

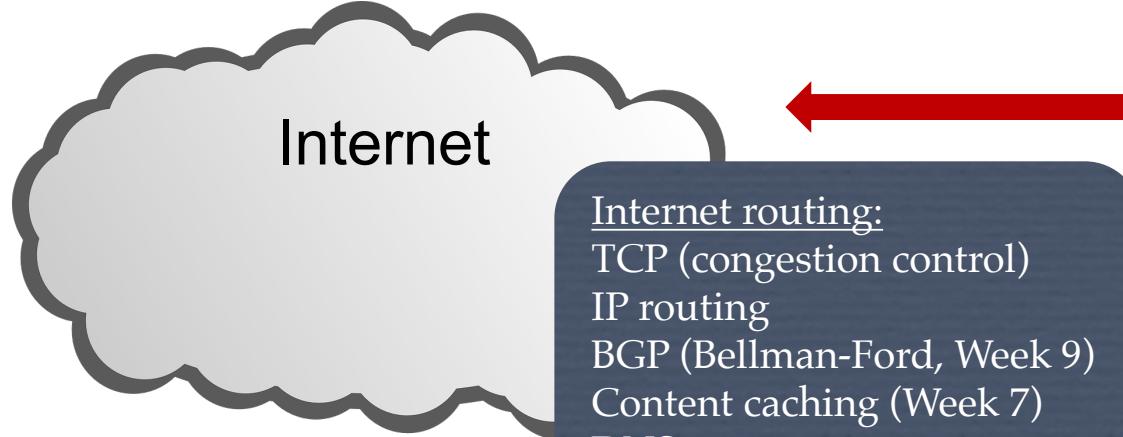
CS2040S

Data Structures and Algorithms

Welcome!

Algorithms Everywhere

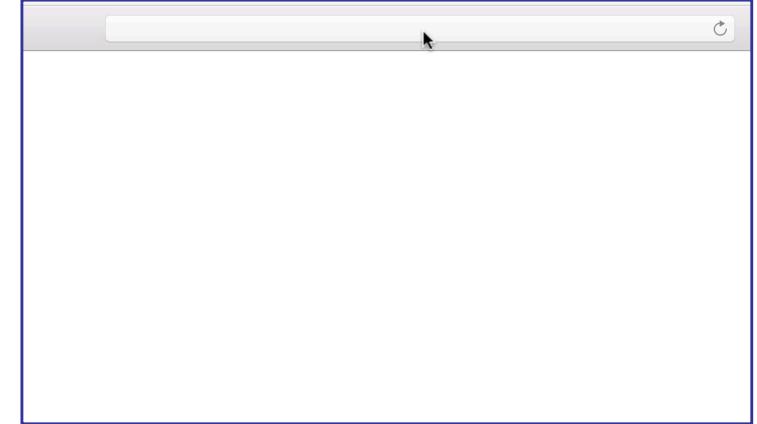
Web browser:
Parsing
Substring manipulation (Week 7)
XML trees (Week 5)



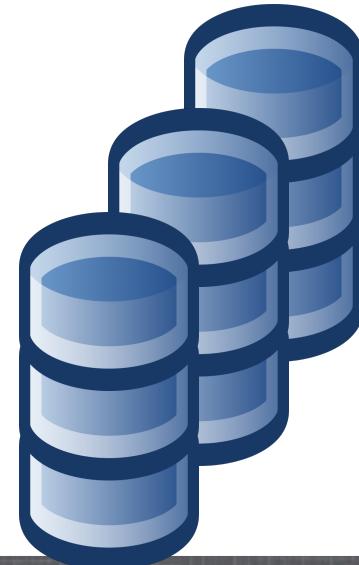
Internet routing:
TCP (congestion control)
IP routing
BGP (Bellman-Ford, Week 9)
Content caching (Week 7)
DNS



Web servers:
Load balancing (PS 2)
Scheduling (Week 8)
Memory allocation



Google:
PageRank
(Week 10)
String matching
(Week 7)



Database:
B-trees (Week 5)
Search (Week 2)
Sorting (Week 3)

Data Structures

Problem Solving

Algorithms

Algorithms

What is an *algorithm*?

- Set of instructions for solving a problem
 - "First, wash the tomatoes."
 - "Second, peel and cut the carrots."
 - "Third, mix the olive oil and vinegar."
 - "Finally, combine everything in a bowl."
- *Finite* sequence of steps
- Unambiguous (and precise)
- Designed to accomplish some task

Algorithms

History

- Named for al-Khwārizmī (780-850)
 - Persian mathematician
- Many ancient algorithms



Algorithms

History

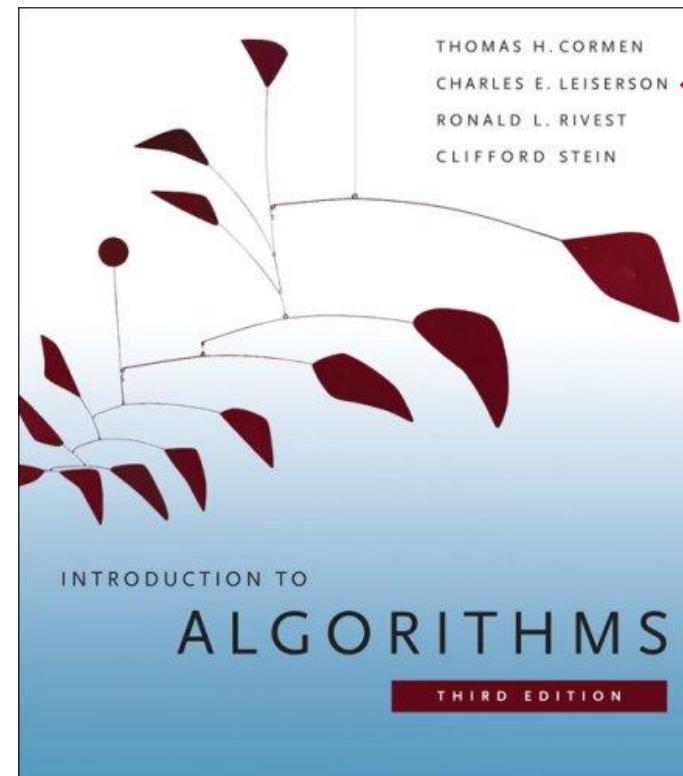
- Named for al-Khwārizmī (780-850)
 - Persian mathematician
- Many ancient algorithms
 - Multiplication: Rhind Papyrus
 - Babylon and Egypt: ~1800BC
 - Euclidean Algorithm: Elements
 - Greece: ~300BC
 - Sieve of Eratosthenes
 - Greece: ~200BC



What do we do in a class on algorithms?



Charles Leiserson
(MIT)



WHAT ARE YOUR GOALS?



BUILD USEFUL SYSTEMS FOR PEOPLE



Jeff Dean
(Google)



Ruchi Sanghvi
(Facebook)

BUILD FAST SYSTEMS

“If you need your software to run twice as fast, hire better programmers.

But if you need your software to run more than twice as fast, use a better **algorithm**.”

-- *Software Lead at Microsoft*

"Bad programmers worry about the code. Good programmers worry about *data structures and their relationships*."

- Linus Torvalds*



*Creator of git and the linux kernel (in Linux OS, Chrome OS, Android)

START A TECH COMPANY



THINK ABOUT BEAUTIFUL ALGORITHMS



Donald Knuth

``People who analyze algorithms have **double happiness**. First of all they experience the sheer beauty of elegant mathematical patterns that surround elegant computational procedures. Then they receive a practical payoff when their theories make it possible to get other jobs done more quickly and more economically.''

CHANGE THE WORLD

COMPUTER SCIENTISTS HAVE CHANGED THE WORLD...



...BY SOLVING PROBLEMS

CS2040S is about **solving problems.**

It prepares you for what lies ahead...

Search

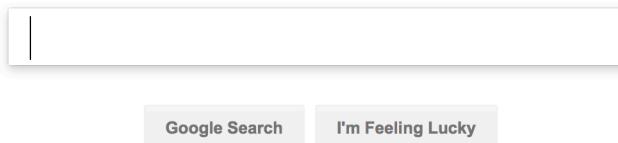
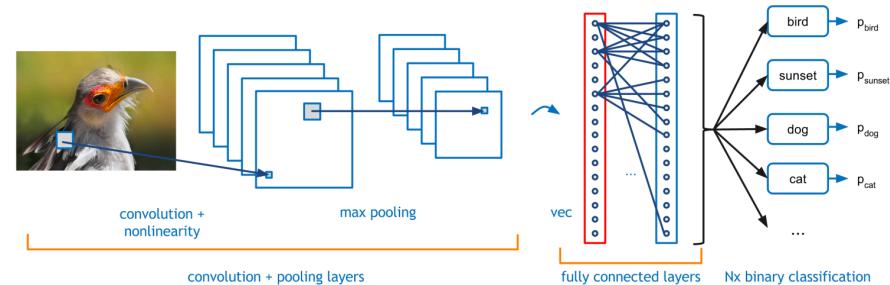


Image Recognition



WHAT ABOUT THE CODE?

WHAT ABOUT THE CODE?

CS2040S is about **solving problems** in Java.

Why Java?

*Language does not
really matter!*

- Good aspects:
 - Common in industry / real-world / web
 - Object-oriented in a deep way
 - Modularity / abstraction via OOP
 - Avoids memory leak issues of C/C++
- Less good aspects:
 - Performance (compare to: C++)
 - More mental overhead (compare to: Python)

WHAT ABOUT THE CODE?

CS2040S is about **solving problems** in Java.

CS2040S is not about learning Java.

CS2030

“If you need your software to run twice as fast,
hire better programmers.”

But if you need your software to run more than
twice as fast, use a better **algorithm.**”

-- *Software Lead at Microsoft*

CS2040S

Assumption:

- You are taking CS2030 this semester.
OR
- You already took CS2030 a previous semester.
OR
- You already are an expert Java programmer.
OR
- You plan to suffer teaching yourself Java.

WHAT ABOUT THE CODE?

CS2040S is about **solving problems** in Java.

CS2040S is not about learning Java.

We want you to be great programmers too!
Staff are here to help.

Always program using the best development environment you can!

CS2040s Recommended IDE: IntelliJ

The screenshot shows the official website for IntelliJ IDEA. At the top, there's a dark navigation bar with the "JET BRAINS" logo on the left and links for Tools, Languages, Solutions, Support, Company, Store, a user icon, and a search icon on the right. Below the navigation bar, the main title "IntelliJ IDEA" is displayed in a large, bold, black font. To the right of the title are links for What's New, Features, Learn, Buy, and a prominent blue "Download" button. A banner at the top features text about an upcoming webinar: "Upcoming Webinar: How We Built Comma, the Raku IDE, on the IntelliJ Platform" on Thursday, January 16, 2020, with a "Register" link and a close "X" button. The central part of the page has a large, stylized "IJ" logo followed by the text "IntelliJ IDEA" in a large, bold, black font. Below this, the tagline "Capable and Ergonomic IDE for JVM" is written in a smaller, black font. At the bottom, there are two calls-to-action: a black button with white text that says "DOWNLOAD" and another black button with white text that says "TAKE A TOUR". The background of the main content area features a dynamic, colorful geometric pattern of overlapping triangles in shades of blue, purple, pink, and white.

Introductions

Teaching Team

Seth Gilbert



Ben Leong



Soo Yuen Jien



Teaching Team

“Prof. Seth”



“Prof. Ben”



“Uncle Soo”



Teaching Team

“Prof. Seth”



“Prof. Ben”



“Uncle Soo”



What should I call you?

- If I mispronounce your name, please correct me.
- If the name you use is different than the one I have, please tell me.
- If I am addressing you incorrectly, let me know.

Teaching Team

Seth Gilbert



Ben Leong

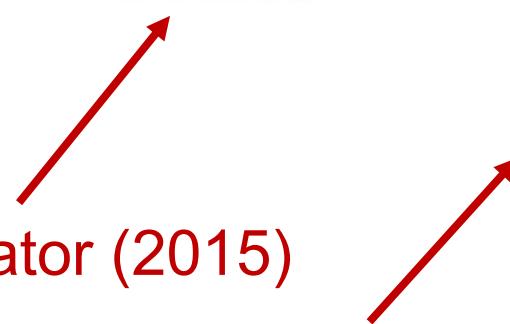


Soo Yuen Jien



NUS Outstanding Educator (2015)

NUS Outstanding Educator (2018)



Teaching Team

Seth Gilbert



Interests:

Algorithms

Distributed Algorithms

Parallel Algorithms

Optimization

Ben Leong



Interests:

Distributed Systems

Networking

Mobile Networks

SDN

Soo Yuen Jien



Interests:

Education Technology

Computer Architecture

Parallel Programming

Systems

Teaching Team

Seth Gilbert



Talk to me about:

*Curriculum questions
Algorithms questions
CS Puzzles*

Ben Leong



Talk to me about:

*Logistics issues
Tutorial scheduling
Coursemology
How to succeed in life*

Soo Yuen Jien



Talk to me about:

Everything else.

Teaching Staff

Tutors:

38 tutors

NUS undergrads

former CS2040 students

Teaching Assistants:

3 TAs

PhD students in CS

former CS2040 students

Administrative Details

WEEKLY SCHEDULE

2x Lectures @ UT-Aud2

- Monday: 4pm-6pm
- Thursday: 2pm-3:pm

1x Recitation

- 12+ slots (Tuesdays/Wednesdays)
- **Starts in Week 3**

1x Tutorial

- 35 slots (Thursdays/Fridays)
- **Starts in Week 3**

Administrative Details

Lectures:

- Two lectures:
 - Mon. 4pm-6pm
 - Thurs. 2pm-3pm
- Lecturer: me!
- Location: here! (UT-Aud2)

Webcast/slides:

- CIT is recording webcasts
- Slides posted after lecture

Let's hope for no technical difficulties!

Administrative Details

Recitations:

- One recitation: Tuesday/Wednesday (1 hours)
12-15 different sessions
- Size: ~35 students
- Goal: algorithm design and problem solving

Instructors:

- Prof. Ben, Uncle Soo, me...
- 3 Teaching Assistants

Administrative Details

Recitations:

- One recitation: Tuesday/Wednesday (1 hours)
12-15 different sessions
- Size: ~35 students
- Goal: algorithm design and problem solving

Register:

- Sign up on ModReg.
- Sessions start Week 3.

Administrative Details

Tutorials:

- One tutorial: Thursday/Friday (2 hours)
35 different sessions
- Size: ~15 students

Your tutor's job:

- Help you learn the material.
- Provide advice on how best to learn.
- Help you catch up if you fall behind.
- Challenge you if you are ahead.
- Show you neat exciting aspects of CS2040S.

*Tutorial Participation:
10% of your grade*

Administrative Details

Tutorials:

- One tutorial: Thursday/Friday (2 hours)
35 different sessions
- Size: ~15 students

How to sign up?

- Manual process. Messy process.
- Survey on Coursemology (this week).
- PLEASE be flexible.
- PLEASE be patient.
- Sessions start on Week 3.

WEEKLY SCHEDULE

2x Lectures @ UT-Aud2

- Monday: 4pm-6pm
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1x Recitation

- 12+ slots (Tuesdays/Wednesdays)
- **Starts in Week 3**

1x Tutorial

- 35 slots (Thursdays/Fridays)
- **Starts in Week 3**

Administrative Details

Midterm:

- March 9
- If you cannot make it, notify us *at least* two weeks in advance. (*Exception: illness.*)

Final Exam:

- Mon. May 4 (17:00) --- *check for updates.*

DROP DATES

Refer to Modreg: <http://www.nus.edu.sg/ModReg/>

Drop with:

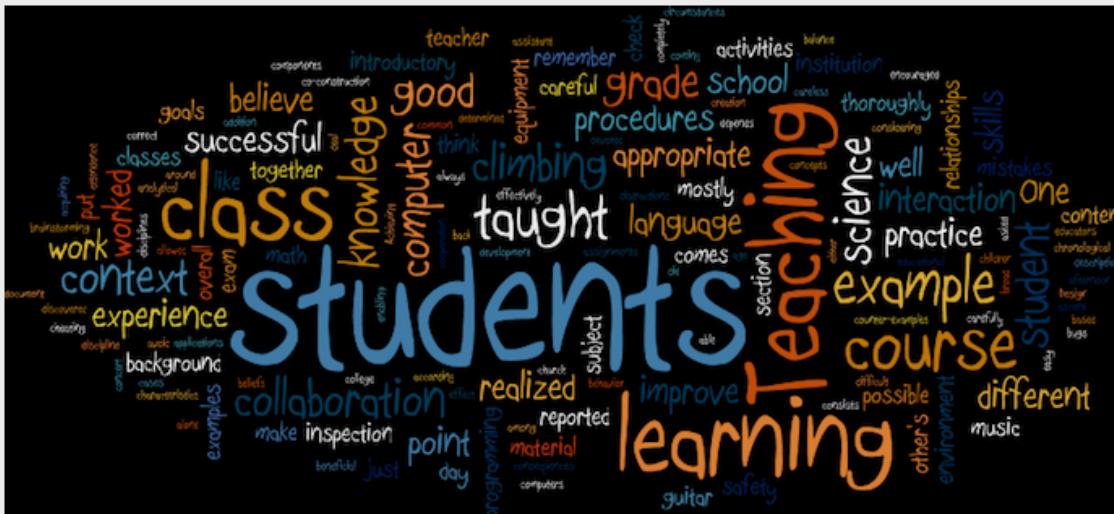
- **No record:** until **26/01/2020 11:59pm.**
- 'W' grade: **27/01/2020 00:00** through **01/03/2020 11:59pm.**
- 'F' grade: **02/03/2020 00:00** onwards.



coursemology

Gamified Online Education Platform:

Making your class a world of games in a universe of fun.



Name

Email

Password

Password confirmation

Sign up

✓ Engaging

Coursemology allows educators to add gamification elements, such as experience points, levels, achievements, to their classroom exercises and assignments.

The gamification elements of Coursemology motivate students to do assignments and trainings.

✓ General

It's built for all subjects. The gamification system of Coursemology doesn't make assumption on the course's subject.

Through Coursemology, any teacher who teaches any subject can turn his course excercises into a online game.

✓ Simple

It's built for all teachers. You don't need to have any programming knowledge to master the platform.

Coursemology is easy and intuitive to use for both teachers and students.

Coursemology

Platform for course management:

- Announcements
- Lecture slides
- Problem sets
- Feedback
- Discussion forum
- Etc.

Please check Coursemology,
and read your (Coursemology)
e-mail.

*Built here at NUS
by Prof. Ben and
his team!*

Replacement for LumiNUS/IVLE.

Coursemology

How do you join?

- If you are registered for the class, you have already received an invitation.
- If you are not registered for the class, you will receive an invitation when you do register.
- If you are auditing the class, e-mail us.

If something doesn't work... e-mail **Prof. Ben!**

Luminus

Two reasons to check Luminus:

- Webcast videos will show up on Luminus
- Grades will show up in Luminus grade book

How to be good at ~~anything~~ CS2040S?

Knowledge

Experience

Talent

Practice, practice, practice...

Problem Sets

Practice the techniques from class.

Find out what you do and do not understand.

Practice regularly, every week.

Problem Sets

Practice the techniques from class.

Find out what you do and do not understand.

Practice regularly, every week.

Problem set 1 is available on Coursemology.... now.

Problem Sets

Some problems may be hard.

Some problems may involve figuring something out that we haven't done in class!

Most problems will involve writing some Java code.

Your tutor is there to help!

*Warning:
A tutor is not a compiler.*

Problem Sets

Submit problem sets on Coursemology.

Late submissions:

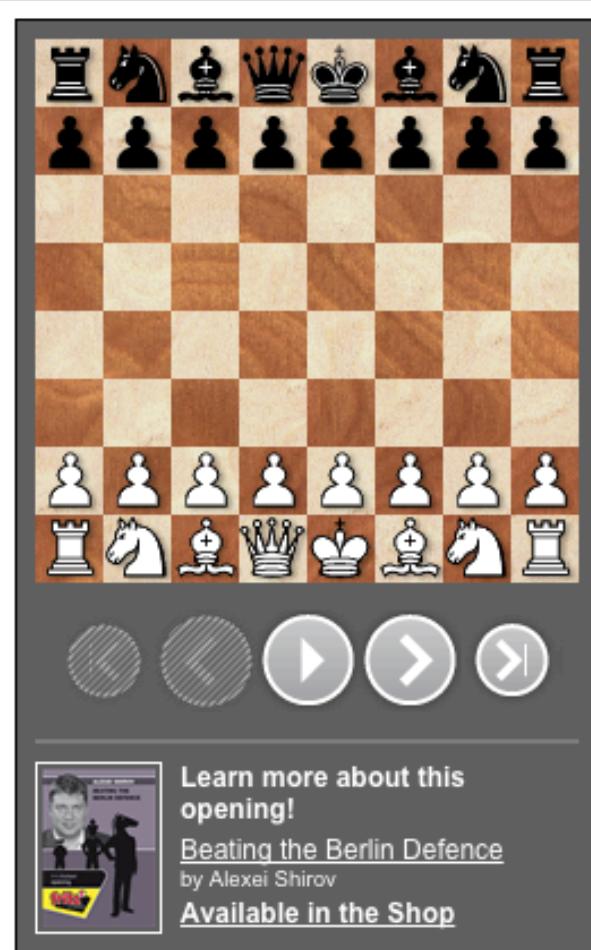
- 1 week: 25% penalty
- Last day of class: 50% penalty

Hand in problem sets on time!

Even if late, do them anyways!

Who here plays chess?

Rybka



Rybka (Computer) – Shredder (Computer) 1–0

C67 WCCC Pamplona Openclass (6) 13.05.2009

1.e4 e5 2.♘f3 ♘c6 3.♗b5 ♘f6 4.0-0 ♖xe4 5.♗e2 ♗g5 6.♗xg5
♗xg5 7.d4 ♖e7 8.dxe5 ♘d4 9.♗d3 ♖xe5 10.♗c3 ♗c5 11.♗d1 ♗e6
12.♗e1 ♖d4 13.♗f3 0-0 14.♗e4 ♖d6 15.♗h4 ♖e5 16.♗d2 f5 17.♗e1
♗f6 18.♗h3 ♖g6 19.♗d5 c6 20.♗xe6 ♖xe6 21.♗f4 ♖xa2 22.♗xh7
cx b5 23.g3 ♗f6 24.♗c3 ♗f7 25.♗h4 ♖a1+ 26.♗g2 ♖a6 27.♗xf6
♗xf6 28.♗h5+

1–0

[Download PGN](#)

Won four consecutive World Chess Championships (2007-2011).

Computer chess reels from 'biggest sporting scandal since Ben Johnson'

Czech mate, Mr Cheat

IT'S a story that has sent pawns and rooks spinning off chess boards across the world.

Rybka, the best chess-playing computer on the planet, is a cheat.

And its developer, Vassil Rajlich – one half of a couple dubbed the Posh and Becks of the game – has been shamed as a plagiarist, banned from competing, stripped of his titles and ordered to hand back his trophies and prize money.

Rajlich, himself an international master of the game, was found guilty by his peers of basically copying earlier chess programs when creating Rybka.

A 14-member panel found the 40-year-old Czech from Ohio, but now living in Hungary, plagiarised two other programs, Crafty and Frost. Their report states: 'Not a single panel member believed him innocent. Vassil Rajlich's claims of complete originality are contrary to the facts.'

Not since IBM's Deep Blue computer defeated grand master Gary Kasparov in 1997 – and was subsequently accused of cheating – has the world of computer chess been in such sprout. Rybka won

By Tariq Tahir

the International Computer Games Association world championship from 2000 to 2010.

Peter Doggers, from online site Chess Vibes, said: 'The impact in the computer chess world must be comparable to arguably the most famous example of doping in athletics – the positive drug testing of Canadian sprinter Ben Johnson.'

For his part, Rajlich has not commented, save an email sent to the association in which he disputed Rybka included code written by others.

He never made grand master as a player so turned to programming. 'I figured there were about 2,000 people in the world stronger than me in chess,' he once said. 'But not one chess player that was stronger than me in programming.'

By 2005, Rybka – Czech for 'little fish' – was ready. The chief tester is his wife, Iweta, herself an international master. David Levy, president of the ICGA, said: 'We are convinced the evidence against Rajlich is both overwhelming in its volume and beyond reasonable question in its nature.'



**Posh and
cheats:**
Vassil
Rajlich
and his
chief
tester,
wife
Iweta

Disqualified!

Titles revoked!

Arguments against:

- Relied on code from Crafty and Fruit.
- Did not meet the "originality" rules for the tournament.

Arguments for:

- It was much, much better than Crafty, Fruit, or any existing chess player!

Friday, July 1, 2011 **MIKE** 

Computer chess reels from 'biggest sporting scandal since Ben Johnson'

Czech mate, Mr Cheat

By Tariq Tahir

The International Computer Games Association world championship from 2000 to 2010

Peter Doggers' chess online site

Chess.com's website

The impact in the computer chess world must be

comparable to arguably the most

controversial moment in all

leaves a positive shadow of

Canadian sprinter Ben Johnson.

For his part, Rallich has not com-

mented on the accusations or the

suspicion in which he disputed Ryba-

ka's claimed originality.

A Malaysian named David Levy found the

40-year-old Czech from Ohio, but

now living in Hungary, plagiarized

two other programs, Crafty and

Fruit. They were stunned. Not a

single panel member believed him

innocent. Vassil Rallich's claims of

originality originally are contrary

to the facts.

Not since IBM's Deep Blue com-

puter defeated grand master Garry

Kasparov in 1997 has anyone sub-

sequently accused of cheating —

has the world of computer chess

been in such sprit. Ryba was



Posh and
checks:
Vassil
Rallich
and his
chief
taster,
wife
Beata

Problem Sets

Collaboration Policy

- Working together is strongly encouraged!
- You must write/code your problems sets alone.
- Cheating / plagiarism will be dealt with harshly.

WHAT ARE YOUR GOALS?

- Learn something.
- Become a better person.
- Position yourself to succeed after graduation.
- *Get a good grade on a problem set in CS2040S??*



WHY DID YOU CHEAT?

Computer chess reels from 'biggest sporting scandal since Ben Johnson'

Czech mate, Mr Cheat

By Tariq Tahir

IT'S a story that has sent pawns and rooks flying in chess clubs and arenas across the world.

Rybka, the best chess-playing computer on the planet, is a cheater. And its creator, Vassik Rajlich – author of a now-deleted Poch and Reeks of game database – has been shamed as a plagiarist, banned from competing, stripped of his titles and ordered to hand back his £100,000 prize money.

Rajlich, himself an emeritusial master of the game, was found guilty by his peers of basically copying and pasting programs when creating Rybka.

A 14-member panel found the 40-year-old Czech from Olomouc, but now living in Hungary, plagiarised two other programs, Crafty and Fine. The panel's report said the single panel member believed him innocent. Vassik Rajlich's claims of complete originality are contrary to the facts.

When IBM's Deep Blue computer defeated grand master Garry Kasparov in 1997 – and was subsequently accused of cheating – the world of computing was shocked at such a spate. Rybka will



Poch and checks: Vassik Rajlich and his chess tester, wife Irina

the International Computer Games Association world championship from 2003 to 2010.

Poch, Rajlich's front online site ChessVise.com. The impact in the computer chess world must be comparable to arguably the most famous example of doping in athletics – the positive drug testing of US athlete Marion Jones.

For his part, Rajlich has not commented, save an email sent to the association in which he disputed Rybka's case and wrote by others.

He never made Rybka into a player so naïve as programming. "I figured there were about 2,000 people in the world stronger than me myself," he once said, "but not necessarily as good programmers as me or as strong."

By 2005, Rybka – "Czech for 'little fish'" – was ready. The chief architect is his friend, Israeli international master David Levy, president of the ICGA, said. "We are convinced the evidence against Rajlich is both overwhelming in as solid and beyond reasonable question in its nature."

WHY DID YOU CHEAT?

- I thought I was going to fail the class!

If you put in the time, you will not fail the class.

Friday July 1, 2011 METRO

Computer chess reels from 'biggest sporting scandal since Ben Johnson'

Czech mate, Mr Cheat

IT'S a story that has sent pawns and rooks flying in chess clubs and tournaments across the world.

Rybka, the best chess-playing computer on the planet, is a cheat. And its creator, Vassik Rajlich – author of a now-deleted Poch and Reeks of the game – has been shamed as a plagiarist, banned from competing, stripped of his titles and ordered to hand back his £100,000 prize money.

Rajlich, himself an emeritus master of the game, was found guilty by his peers of basically copying and then reprogramming

A 14-member panel found the 40-year-old Czech from Olomouc, but now living in Hungary, plagiarised two other programs, Crafty and Frost. The panel's report said the single panel member believed him innocent. Vassik Rajlich's claims of complete originality are contrary to the facts.

In 2005, IBM's Deep Blue computer defeated grand master Garry Kasparov in 1997 – and was subsequently accused of cheating – in a world of computers that have beaten us such splice. Rybka won

by Tariq Tahir

the International Computer Games Association world championship from 2003 to 2010.

Poch (left) from online site ChessVid.com. The impact in the computer chess world must be comparable to arguably the most famous example of doping in athletics – the positive drug testing of

Ben Johnson at the 1988 Seoul Olympics.

For his part, Rajlich has not commented, save an email sent to the association in which he disputed Rybka's claim and wrote by others.

He never made a claim to be a player so novice as programming.

I figured there were about 2,000 people in the world stronger than me in chess," he once said, "but not necessarily as good as me or stronger than me in programming."

By 2005, Rybka – "Czech for 'little fish'" – was ready. The chief architect was Vassik Rajlich, a British international master David Levy, president of the ICGA, said. "We are convinced the evidence against Rajlich is both overwhelming in as well as beyond reasonable

suspicion in its nature."



Poch and checks: Vassik Rajlich and his chess tester, wife Irina

If you cheat, you will learn less, and likely do worse in the end.

WHY DID YOU CHEAT?

- I'm not smart enough...
- Everyone else is smarter than I am...

You are smart enough; but you need to keep practicing, keep working at it.

Friday July 1, 2011 METRO

Computer chess reels from 'biggest sporting scandal since Ben Johnson'

Czech mate, Mr Cheat

IT'S a story that has sent pawns and rooks flying in chess clubs and tournaments across the world.

Rybka, the best chess-playing computer on the planet, is a cheat. And its creator, Vlastimil Rajlich – a man of a very dubious past, with Poch and Becks of a game delayed – has been shamed as a plagiarist, banned from competing, stripped of his titles and ordered to hand back his £100,000 prize money.

Rajlich, himself an emeritus master of the game, was found guilty by his peers of basically copying and then reprogramming

A 14-member panel found the 40-year-old Czech from Olomouc, but now living in Hungary, plagiarised two other programs, Crafty and Fine. The panel's report said the single panel member believed him innocent. Vlastim Rajlich's claims of complete originality are contrary to the facts.

In 1997, IBM's Deep Blue computer defeated grand master Garry Kasparov – and was subsequently accused of cheating – as was a host of computers before and since. Rybka was

By Tariq Tahir

the International Computer Games Association world championship from 2003 to 2010.

Poch, Becks, from online site ChessVid.com. The impact in the computer chess world must be comparable to arguably the most famous example of doping in athletics – the positive drug testing of

For his part, Rajlich has not commented, save an email sent to the association in which he disputed Rybka's claim that he was "written by others".

He never made a claim to be a player so novice as programming. "I figured there were about 2,000 people in the world stronger than me in chess," he once said, "but not necessarily as good programmers as me in programming."

By 2005, Rybka – "Czech for 'little fish'" – was ready. The chief suspect in the case is British international master David Levy, president of the ICGA, said. "We are convinced the evidence against Rajlich is both overwhelming, in as solid and beyond reasonable question in its nature."



Poch and
checkmate:
Vlastimil
Rajlich
and his
cheat,
wife
Iveta

WHY DID YOU CHEAT?

- I thought I was going to fail the class! *You won't (unless you cheat).*
- Everyone else is cheating! *No, they aren't.*

Friday July 1, 2011 METRO

Computer chess reels from 'biggest sporting scandal since Ben Johnson'

Czech mate, Mr Cheat

IT'S a story that has sent pawns and rooks flying in chess clubs across the world.

Rybka, the best chess-playing computer on the planet, is a cheater. And its creator, Vassik Rajlich – author of a now-deleted Poch and Becks of the game – has been shamed as a plagiarist, banned from competing, stripped of his titles and ordered to hand back his £100,000 prize money.

Rajlich, himself an emeritus master of the game, was found guilty by his peers of basically copying and then programs

when creating Rybka.

A 14-member panel found the 40-year-old Czech from Olomouc, now living in Hungary, plagiarised two other programs, Crafty and Frost. The only member who believed him innocent, Vassik Rajlich's claims of complete originality are contrary to the facts.

When IBM's Deep Blue computer defeated grand master Garry Kasparov in 1997 – and was subsequently accused of cheating – it was a world of controversy, but not quite on such a scale. Rybka was

By Tariq Tahir

the International Computer Games Association world championship from 2003 to 2010.

Poch (left) from online site ChessVid.com. The impact in the computer chess world must be comparable to arguably the most famous example of doping in athletics – the positive drug testing of

Ben Johnson at the 1988 Seoul Olympics.

For his part, Rajlich has not com-

mented, save an email sent to the asso-

ciation in which he disputed Rybka's claim and was rebuked by others.

He never made a good chess

player so turned to programming. I figured there were about 2,000 people in the world stronger than me in chess," he once said, "but not many more than me in chess and stronger than me in programming."

By 2005, Rybka – "Czech for 'little fish'" – was ready. The chief architect was Rajlich, a former international master. David Levy, president of the ICGA, said: "We are convinced the evidence against Rajlich is both overwhelming as well as solid beyond reasonable

doubt in its nature."



Poch and
cheeks:
Vassik
Rajlich
and his
cheat,
wife
Irina

WHY DID YOU CHEAT?

- I thought I was going to fail the class! *You won't (unless you cheat).*
- Everyone else is cheating! *No, they aren't.*
- It wasn't really cheating... *The rules are the rules.*

Friday July 1, 2011 METRO

Computer chess reels from 'biggest sporting scandal since Ben Johnson'

Czech mate, Mr Cheat

IT'S a story that has sent pawns and rooks into all sorts of alehouse across the world.

Rybka, the best chess-playing computer on the planet, is a cheater. And its creator, Vassik Rajlich – author of a now deleted Poch and Reeks of the game – has been shamed as a plagiarist, banned from competing, stripped of his titles and ordered to hand back his £100,000 prize money.

Rajlich, himself an emeritus master of the game, was found guilty by his peers of basically copying and then programs when creating Rybka.

A 14-member panel found the 40-year-old Czech from Olomouc, but now living in Hungary, plagiarised two other programs, Crafty and Frost. The panel's only dissenting single panel member believed him innocent. Vassik Rajlich's claims of complete originality are contrary to the facts.

In 1997, IBM's Deep Blue computer defeated grand master Garry Kasparov in 1997 – and was subsequently accused of cheating – however, a world of computer chess has moved beyond reasonable suspicion in its nature.

By Tariq Tahir

the International Computer Games Association world championship from 2003 to 2010.

Poch (left) from online site ChessVid.com. The impact in the computer chess world must be comparable to arguably the most famous example of doping in athletics – the positive drug testing of Marion Jones.

For his part, Rajlich has not commented, save an email sent to the association in which he disputed Rybka's claim to have written by others.

He never made a claim to be a player so novice as programming. I figured there were about 2,000 people in the world stronger than me in chess," he once said. "but not necessarily more intelligent or stronger than me in programming."

By 2005, Rybka – "Czech for 'little fish'" – was ready. The chief architect was Rajlich, but American international master David Levy, president of the ICGA, said: "We are convinced the evidence against Rajlich is both overwhelming as is possible and beyond reasonable suspicion in its nature."



Poch and chess
Vassik
Rajlich
and his
cheat
tester,
wife
Irina

WHAT ARE YOUR GOALS?

- Learn something.
- Become a better person.
- Position yourself to succeed after graduation.



Where can I get help?

Your tutor!

Discussion Forums

Coursemology forums:

- Lectures
- Problem Sets
- Java
- Recitations & Tutorials
- and more....

Ask questions on Coursemology

(Don't e-mail unless it is private.)

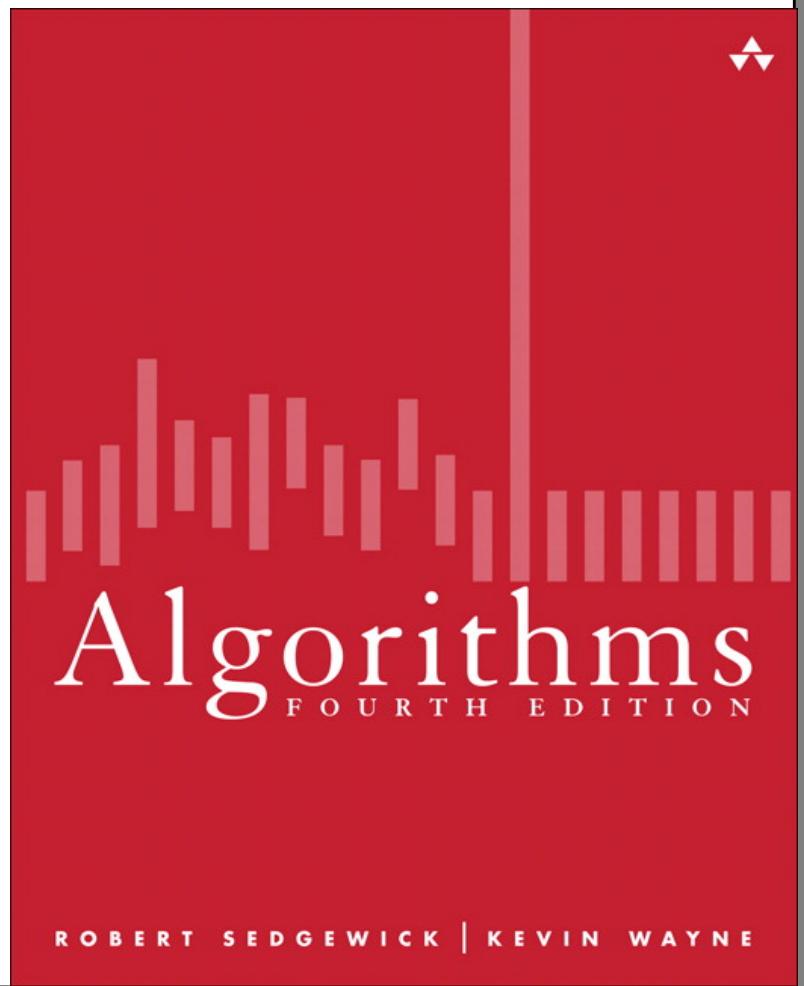
Other questions

Options:

- Chat with me after lecture.
- Talk after recitation (with instructor).
- Schedule an appointment with me.

Textbook: Algorithms

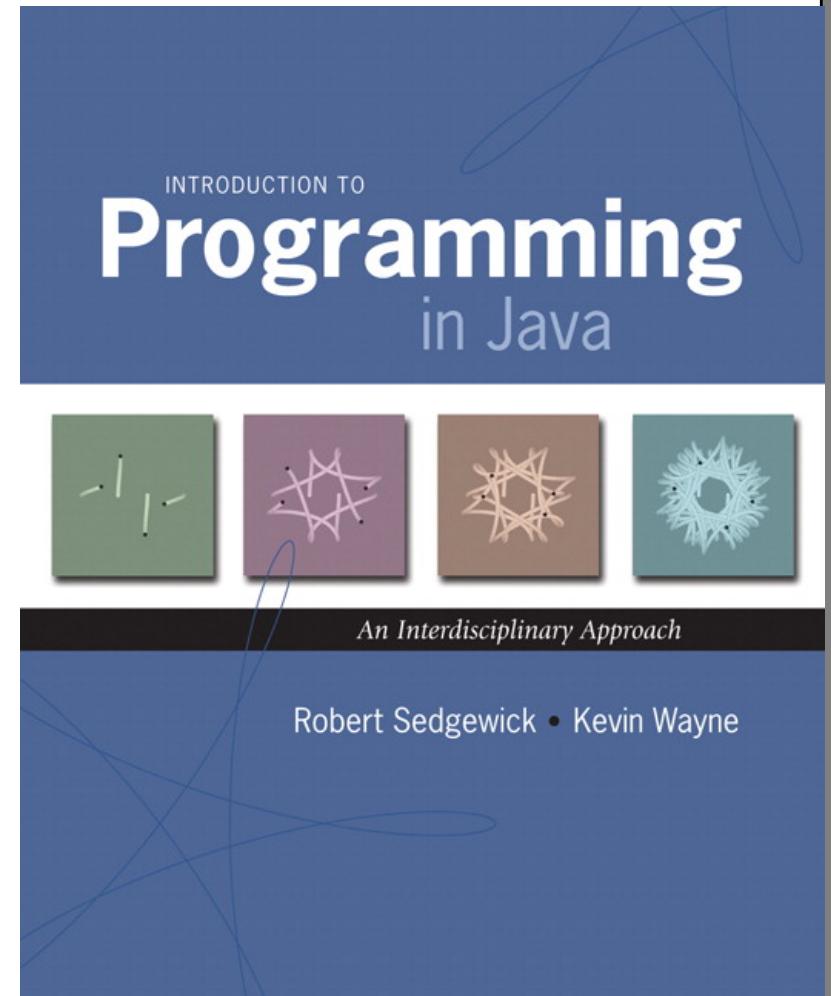
Robert Sedgewick and Kevin Wayne



Optional:

Introduction to Programming in Java

Robert Sedgewick and Kevin Wayne



VISUALGO.NET

The screenshot shows the homepage of VISUALGO.NET. At the top, there's a navigation bar with links for 'Training', 'Translation', and 'Login'. Below the navigation is the main title 'VISUALGO .NET/EN' followed by the subtitle 'visualising data structures and algorithms through animation'. A search bar is present. To the right, there's a book cover for 'Competitive Programming 3' and a 'Buy Now!' button on Lulu.com.

Do You Know? (Next Random Tip)

Search the term 'algorithm visualization' in your favorite Search Engine, do you see VisuAlgo in the first page of the search result :)? Next level: Search that term again, but in your native language (if it is not English). Is VisuAlgo still listed in the first page? :). And get ready to be surprised: Search the name of your favorite data structure or algorithm without mentioning the keyword 'animation' or 'visualization'. Is VisuAlgo still listed in the first page? :) .

Sorting (Training)

array, algorithm, bubble, select

Bitmask (Training)

bit manipulation, set, cs3233

Linked List (Training)

stack, queue, doubly, deque

Stress?

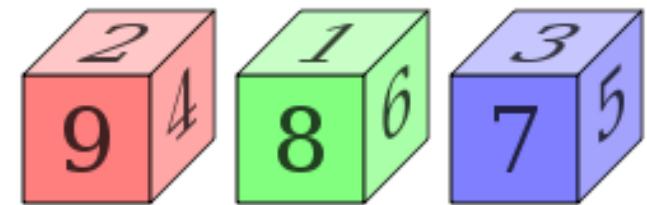
If stress is getting high:

- Chat with University Counselling Services.
- They have lots of good advice on stress management, organization, how to achieve your goals!

Puzzle of the Week

Imagine three dice:

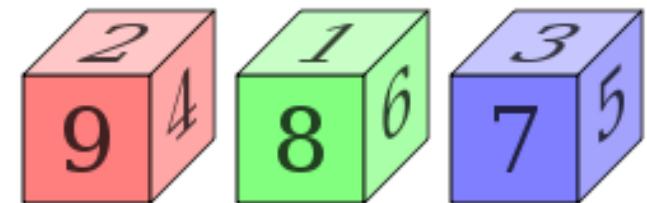
- A has six sides: 2, 2, 4, 4, 9, 9
- B has six sides: 1, 1, 6, 6, 8, 8
- C has six sides: 3, 3, 5, 5, 7, 7



Puzzle of the Week

Imagine three dice:

- A has six sides: 2, 2, 4, 4, 9, 9
- B has six sides: 1, 1, 6, 6, 8, 8
- C has six sides: 3, 3, 5, 5, 7, 7



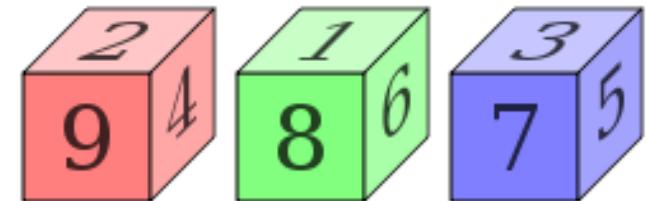
Game:

- Alice chooses a die.
- Bob chooses a die.
- Alice and Bob both roll.
- The higher value wins.

Puzzle of the Week

Imagine three dice:

- A has six sides: 2, 2, 4, 4, 9, 9
- B has six sides: 1, 1, 6, 6, 8, 8
- C has six sides: 3, 3, 5, 5, 7, 7



Game:

- Alice chooses a die.
- Bob chooses a die.
- Alice and Bob both roll.
- The higher value wins.

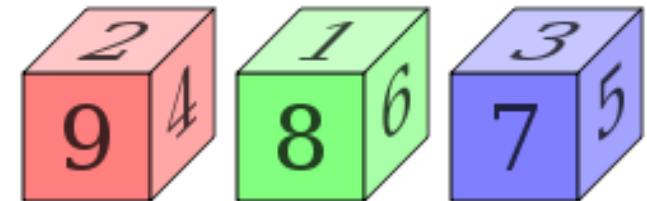
Questions:

- Which die should Alice choose?
- Which die should Bob choose?
- Who is more likely to win?

Puzzle of the Week

Imagine three dice:

- A has six sides: 2, 2, 4, 4, 9, 9
- B has six sides: 1, 1, 6, 6, 8, 8
- C has six sides: 3, 3, 5, 5, 7, 7



Game:

- Alice chooses a die.
- Bob chooses a die.
- Alice and Bob both roll.
- The higher value wins.

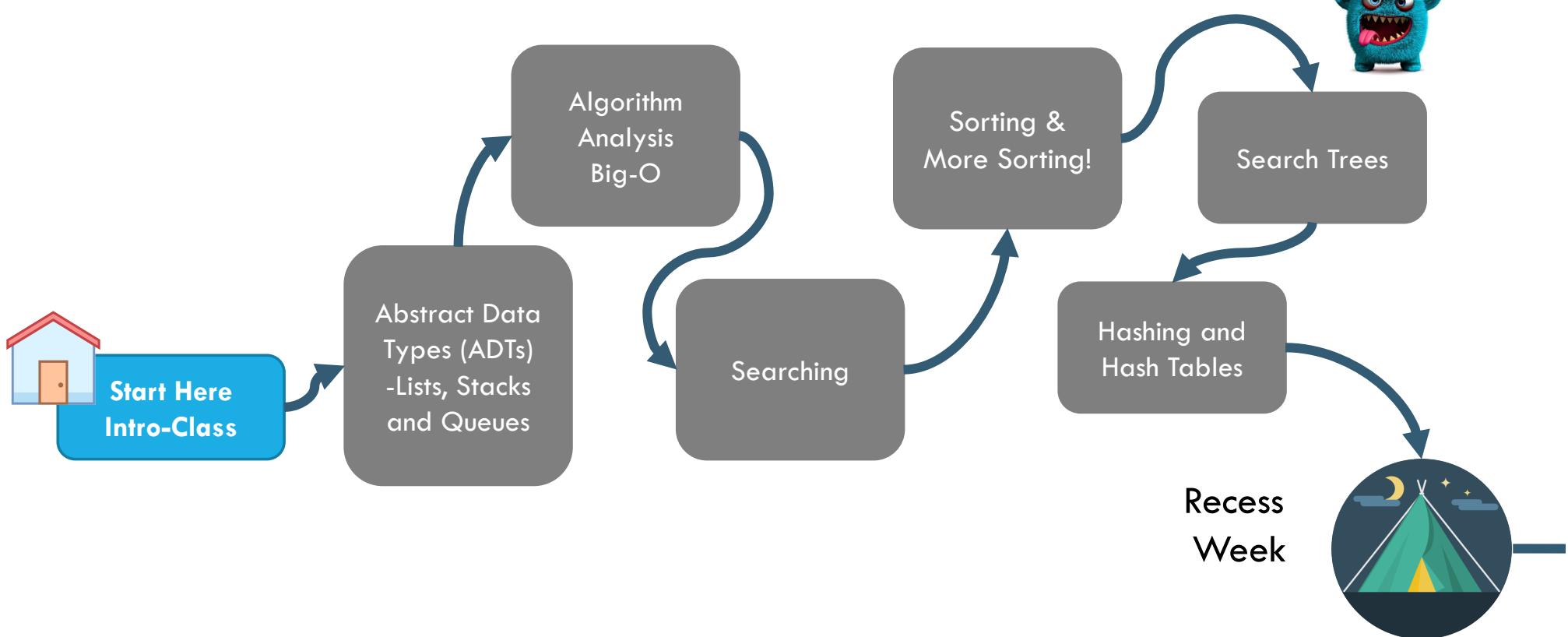
Questions:

- Which die should Alice choose?
- Which die should Bob choose?
- Who is more likely to win?

What is CS2040S about?

COURSE STRUCTURE

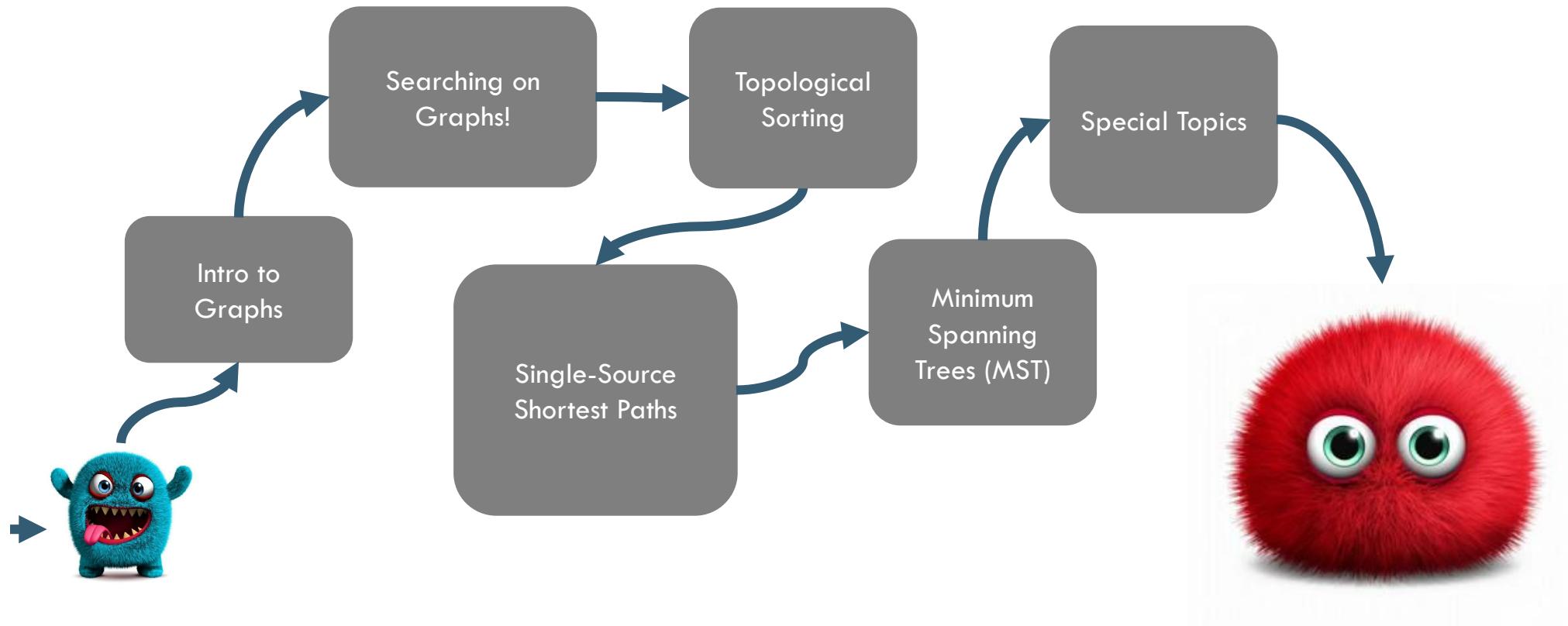
DRAFT



PART I: ORGANIZING YOUR DATA

DRAFT

COURSE STRUCTURE



PART II: MODELLING AND SOLVING PROBLEMS

Desirable features of your algorithm:

Correct

Fast

Modular

Easy to understand

Privacy preserving

Efficient

Trade Offs

Easy to maintain

Parallel

Fair

Cache efficient

Elegant

Small Memory

Secure

Desirable features of your algorithm:

Correct

Fast

Modular

Easy to understand

Privacy preserving

Efficient

Trade Offs

Easy to maintain

Fair

Cache efficient

Elegant

Small Memory

Parallel

Secure

How do you choose the right
algorithm for the right problem?

How do you design new
algorithms for new problems?

Algorithms

Goals of this course:

- How to organize and manipulate data?
 - Efficiency
 - Time: *How long does it take?*
 - Space: *How much memory? How much disk?*
 - Others: Energy, parallelism, etc.
 - Scalability
 - Inputs are *large* : e.g., the internet.
 - Bigger problems consume more resources.
- Solve real (fun!) problems

FRAMEWORK: ALGORITHM & DATA STRUCTURE

What problem does it solve?

How does it work?

How to implement it?

What is its asymptotic performance?

What is its real world performance?

What are the trade-offs?



GOALS

By the end of this course, you should be able to:

- **Apply algorithmic thinking and techniques** for solving computational problems.
- **Describe the structure and operation** of different **data structures and algorithms** under the standard computational model.
- **Assess the suitability** of different data-structures and algorithms for a specific computational problem.
- **Adapt existing data-structures and algorithms** to solve specific computational problems.

A little algorithmic thinking...

Searching

Finding a big item.
Finding many big items.
Searching an array.
Searching faster?

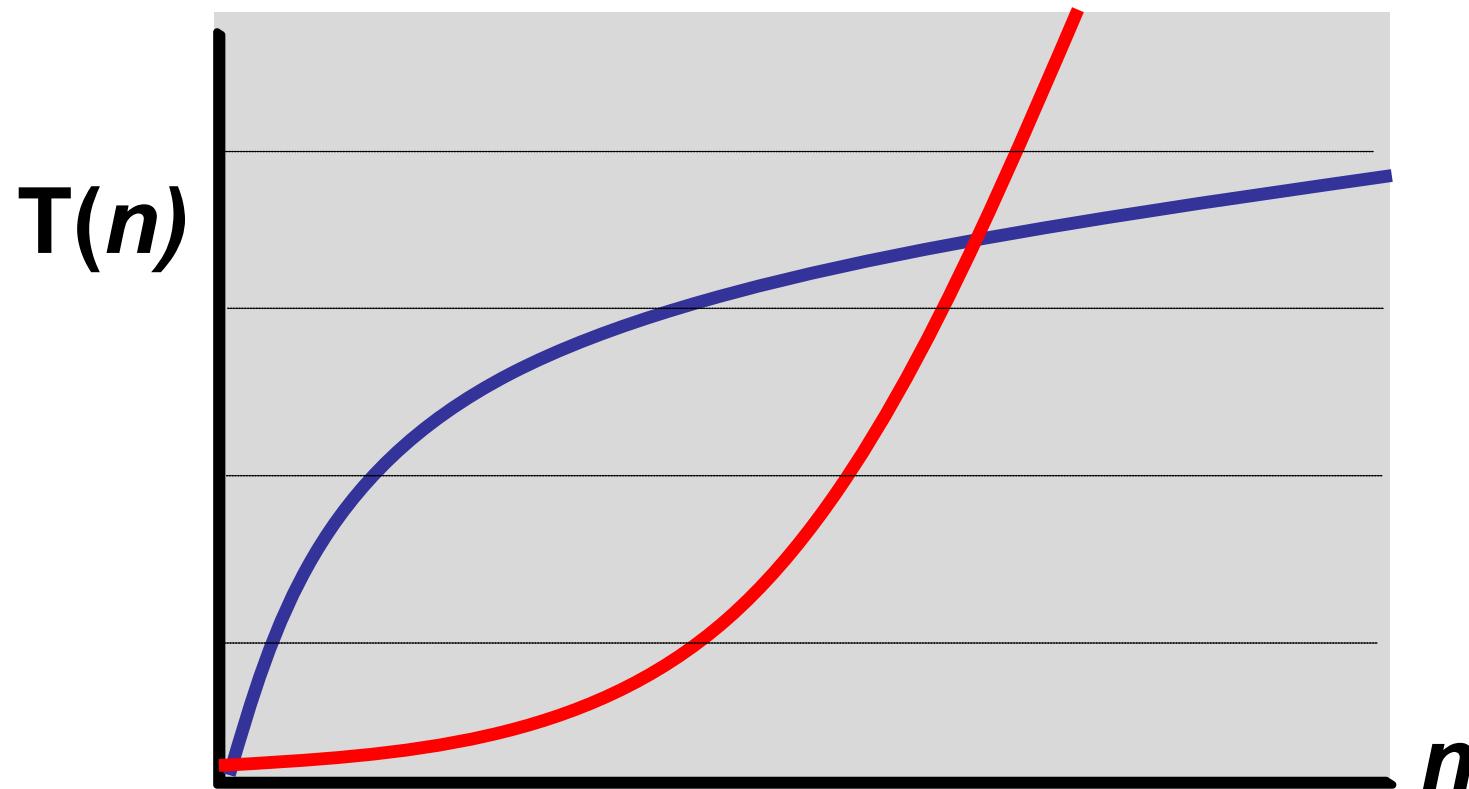
Similarity Test

Comparing two texts
An algorithm
Performance profiling
Fixing a few mistakes

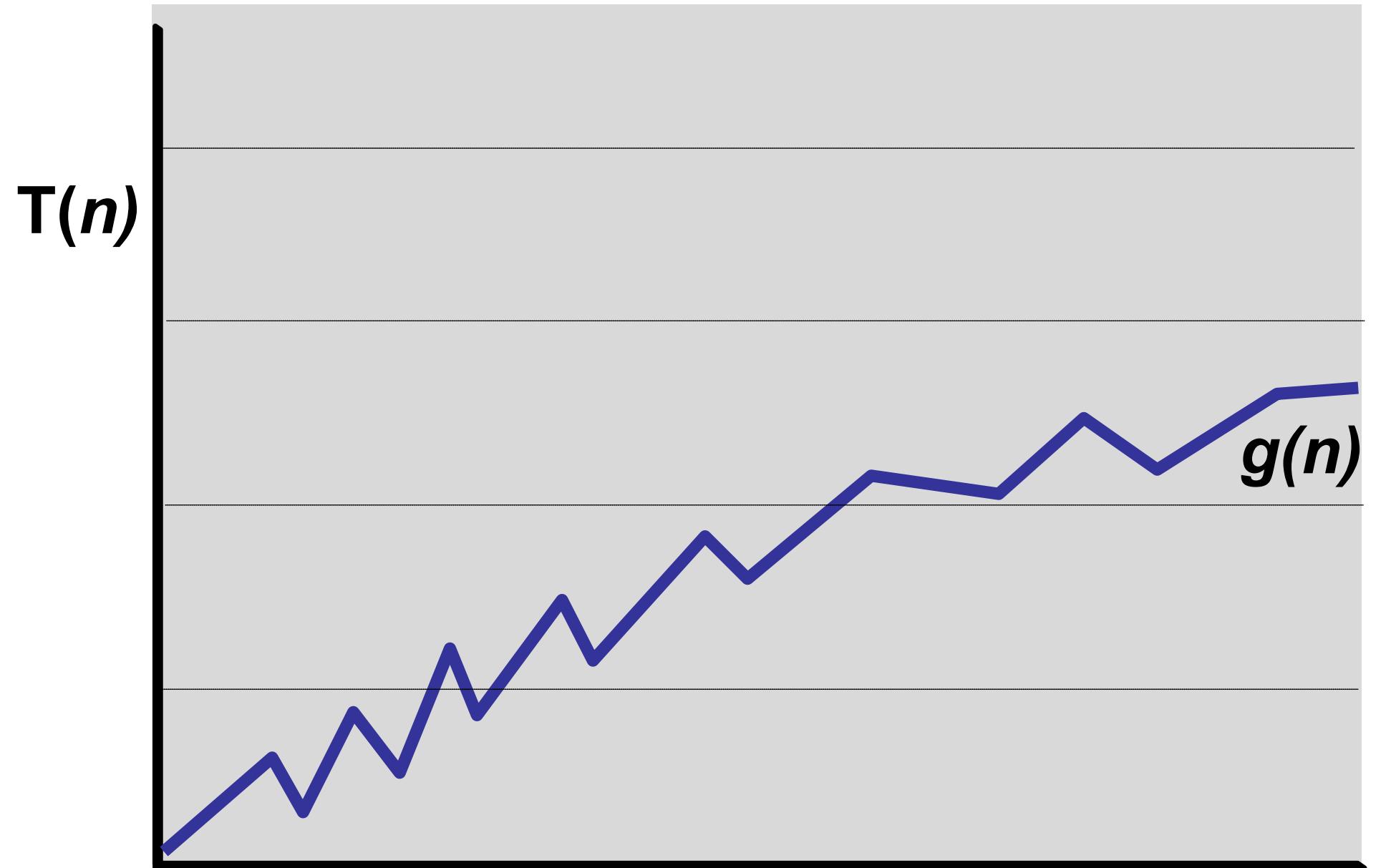
Big-O Notation

How does an algorithm scale?

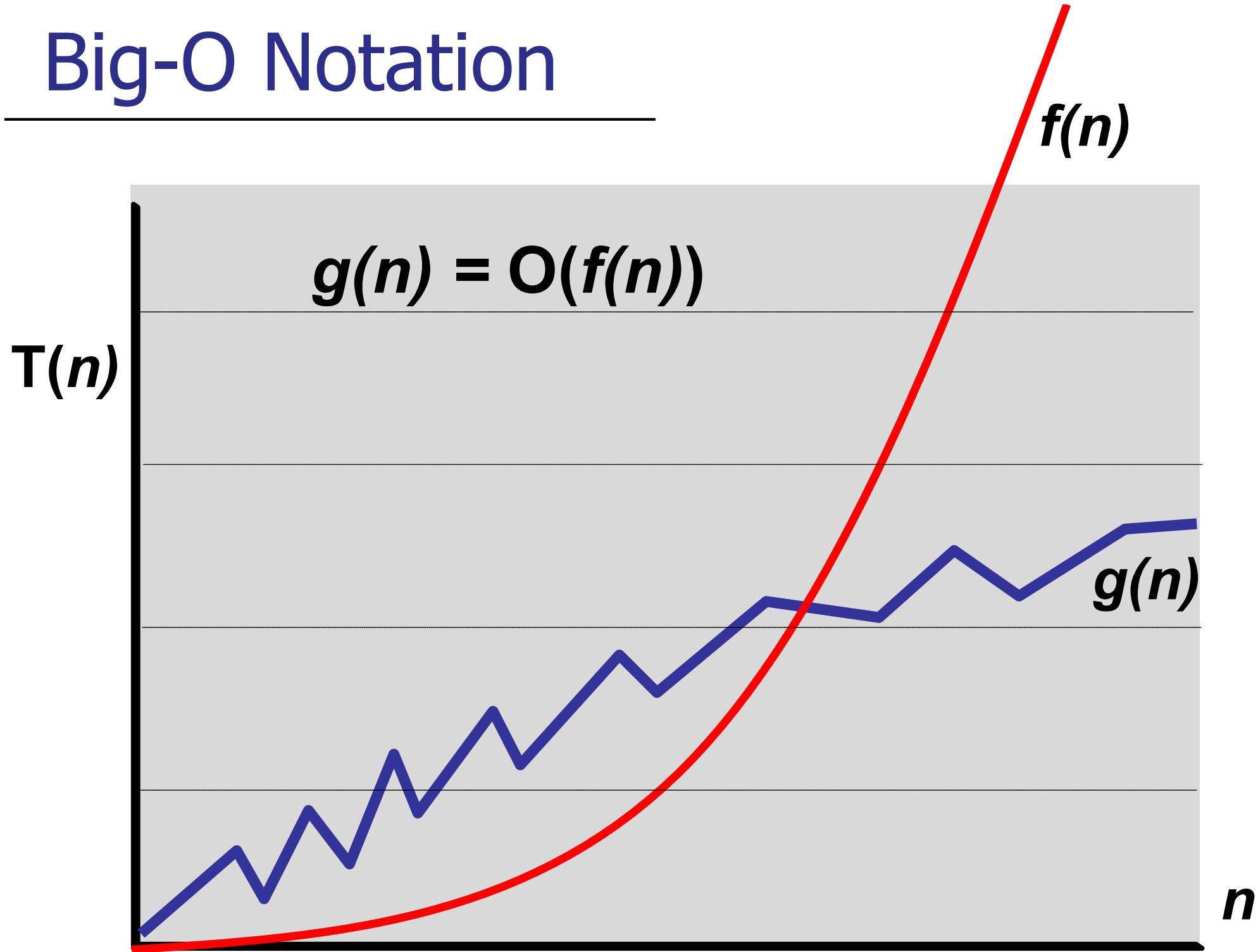
- For large inputs, what is the running time?
- $T(n)$ = running time on inputs of size n



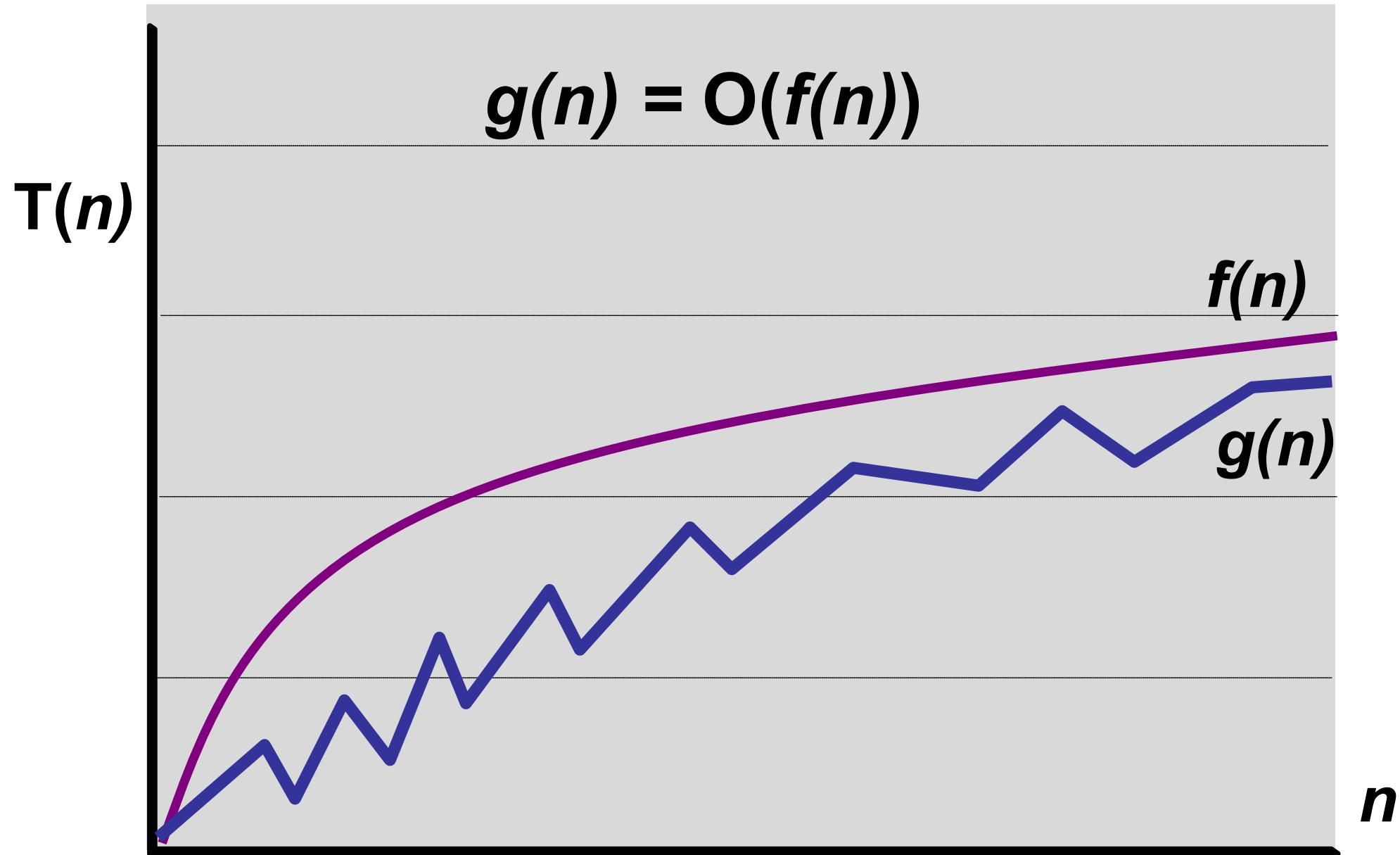
Big-O Notation



Big-O Notation



Big-O Notation



Example

$T(n)$	$f(n)$	big-O
$T(n) = 1000n$	$f(n) = n$	$T(n) = O(n)$
$T(n) = 1000n$	$f(n) = n^2$	$T(n) = O(n^2)$
$T(n) = n^2$	$f(n) = n$	$T(n) \neq O(n)$
$T(n) = 13n^2 + n$	$f(n) = n^2$	$T(n) = O(n^2)$

Do asymptotics matter?

Algorithms are more important than language:

Fact: C can be 20x as fast as Python!

Algorithm	Language	Time	10,000 elements
Fast (MergeSort)	Slow (Python)	$2n \log(n) \mu s$	0.266s
Slow (InsertionSort)	Fast (C)	$0.01n^2 \mu s$	1s

(Source: MIT 6.006)

Simple Problem: Searching

Given:
a collection of **n** items

Find:
the largest item in the collection

Algorithm 1.

1. Sort the collection.
2. Return the largest item.

Simple Problem: Searching

Given:
a collection of n items

Find:
the largest item in the collection

Algorithm 1.

1. Sort the collection.
2. Return the largest item.

Algorithm 2.

1. Iterate through the collection.
2. Return the largest item.

Simple Problem: Searching

Given:
a collection of n items

Find:
the largest item in the collection

Algorithm 1.

1. Sort the collection.
2. Return the largest item.

$O(n \log n)$

Algorithm 2.

1. Iterate through the collection.
2. Return the largest item.

Simple Problem: Searching

Given:
a collection of n items

Find:
the largest item in the collection

Algorithm 1.

1. Sort the collection.
2. Return the largest item.

$O(n \log n)$

Algorithm 2.

1. Iterate through the collection.
2. Return the largest item.

$O(n)$

Simple Problem: Searching

Given:
a collection of n items

Find:
the largest k items
in the collection

Algorithm 1.

1. Sort the collection.
2. Return the largest k items.

Algorithm 2.

1. Iterate through the collection. Store the largest k items seen.
2. Return the largest k items.

Simple Problem: Searching

Extra memory: 1

Time: $O(n \log n + k)$

Algorithm 1.

1. Sort the collection.
2. Return the largest k items.

Extra memory: k

Time: ??

Algorithm 2.

1. Iterate through the collection. Store the largest k items seen.
2. Return the largest k items.

Simple Problem: Searching

Extra memory: 1

Time: $O(n \log n + k)$

Algorithm 1.

1. Sort the collection.
2. Return the largest k items.

Extra memory: k

Time: ??

Store k largest items in a sorted array. Insert new big items into the array.

Algorithm 2.

1. Iterate through the collection. Store the largest k items seen.
2. Return the largest k items.



Simple Problem: Searching

Example: $k = 3$

Collection:

1	3	5	6	2	7	1	3	1	1
---	---	---	---	---	---	---	---	---	---



Big items:

1		
---	--	--

Simple Problem: Searching

Example: $k = 3$

Collection:

1	3	5	6	2	7	1	3	1	1
---	---	---	---	---	---	---	---	---	---



Big items:

1	3	
---	---	--

Simple Problem: Searching

Example: $k = 3$

Collection:

1	3	5	6	2	7	1	3	1	1
---	---	---	---	---	---	---	---	---	---



Big items:

1	3	5
---	---	---

Simple Problem: Searching

Example: $k = 3$

Collection:

1	3	5	6	2	7	1	3	1	1
---	---	---	---	---	---	---	---	---	---



Big items:

1	3	5
---	---	---

Simple Problem: Searching

Example: $k = 3$

Collection:

1	3	5	6	2	7	1	3	1	1
---	---	---	---	---	---	---	---	---	---



Big items:

	3	5
--	---	---

Simple Problem: Searching

Example: $k = 3$

Collection:

1	3	5	6	2	7	1	3	1	1
---	---	---	---	---	---	---	---	---	---



Big items:

3		5
---	--	---

Simple Problem: Searching

Example: $k = 3$

Collection:

1	3	5	6	2	7	1	3	1	1
---	---	---	---	---	---	---	---	---	---



Big items:

3		5
---	--	---

Simple Problem: Searching

Example: $k = 3$

Collection:

1	3	5	6	2	7	1	3	1	1
---	---	---	---	---	---	---	---	---	---



Big items:

3	5	
---	---	--

Simple Problem: Searching

Example: $k = 3$

Collection:

1	3	5	6	2	7	1	3	1	1
---	---	---	---	---	---	---	---	---	---



Big items:

3	5	6
---	---	---

Cost of processing 6: k operations

Simple Problem: Searching

Example: $k = 3$

Collection:

1	3	5	6	2	7	1	3	1	1
---	---	---	---	---	---	---	---	---	---

↑

Big items:

3	5	6
---	---	---

Cost of processing 2: 0 array operations

Simple Problem: Searching

Example: $k = 3$

Collection:

1	3	5	6	2	7	1	3	1	1
↑									

Big items:

3	5	6
---	---	---

Cost of processing 7: k array operations

Simple Problem: Searching

Example: $k = 3$

Collection:

1	3	5	6	2	7	1	3	1	1
↑									

Big items:

5	6	7
---	---	---

Cost of processing 7: k array operations

Simple Problem: Searching

Example: $k = 3$

Collection:

1	3	5	6	2	7	1	3	1	1
↑									

Big items:

5	6	7
---	---	---

Worst case cost to process collection: $O(nk)$

Simple Problem: Searching

Extra memory: 1

Time: $O(n \log n + k)$

Algorithm 1.

1. Sort the collection.
2. Return the largest k items.

Extra memory: k

Time: $O(nk)$

Algorithm 2.

1. Iterate through the collection. Store the largest k items seen.
2. Return the largest k items.

Simple Problem: Searching

Extra memory: 1

Time: $O(n \log n + k)$

Algorithm 1.

1. Sort the collection.
2. Return the largest k items.

Extra memory: k

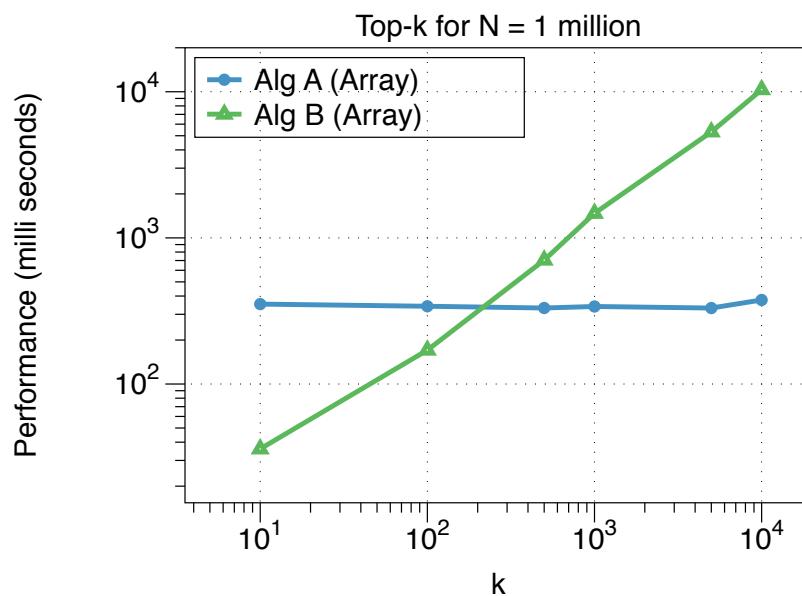
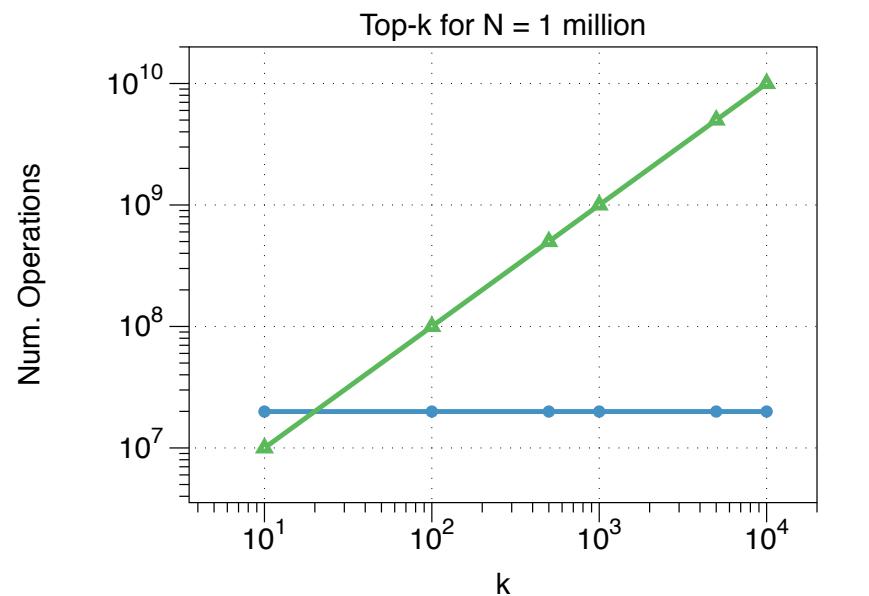
Time: $O(nk)$

Algorithm 2.

1. Iterate through the collection. Store the largest k items seen.
2. Return the largest k items.

Better solution in Week 5.

Theoretical & Real-World Performance



(Hat tip: Harold Soh)

More Searching

Given:
a sorted array of n items

Find:
find smallest item at least as
big as value x ?

Algorithm 1.
Linear search

More Searching

Given:
a sorted array of n items

Find:
find smallest item at least as
big as value x ?

Week 2:
Check midpoint and recurse
into one of the two halves.

Algorithm 1.
Linear search

Algorithm 2.
Binary search

More Searching

Given:
a sorted array of n items

Find:
find smallest item at least as
big as value x ?

Algorithm 1.
Linear search

$O(n)$

Algorithm 2.
Binary search

$O(\log n)$

More Searching

Are we done?

Information theory says
that this problem requires
at least $\Omega(\log n)$ ops.

Algorithm 1.
Linear search

$O(n)$

Algorithm 2.
Binary search

$O(\log n)$

Predicting Performance

Example: 100 TB of data

1) Store data sorted in an array

- ⇒ Scan all the data: $O(n)$
- ⇒ (Binary) search: $O(\log n)$

2) Store data in a linked list

- ⇒ Scan all the data: $O(n)$
- ⇒ Search: $O(n)$

3) Store data in a balanced tree

- ⇒ Scan all the data: $O(n)$
- ⇒ Search: $O(\log n)$

Predicting Performance

Example: 100 TB of data

1) Store data sorted in an array

- ⇒ Scan all the data: $O(n)$
- ⇒ (Binary) search: $O(\log n)$

2) Store data in a linked list

- ⇒ Scan all the data: $O(n)$
- ⇒ Search: $O(n)$

Same
performance!

3) Store data in a balanced tree

- ⇒ Scan all the data: $O(n)$
- ⇒ Search: $O(\log n)$

Predicting Performance

Example: 100 TB of data

1) Store data sorted in an array

- ⇒ Scan all the data: $O(n)$
- ⇒ (Binary) search: $O(\log n)$

This is MUCH faster by an order of magnitude.

2) Store data in a linked list

- ⇒ Scan all the data: $O(n)$
- ⇒ Search: $O(n)$

3) Store data in a red-black tree

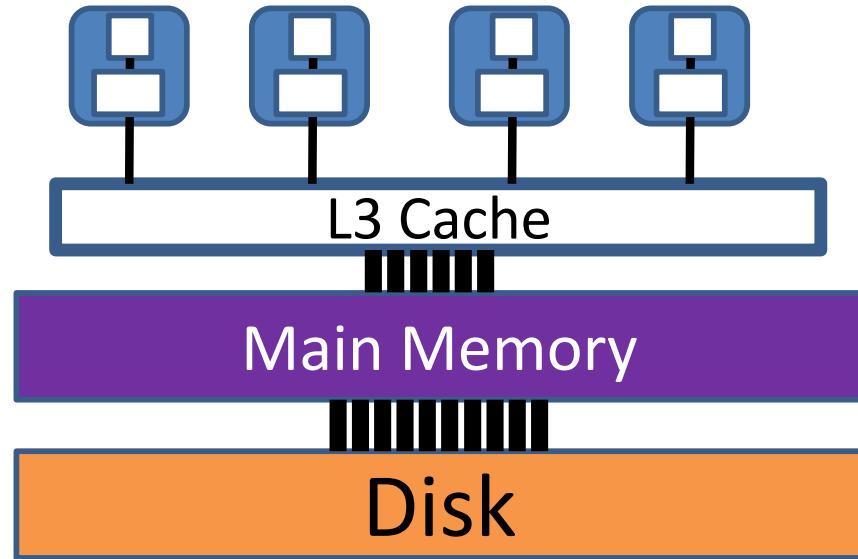
- ⇒ Scan all the data: $O(n)$
- ⇒ Search: $O(\log n)$

Haswell Architecture (2-18 cores)

Memory Type	size	line size	clock cycles
L1 cache	64 KB	64 B	~4
L2 cache	256 KB	64 B	~10
L3 cache	2-40 MB	64 B	40-74
L4 (optional)	128 MB		
Main Memory	< 128 GB	16 KB	~200-350
SSD Disk	BIG	Variable (e.g., 16KB)	~20,000
Disk	BIGGER	Variable (e.g., 16KB)	~20,000,000

Notes:

- Several other "caches" e.g., TLB, micro-op cache, instruction cache, etc.
- L1/L2 caches are per core.
- L3/L4 cache are shared per



More Searching

Faster to keep your data stored in a B-tree than in a sorted array!

Array: $O(\log(n/B))$

B-tree: $O(\log_B n)$

B is a parameter of the cache.

Algorithm 1.
Linear search

Algorithm 2.
Binary search

Algorithm 3.
Store data in B-tree

A little algorithmic thinking...

Searching

Finding a big item.

Finding many big items.

Searching an array.

Searching faster?

Similarity Test

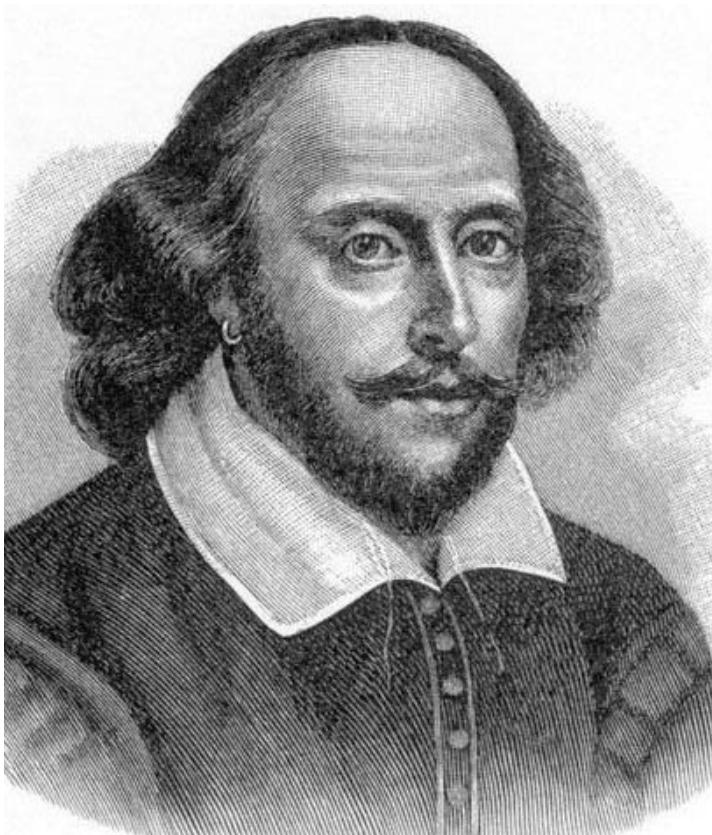
Comparing two texts

An algorithm

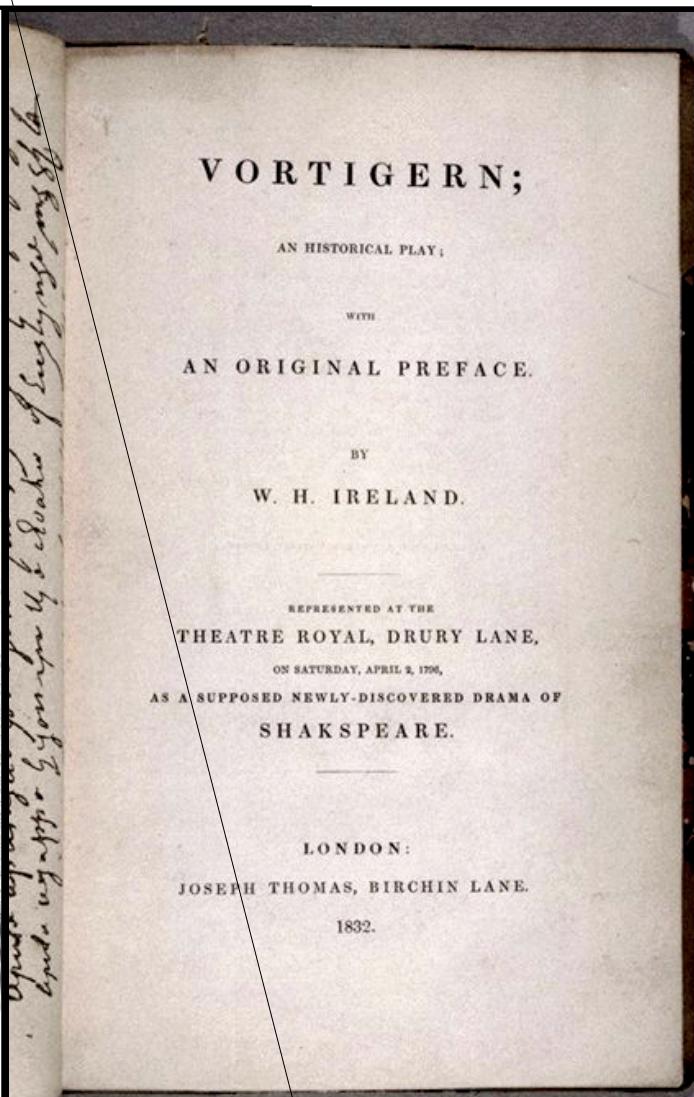
Performance profiling

Fixing a few mistakes

Who wrote this?



William
Shakespeare??



mystery play
“found” in 1796



William Henry
Ireland??

Document distance

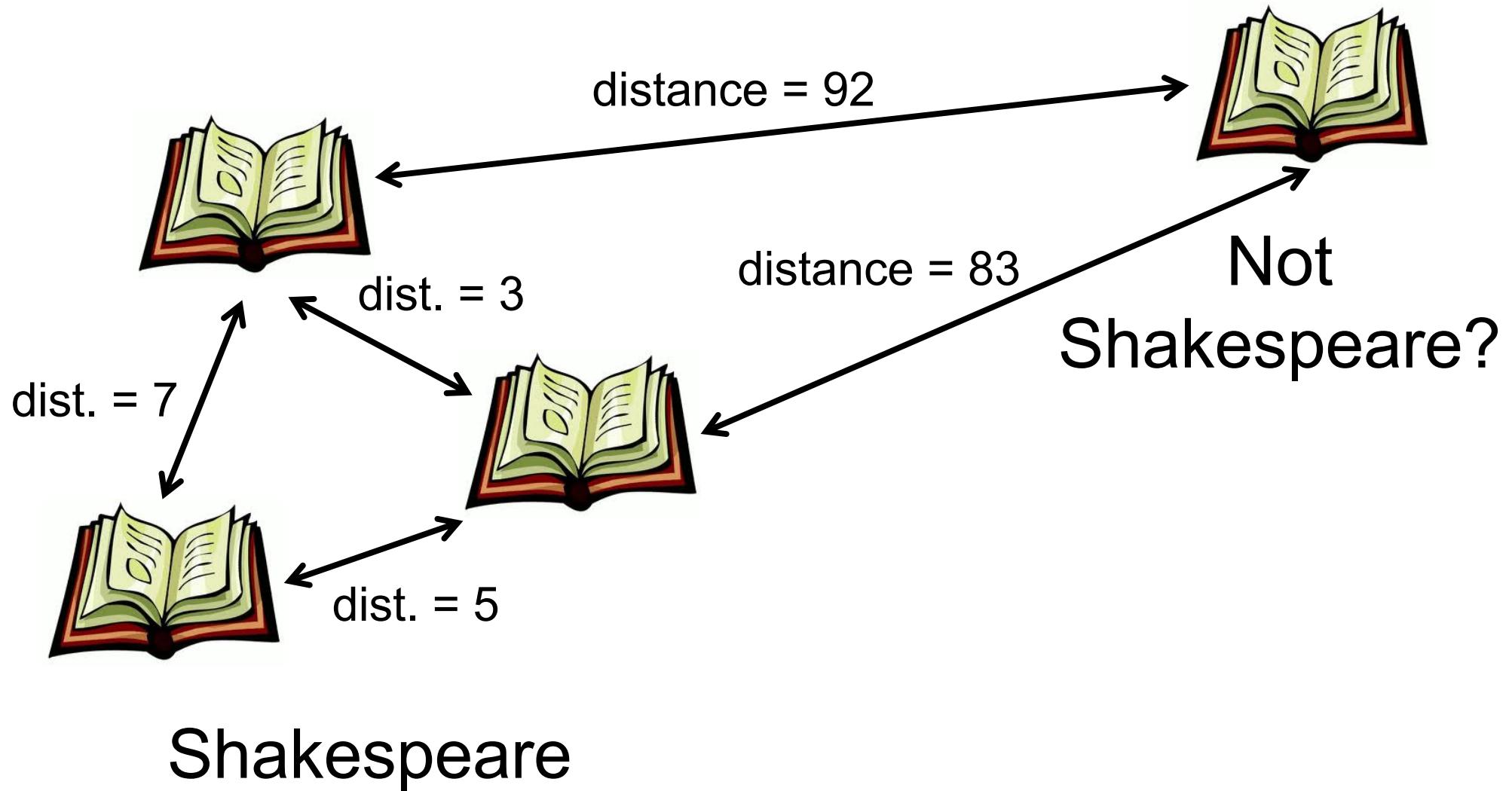
- How similar are two documents?
 - Are two documents written by the same author?
 - Detect forgeries
 - Find plagiarism / cheating
 - Was Homer one author or many?
- What does “similar” mean?

Metrics of similarity

- Binary: (e.g., detect plagiarism)
 - Exactly same words in same order
- Scalar:
 - Number of words in the same order
 - Number of shared *uncommon* words
 - Same # of words per sentence
 - Same ratio of adjectives / nouns
 - Written on similar paper / using similar ink

Document distance

How similar are two documents?

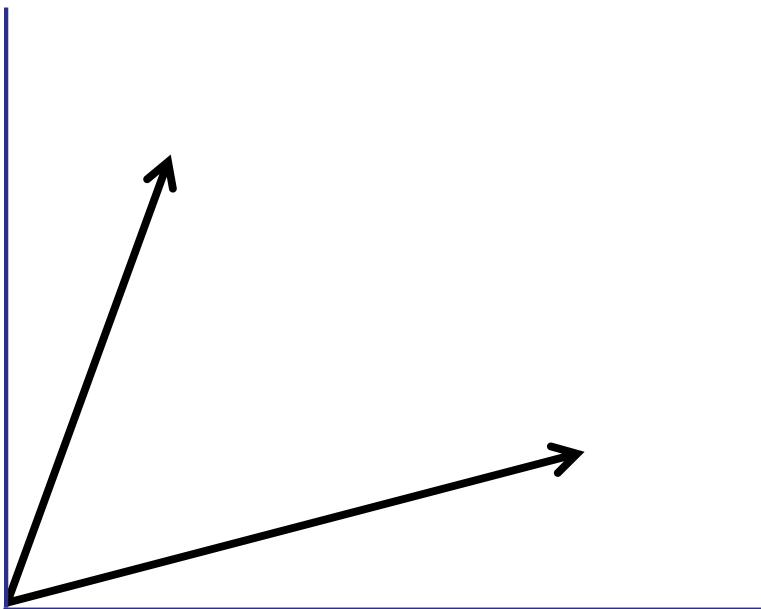


Vector Space Model

Strategy:

- View each document as a high-dimensional vector.

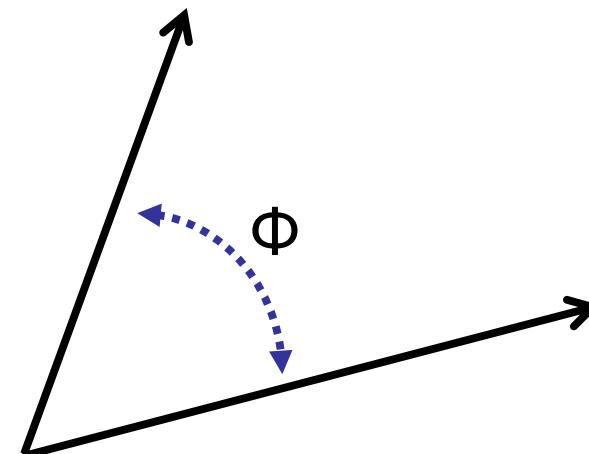
[Salton, Wang, Yang '75]



Vector Space Model

Strategy:

- View each document as a high-dimensional vector.
- The *metric of similarity* is the angle between the two vectors.



- Identical: $\Phi = 0$
- No words in common: $\Phi = \pi/2$

[Salton, Wang, Yang '75]

Compare Two Documents

Given: documents A and B

1. Create vectors v_A and v_B
→ count number of times each word appears
2. Calculate vector norms
3. Calculate dot product: $(v_A \cdot v_B)$
4. Calculate angle $\Phi(v_A, v_B)$

Performance Profiling

(Dracula vs. Lewis & Clark)

Step	Function	Running Time
Create vectors:	Read each file	1,824.00s
	Parse each file	0.20s
	Sort words in each file	328.00s
	Count word frequencies	0.31s
Dot product:		6.12s
Norm:		3.81s
Angle:		6.56s
Total:		72minutes ≈ 4,311.00s

Profiler

Profiling and Logging - CS2020 Test/src/sg/edu/nus/cs2020/DocumentDistanceMain.java - Eclipse Platform

File Edit Source Refactor Navigate Search Project Run Window Help

Execution Statistics - sg.edu.nus.cs2020.DocumentDistanceMain at gilbert-d960 [PID: 7180]

Session summary

Highest 10 base time

Package	Base Time (seconds)	Average Base Time (seconds)	Cumulative Time (seconds)	Calls
sg.edu.nus.cs2020	5,003.303381	0.012981	5,003.303381	38...
VectorTextFile	4,311.153603	215.557680	4,311.986191	20
ReadFile(java.lang.String) java.lang.String	3,648.053534	1,824.026767	3,648.053534	2
InsertionSortWords() void	656.330413	328.165206	656.330413	2
DotProduct(sg.edu.nus.cs2020.VectorTextFile, sg.edu.nus.cs2020.VectorTextFile) double	6.134406	2.044802	6.533115	3
SplitString(java.lang.String) void	0.390386	0.195193	0.390386	2
CountWordFrequencies() void	0.185574	0.092787	0.619453	2
VerifySort() void	0.034114	0.017057	0.034114	2
Angle(sg.edu.nus.cs2020.VectorTextFile, sg.edu.nus.cs2020.VectorTextFile) double	0.024622	0.024622	6.557860	1
VectorTextFile(java.lang.String)	0.000273	0.000136	4,305.428330	2
ParseFile(java.lang.String) void	0.000158	0.000079	3,648.444078	2
Norm() double	0.000123	0.000062	3.814559	2
VectorTextFile2	676.500618	33.825031	680.487998	20
WordCountPair	6.706844	0.000021	6.706844	31...
VectorTextFile3	6.594781	0.000101	8.481658	65,...
VectorTextFile4	0.247524	0.001255	0.247524	1

Session summary Execution Statistics Call Tree Method Invocation Details Method Invocation

Console Problems

<terminated> DocumentDistanceMain [Java Application] java.exe (January 5, 2011 3:59:34 PM)

The angle between A and B is: 0.5708476330610679

The angle between A and B is: 0.5708476276825866

The angle between A and B is: 0.5708476276825866

Test.java VectorTextFile2.java VectorTextFile.java DocumentDistanceMain hamlet.txt midsummer.txt Tom Sawyer.txt JFK.txt verne.txt

```
package sg.edu.nus.cs2020;

import java.io.IOException;

public class DocumentDistanceMain
```

Performance Profiling

(Dracula vs. Lewis & Clark)

Step	Function	Running Time
Create vectors:	Read each file	1,824.00s
	Parse each file	0.20s
	Sort words in each file	328.00s
	Count word frequencies	0.31s
Dot product:		6.12s
Norm:		3.81s
Angle:		6.56s
Total:		72minutes ≈ 4,311.00s

Problem 1: Why does it take SO long to read the file?

ReadFile (excerpt)

```
// Open the file as a stream and find its size
inputStream = new FileInputStream(fileName);
iSize = inputStream.available();

// Read in the file, one character at a time, normalizing as we go.
for (int i=0; i<iSize; i++)
{
    // Read a character
    char c = (char)inputStream.read();

    // Ensure that the character is lower-case
    c = Character.toLowerCase(c);

    // Check if the character is a letter
    if (Character.isLetter(c))
    {
        strTextFile = strTextFile + c;
    }
    // Check if the character is a space or an end-of-line marker
    else if (((c == ' ') || (c == '\n')) && (!strTextFile.endsWith(" ")))
    {
        strTextFile = strTextFile + ' ';
    }
}
```

String Problem!

What happens when:

`textFile = textFile + c`

1. Creates new temporary string.
2. Copies `textFile` to the new string.
3. Adds the new character `c`.
4. Reassigns `textFile` to point to the new string.

String Problem!

What happens when:

`textFile = textFile + c`

1. Creates new temporary string.
2. **Copies `textFile` to the new string.**
3. Adds the new character `c`.
4. Reassigns `textFile` to point to the new string.

Copying a string of k characters takes time $k!$

String Problem!

How long to read in a file of n characters?.

String Problem!

How long to read in a file of n characters?.

$$1 + 2 + 3 + 4 + \dots + n = n(n+1)/2 = \Theta(n^2)$$

Very, very, very slow!

Fix the string problem!

```
// Open the file as a stream and find its size
inputStream = new FileInputStream(fileName);
iSize = inputStream.available();

// Initialize the char buffer to be arrays of the appropriate size.
charBuffer = new char[iSize];

// Read in the file, one character at a time, normalizing as we go.
for (int i=0; i<iSize; i++)
{
    // Read a character
    char c = (char)inputStream.read();

    // Ensure that the character is lower-case
    c = Character.toLowerCase(c);

    // Check if the character is a letter
    if (Character.isLetter(c))
    {
        charBuffer[iCharCount] = c;
        iCharCount++;
    }
    // Check if the character is a space or an end-of-line marker
    else if (((c == ' ') || (c == '\n')) && (!strTextFile.endsWith(" ")))
    {
        charBuffer[iCharCount] = ' ';
        iCharCount++;
    }
}
```

Performance Profiling, V2

(Dracula vs. Lewis & Clark)

Step	Function	Running Time
Create vectors:	Read each file	1.09s
	Parse each file	3.68s
	Sort words in each file	332.13s
	Count word frequencies	0.30s
Dot product:		6.06s
Norm:		3.80s
Angle:		6.06s
Total:		11minutes ≈ 680.49s

Problem 2: Can we sort faster?

Performance Profiling

(Dracula vs. Lewis & Clark)

Version	Change	Running Time
Version 1		4,311.00s
Version 2	Better file handling	676.50s
Version 3	Faster sorting	6.59s

Use $O(n \log n)$ sorting algorithm ([MergeSort](#)) instead of $O(n^2)$ sorting algorithm ([InsertionSort](#)).

Problem 3: Do we need to sort at all?

Document Distance

(Dracula vs. Lewis & Clark)

Version	Change	Running Time
Version 1		4,311.00s
Version 2	Better file handling	676.50s
Version 3	Faster sorting	6.59s
Version 4	No sorting!	2.35s

Use **O(n)** hashing approach
instead of **O(n log n)** sorting algorithm (**MergeSort**).

Goals for the Semester

*Speed up your code
by a factor of 2040!*

Algorithms:

- Design of efficient algorithms
- Analysis of algorithms

Implementation:

- Solve real problems
- Analyze and measure performance
- Improve performance via better algorithms

For next time...

Thursday lecture:

- Java introduction, OOP
- Stacks, Queues, Lists

Problem Set 1:

- Released. Due next week.

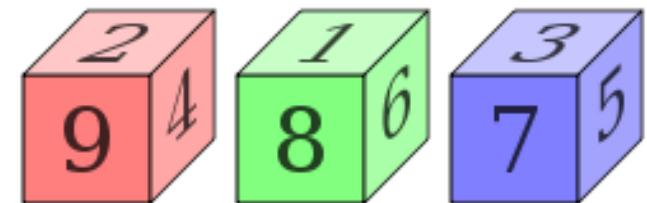
Admin:

- Log in to Coursmology.
- Sign up for recitation (EduReg)
- Fill out tutorial survey (Coursemology)

Puzzle of the Week

Imagine three dice:

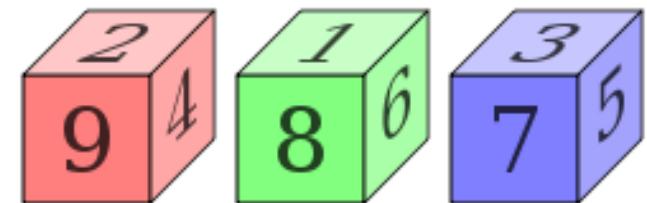
- A has six sides: 2, 2, 4, 4, 9, 9
- B has six sides: 1, 1, 6, 6, 8, 8
- C has six sides: 3, 3, 5, 5, 7, 7



Puzzle of the Week

Imagine three dice:

- A has six sides: 2, 2, 4, 4, 9, 9
- B has six sides: 1, 1, 6, 6, 8, 8
- C has six sides: 3, 3, 5, 5, 7, 7



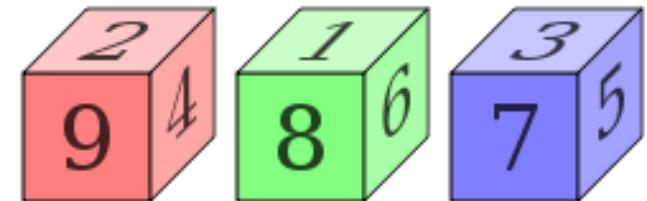
Game:

- Alice chooses a die.
- Bob chooses a die.
- Alice and Bob both roll.
- The higher value wins.

Puzzle of the Week

Imagine three dice:

- A has six sides: 2, 2, 4, 4, 9, 9
- B has six sides: 1, 1, 6, 6, 8, 8
- C has six sides: 3, 3, 5, 5, 7, 7



Game:

- Alice chooses a die.
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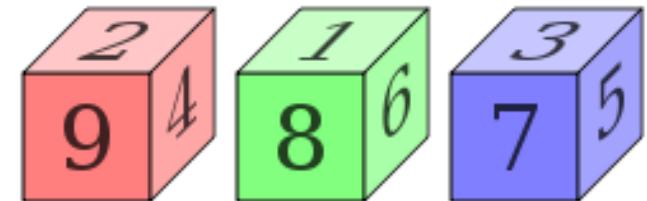
Questions:

- Which die should Alice choose?
- Which die should Bob choose?
- Who is more likely to win?

Puzzle of the Week

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