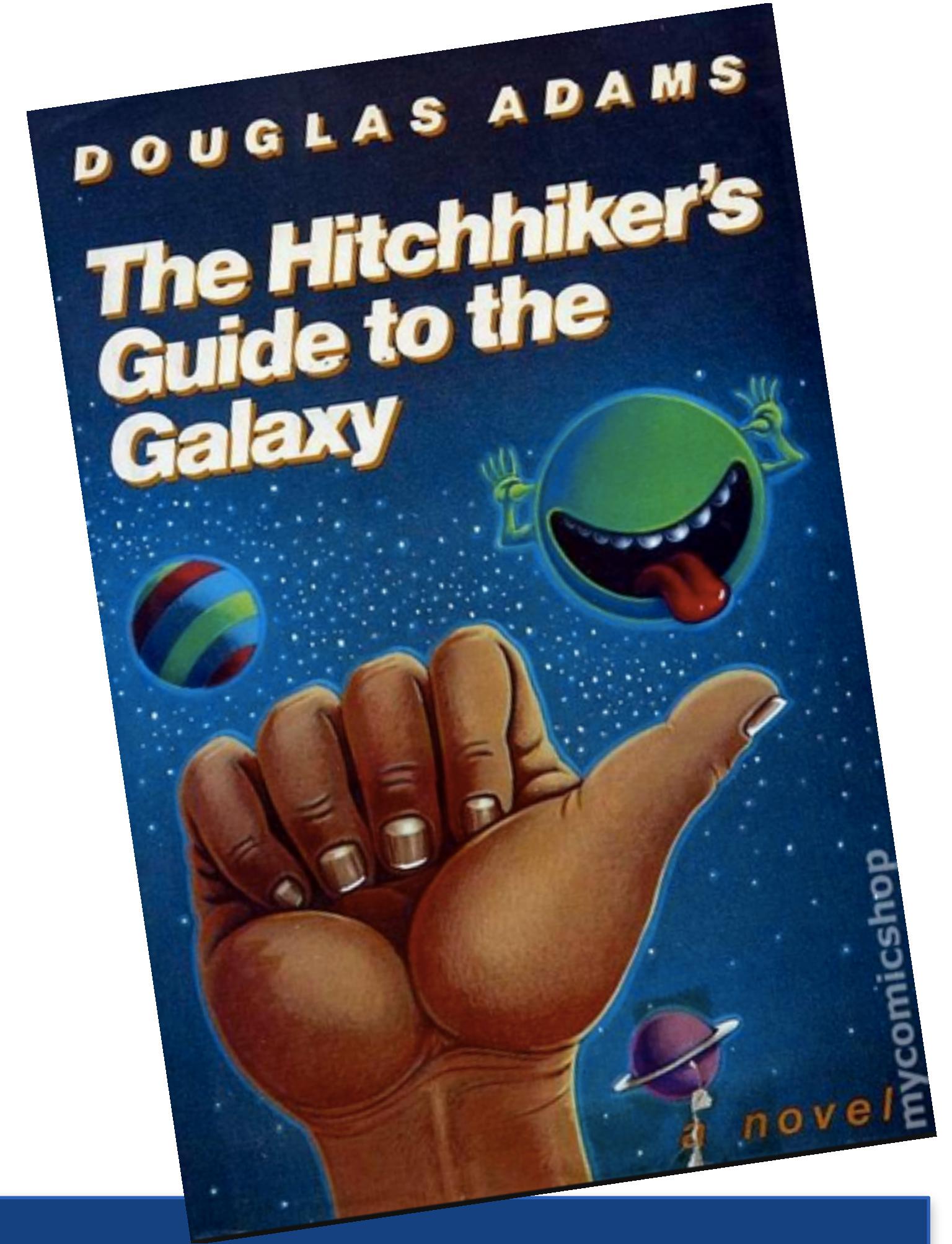
Observations

1. Technology inevitably alters our perception of reality.
2. Computers are increasingly defining our experiences in the real world.



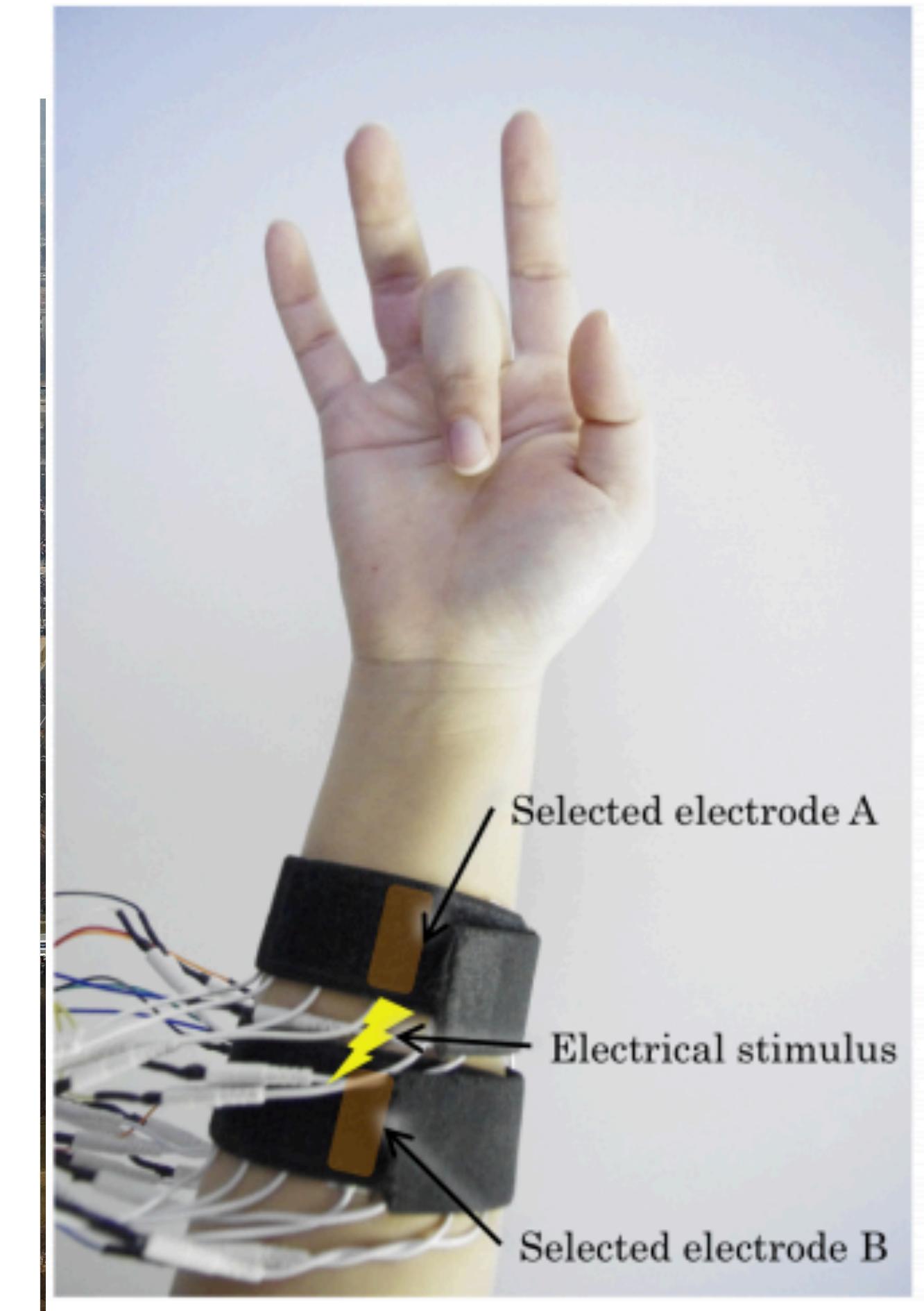
Observations

1. Technology inevitably alters our perception of reality.
2. Computers are increasingly defining our experiences in the real world.
3. We engineer a world where humans live in the I/O system of a giant computer.



Observations

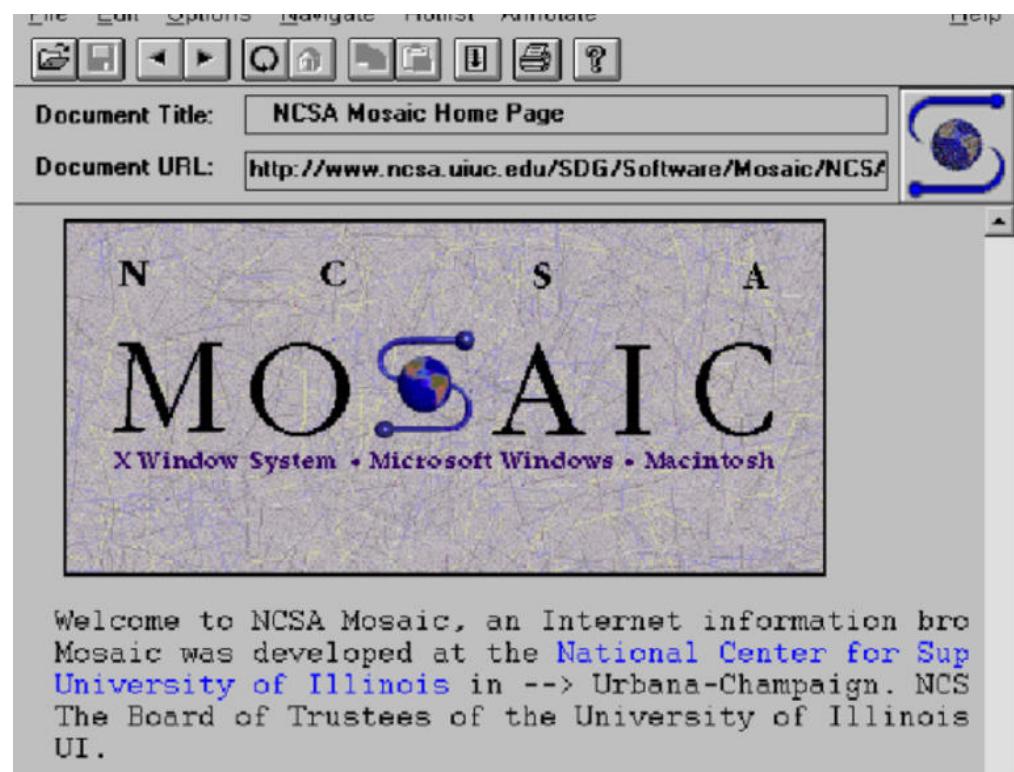
1. Technology inevitably alters our perception of reality.
2. Computers are increasingly defining our experiences in the real world.
3. We engineer a world where humans live in the I/O system of a giant computer.
4. With computers and technologies we manipulate humans.



Observations

1. Sensors as a Driver for Ubiquitous Computing Technologies
2. What Constitutes a Sensor?
3. Challenges when Dealing with Sensor Data
4. Sensor Signal Processing: Dealing with these challenges

Learning Outcomes



Recap: Ubiquitous Computing - The Third Wave

In the Environment



IBM PC

On the User



Osborne 1

Two fundamentally different approaches for ubiquitous interaction

In the Environment



Kinect

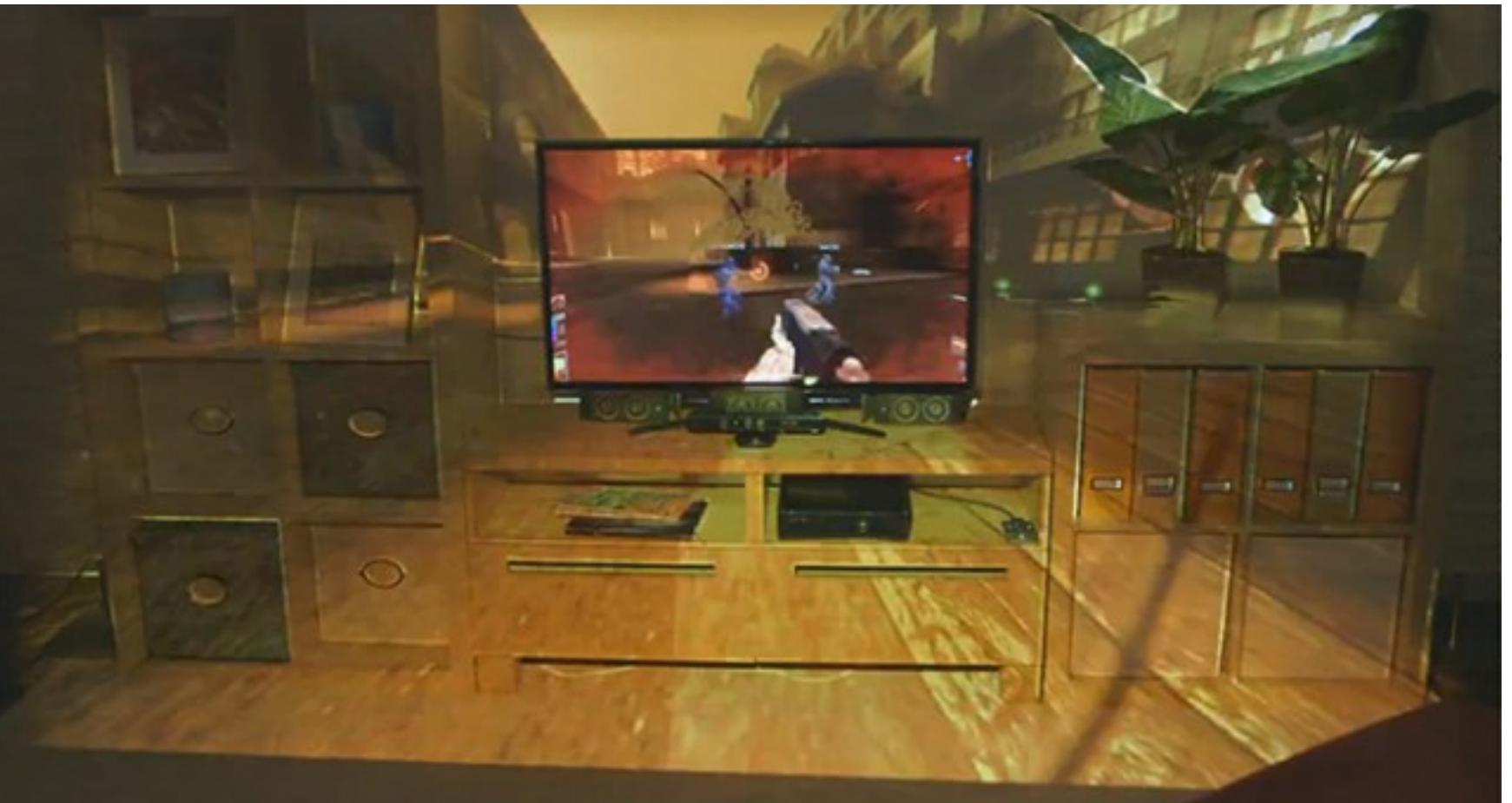
On the User



PS Vita

Two fundamentally different approaches for ubiquitous interaction

In the Environment



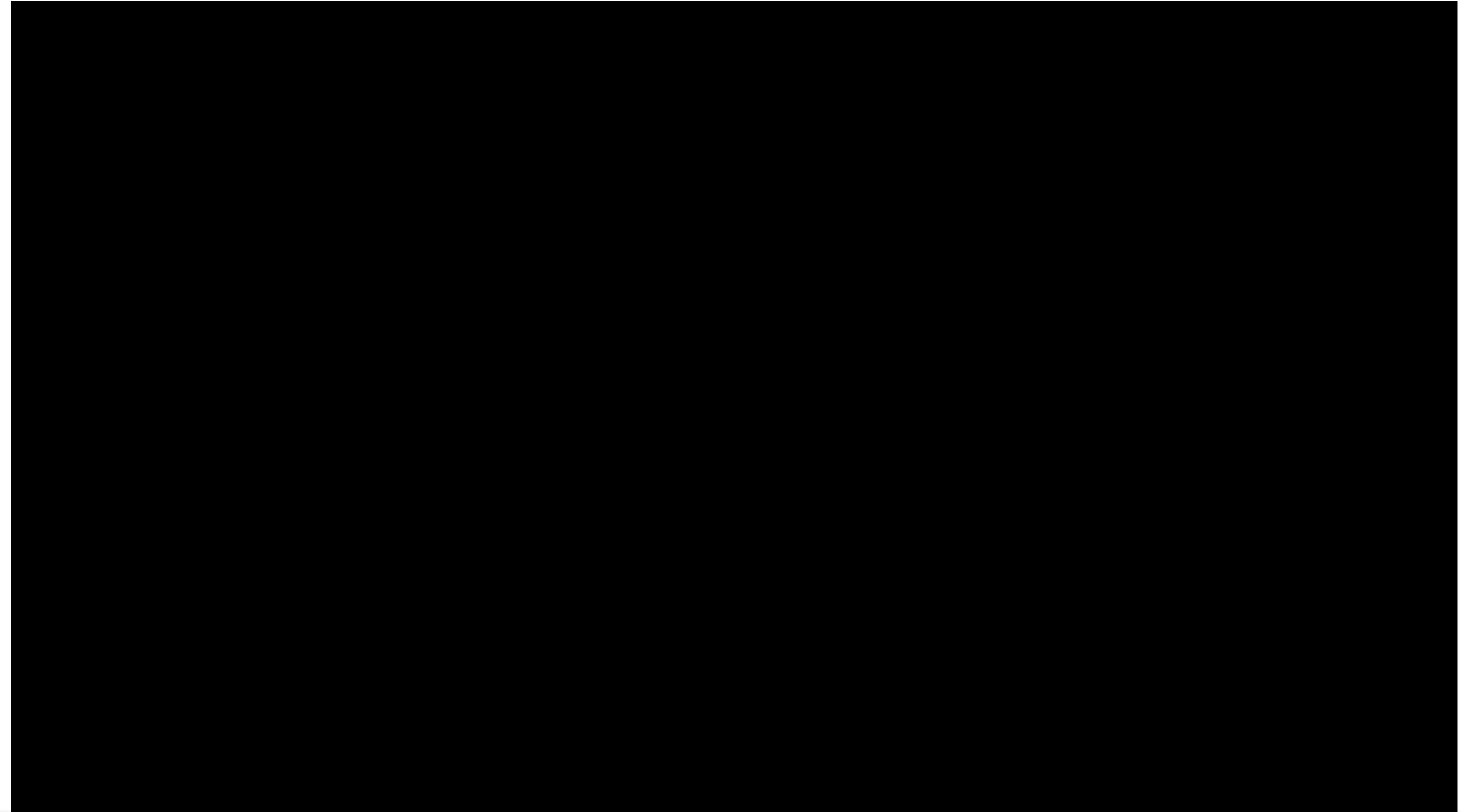
Illumiroom

On the User



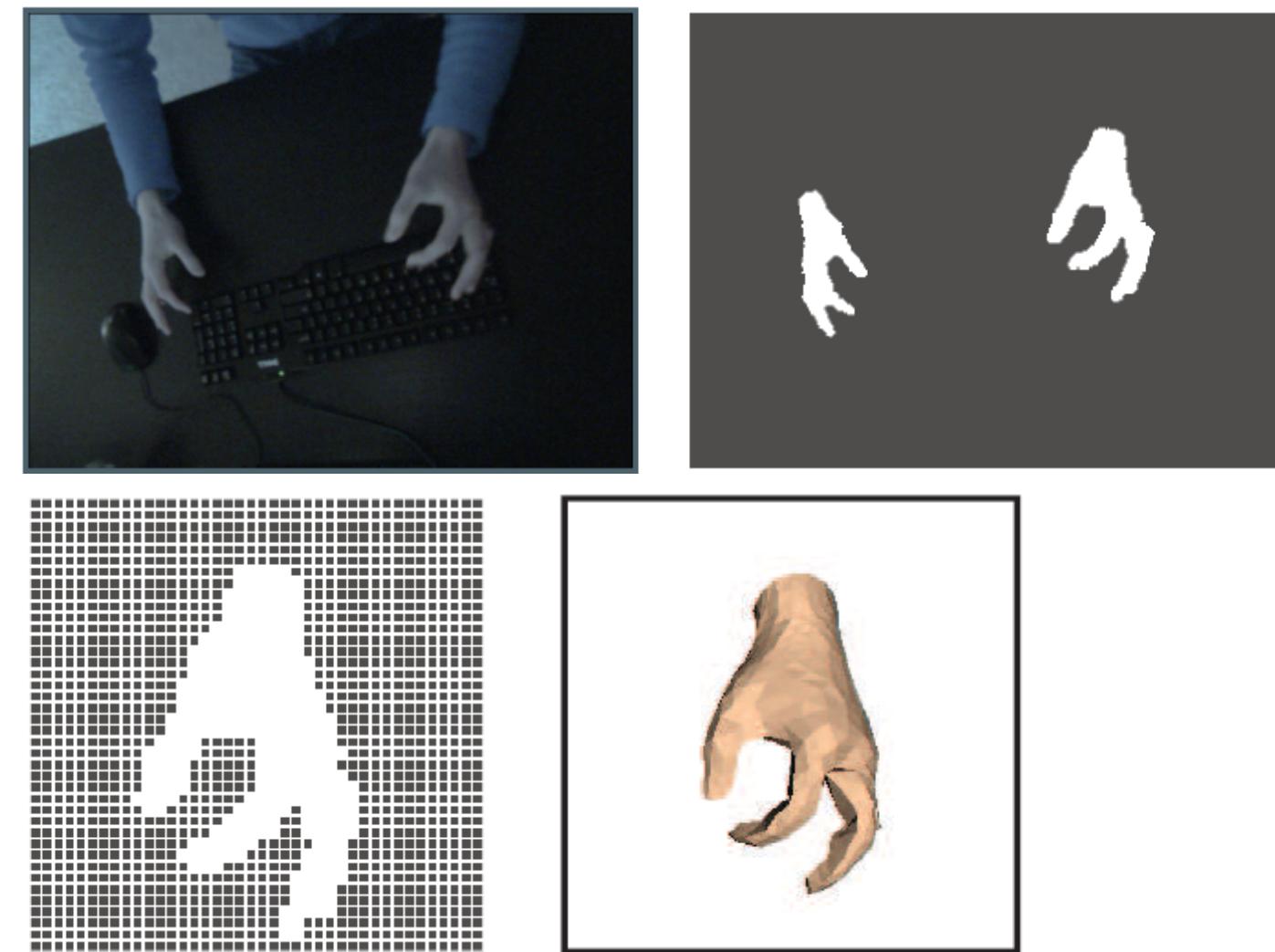
Junaio by Metaio

Two fundamentally different approaches for ubiquitous interaction



IllumiRoom

In the Environment



On the User



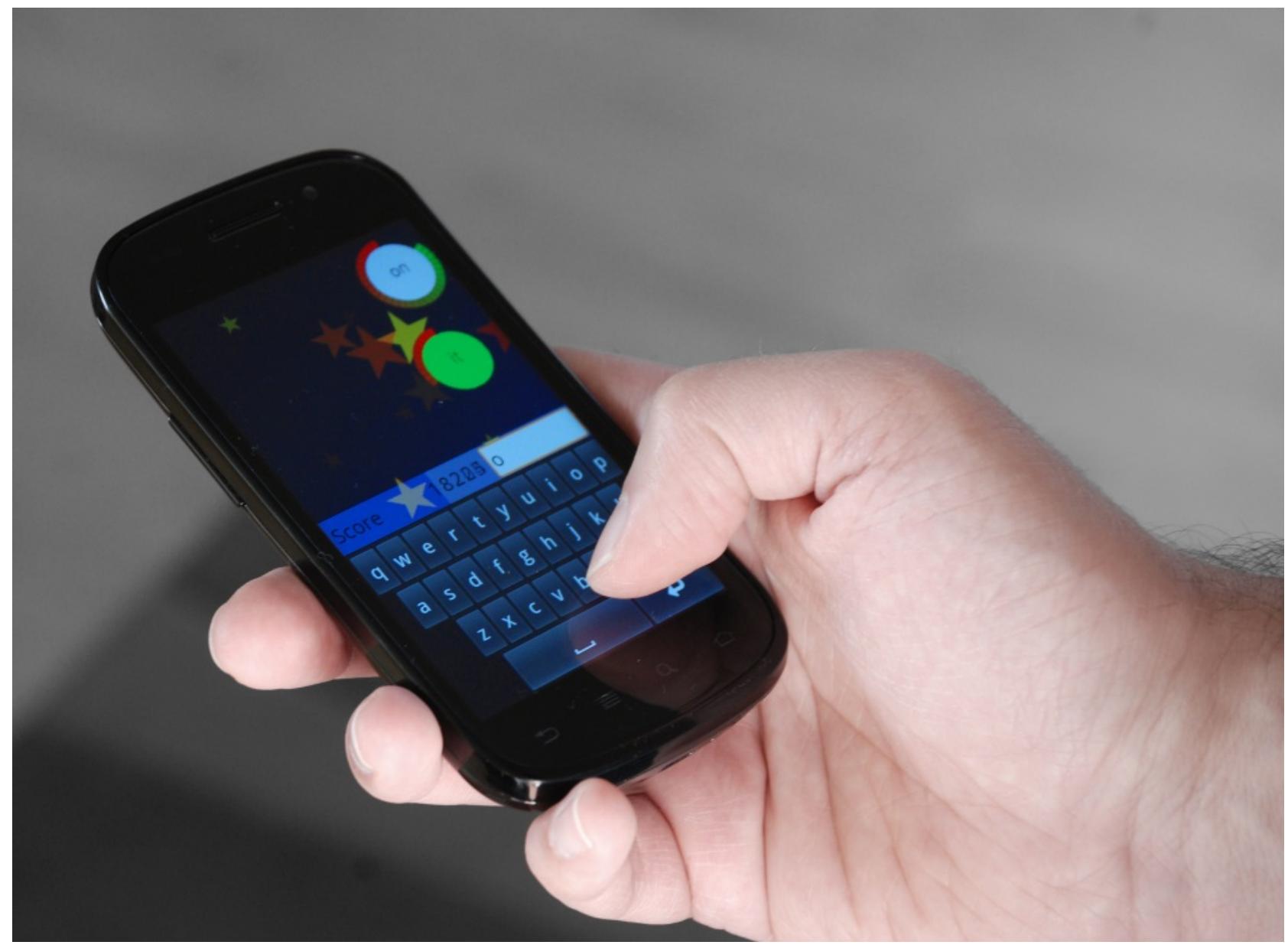
Gesture Recognition

Two fundamentally different approaches for
ubiquitous interaction

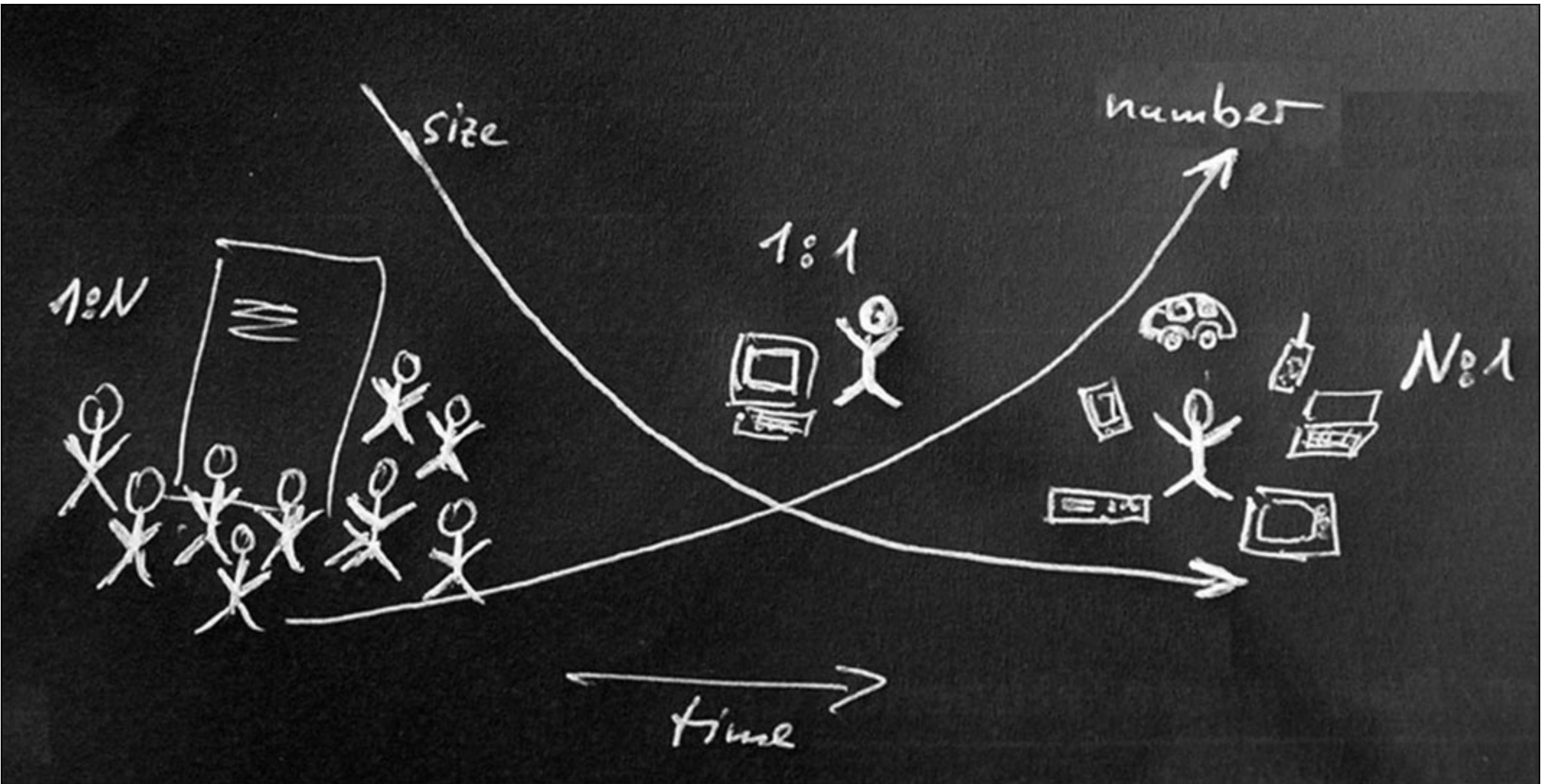
In the Environment



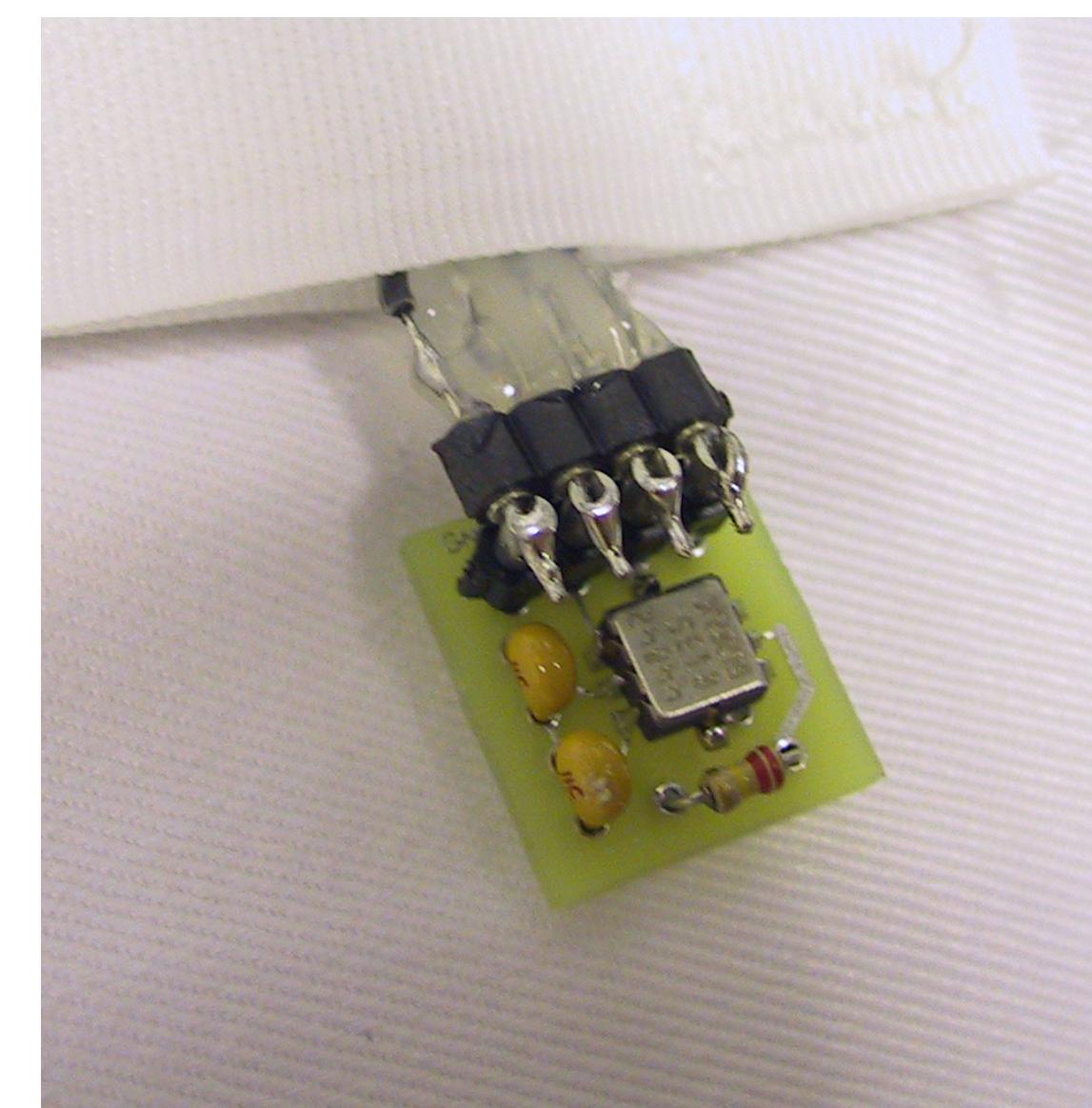
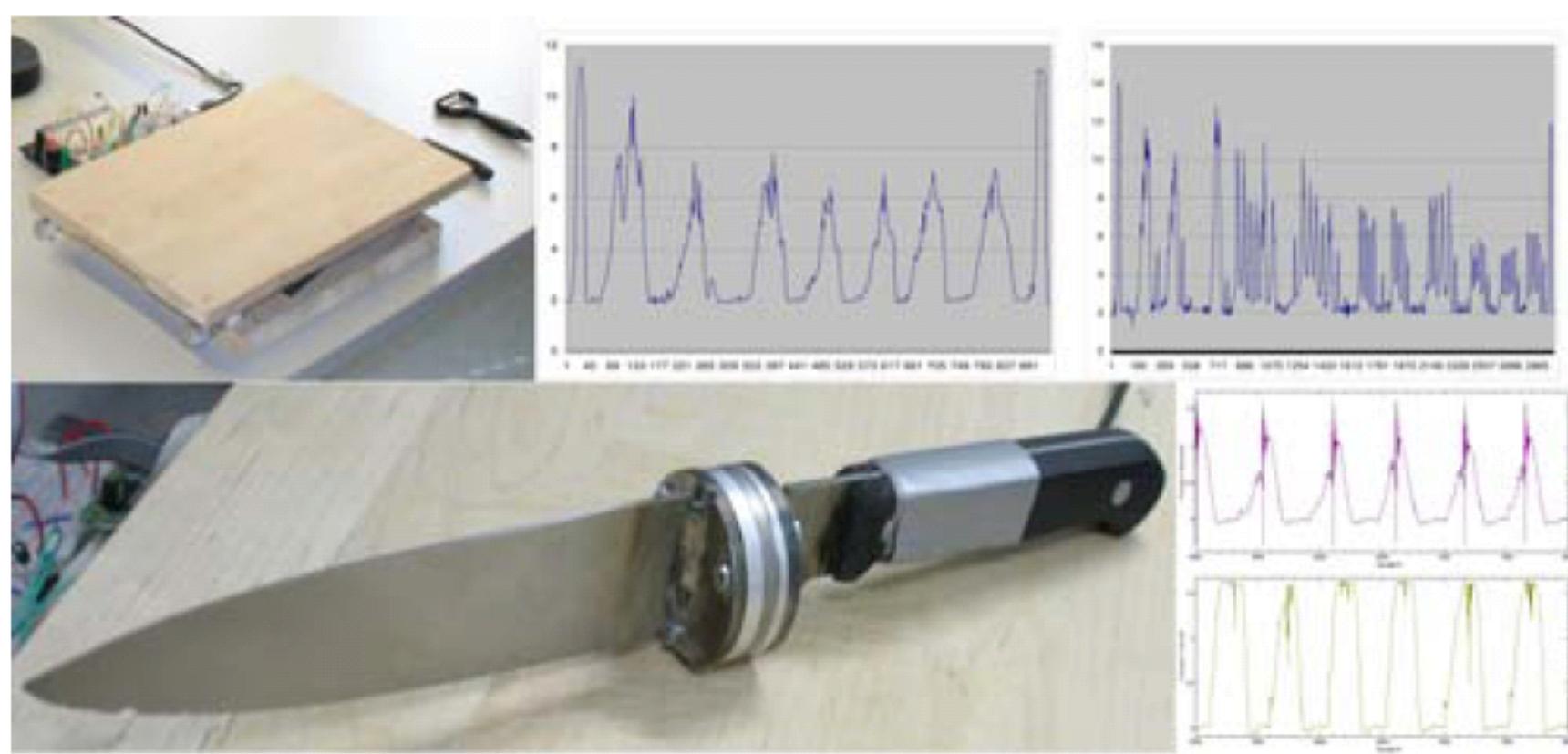
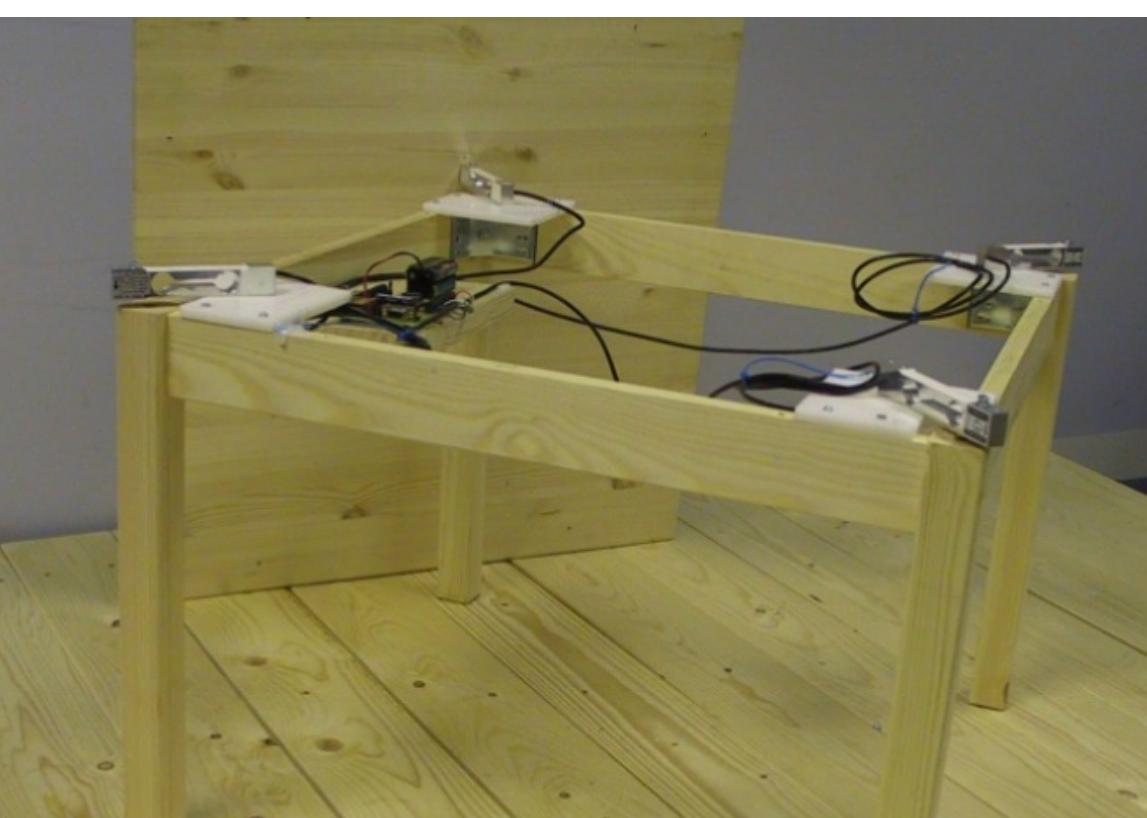
On the User



Two fundamentally different approaches for ubiquitous interaction



Ubiquitous Computing



Aware – Everything



Trends and Drivers



Mobile devices are the main technology for accessing the WEB

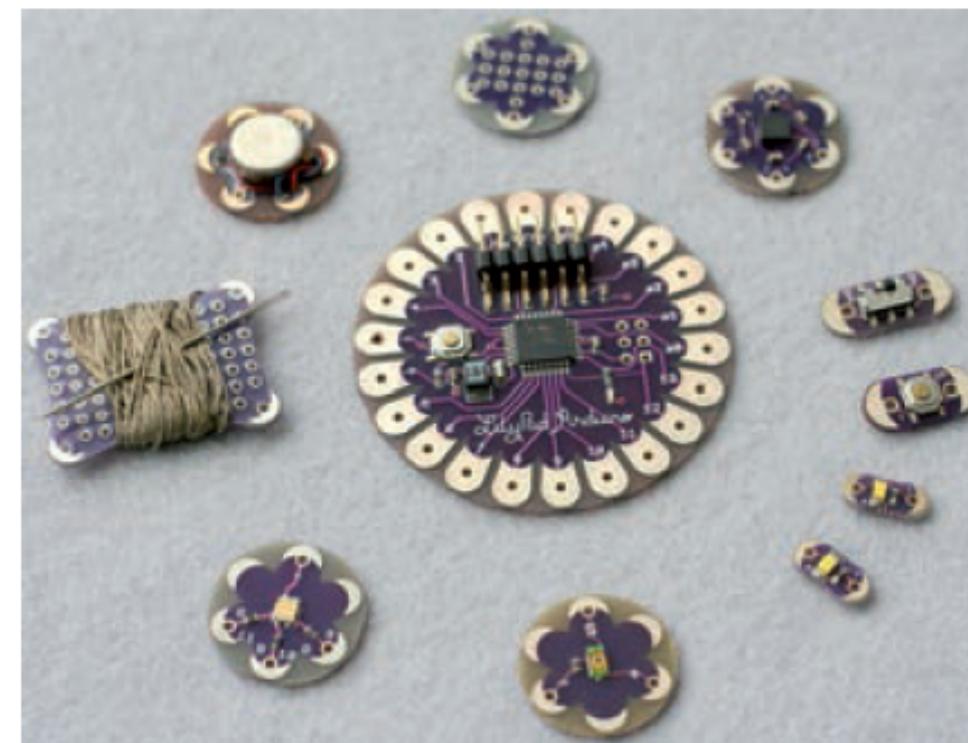
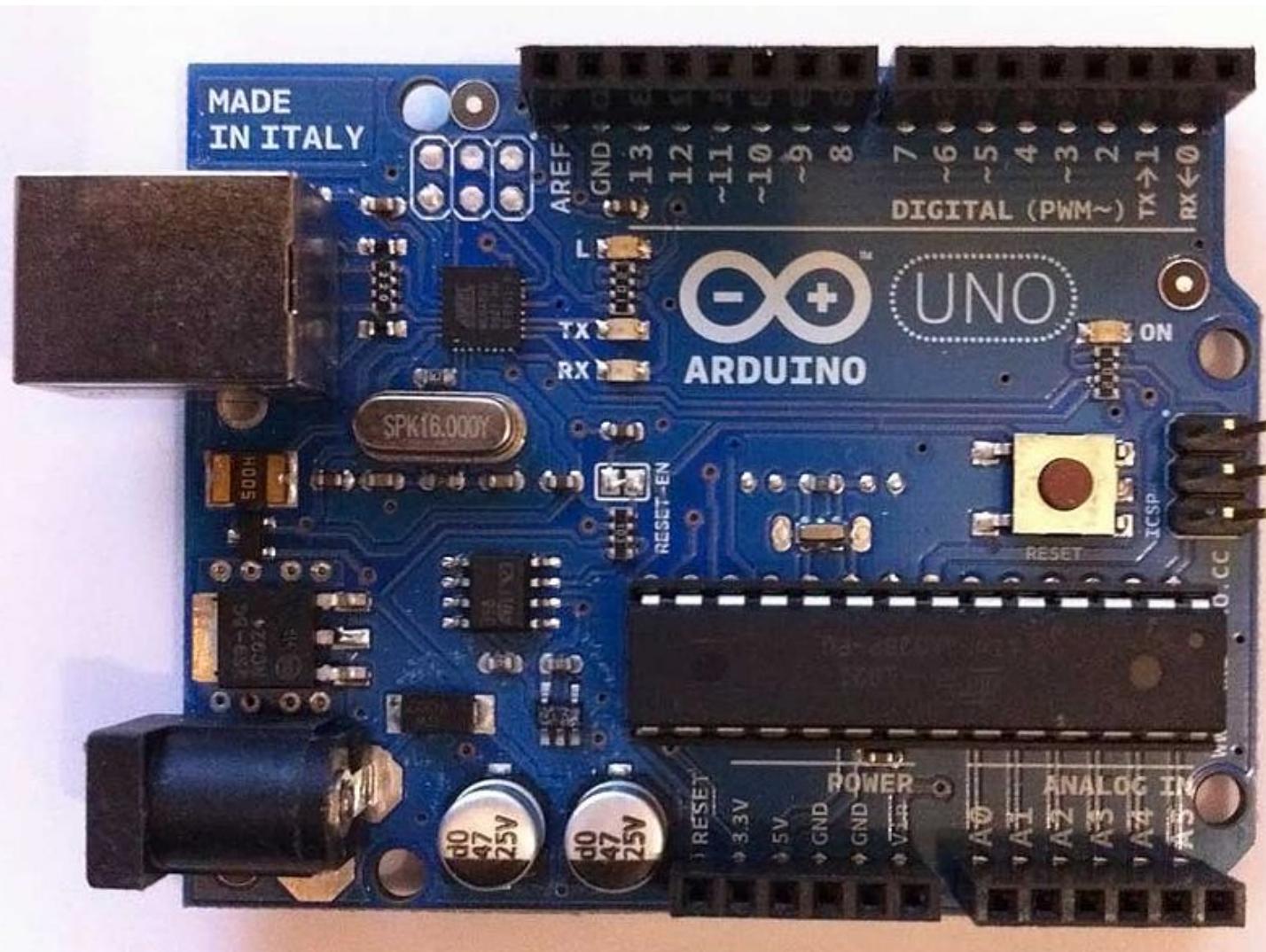
“In theory there is no difference between theory and practice. In practice there is.” - Yogi Berra



Pebble Smartwatch

The Hardware Renaissance

- Rapid Prototyping
- Mass Customisation
- Cheap Deployment



Arduino - 0011 Alpha

```

File Edit Sketch Tools Help
Blink
/*
 * Blink
 *
 * The basic Arduino example. Turns on an LED on for one second,
 * then off for one second, and so on... We use pin 13 because,
 * depending on your Arduino board, it has either a built-in LED
 * or a built-in resistor so that you need only an LED.
 *
 * http://www.arduino.cc/en/Tutorial/Blink
 */

int ledPin = 13; // LED connected to digital pin 13

void setup() // run once, when the sketch starts
{
  pinMode(ledPin, OUTPUT); // sets the digital pin as output
}

void loop() // run over and over again
{
  digitalWrite(ledPin, HIGH); // sets the LED on
  delay(1000); // waits for a second
  digitalWrite(ledPin, LOW); // sets the LED off
  delay(1000); // waits for a second
}

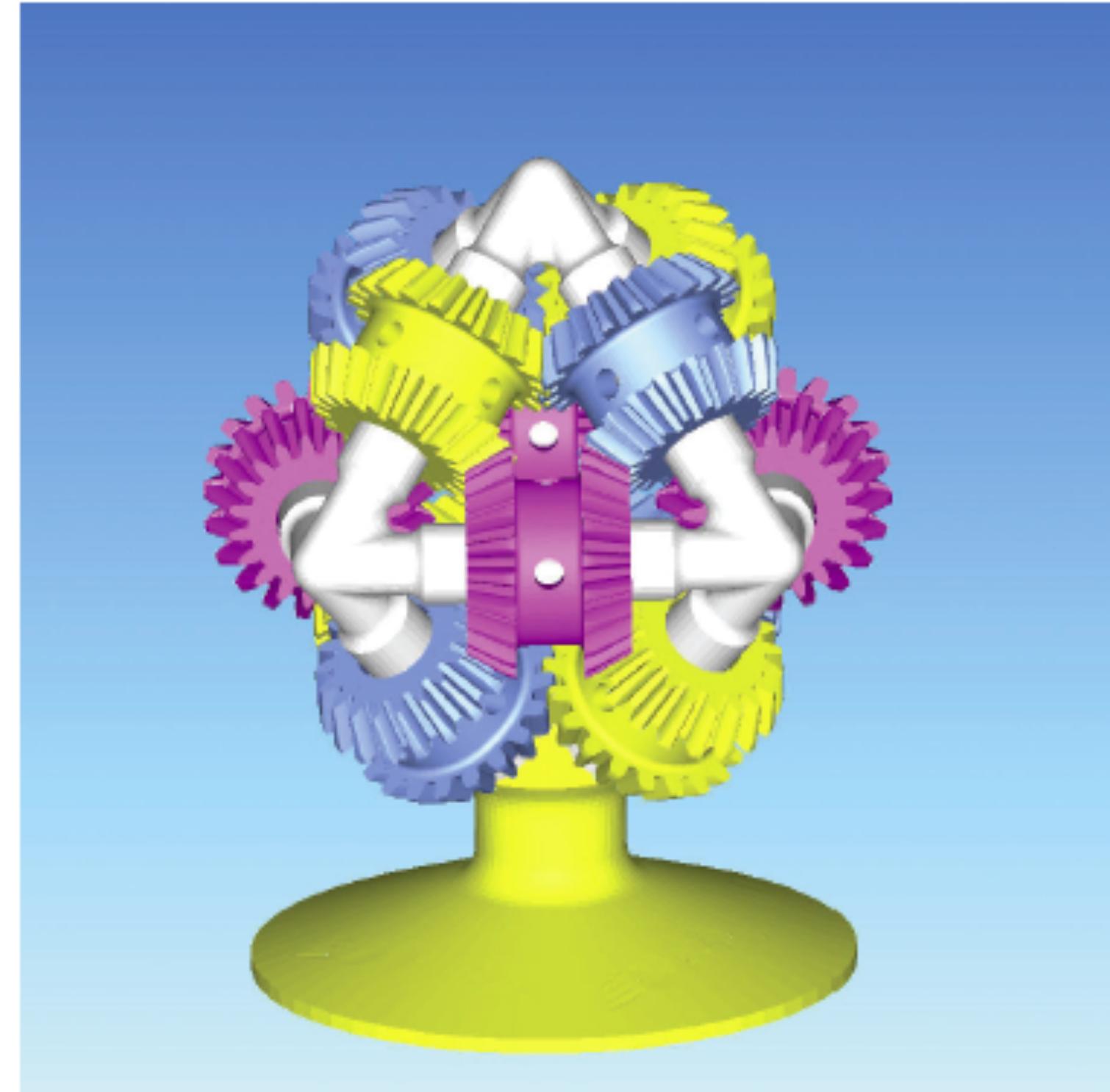
Done compiling.

Binary sketch size: 1098 bytes (of a 14336 byte maximum)
22

```

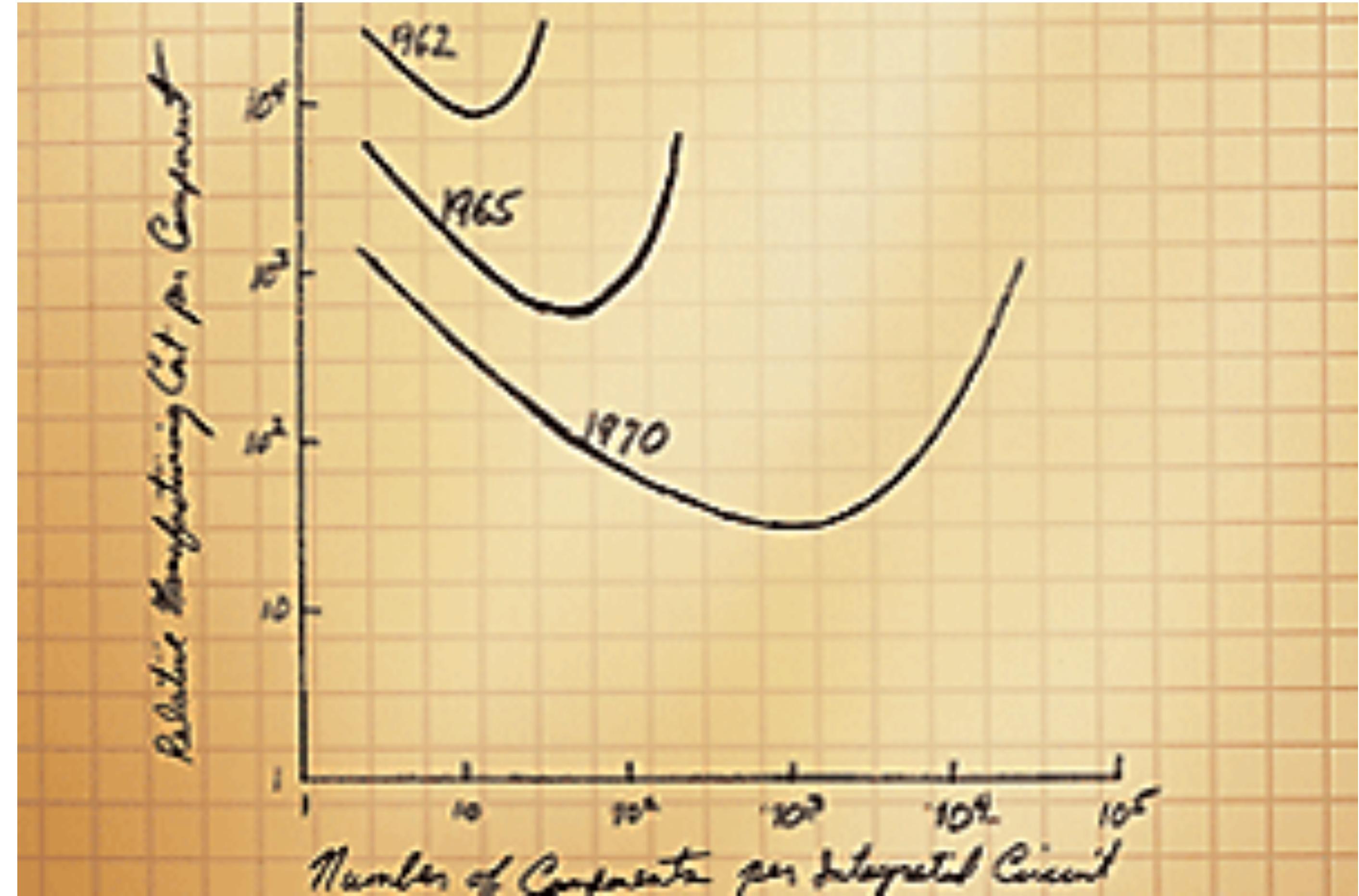
The Hardware Renaissance

- Rapid Prototyping
- Mass Customisation
- Cheap Deployment
- 3D Fabrication



The Hardware Renaissance

In 1965, Gordon Moore noticed that the number of transistors per square inch on integrated circuits had doubled every year since their invention.



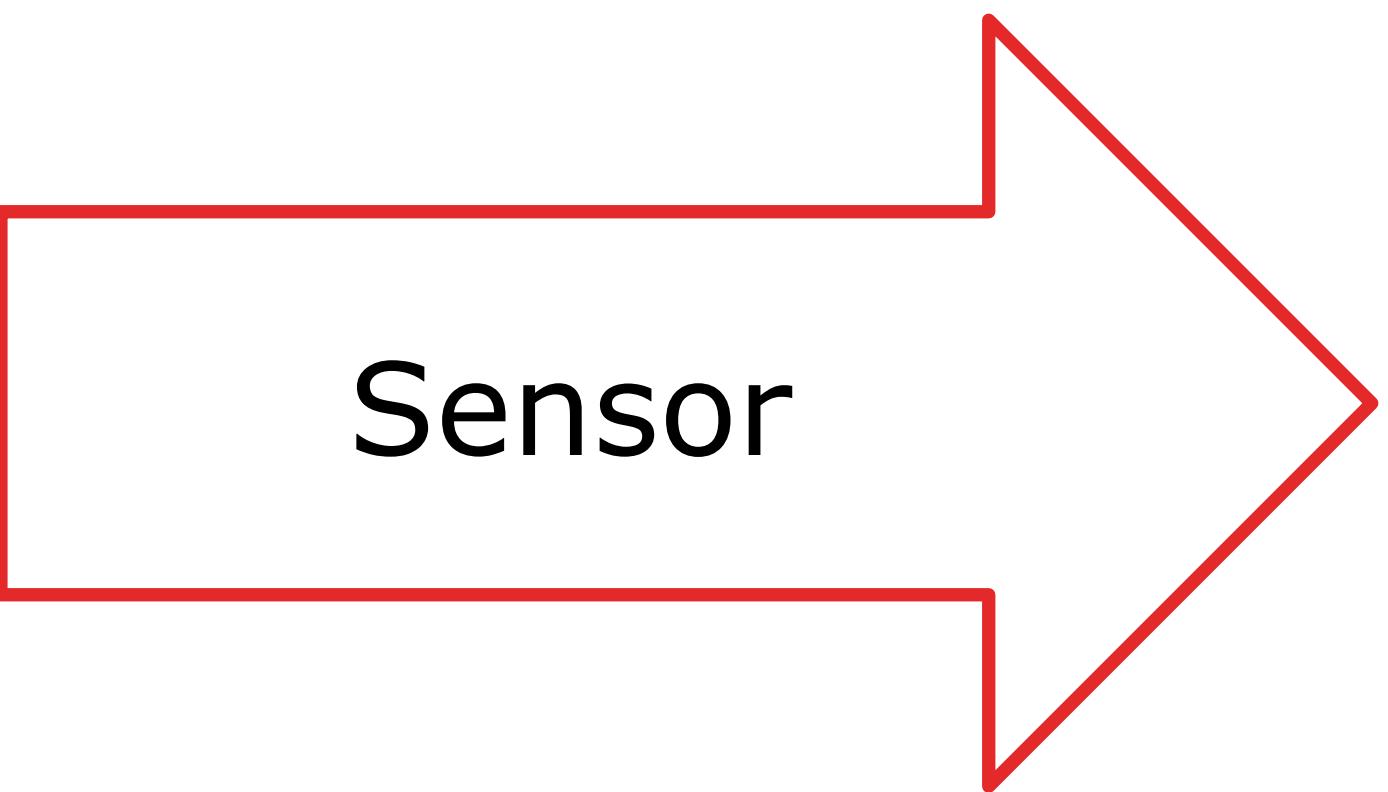
Moore's Law



Sensors

**Physical magnitude
or phenomenon**

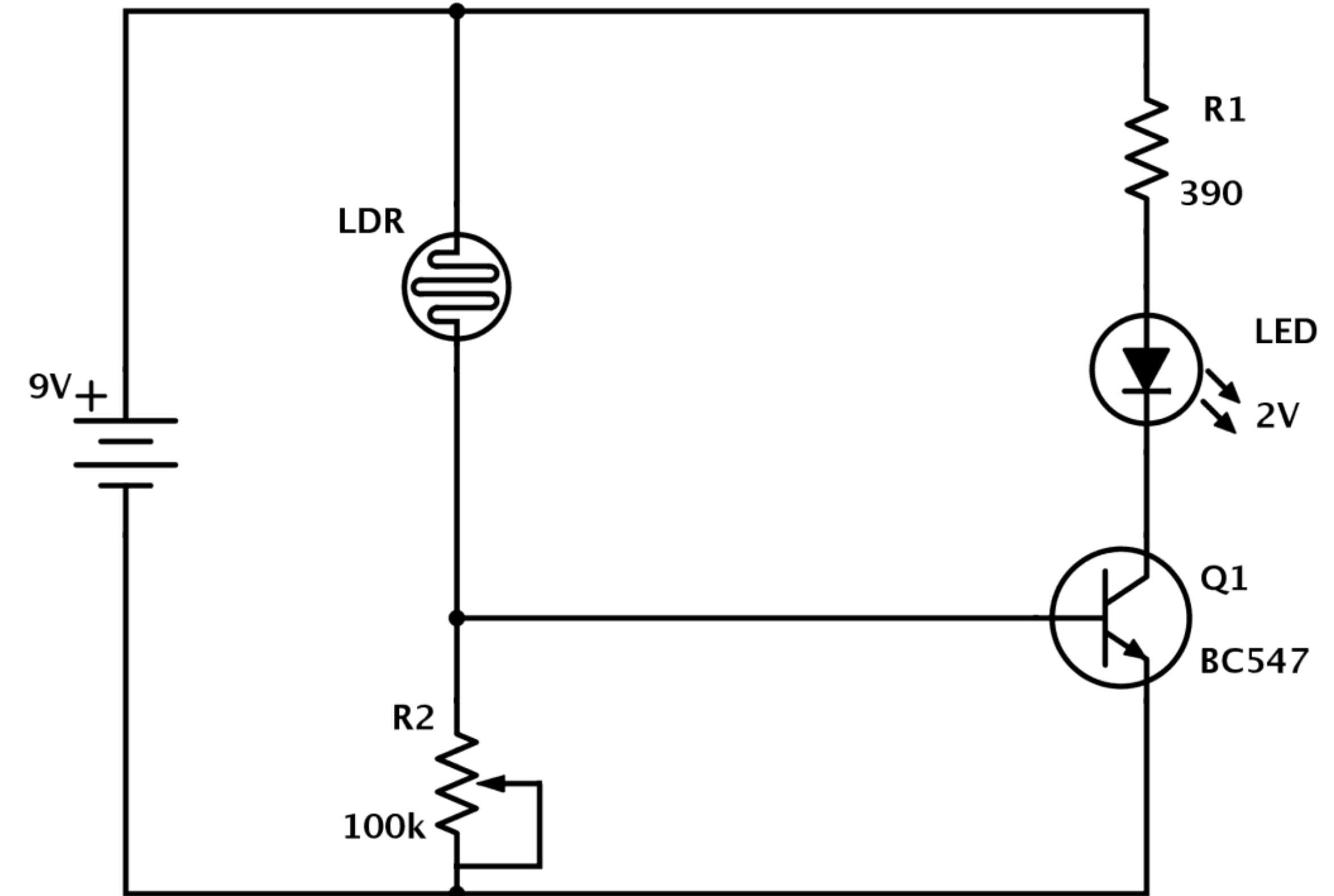
temperature
location
motion
...



Data

What is a sensor?

- A **sensor** is a **device**, module, or subsystem
- **Detects events or changes in its environment**
- By translating a physical magnitude into electrical properties
- **Sends the information** to other electronics



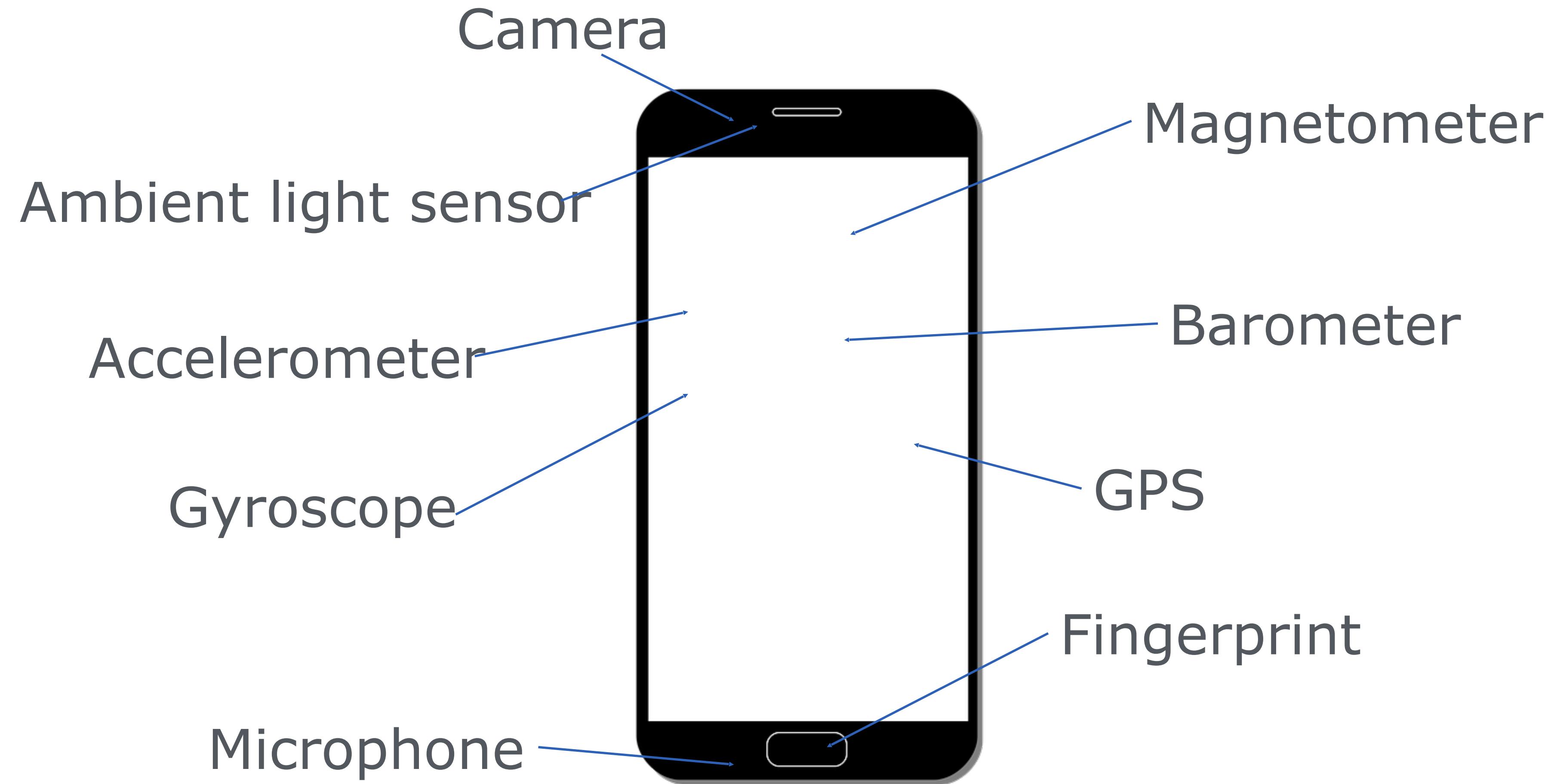
Sensor



Back then...

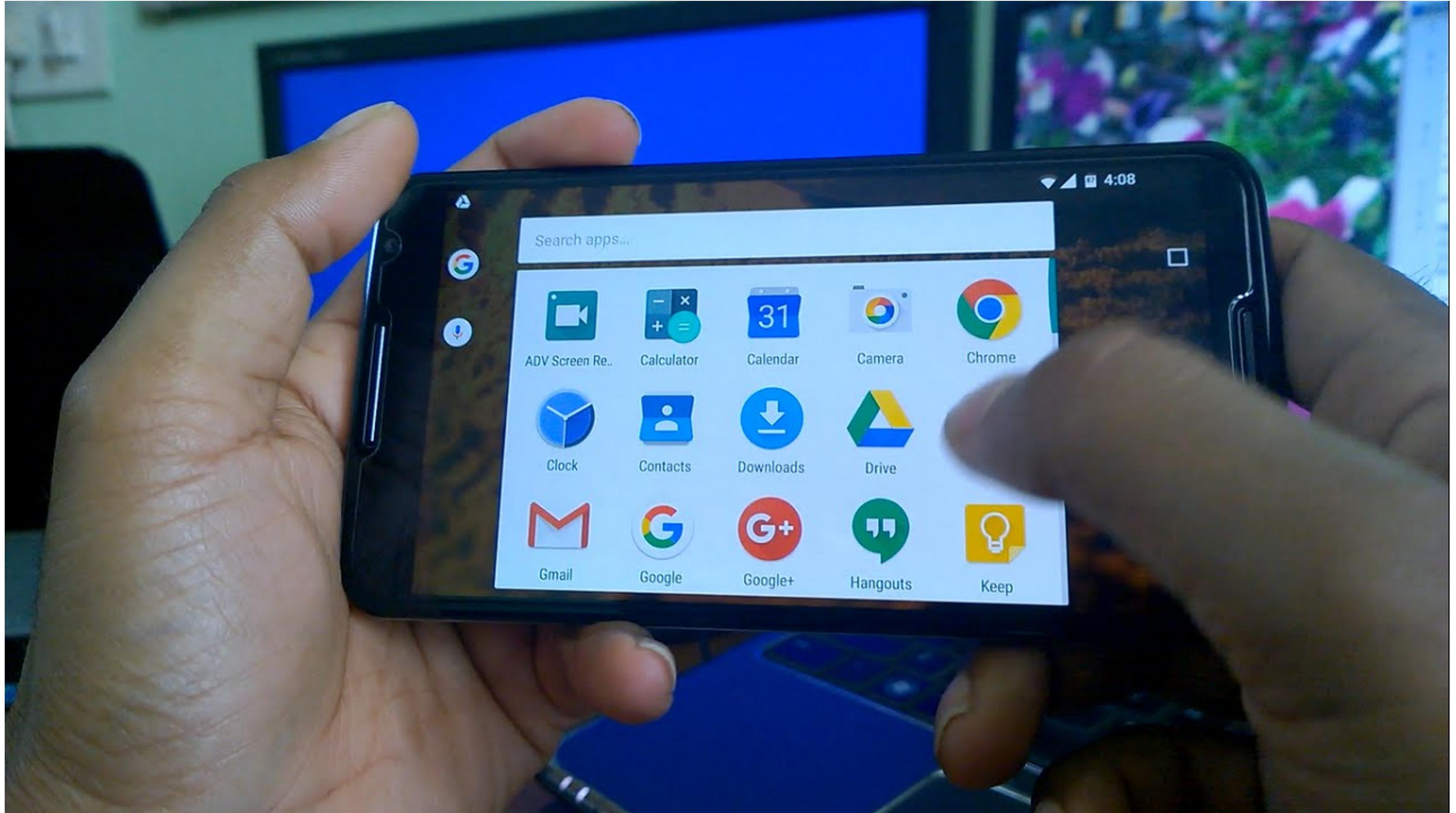


... now.



Sensors

Sensor?



Screen Rotation

Sensor?



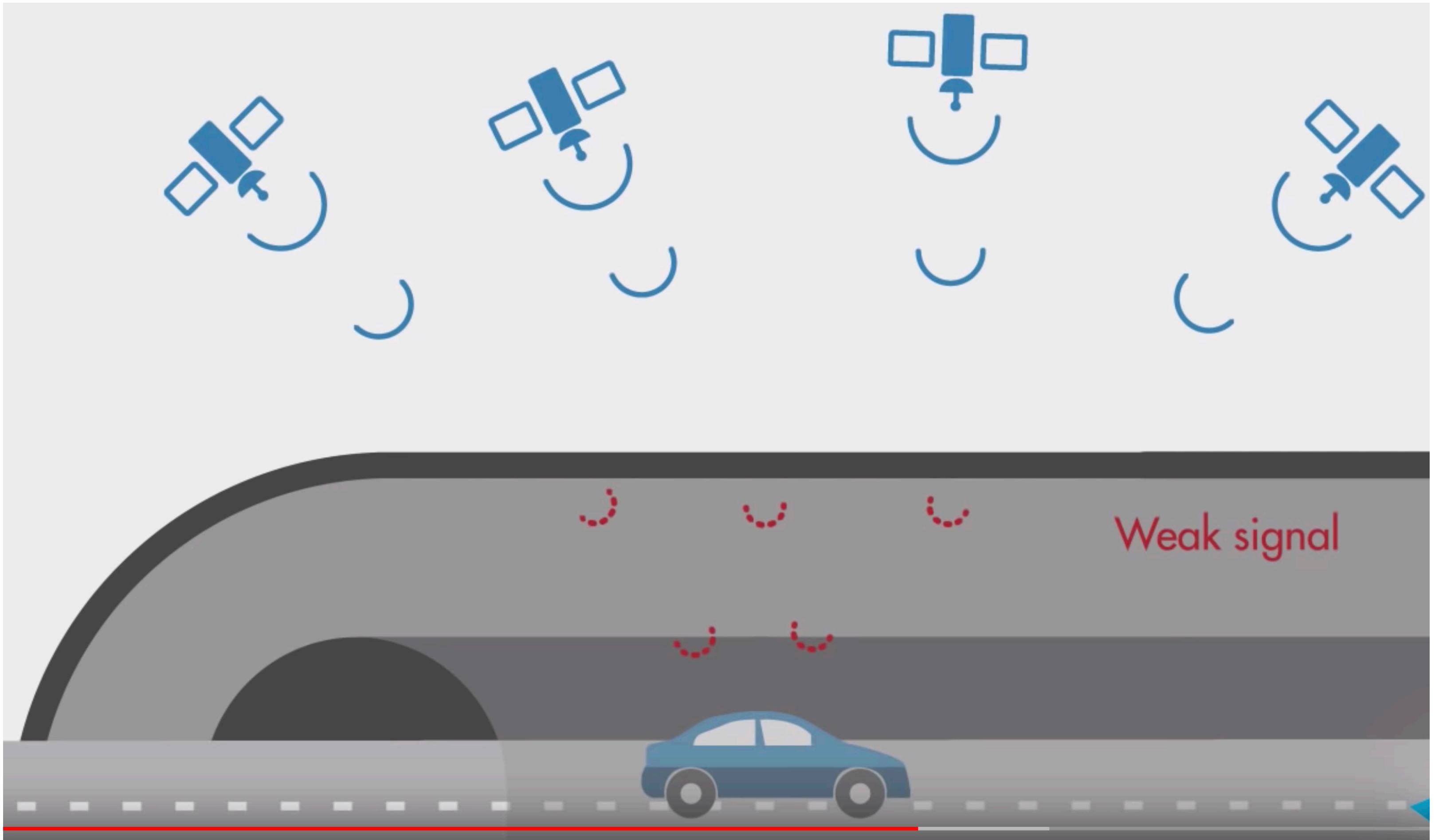
Avoiding Accidental Touches

Sensor?



Pokémon GO?

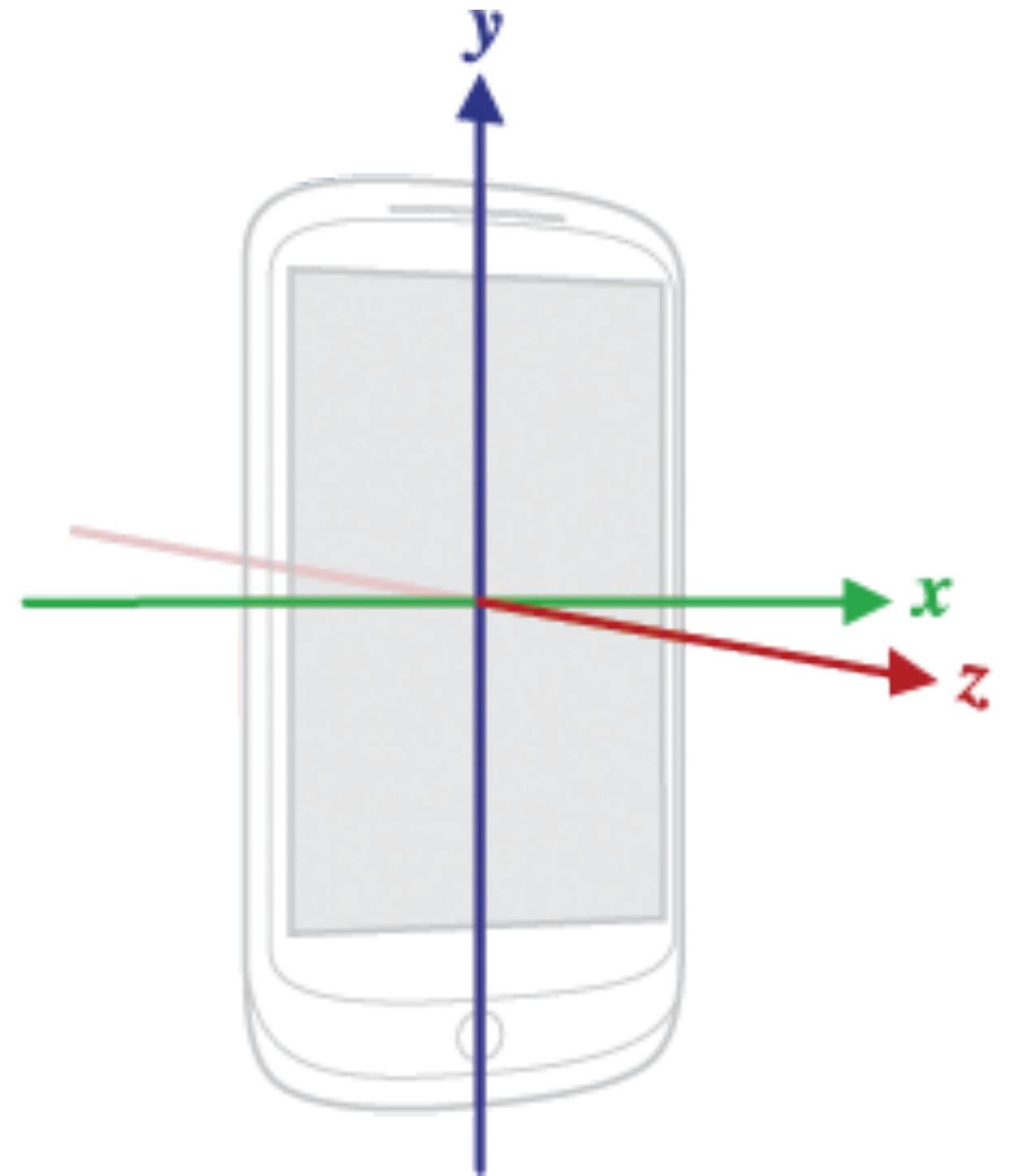
Sensor?



Driving through a Tunnel

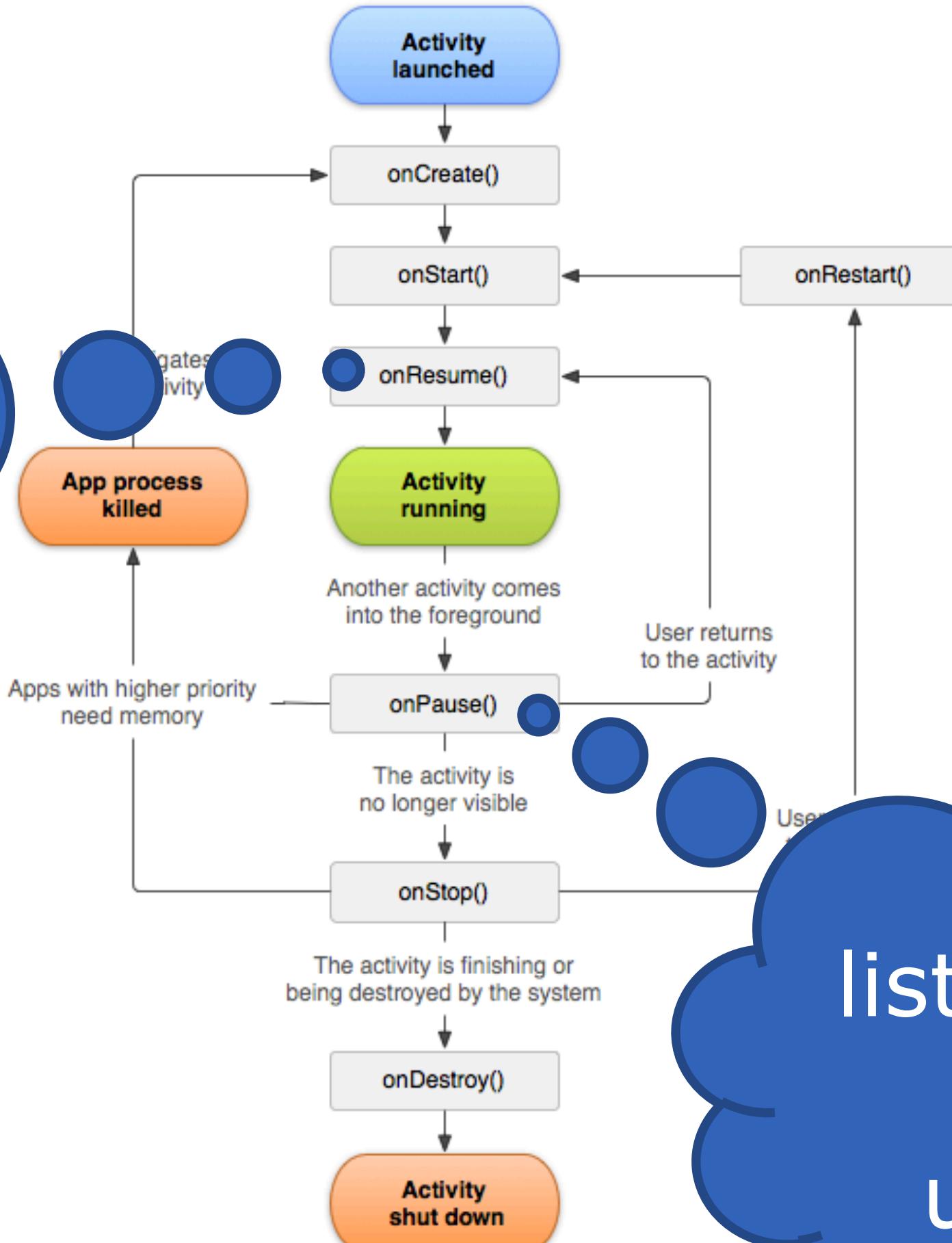


- Raw sensor data
- Higher abstraction (e.g. step counter)
- Events and Callbacks
- Device independent (as long as present!)



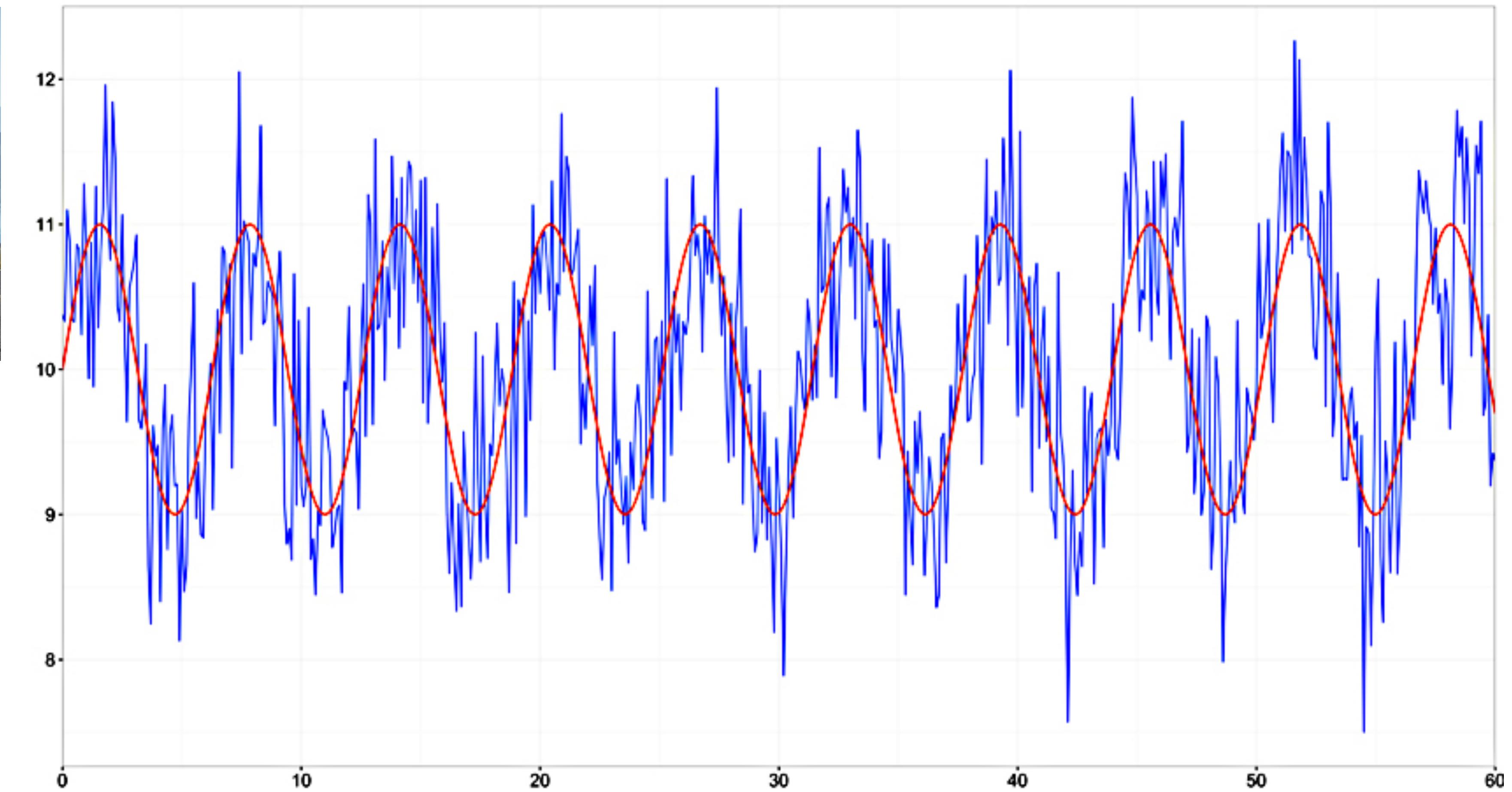
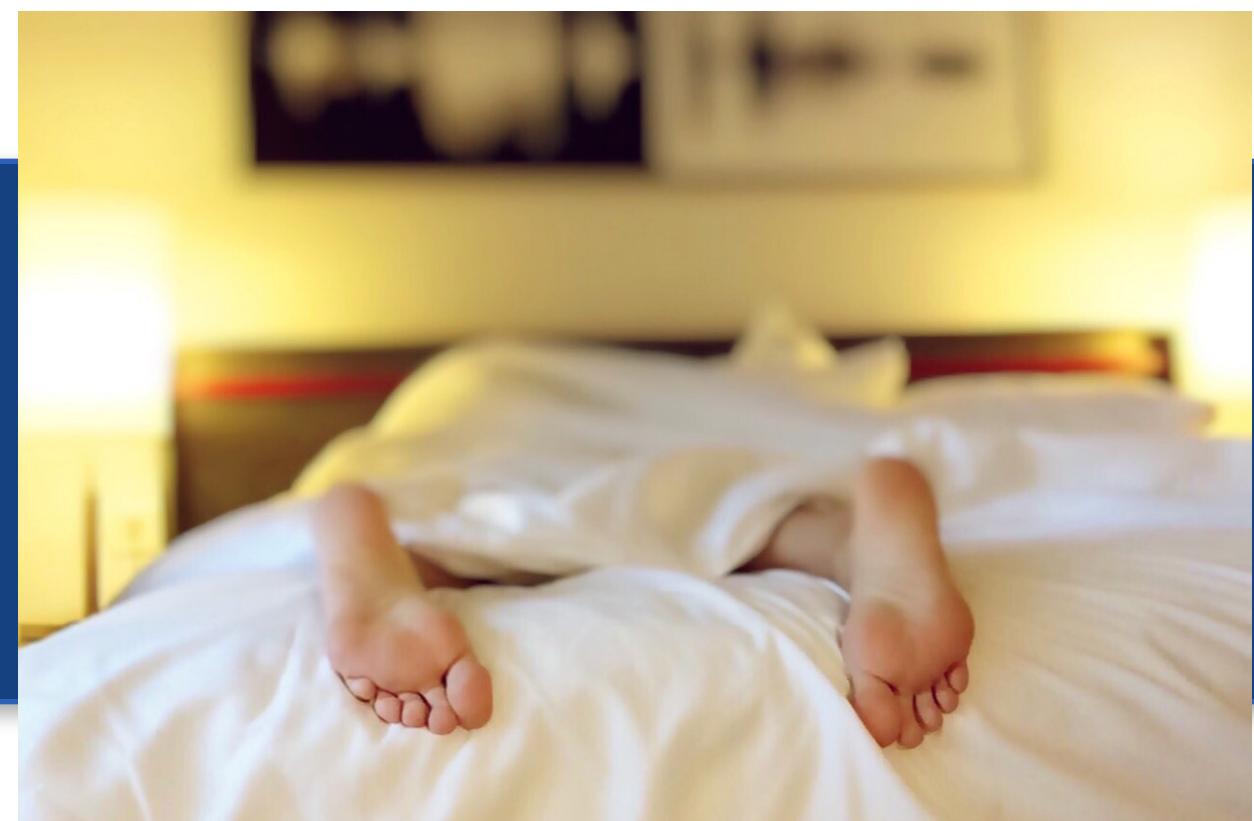
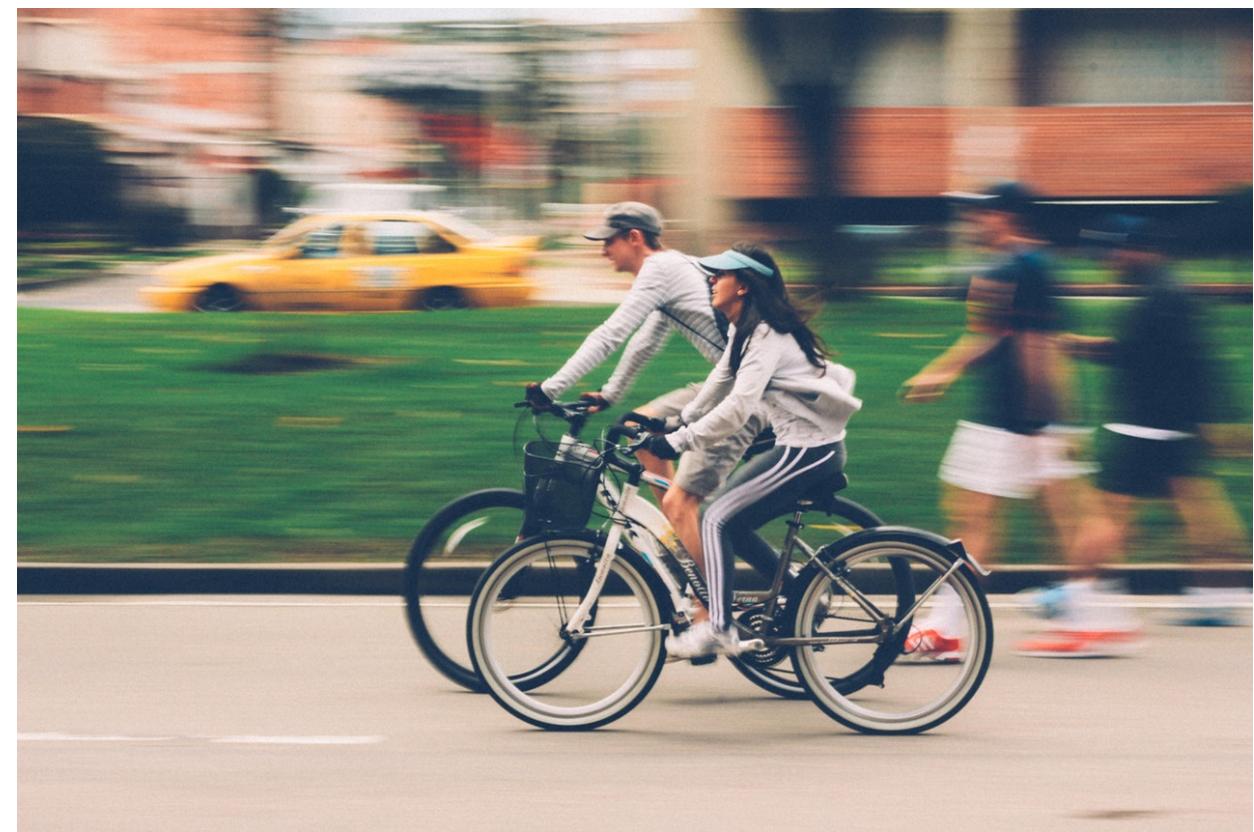
Sensors in Android / iOS

Start
listening for
sensor
updates

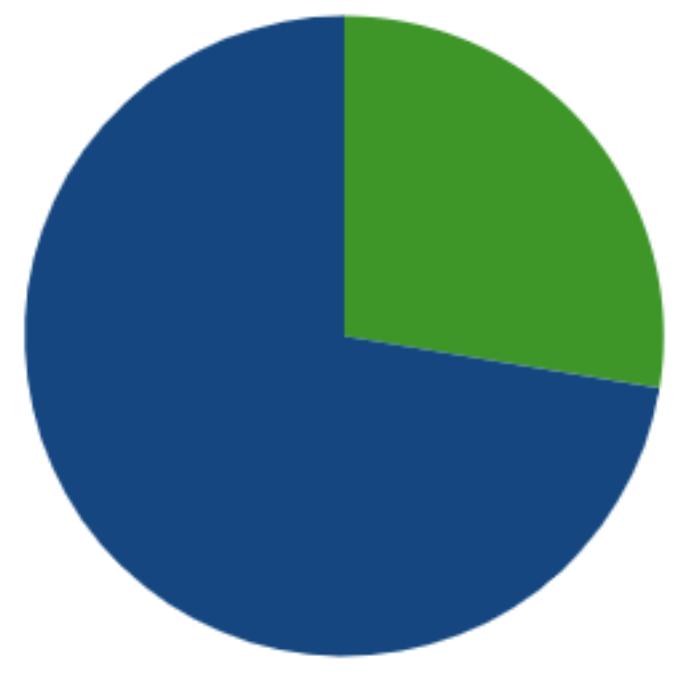


Stop
listening for
sensor
updates

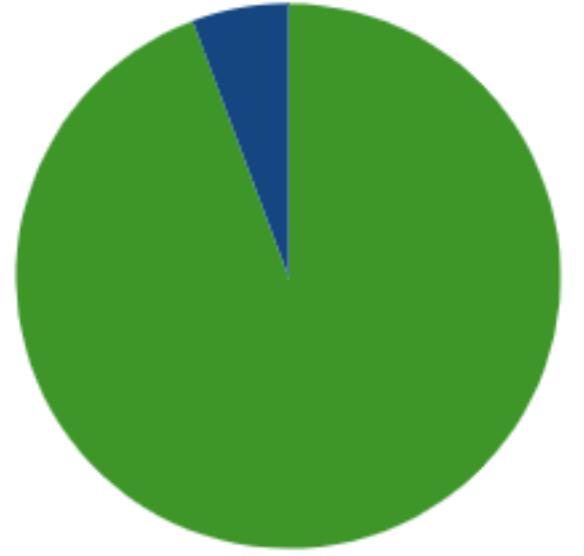
Respect the Activity Lifecycle



Signal Processing

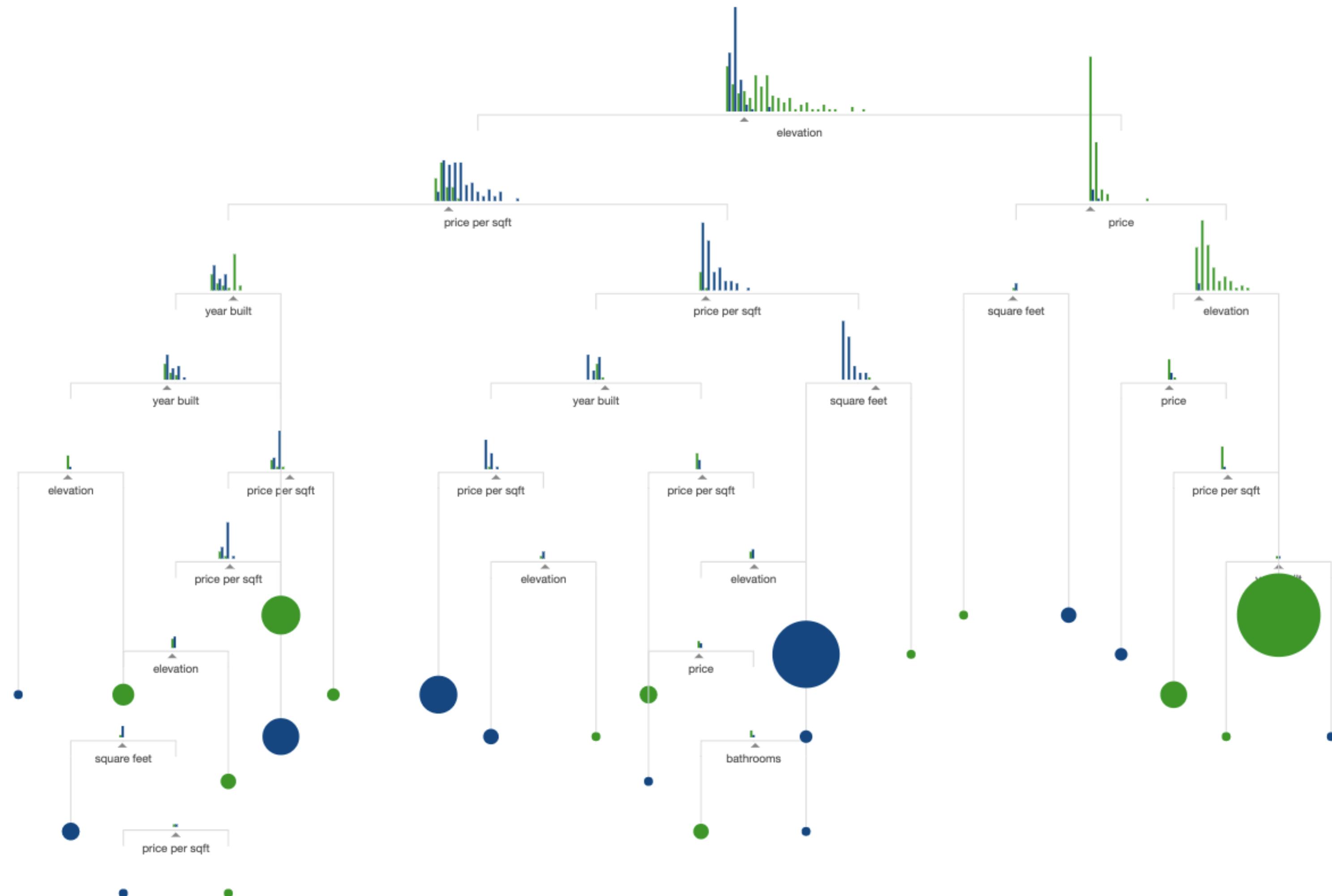


105
NY
40
SF

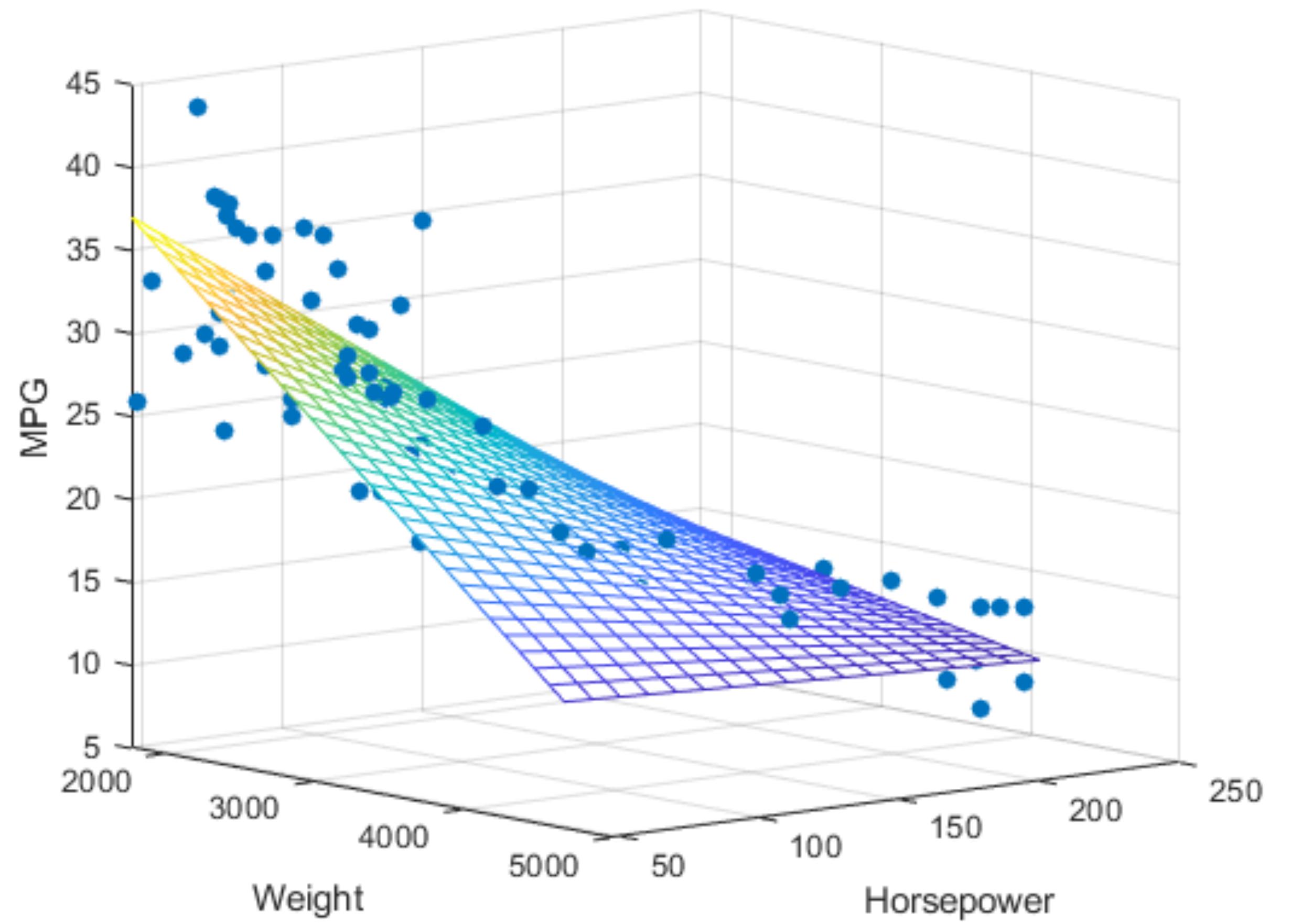


6
NY
99
SF

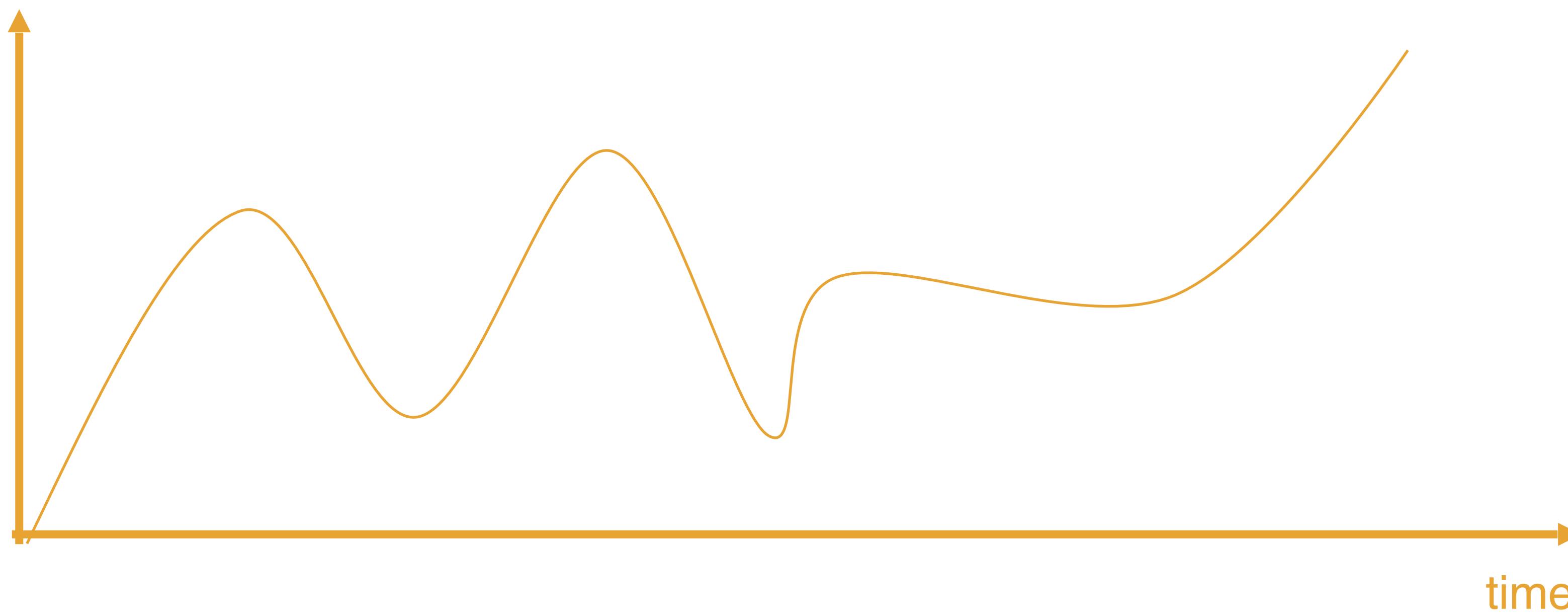
82
% correct



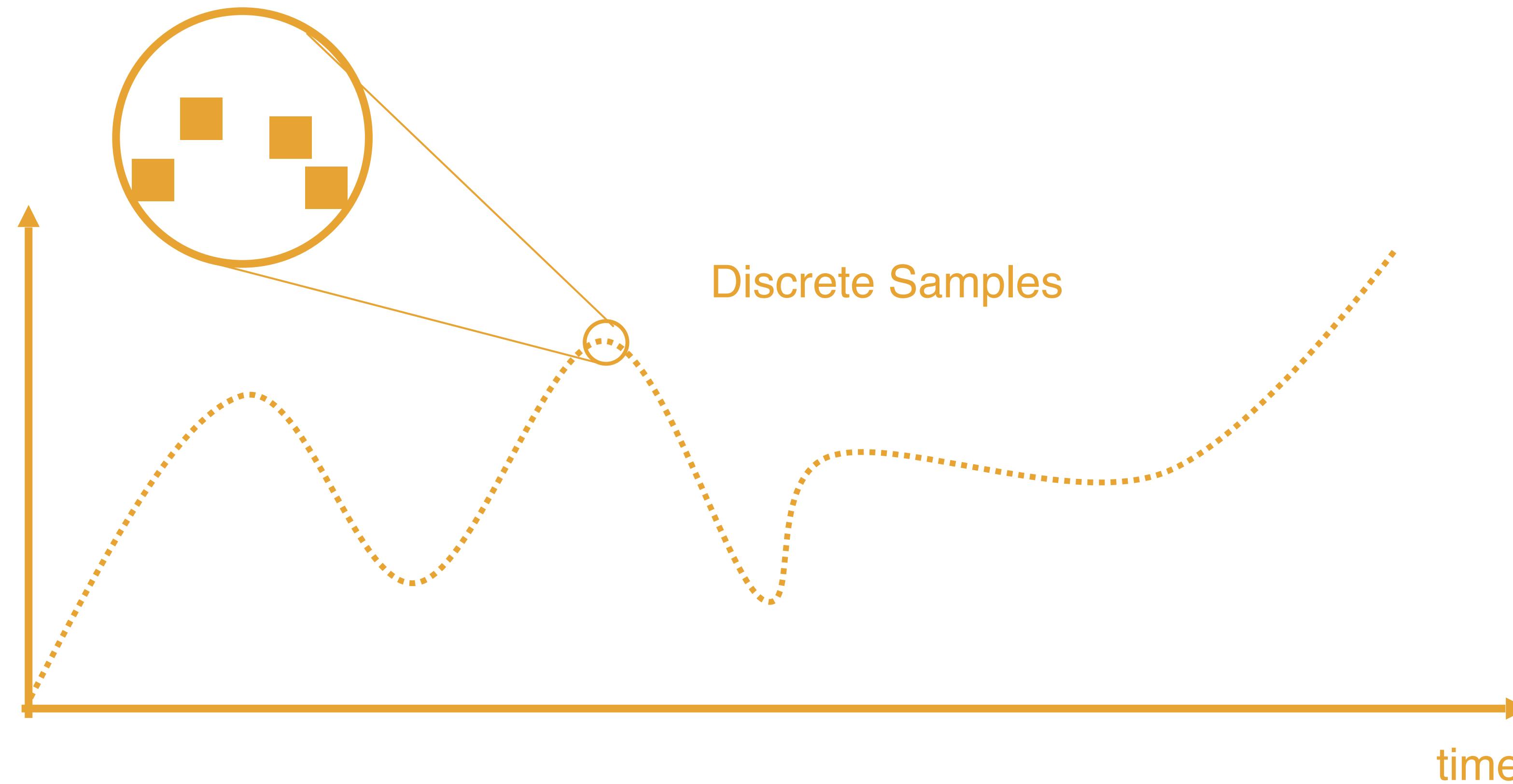
Machine Learning



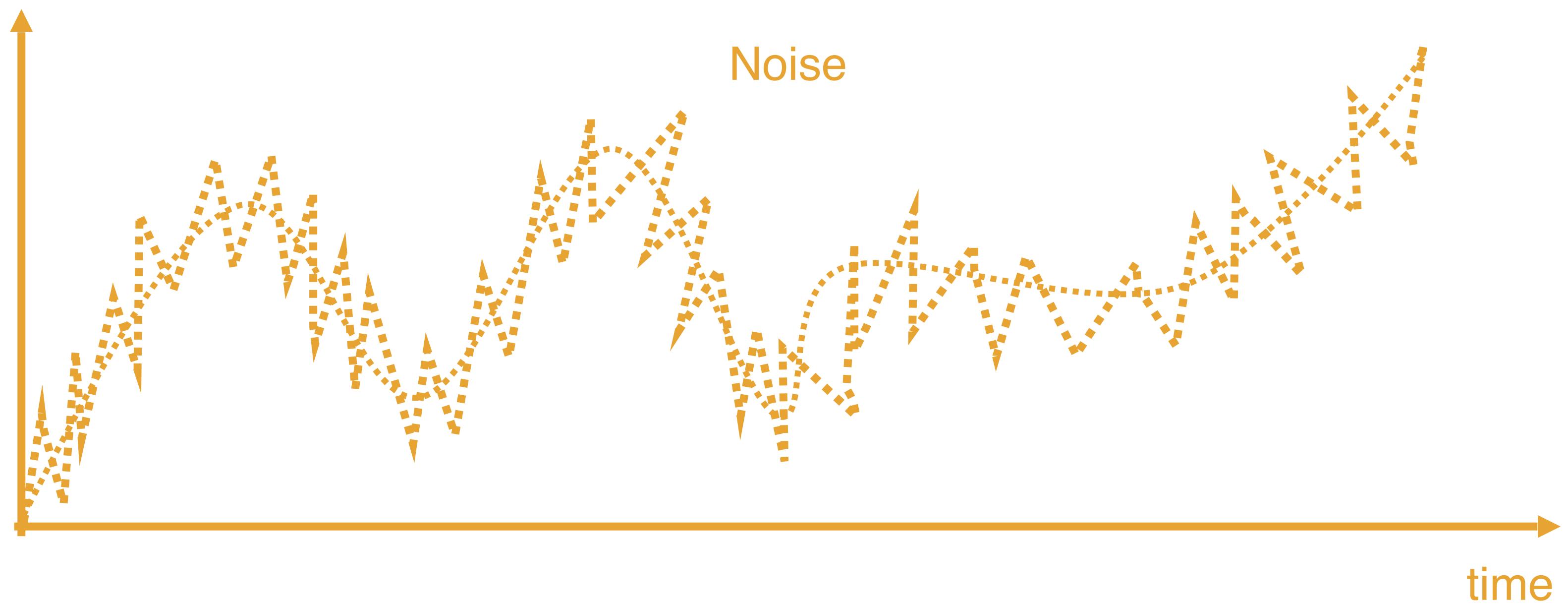
Linear Regressions



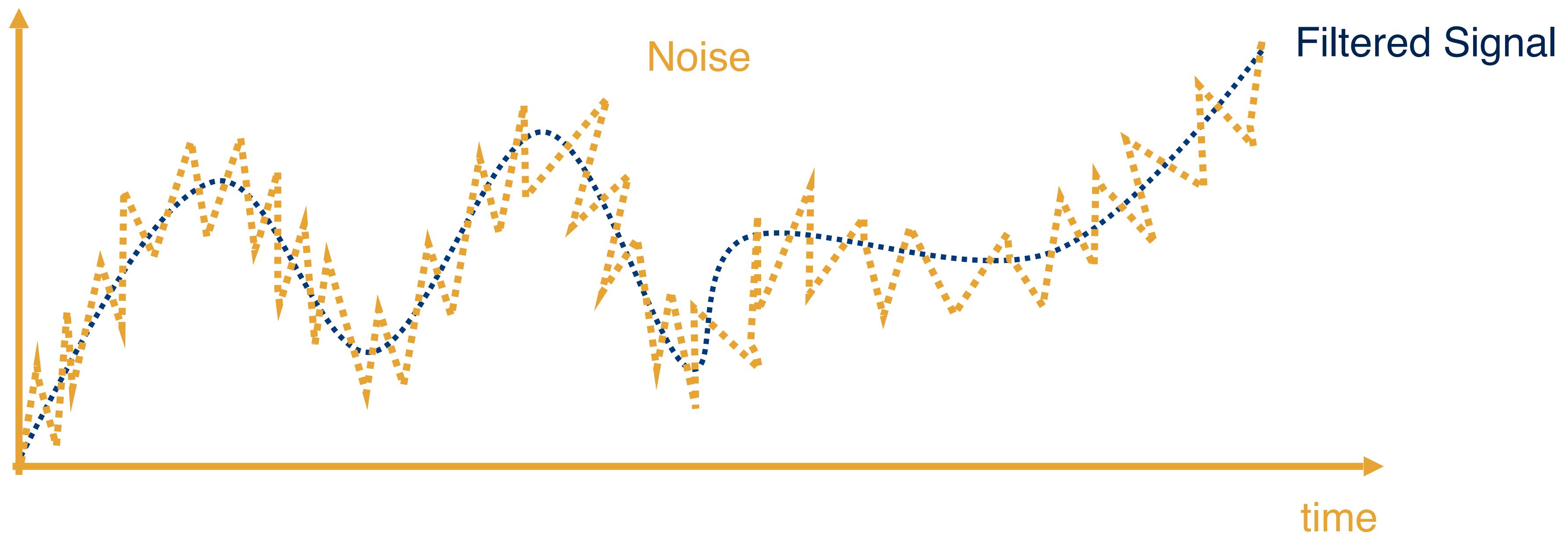
Sensor Data



Sensor Data



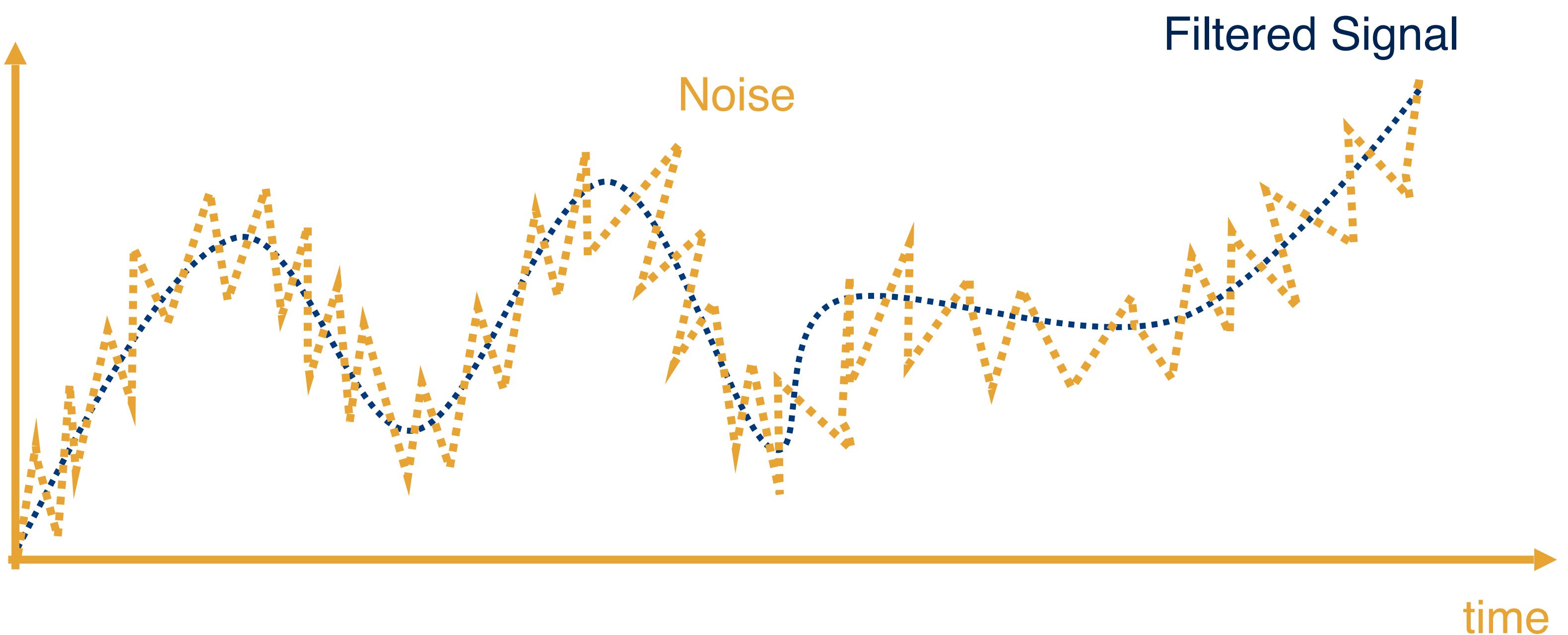
Sensor Data

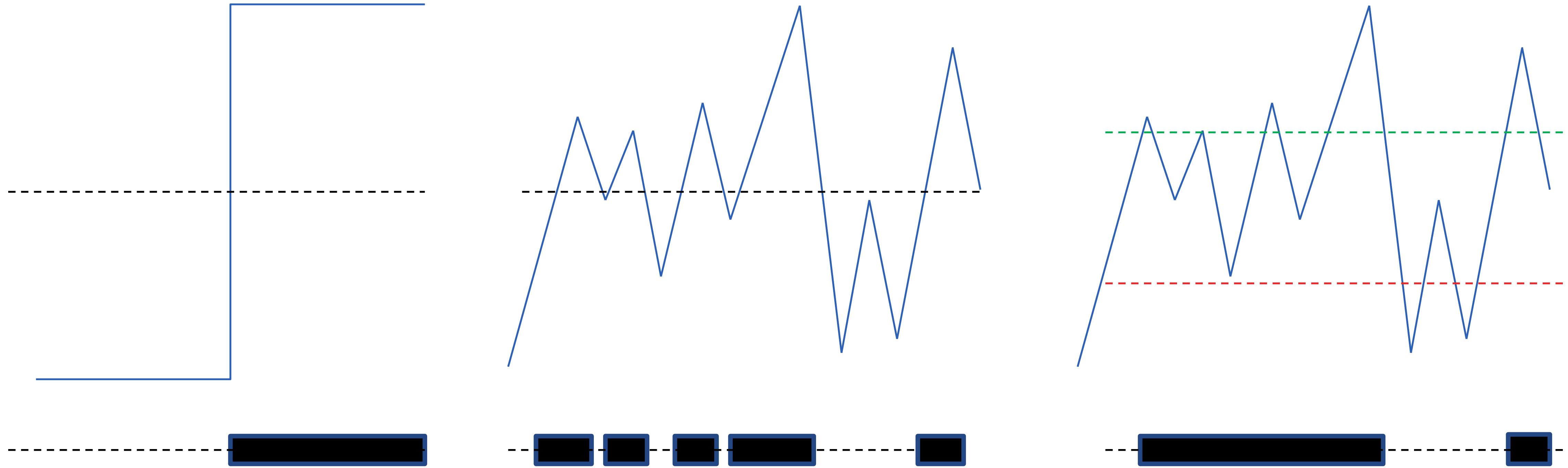


Signal to Noise Ratio: SNR

Sensor Data Processing

- 1.Thresholds
- 2.Mean Filters
- 3.Median Filters
- 4.Kalman Filters
- 5.Particle Filters





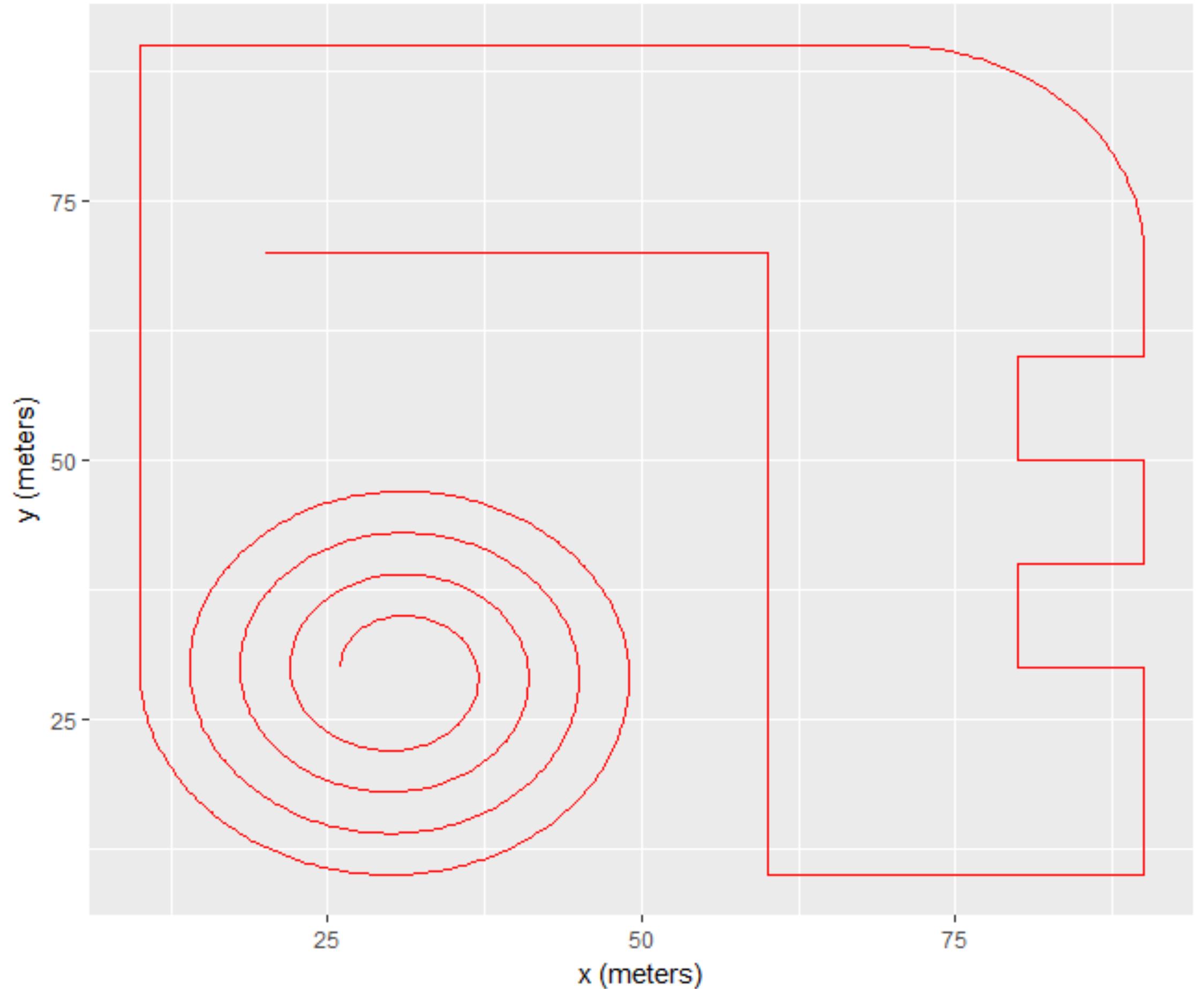
Thresholds

$$z_i = x_i$$

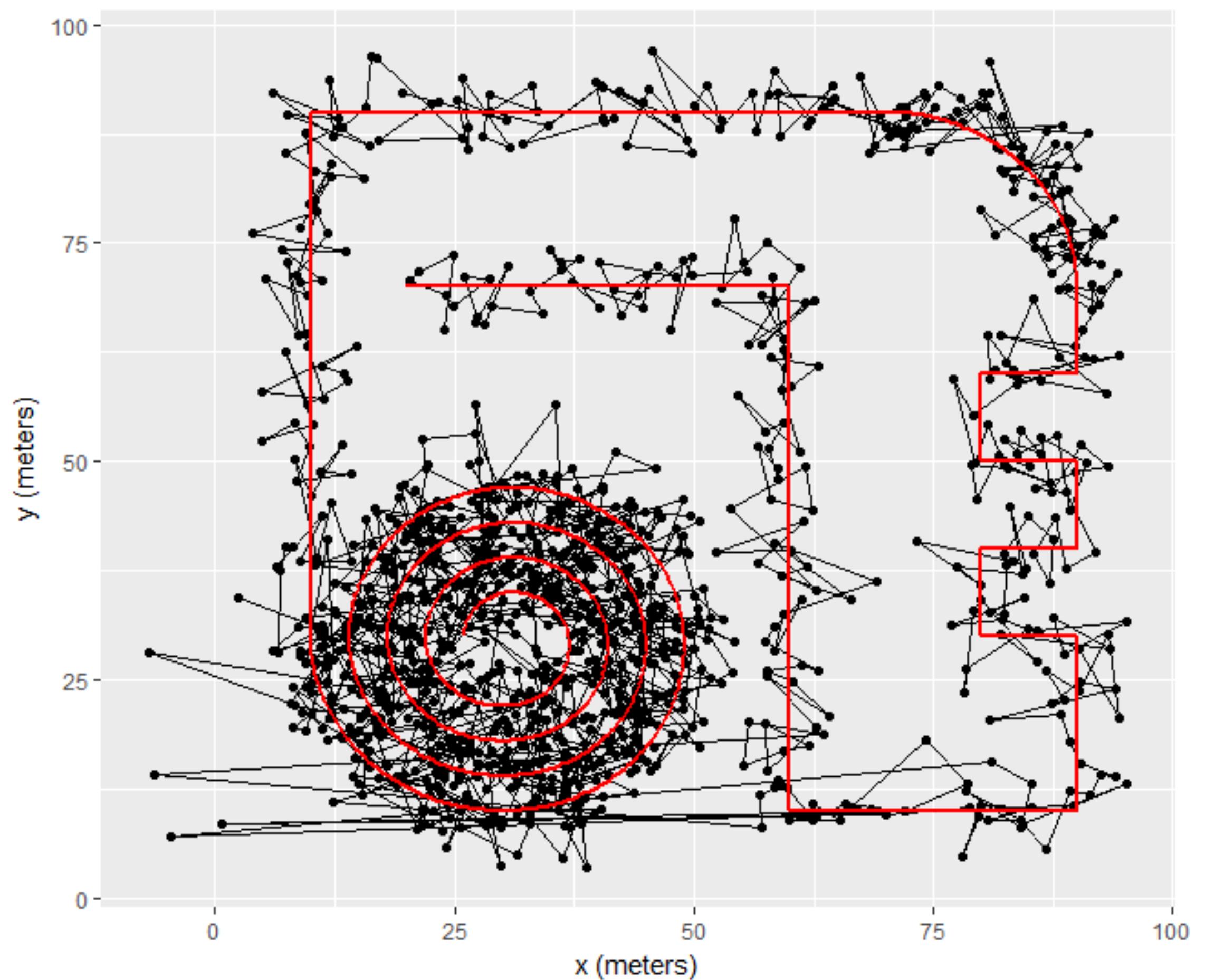
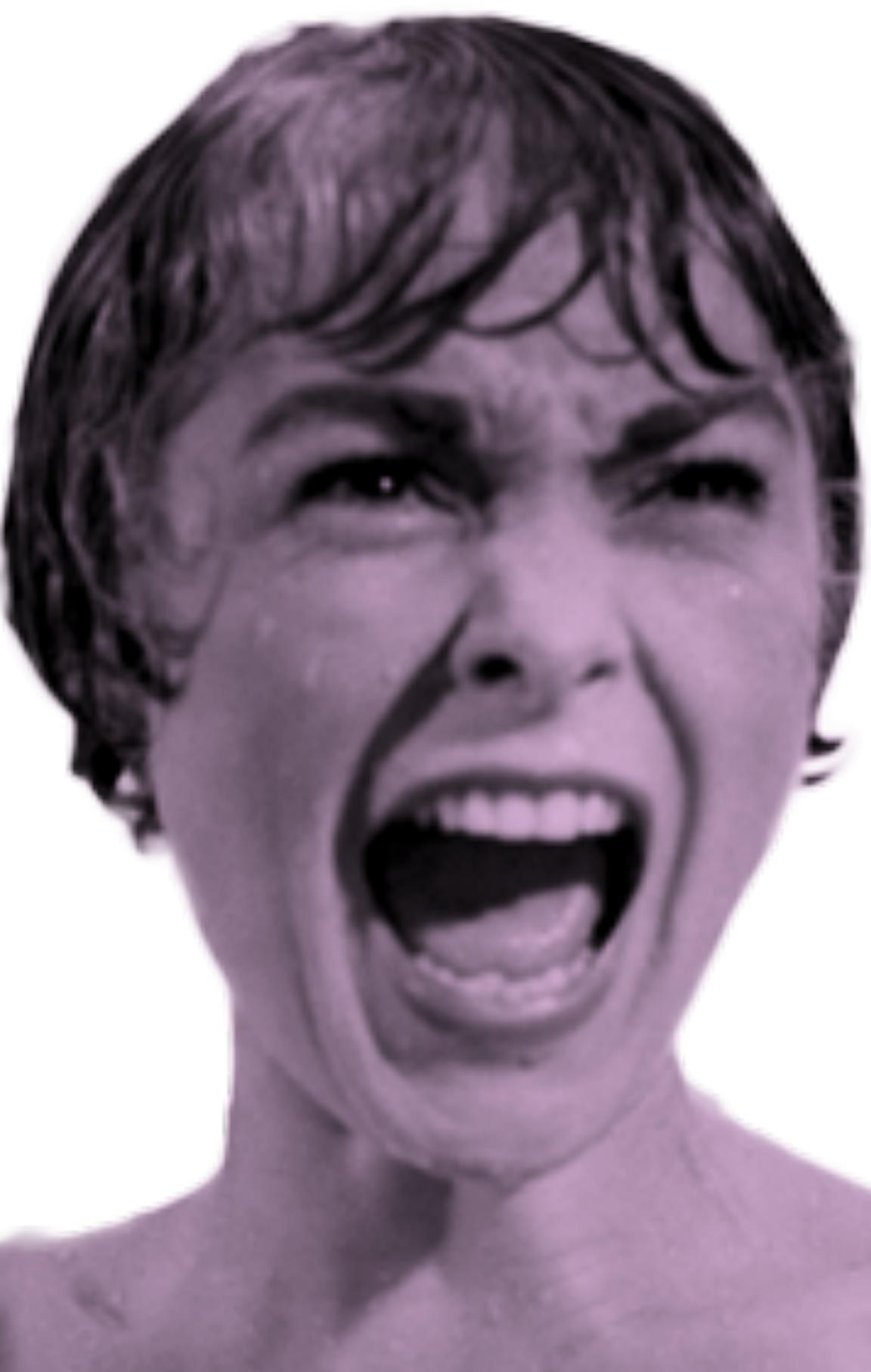
Measurement from sensor

Actual Value or Ground Truth

Measurement vs. State



Measurement vs. State



Measurement vs. State

$$z_i = x_i + v_i$$

Measurement from sensor

Actual Value or Ground Truth

Sensor noise



Measurement vs. State

Measurement vs. State

Measurement

$$z_i = \begin{pmatrix} z_i^{(x)} \\ z_i^{(y)} \end{pmatrix}$$

State

$$x_i = \begin{pmatrix} x_i \\ y_i \end{pmatrix}$$

Noise

$$v_i = \begin{pmatrix} v_i^{(x)} \\ v_i^{(y)} \end{pmatrix}$$

$$\sim \begin{pmatrix} N(0, \sigma) \\ N(0, \sigma) \end{pmatrix}$$

Measurement from
sensor

$$z_i = x_i + v_i$$

Actual Value
or Ground Truth
(State)

Sensor noise



Actual Value



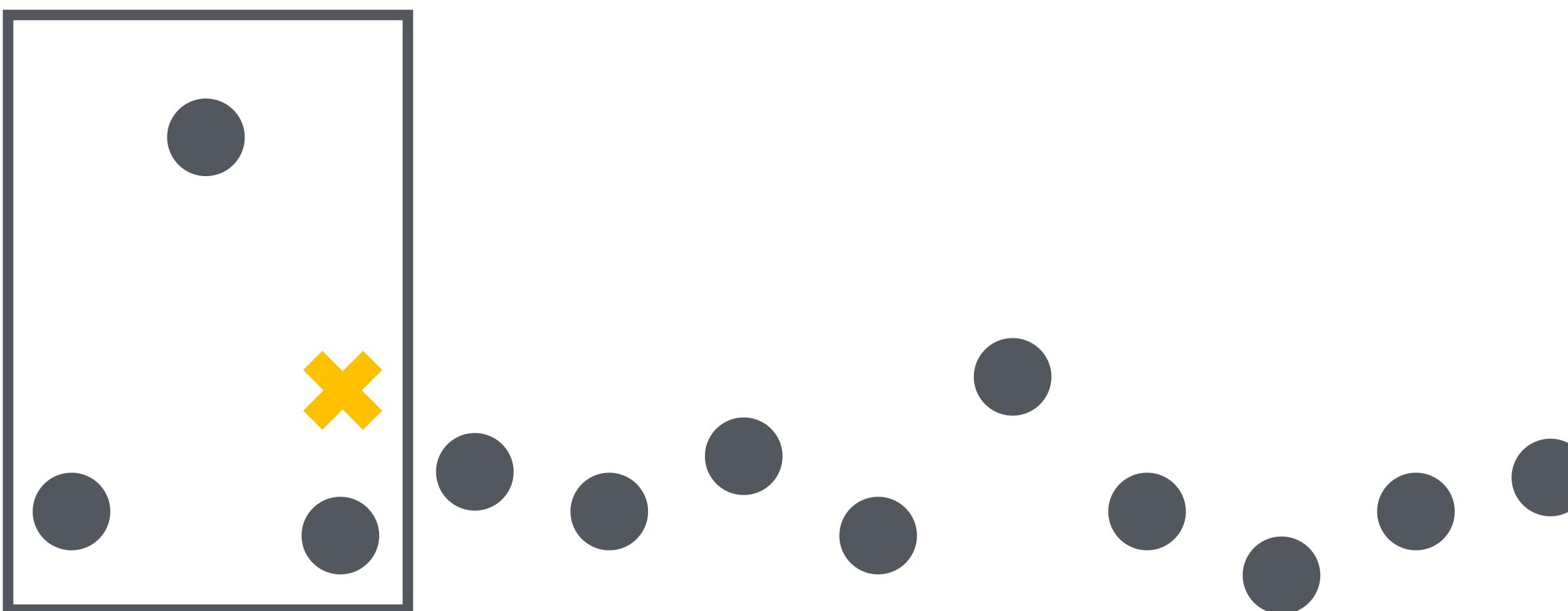
Measurements

$$\bar{x} = \frac{\sum_{i=1}^n x_i}{n}$$



Mean Filter

$$\bar{x} = \frac{\sum_{i=1}^n x_i}{n}$$



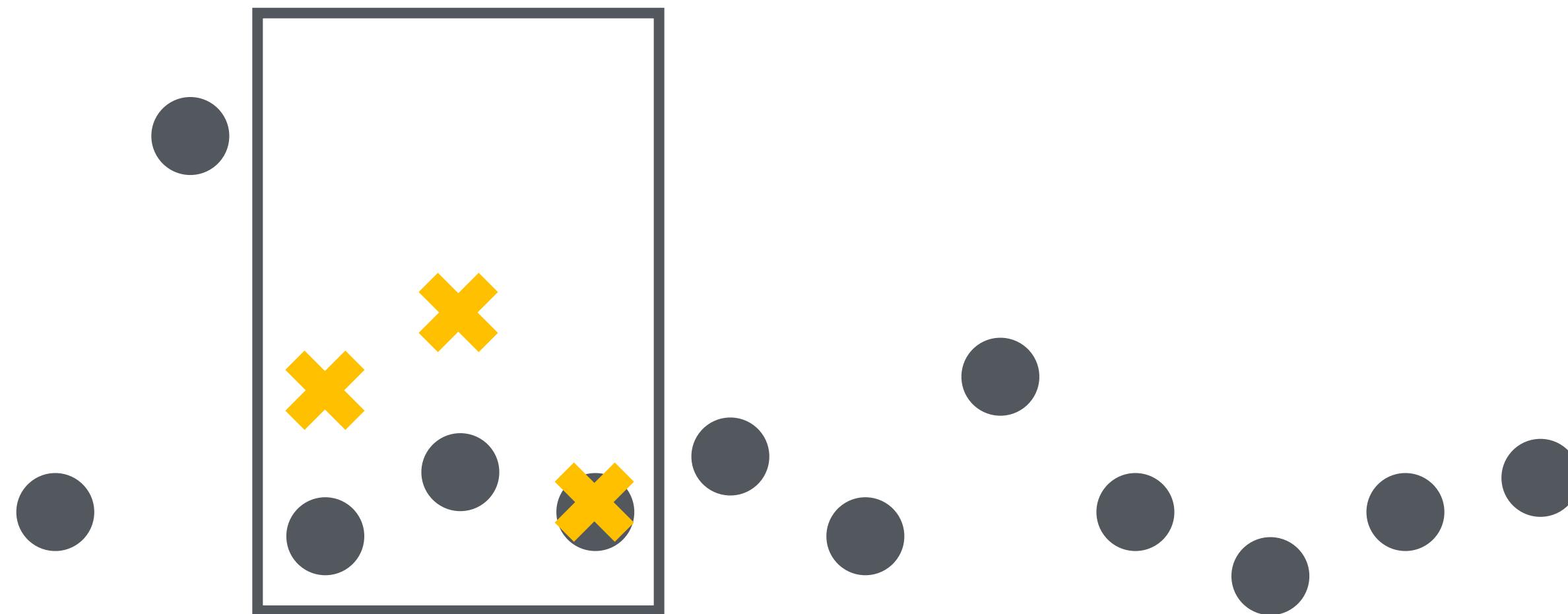
Mean Filter

$$\bar{x} = \frac{\sum_{i=1}^n x_i}{n}$$



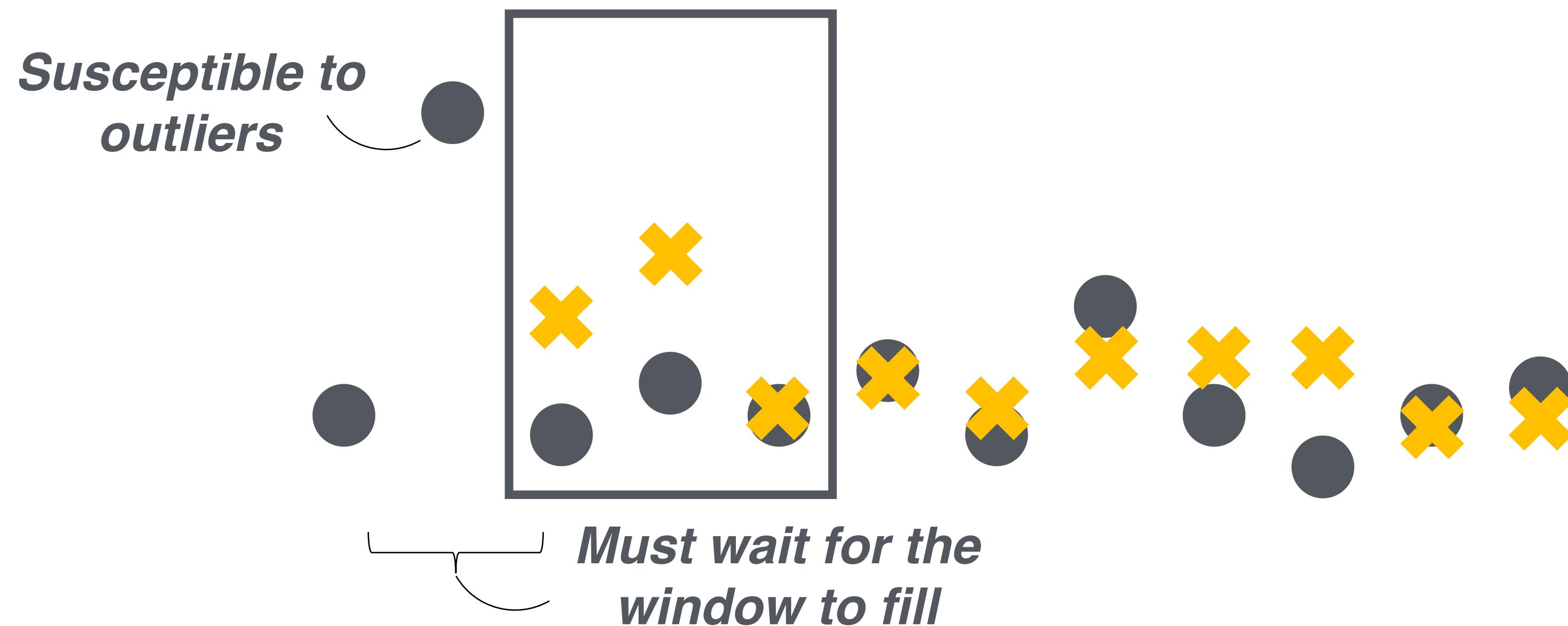
Mean Filter

$$\bar{x} = \frac{\sum_{i=1}^n x_i}{n}$$



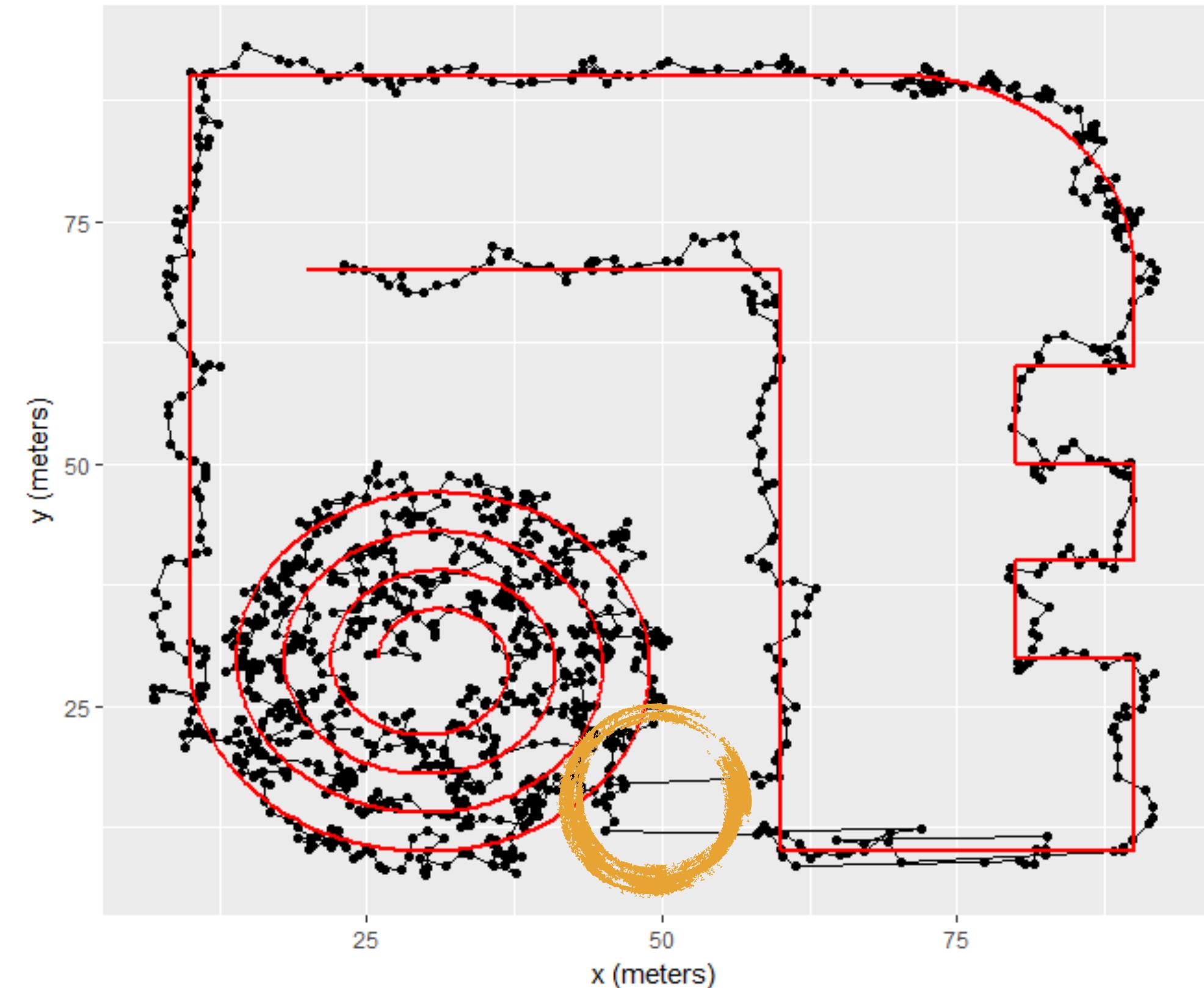
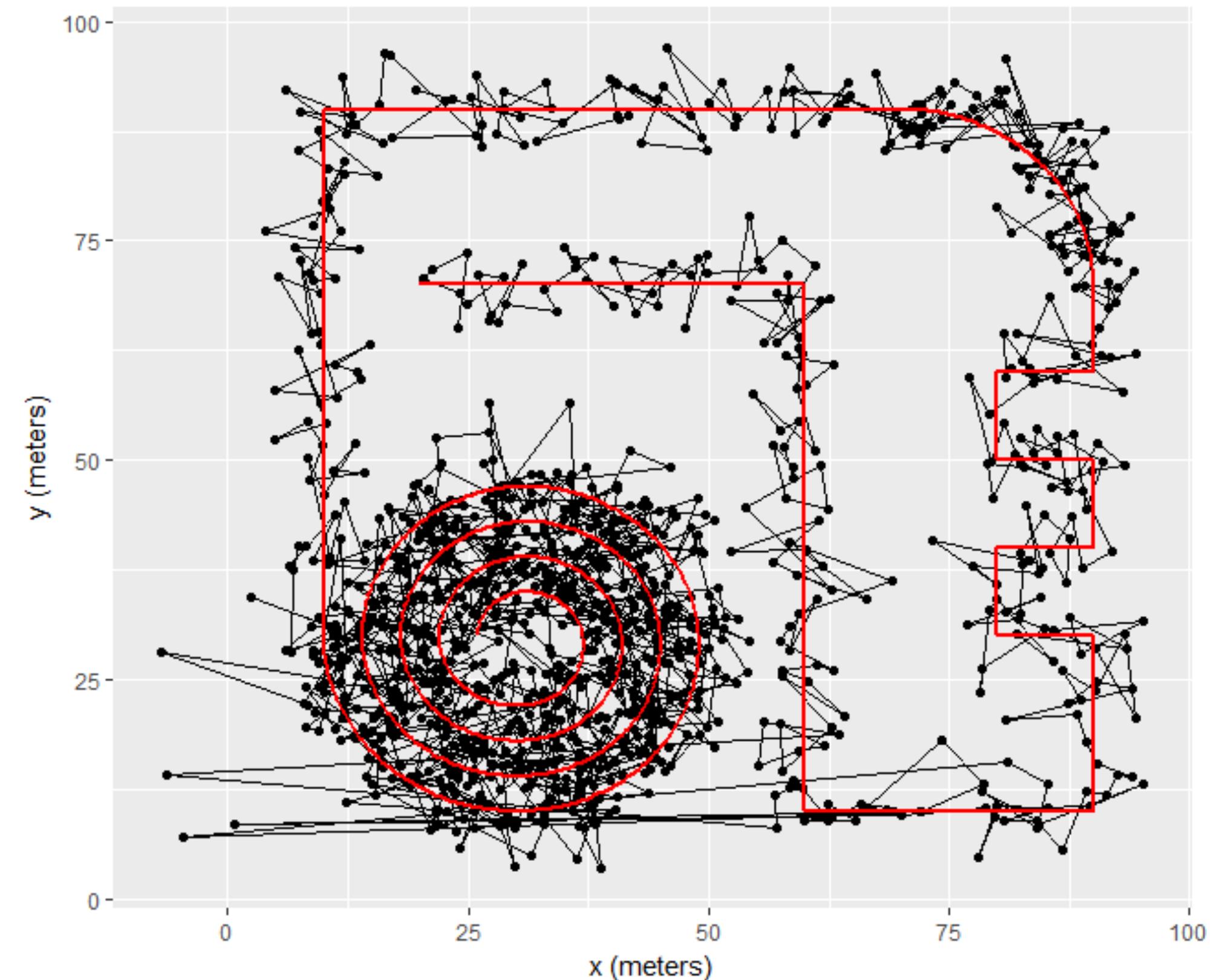
Mean Filter

$$\bar{x} = \frac{\sum_{i=1}^n x_i}{n}$$



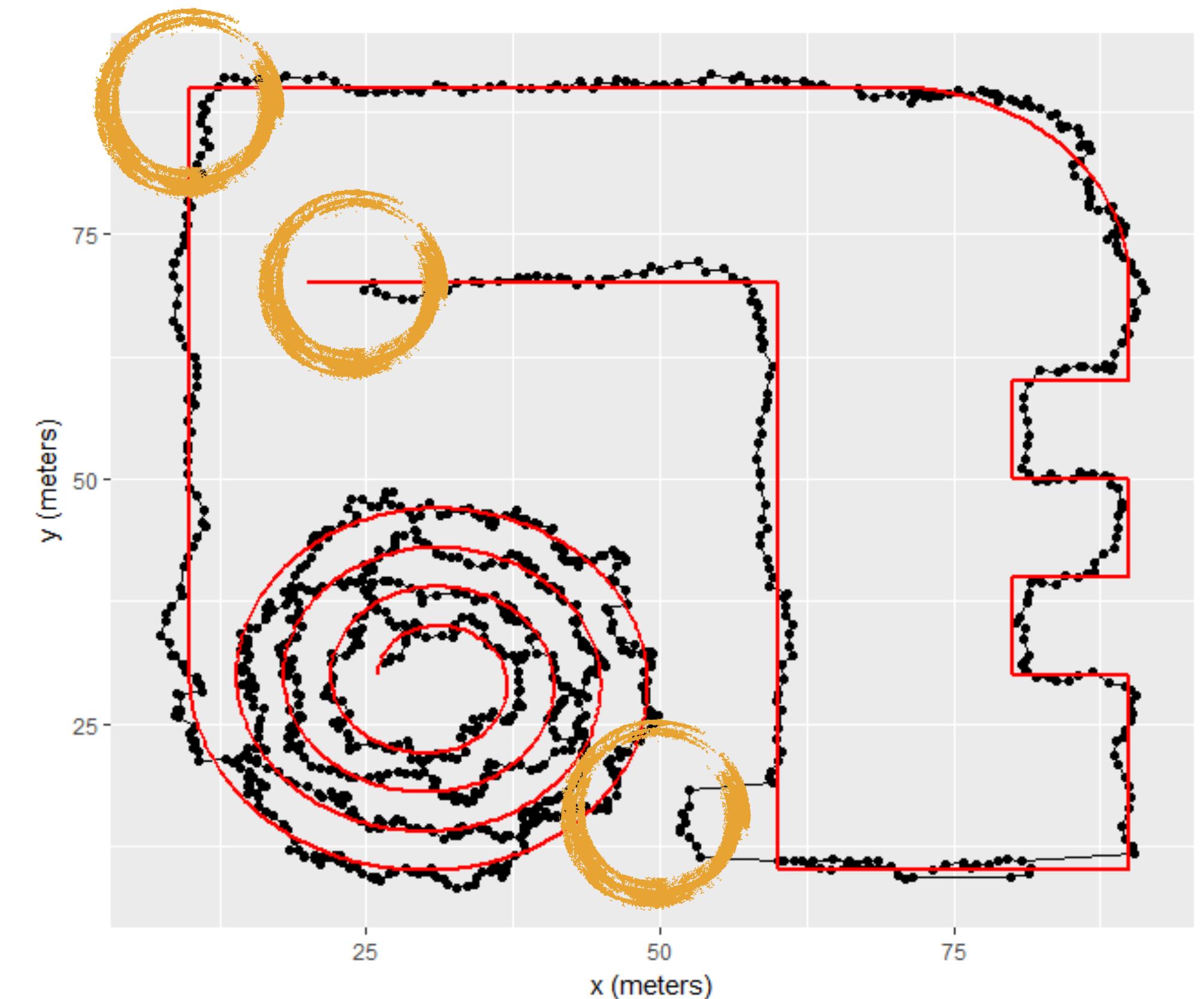
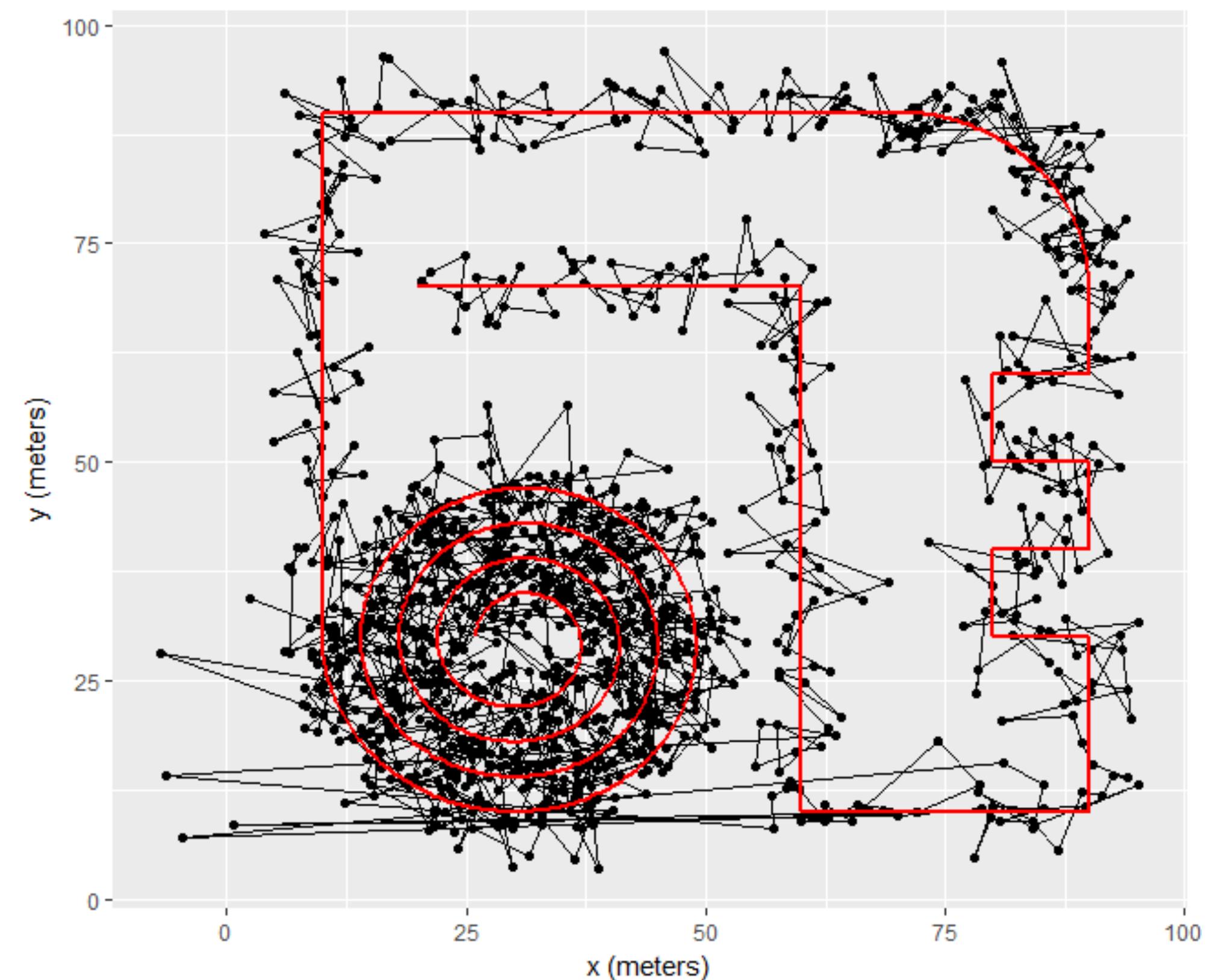
Mean Filter

window = 5



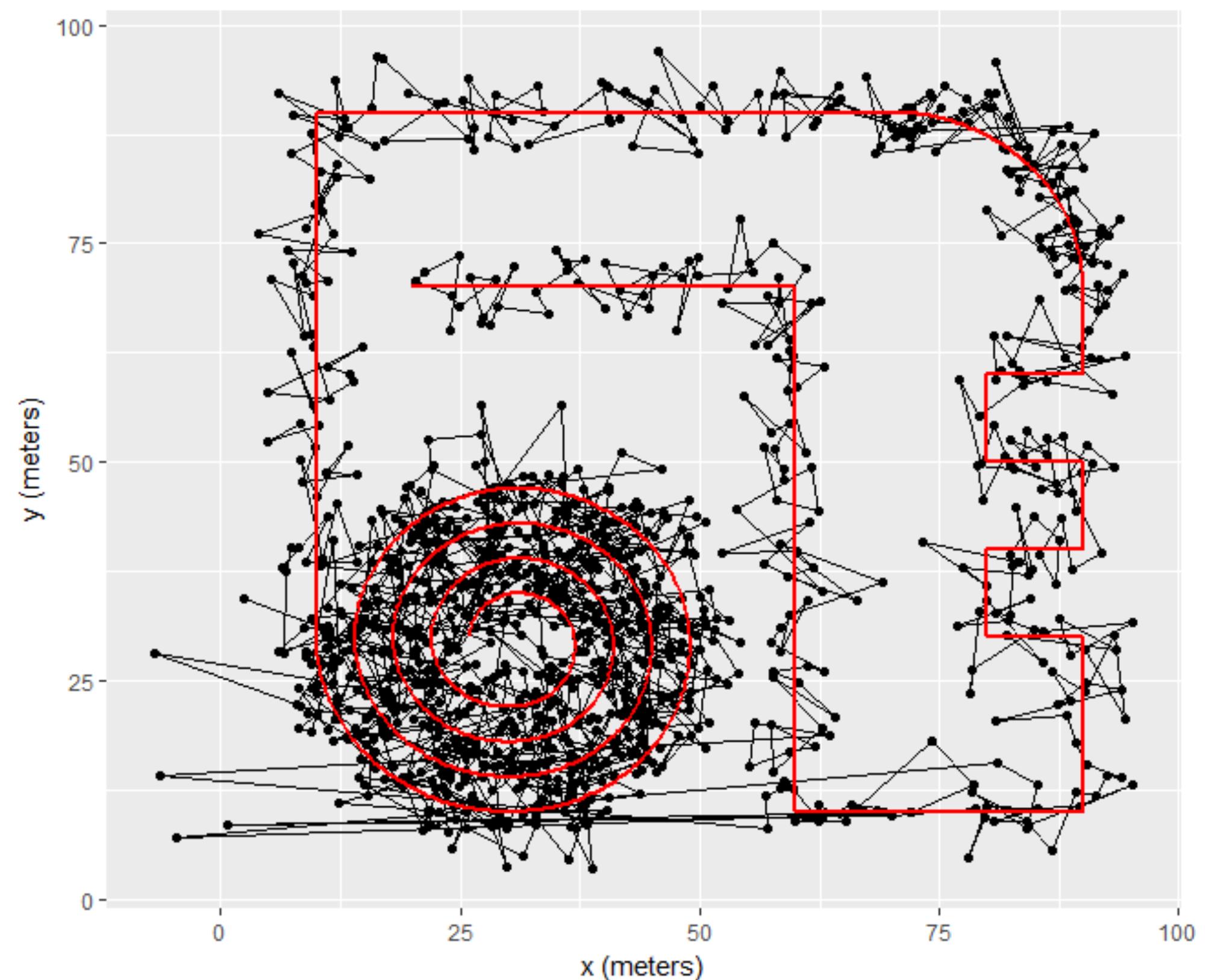
Mean Filter

window = 10



Mean Filter

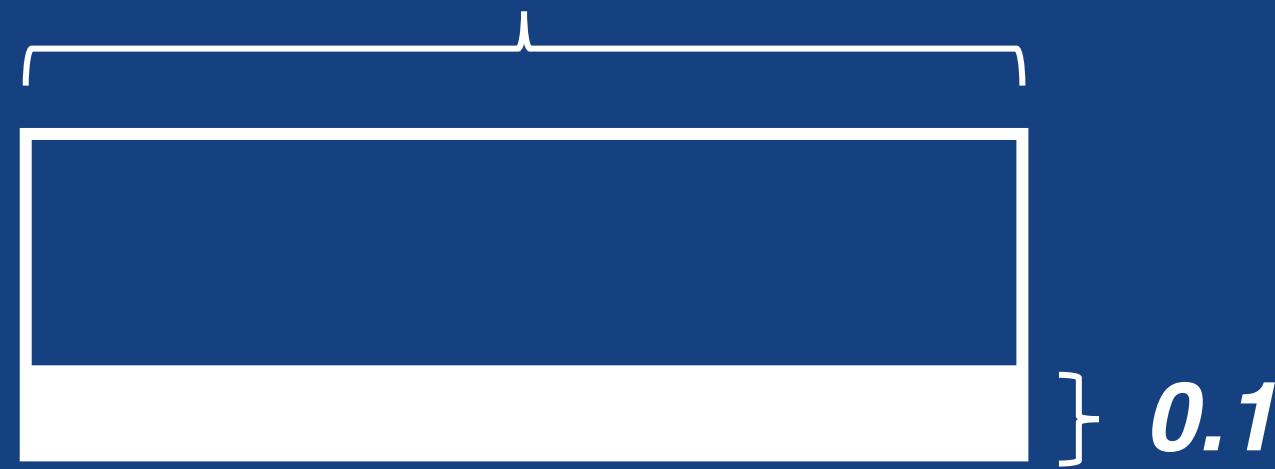
window = 30



Mean Filter

Mean Filter

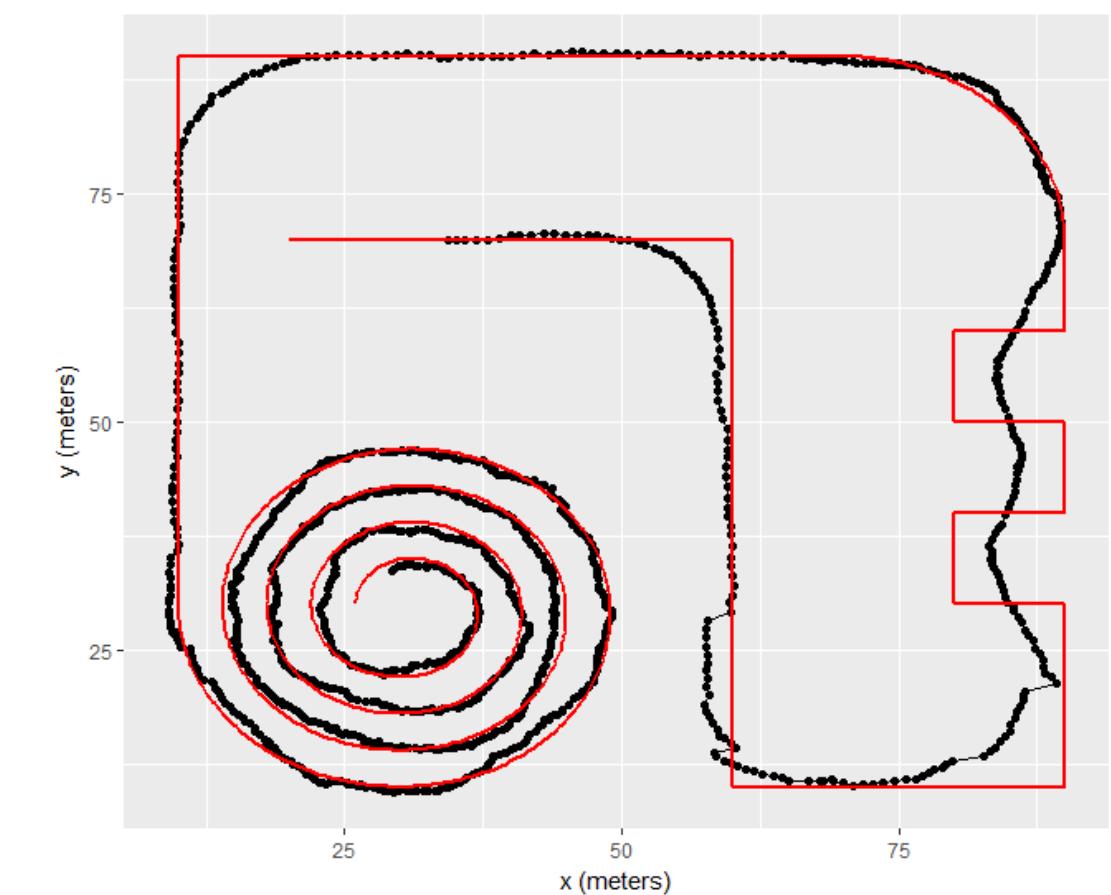
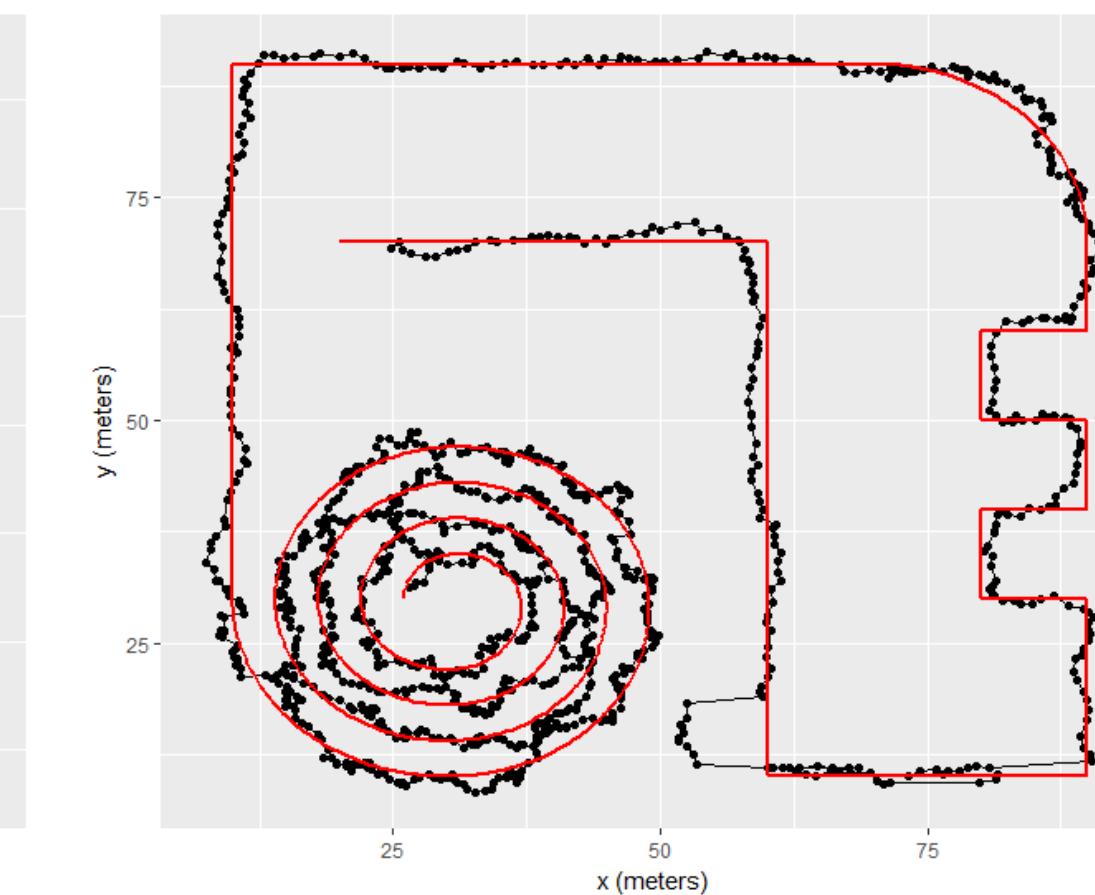
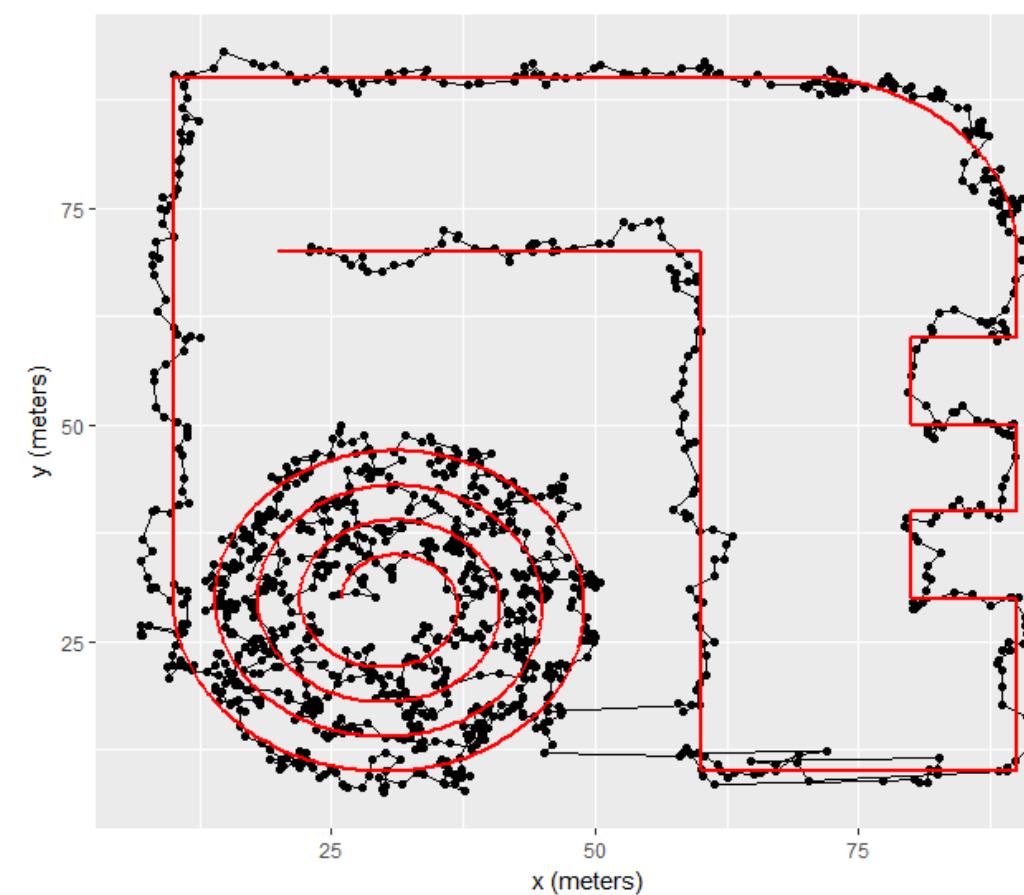
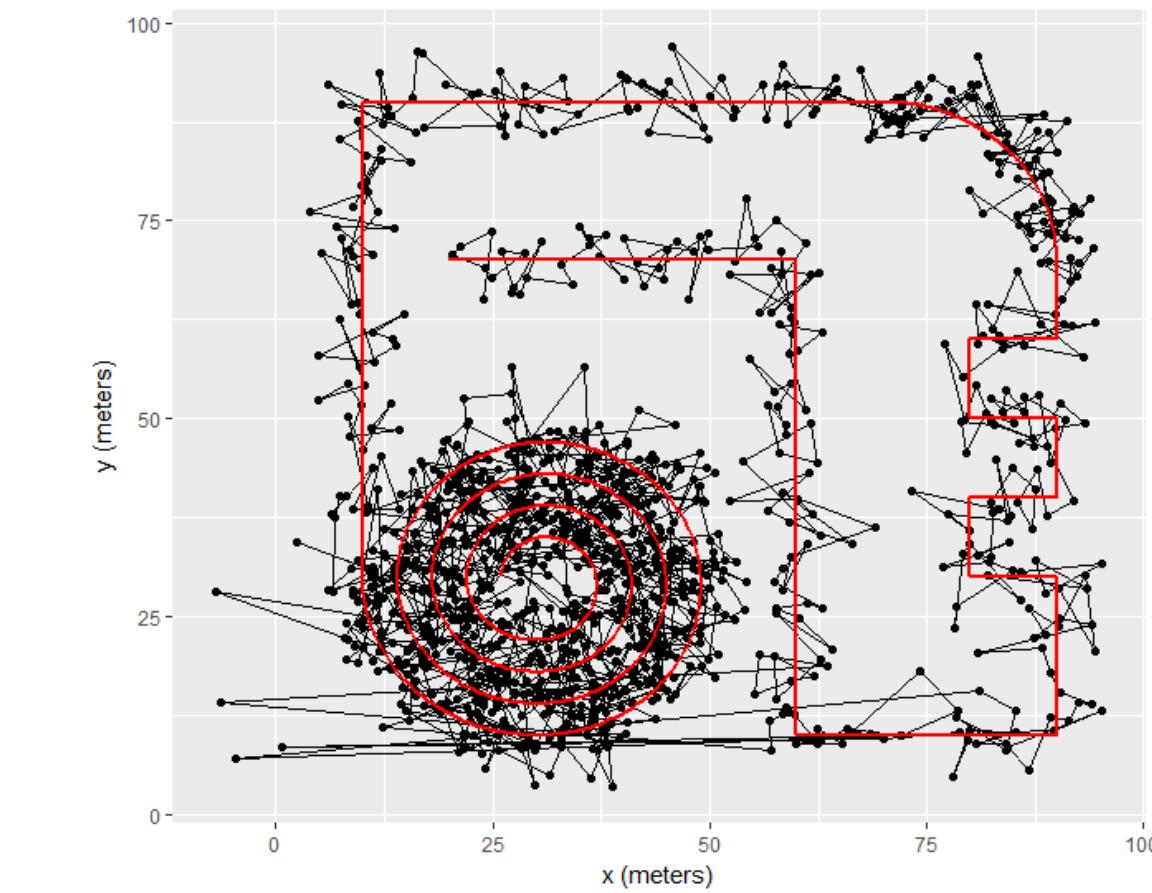
Size = 10

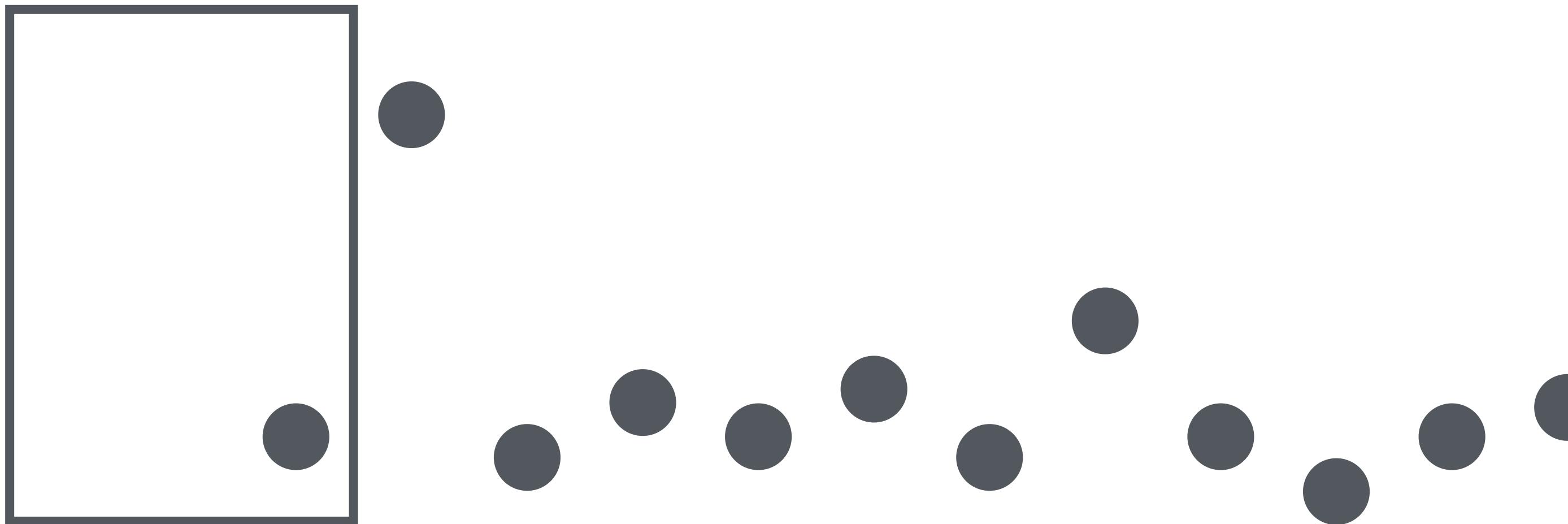


Uniform mean

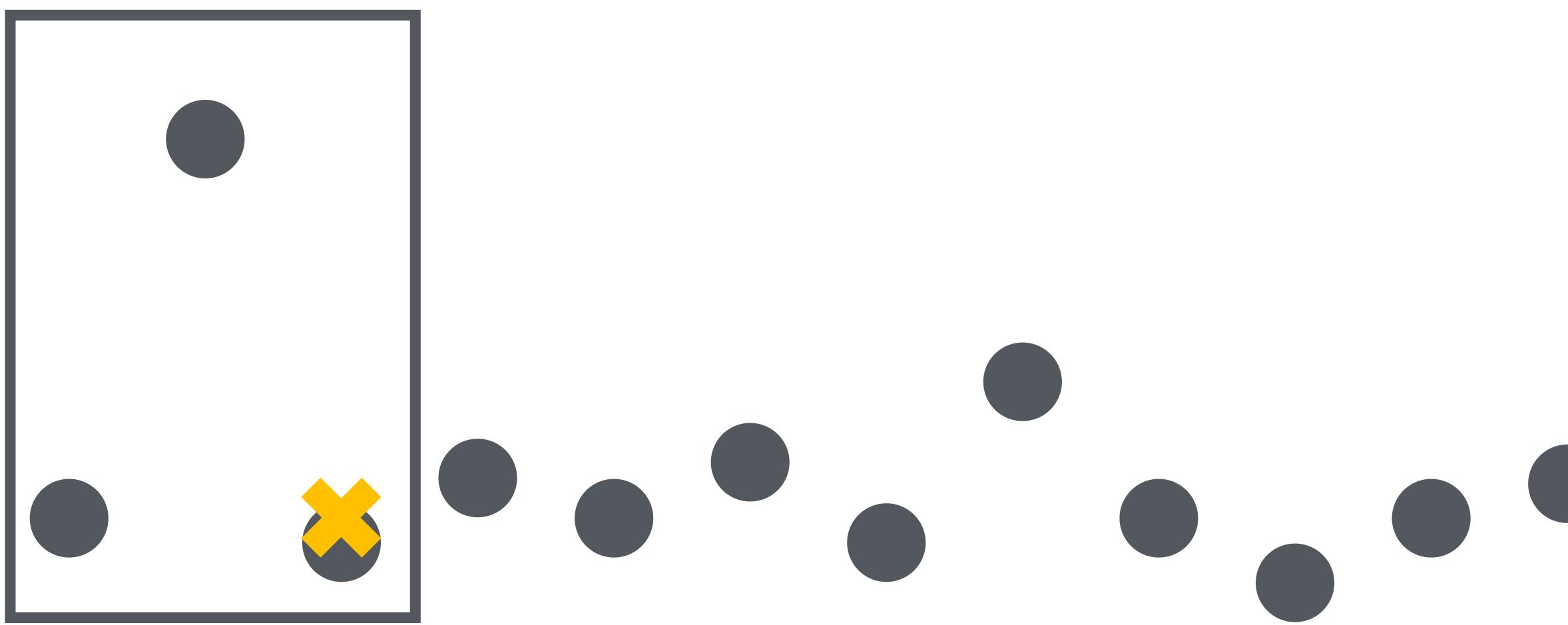


Weighted mean





Median Filter



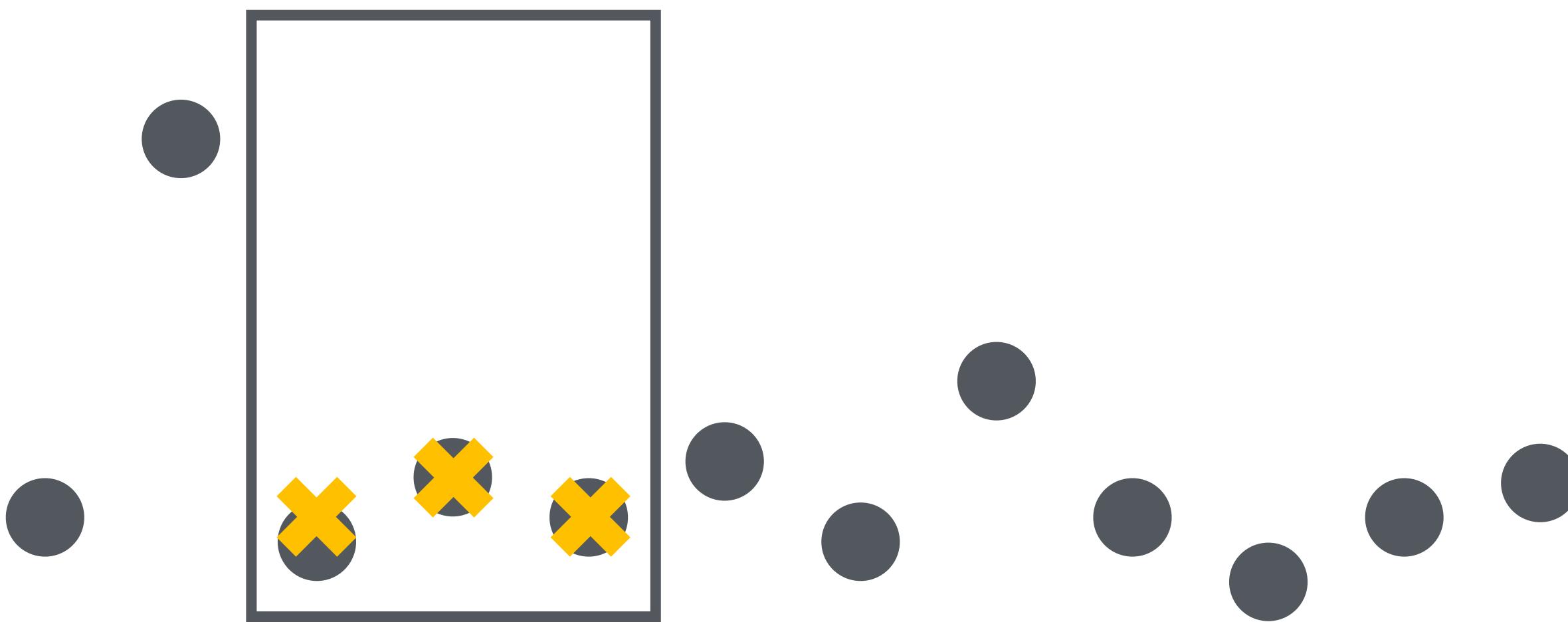
Median Filter



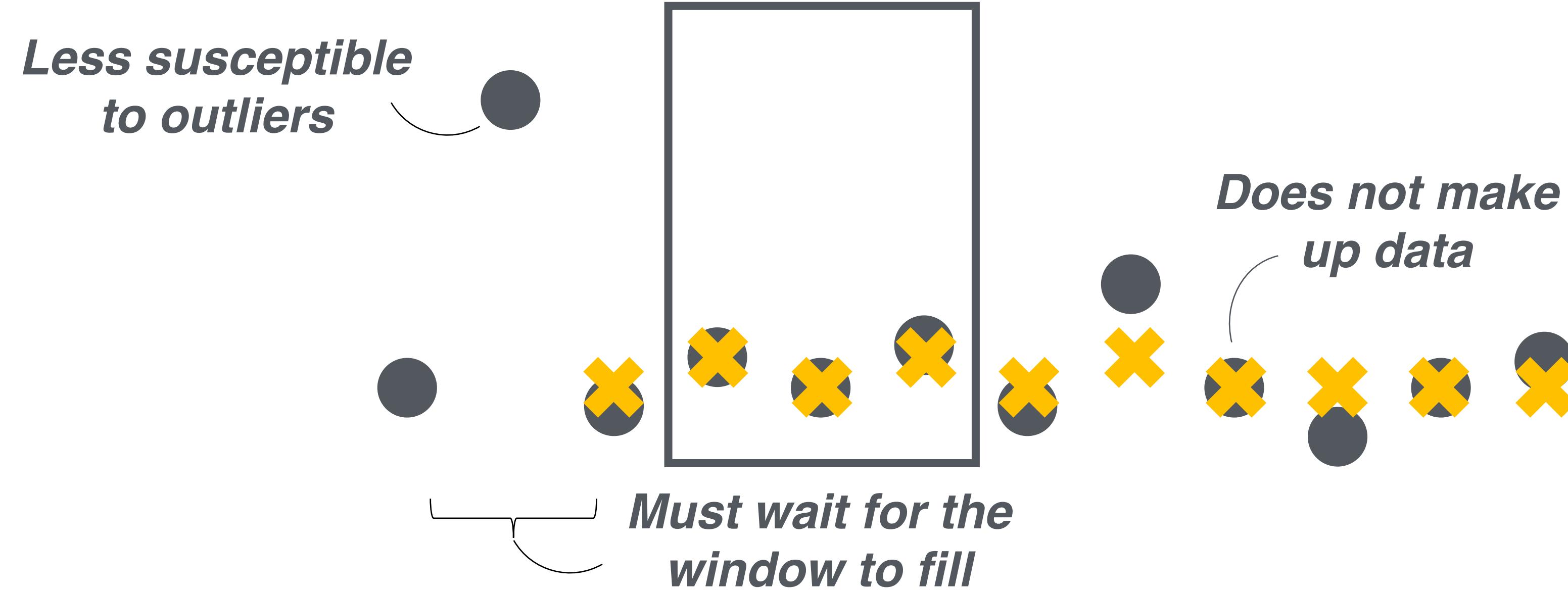
Median Filter



Median Filter

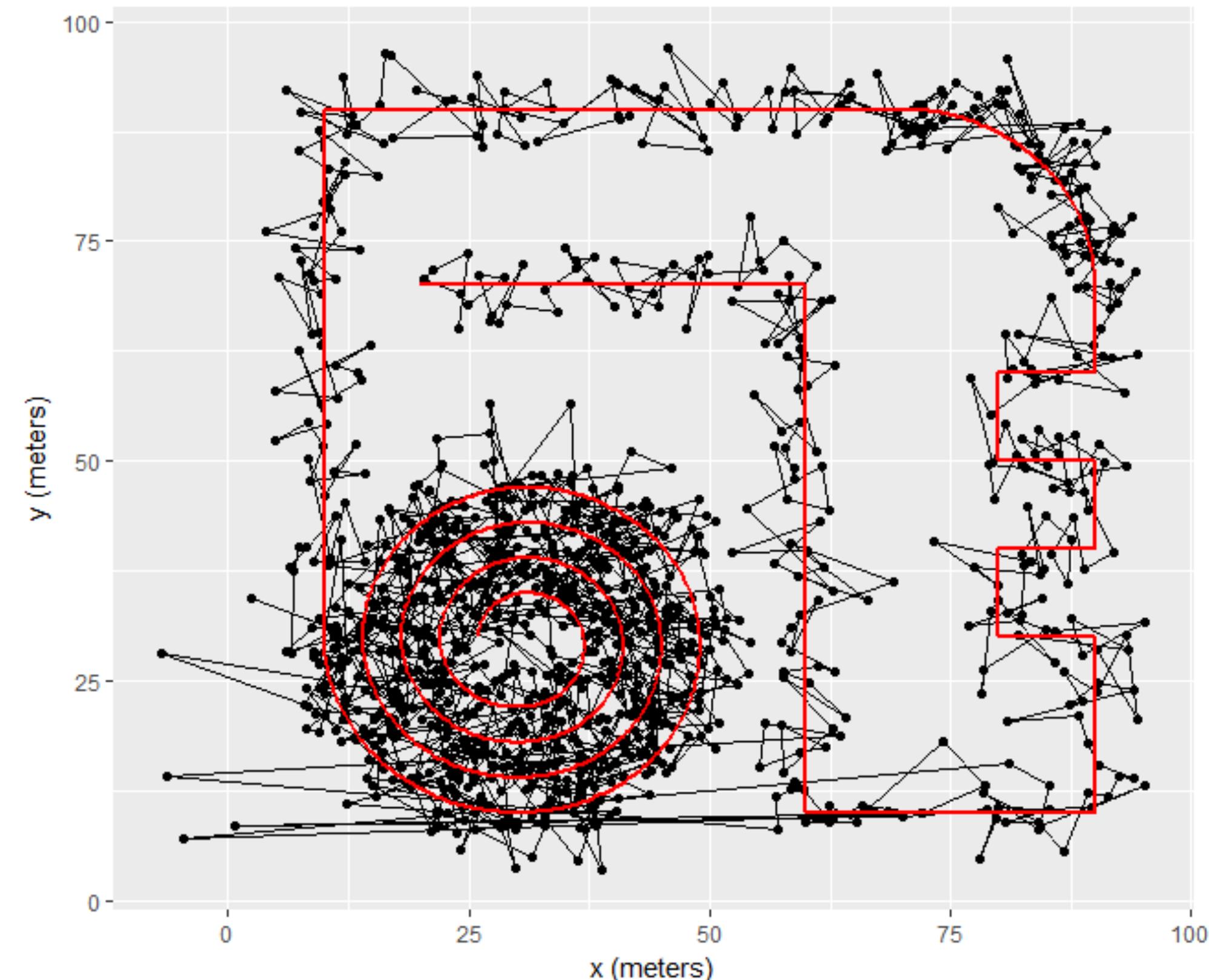


Median Filter



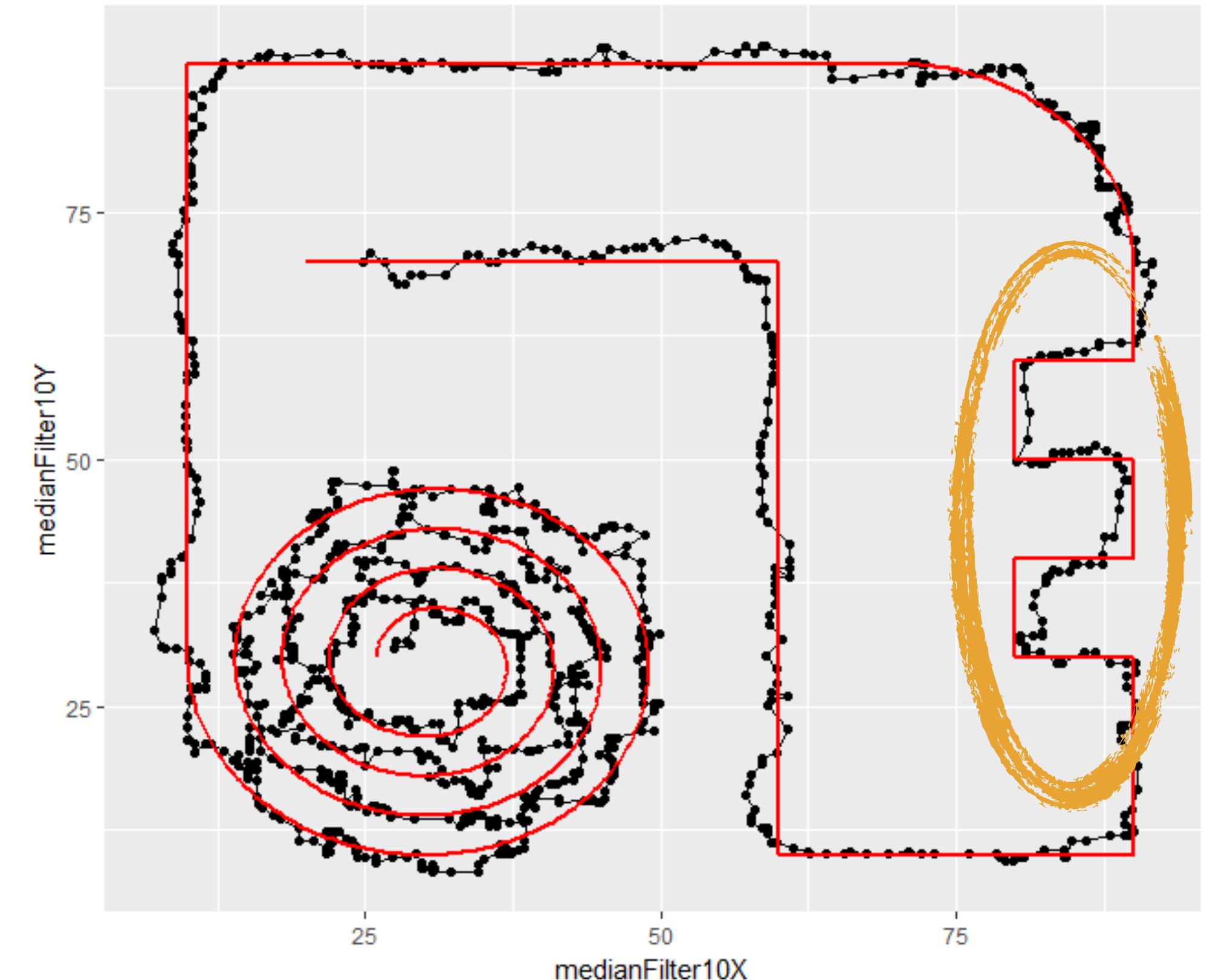
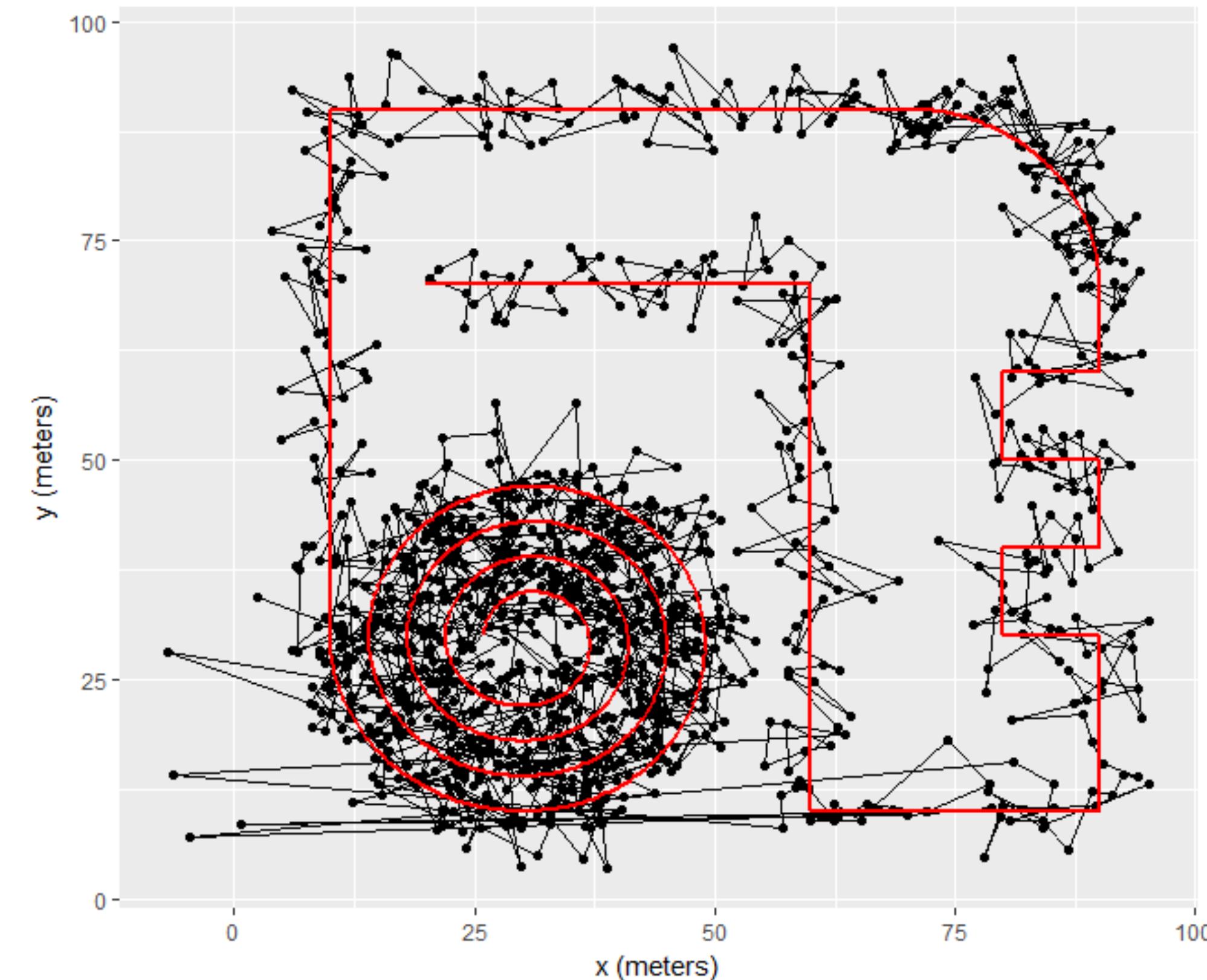
Median Filter

window = 5



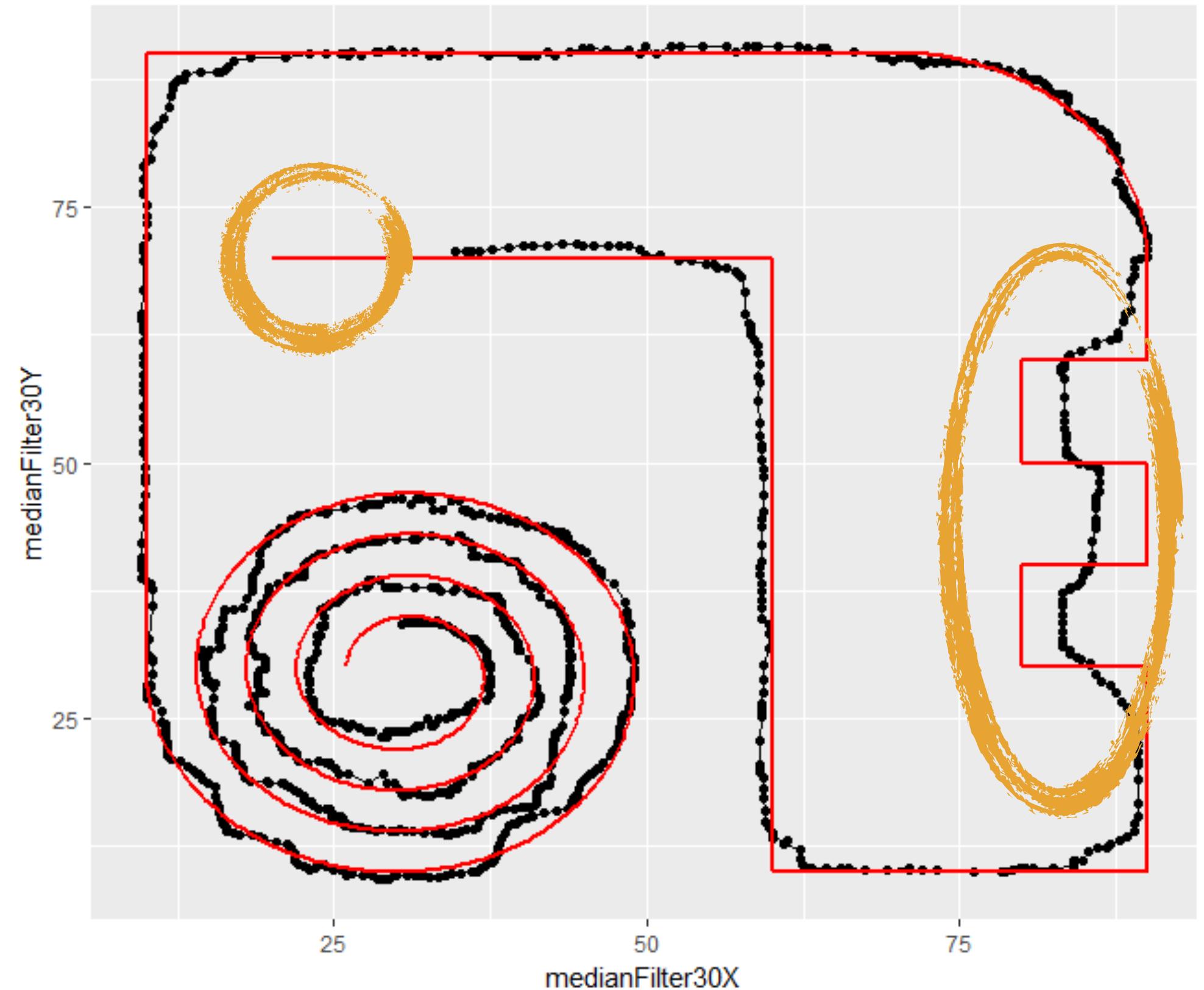
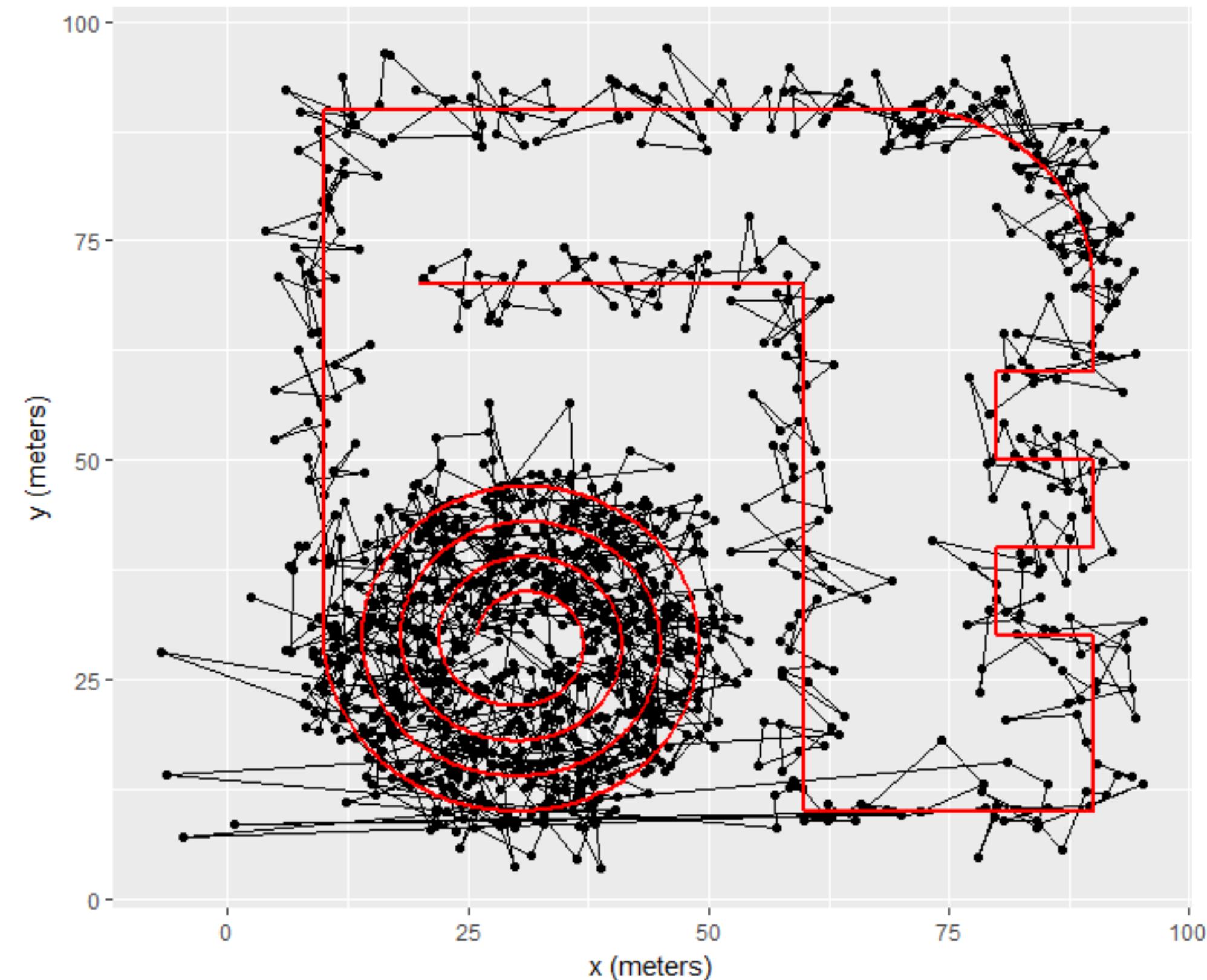
Median Filter

window = 10



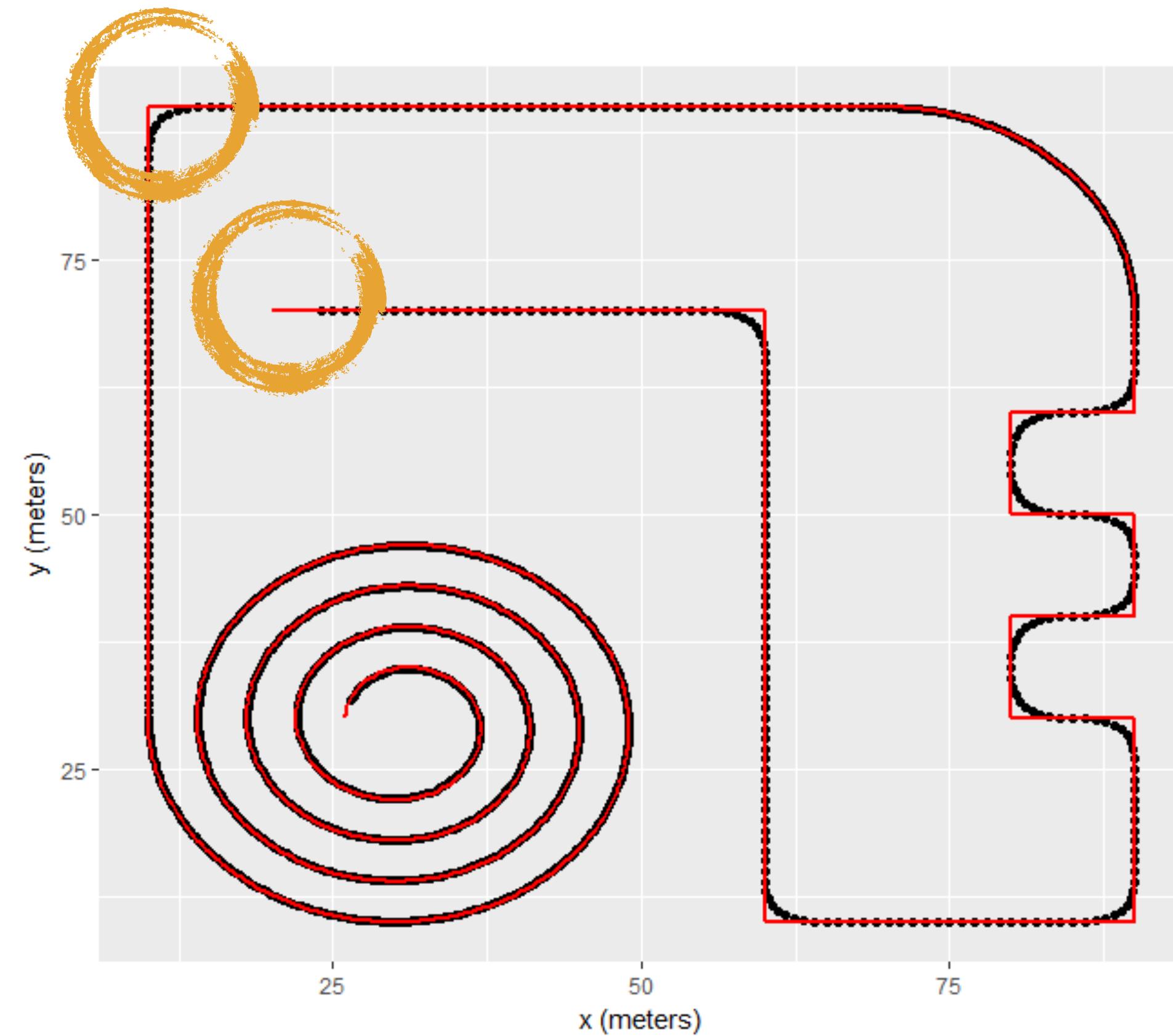
Median Filter

window = 30

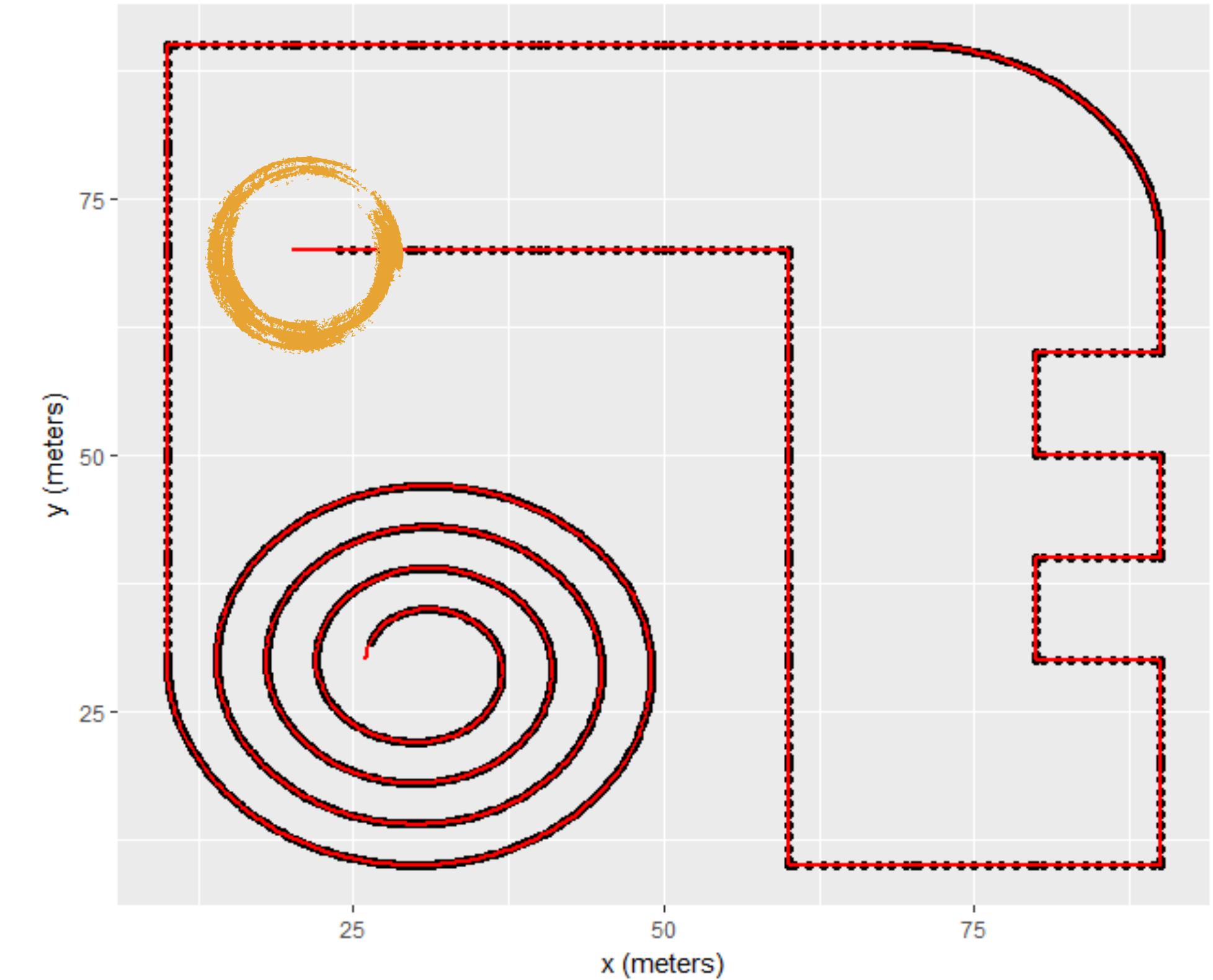


Median Filter

Mean



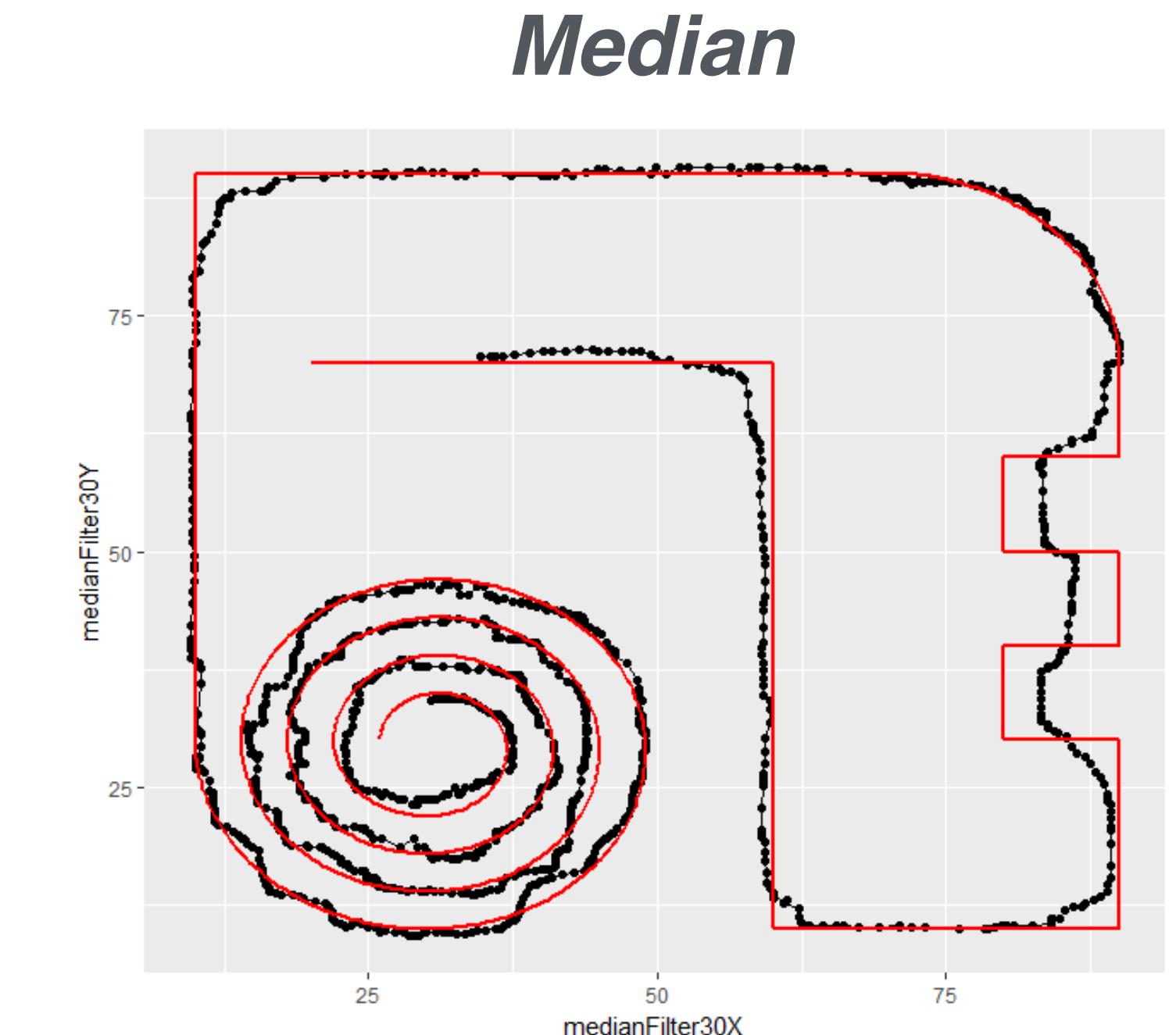
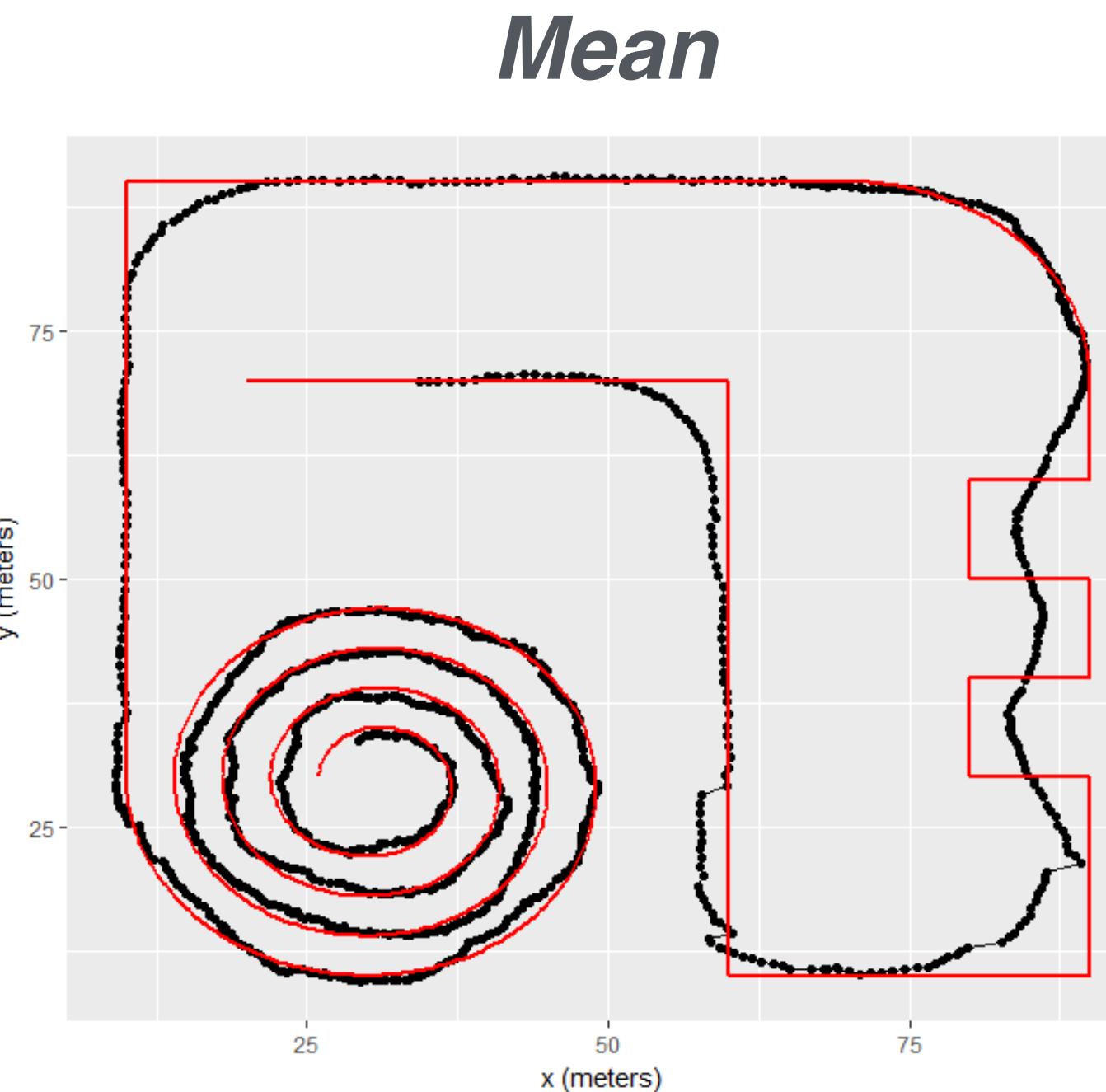
Median



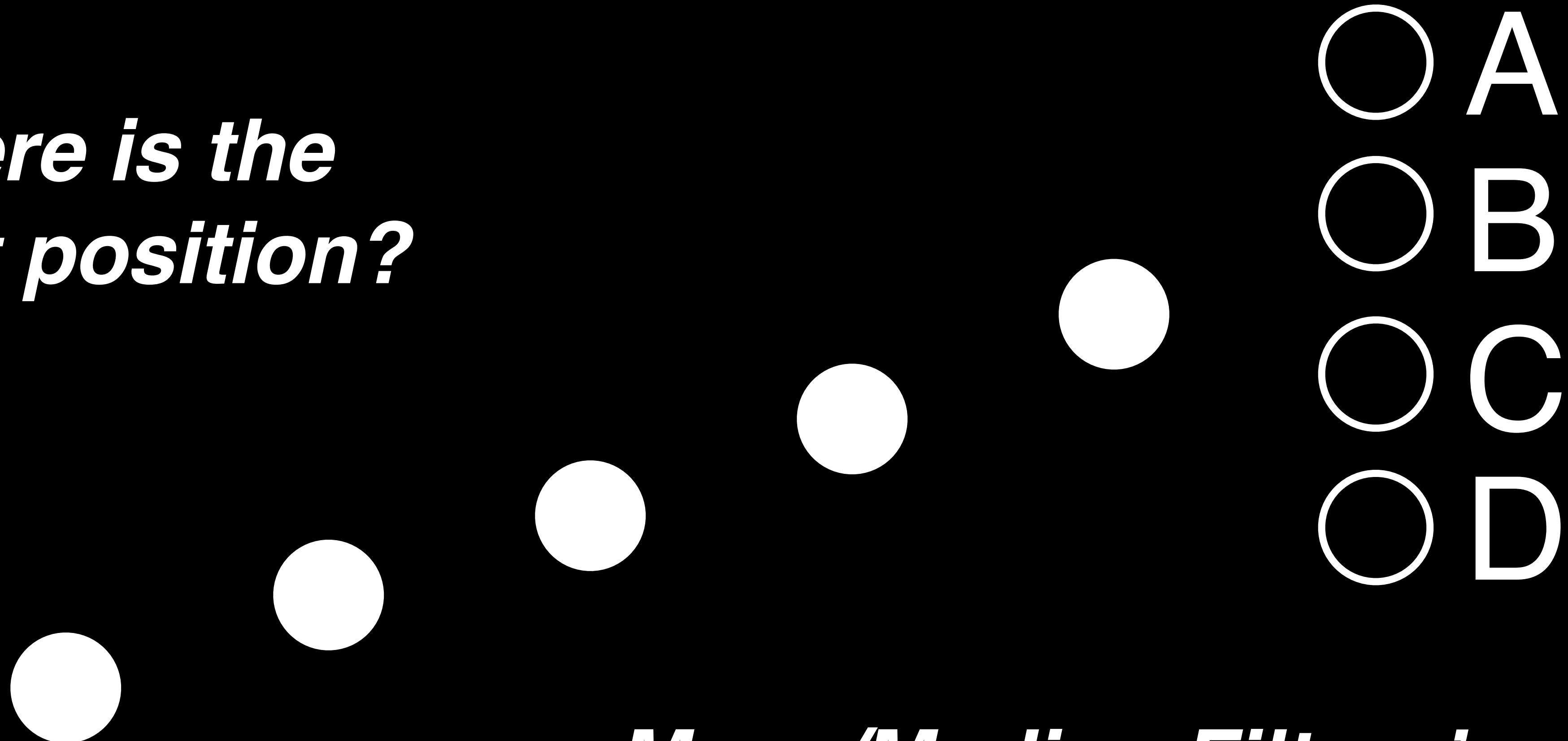
Comparison on Ground Truth Data

Mean/Median Filter

- + easy to implement
- + efficient
- + great cost-benefit
- laggy
- no dynamic model



*Where is the
next position?*



*Mean/Median Filters'
assumption:
Trajectory is smooth*

Kalman Filter

Rudolf Emil Kálmán
(1930 - 2016)



Kalman Filter

Measurement

$$z_i = \begin{pmatrix} z_i^{(x)} \\ z_i^{(y)} \end{pmatrix}$$

State

$$x_i = \begin{pmatrix} x_i \\ y_i \\ v_i^{(x)} \\ v_i^{(y)} \end{pmatrix} \quad \begin{matrix} \} \\ \} \end{matrix} \quad \begin{matrix} \text{positions} \\ \text{velocities} \end{matrix}$$

**Variables that are
not measured
directly**

$$H = \begin{bmatrix} 1 & 0 & 0 & 0 \\ 0 & 1 & 0 & 0 \end{bmatrix}$$

$$\overset{\mathbf{H}}{z_i} = \mathbf{x}_i + \mathbf{v}_i$$

Kalman Filter

Measurement

$$z_i = \begin{pmatrix} z_i^{(x)} \\ z_i^{(y)} \end{pmatrix}$$

State

$$x_i = \begin{pmatrix} x_i \\ y_i \\ v_i^{(x)} \\ v_i^{(y)} \end{pmatrix} \quad \begin{matrix} \} & \text{positions} \\ \} & \text{velocities} \end{matrix}$$

*Variables that are
not measured
directly*

Noise

$$v_i \sim N(0, R_i)$$

$$R_i = \begin{bmatrix} \sigma^2 & 0 \\ 0 & \sigma^2 \end{bmatrix}$$

$$z_i = Hx_i + v_i$$

$$H = \begin{bmatrix} 1 & 0 & 0 & 0 \\ 0 & 1 & 0 & 0 \end{bmatrix}$$

Modelling the Dynamics

$$\begin{pmatrix} x_i \\ y_i \\ v_i^{(x)} \\ v_i^{(y)} \end{pmatrix} \quad \leftarrow \quad \begin{pmatrix} x_{i-1} \\ y_{i-1} \\ v_{i-1}^{(x)} \\ v_{i-1}^{(y)} \end{pmatrix}$$

$$x_i \quad \leftarrow \quad x_{i-1}$$

Modelling the Dynamics

$$\begin{pmatrix} x_i \\ y_i \\ v_i^{(x)} \\ v_i^{(y)} \end{pmatrix} \leftarrow \begin{bmatrix} 1 & 0 & \Delta t & 0 \\ 0 & 1 & 0 & \Delta t \\ 0 & 0 & 1 & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix} \begin{pmatrix} x_{i-1} \\ y_{i-1} \\ v_{i-1}^{(x)} \\ v_{i-1}^{(y)} \end{pmatrix} + \begin{pmatrix} 0 \\ 0 \\ N(0, \sigma_s) \\ N(0, \sigma_s) \end{pmatrix}$$

Newtonian Velocity

$$x_i = x_{i-1} + v_{i-1} \Delta t$$
$$v_i = v_{i-1}$$

$$x_i \leftarrow x_{i-1}$$

Modelling the Dynamics

$$\begin{pmatrix} x_i \\ y_i \\ v_i^{(x)} \\ v_i^{(y)} \end{pmatrix} \leftarrow \underbrace{\begin{bmatrix} 1 & 0 & \Delta t & 0 \\ 0 & 1 & 0 & \Delta t \\ 0 & 0 & 1 & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix}}_{\phi_{i-1}} \begin{pmatrix} x_{i-1} \\ y_{i-1} \\ v_{i-1}^{(x)} \\ v_{i-1}^{(y)} \end{pmatrix} + \underbrace{\begin{pmatrix} 0 \\ 0 \\ N(0, \sigma_s) \\ N(0, \sigma_s) \end{pmatrix}}_{w_{i-1}}$$

ϕ_{i-1}

w_{i-1}

$$w_{i-1} \sim N(0, Q_i)$$

$$Q_i = \begin{bmatrix} 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 \\ 0 & 0 & \sigma_s^2 & 0 \\ 0 & 0 & 0 & \sigma_s^2 \end{bmatrix}$$

$$x_i \leftarrow x_{i-1}$$

Modelling the Dynamics

Putting it all together...

Measurement matrix

$$H = \begin{bmatrix} 1 & 0 & 0 & 0 \\ 0 & 1 & 0 & 0 \end{bmatrix}$$

Dynamics of states

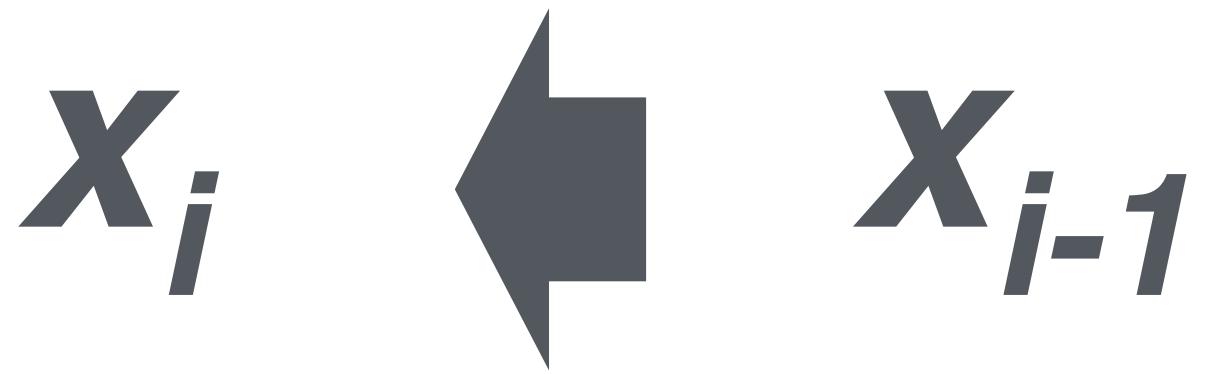
$$\phi_{i-1} = \begin{bmatrix} 1 & 0 & \Delta t & 0 \\ 0 & 1 & 0 & \Delta t \\ 0 & 0 & 1 & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix}$$

Measurement noise

$$v_i \sim N(0, R_i)$$

Dynamic noise

$$w_{i-1} \sim N(0, Q_i)$$



Modelling the Dynamics

Putting it all together...

***Initial state
estimate***

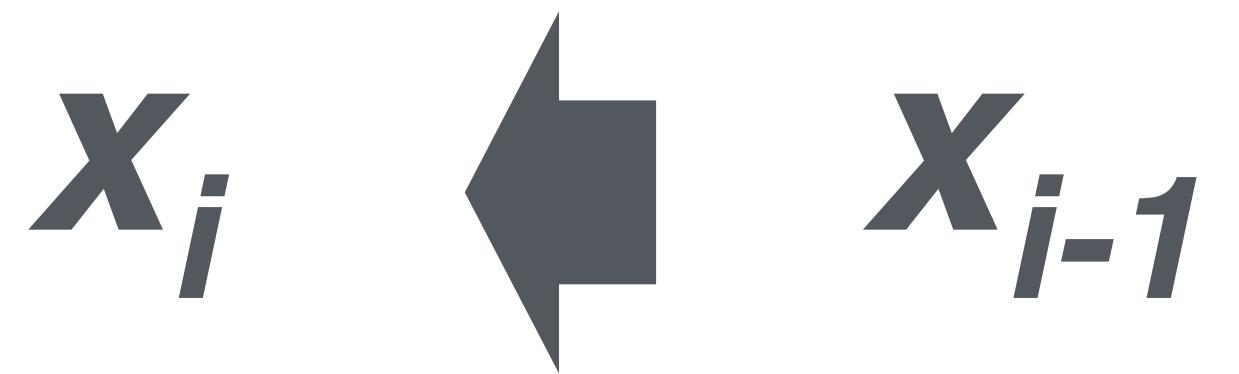
$$x_0 = \begin{pmatrix} x_0 \\ y_0 \\ v_0^{(x)} \\ v_0^{(y)} \end{pmatrix} = \begin{pmatrix} z_0^{(x)} \\ z_0^{(y)} \\ 0 \\ 0 \end{pmatrix}$$

e.g. *First measurement of position*

and zero velocity

***Initial estimate of state
error covariance***

$$P_0 = \begin{bmatrix} \sigma^2 & 0 & 0 & 0 \\ 0 & \sigma^2 & 0 & 0 \\ 0 & 0 & \sigma_s^2 & 0 \\ 0 & 0 & 0 & \sigma_s^2 \end{bmatrix}$$



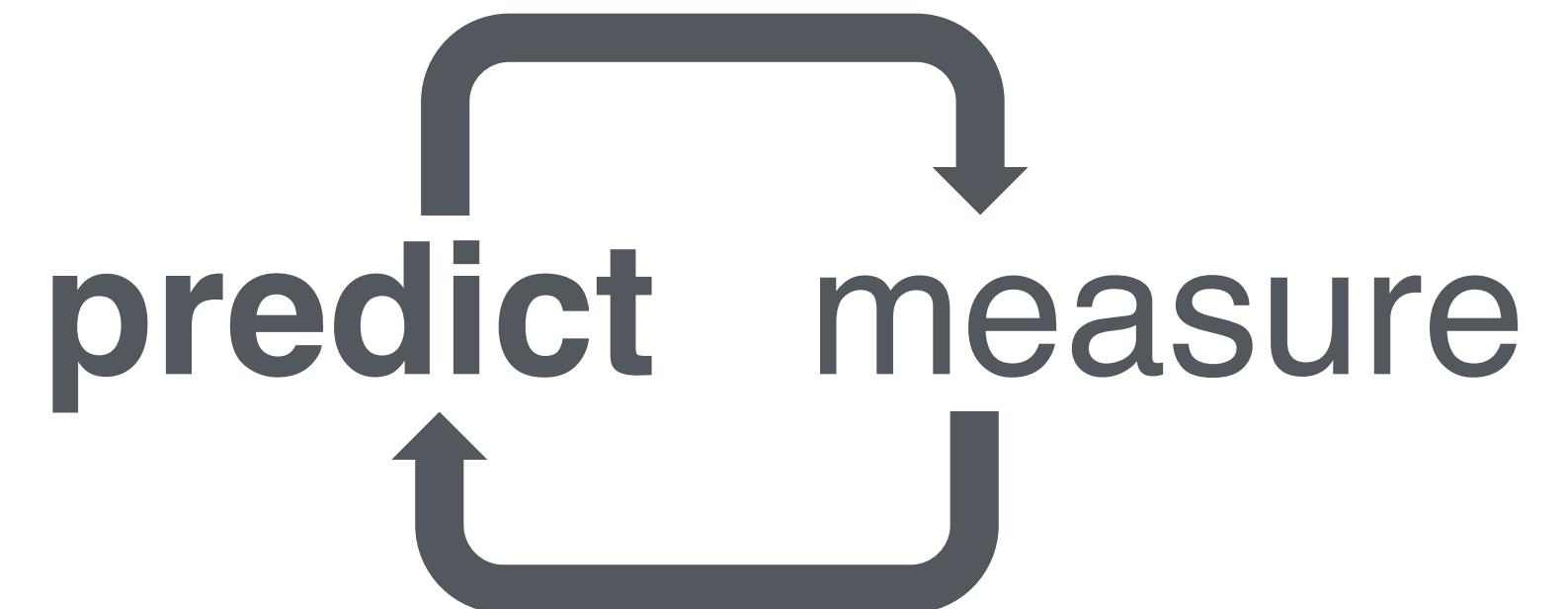
Step 1: Predicting States

1. ***Extrapolate the state:***

$$x_i^{predicted} = \phi_{i-1} x_{i-1}^{corrected}$$

2. ***Extrapolate the state error covariance:***

$$P_i^{predicted} = \phi_{i-1} P_{i-1}^{corrected} \phi_{i-1}^T + Q_{i-1}$$



Step 2: Measure

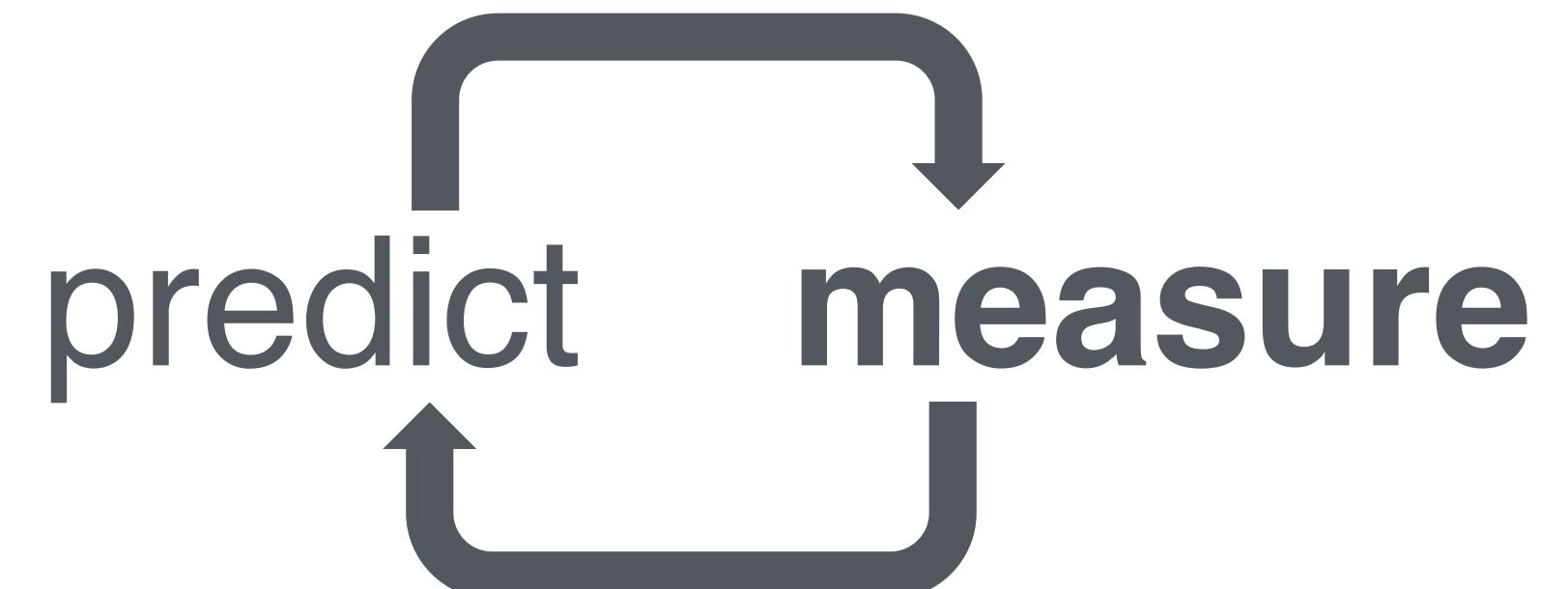
3. Compute the Kalman gain:

$$K_i = \frac{P_i^{predicted} H_i^T}{H_i P_i^{predicted} H_i^T + R_i}$$

Uncertainty propagated by the model

$$= H_i^{-1} \frac{H_i P_i^{predicted} H_i^T}{H_i P_i^{predicted} H_i^T + R_i}$$

Uncertainty from the measurement



Step 2: Measure

3. Compute the Kalman gain:

$$K_i = \frac{P_i^{predicted} H_i^T}{H_i P_i^{predicted} H_i^T + R_i}$$

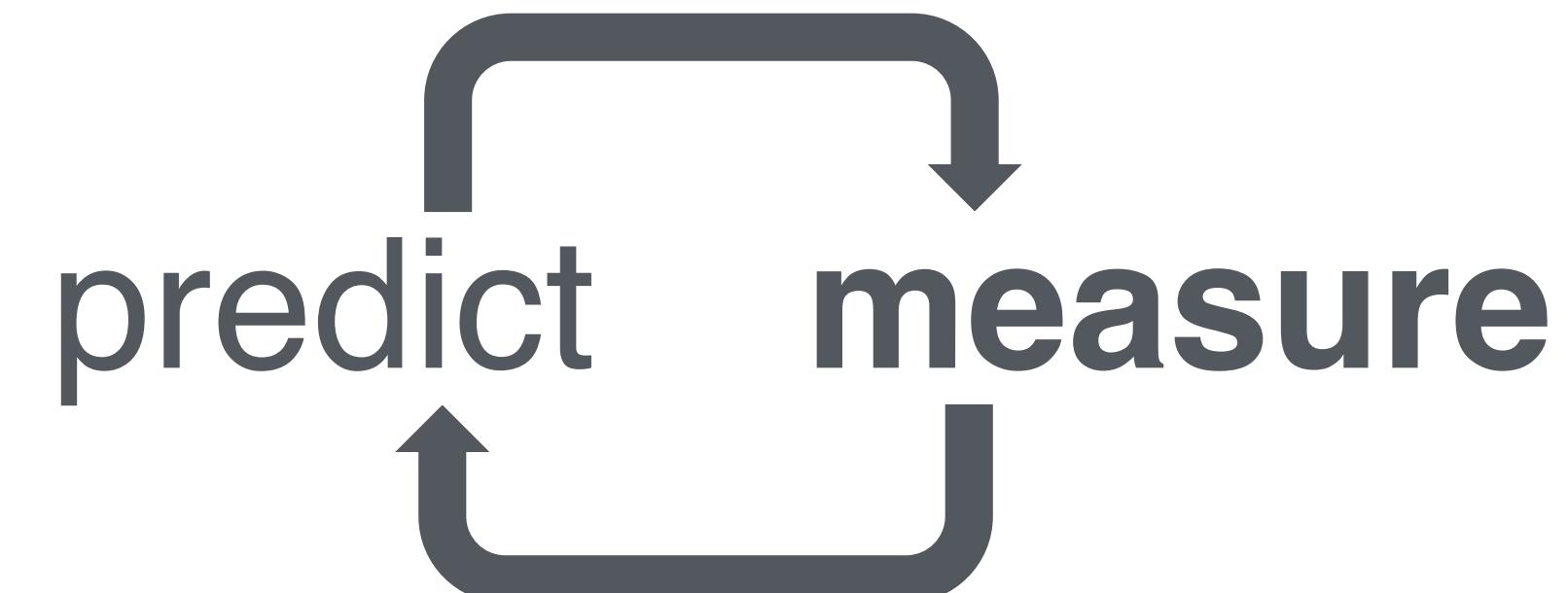
$$= H_i^{-1} \frac{H_i P_i^{predicted} H_i^T}{H_i P_i^{predicted} H_i^T + R_i}$$

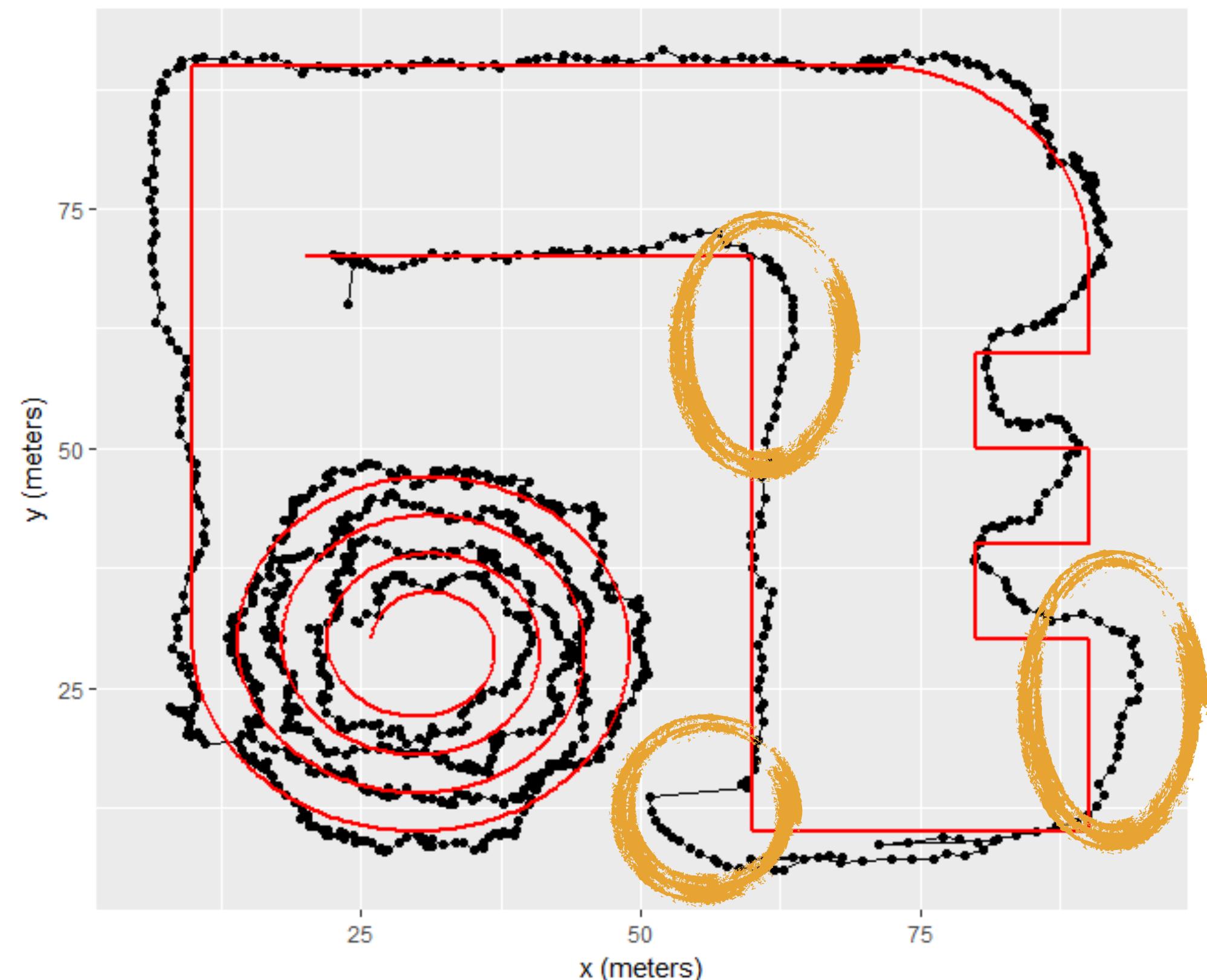
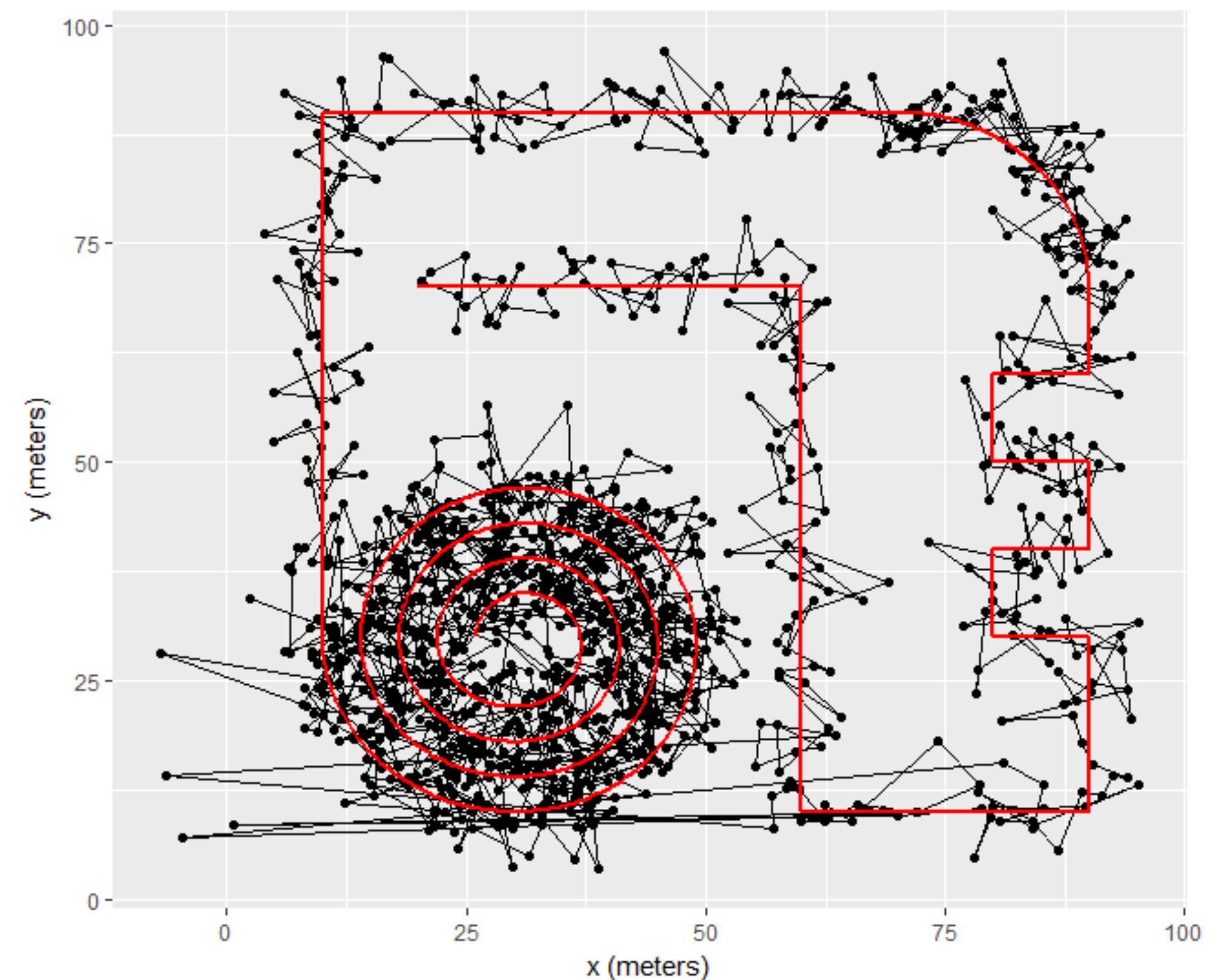
4. Update extrapolations with new measurements:

$$x_i^{corrected} = x_i^{predicted} + K_i (z_i - H_i x_i^{predicted})$$

$$P_i^{corrected} = (I - K_i H_i) P_i^{predicted}$$

Identity

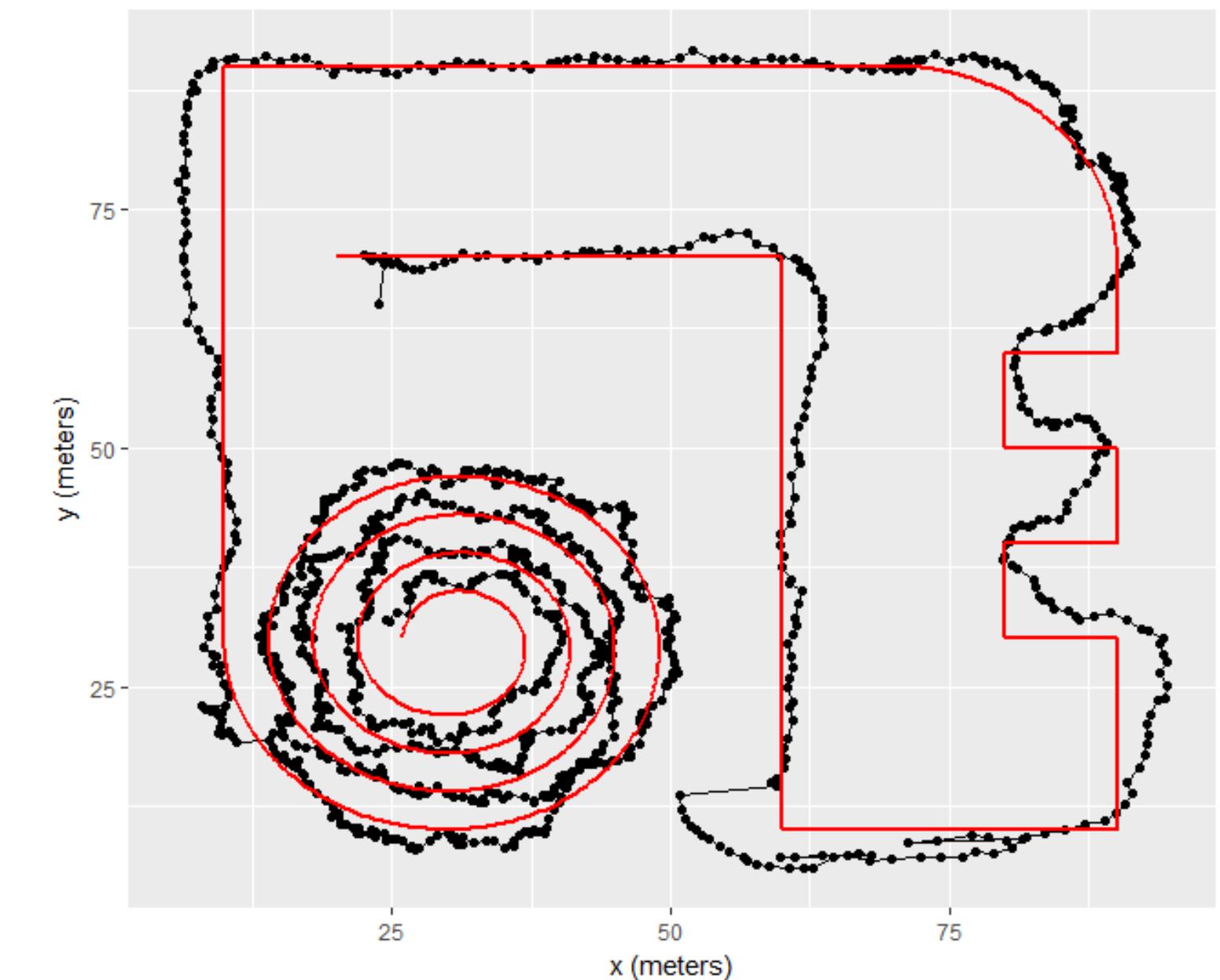
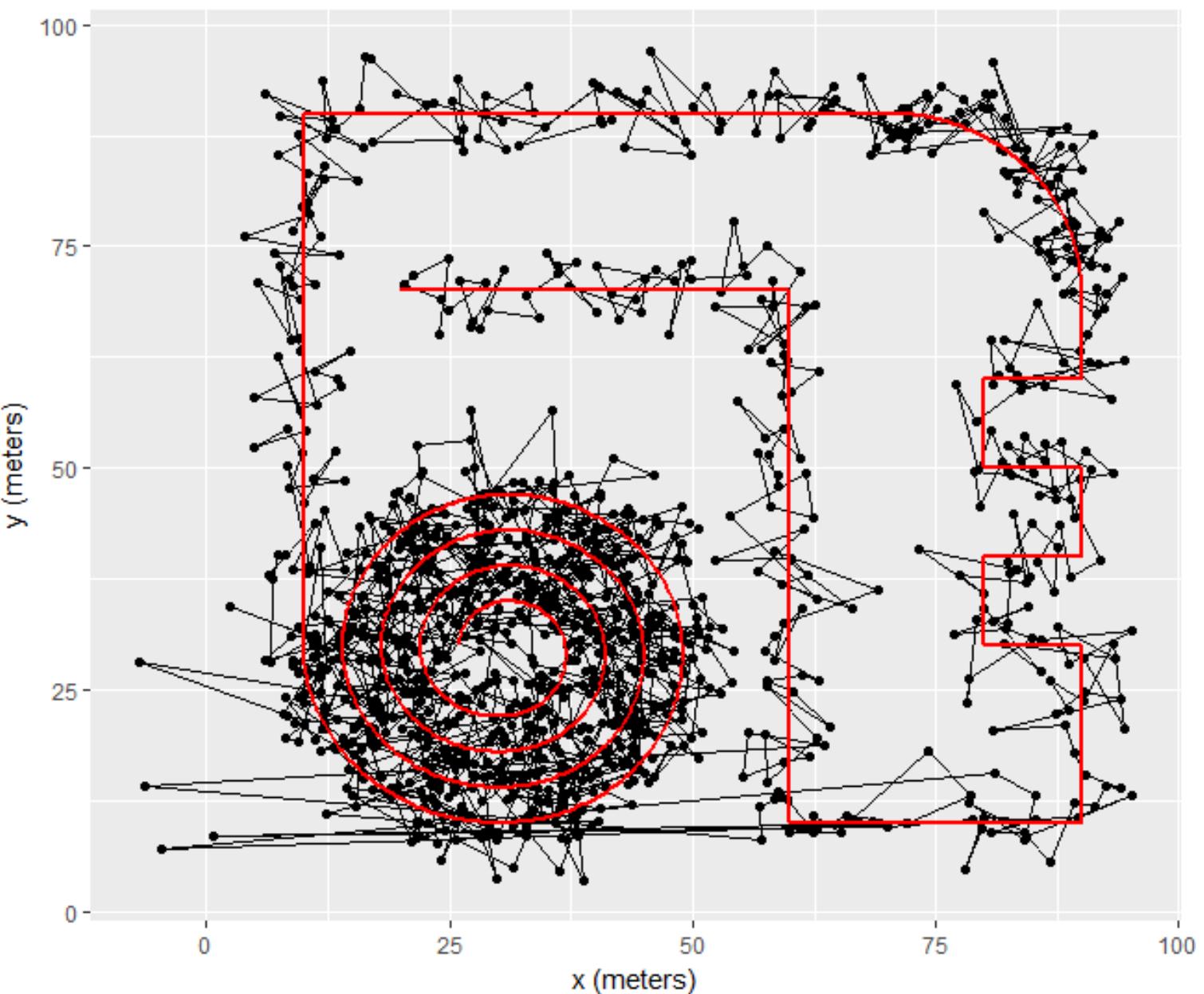




Kalman Filter

Kalman Filter

- + dynamic model of the system
- + no lag
- + tunable trade-off between model and measurement
- + uncertainty estimate
- + cheap to run
- parameters not intuitive
- overshooting



Kalman Filter

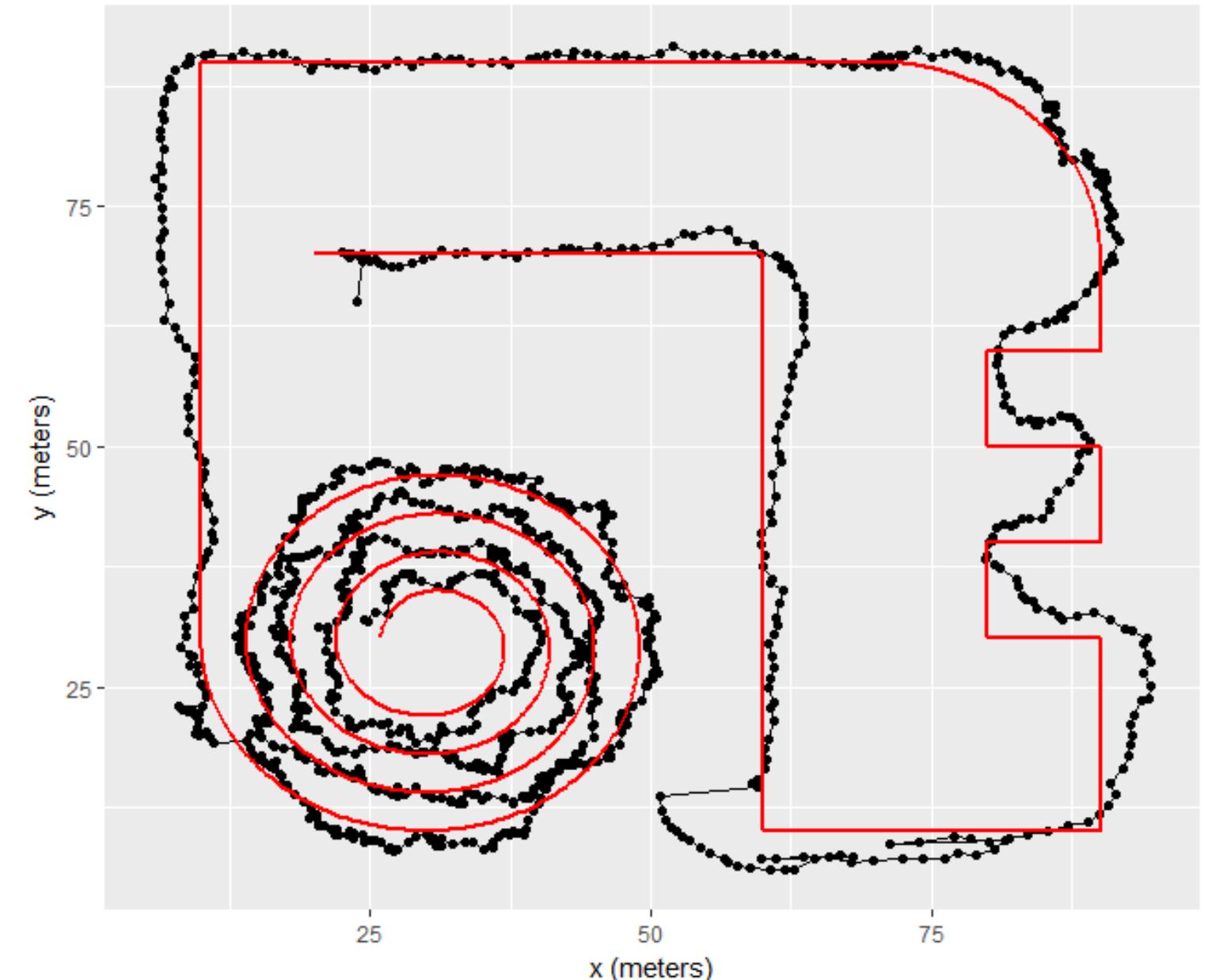
$$P(A \mid B) = \frac{P(B \mid A)P(A)}{P(B)}$$

Bayesian

Gaussian
Linear

Online

*What if this is
not the case?*

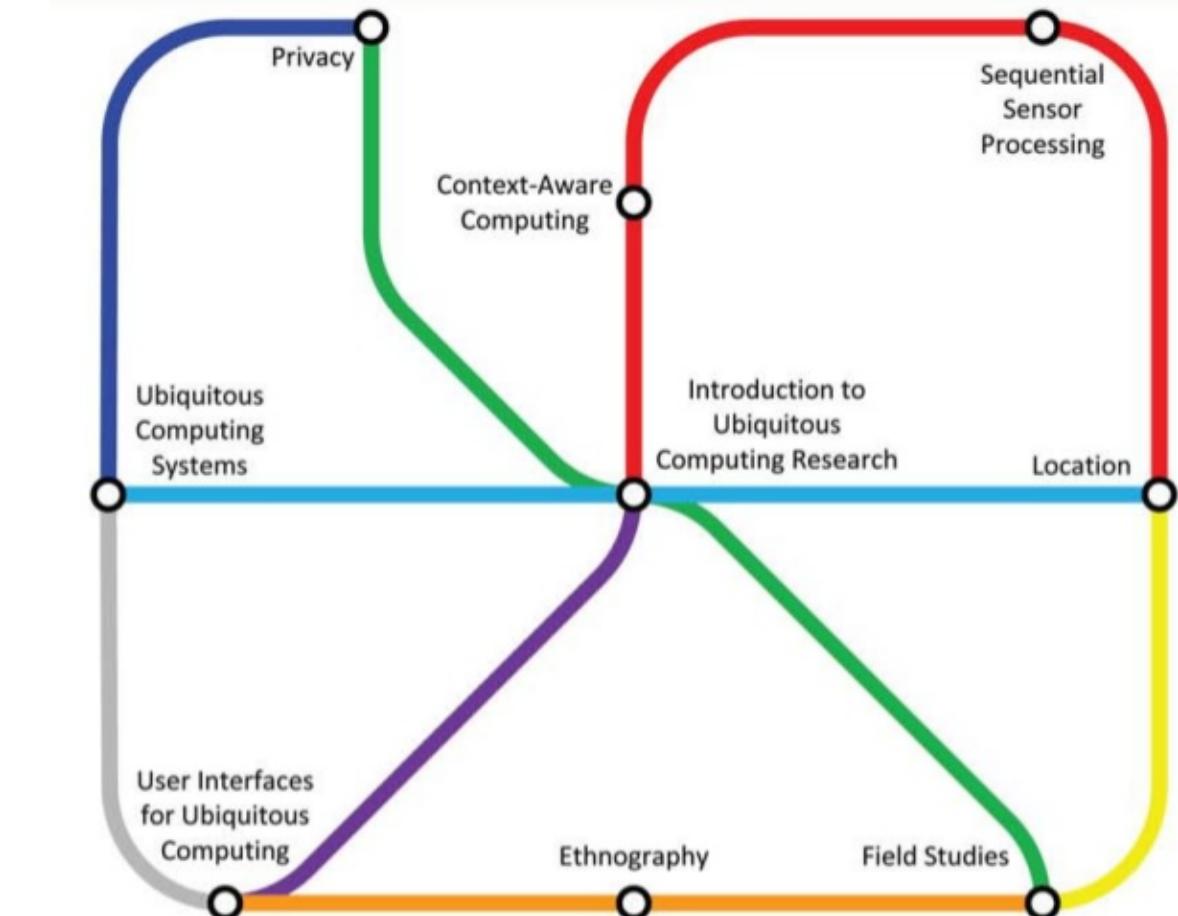


■ Particle Filter

- Generate Hypotheses
- Compute Weights
- Resample

- + general
- + continuous or discrete variables
- + great results
- lots of memory
- very slow

Ubiquitous Computing Fundamentals



Edited by
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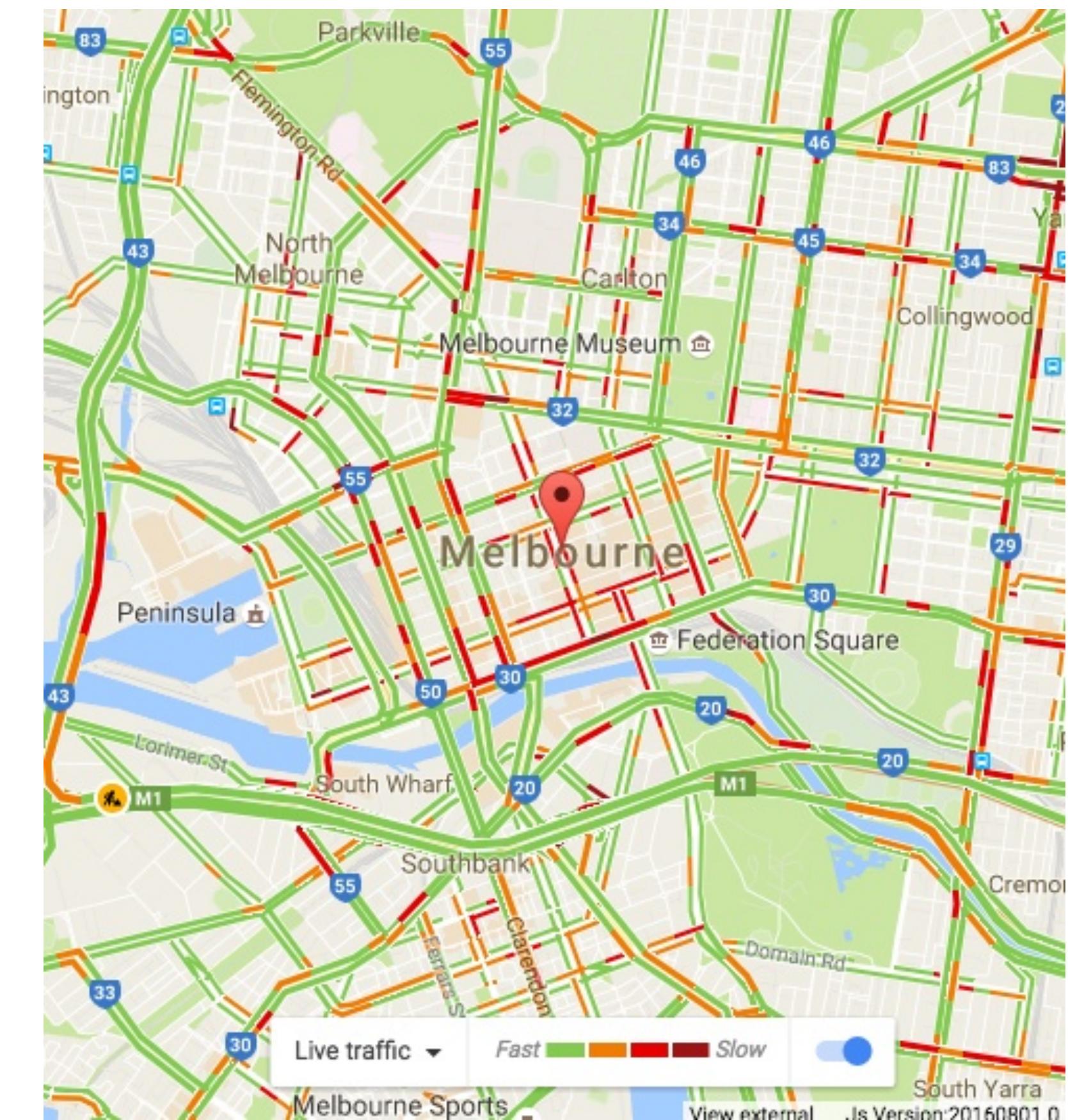
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A CHAPMAN & HALL BOOK

John Krumm's Chapter



Be good.

- Detailed movement profiles of citizens
- Communication data
 - Calls, duration, members, SMS, Email, calendar,...
- Optimising traffic flow
- Choice of public transport
- Personalised suggestions
 - Mode of transport
 - Travel start time
 - Destination



Movement Profiles

1. Sensors as a Driver for Ubiquitous Computing Technologies
2. What Constitutes a Sensor?
3. Challenges when Dealing with Sensor Data
4. Sensor Signal Processing: Dealing with these challenges

Summary