

# **ELEC 3210**

# **Introduction to Mobile Robotics**

## **Lecture 11**

**(Machine Learning and Information Processing for Robotics)**

Huan YIN

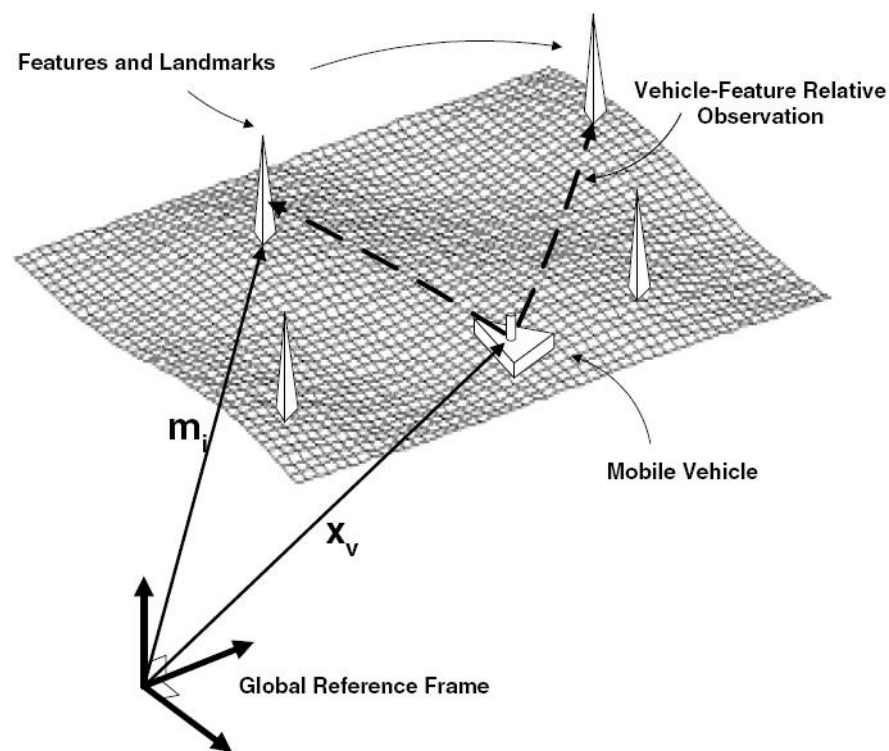
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# Recap L10 - EKF SLAM

- Extended Kalman Filter-based Simultaneous Localization and Mapping (EKF SLAM)
- Obtain both **feature (landmark) map** and **robot poses in real time**



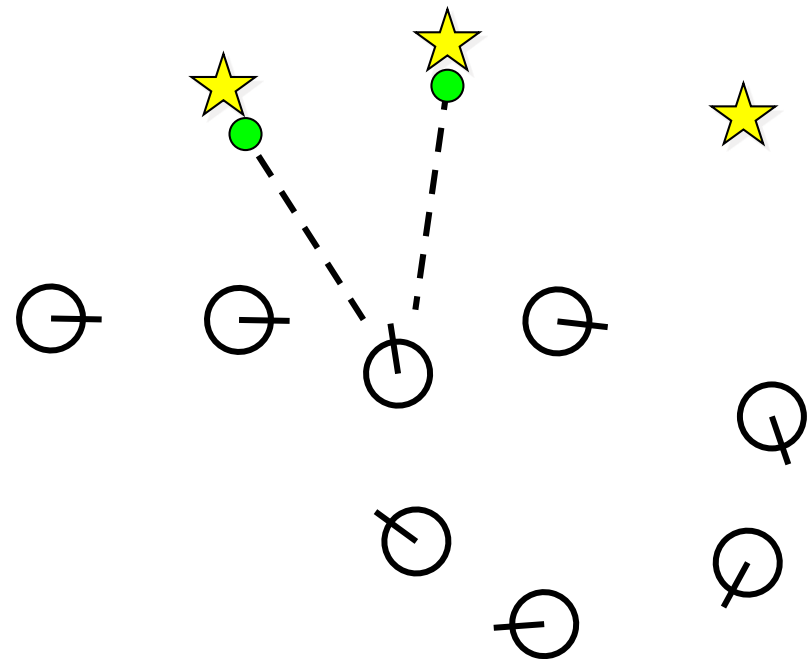
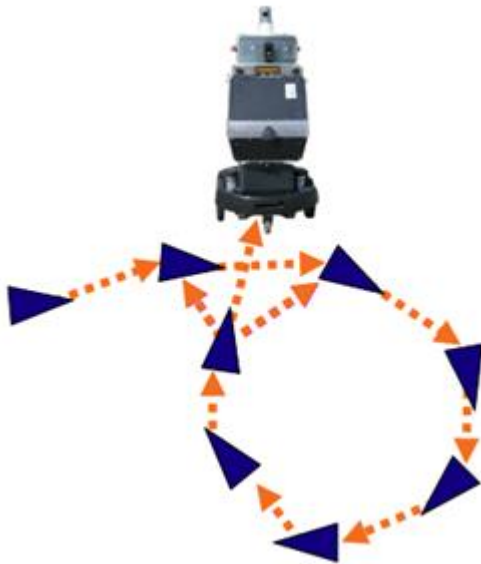
# Recap L10 - EKF SLAM

- Velocity-based Motion
- Range-Bearing Observation

```
1:  Extended_Kalman_filter( $\mu_{t-1}, \Sigma_{t-1}, u_t, z_t$ ):  
2:       $\bar{\mu}_t = g(u_t, \mu_{t-1})$   
3:       $\bar{\Sigma}_t = G_t \Sigma_{t-1} G_t^T + R_t$   
4:       $K_t = \bar{\Sigma}_t H_t^T (H_t \bar{\Sigma}_t H_t^T + Q_t)^{-1}$   
5:       $\mu_t = \bar{\mu}_t + K_t (z_t - h(\bar{\mu}_t))$   
6:       $\Sigma_t = (I - K_t H_t) \bar{\Sigma}_t$   
7:      return  $\mu_t, \Sigma_t$ 
```

# Loop Closing in SLAM

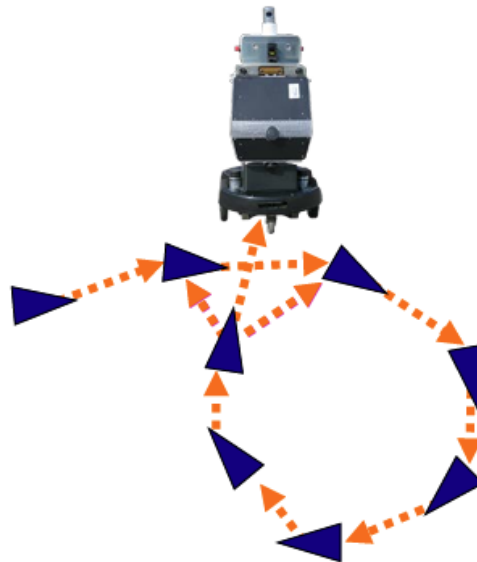
- What if the robot travels a place that it has been before?
- In EKF SLAM, the loop closure could be achieved by landmark data association ( or on a nearest-neighbor basis)



# Loop Closing for EKF SLAM

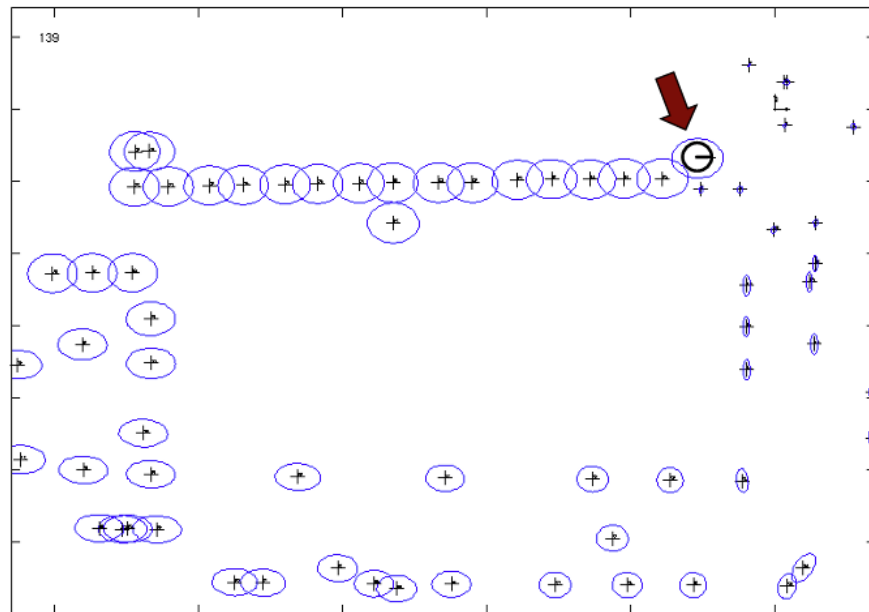
# Loop Closing

- Loop closing means recognizing an already mapped area
- Data association under
  - high ambiguity
  - possible environment symmetries
- Uncertainties collapse after a loop closure (whether the closure was correct or not)

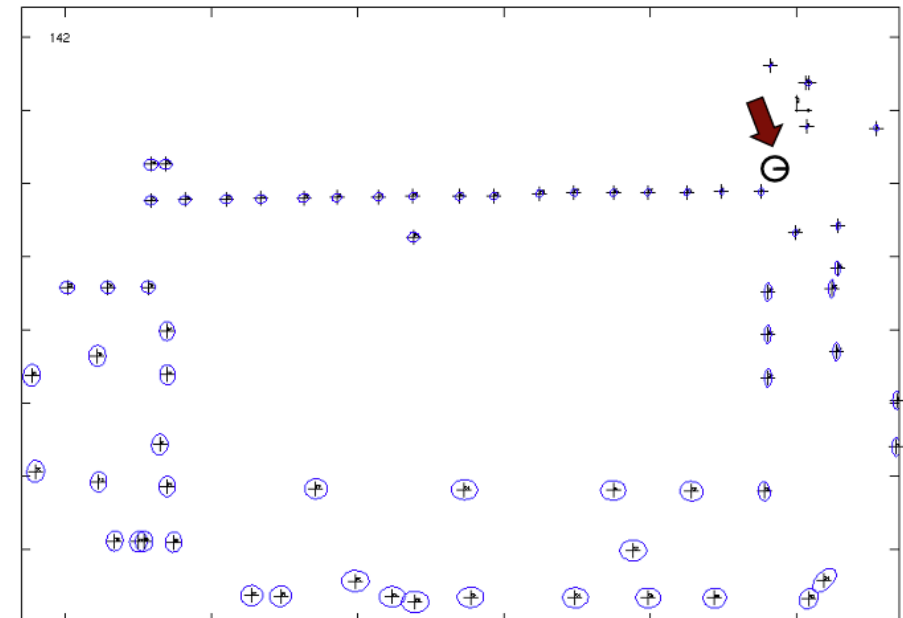


# Loop Closing

- Loop closing reduces the uncertainty in robot and landmark estimates
- This can be exploited when exploring an environment for the sake of better (more accurate) maps
- Wrong loop closures lead to filter divergence



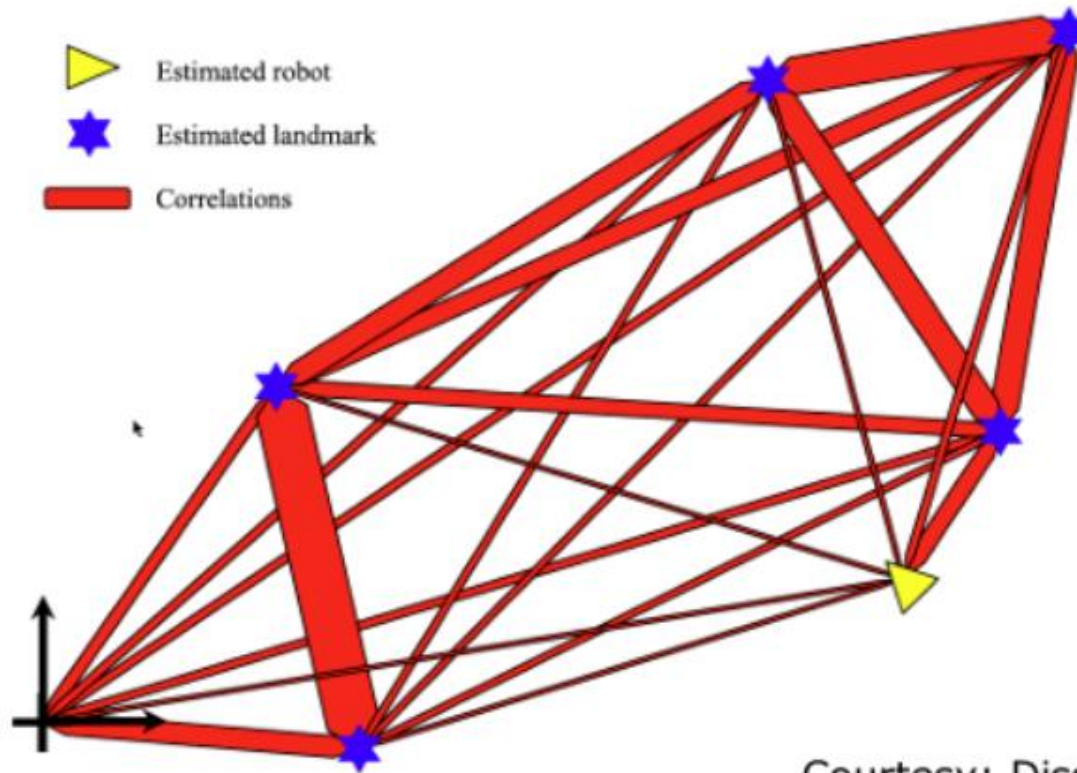
**Before Loop Closing**



**After Loop Closing**

# EKF SLAM Correlations

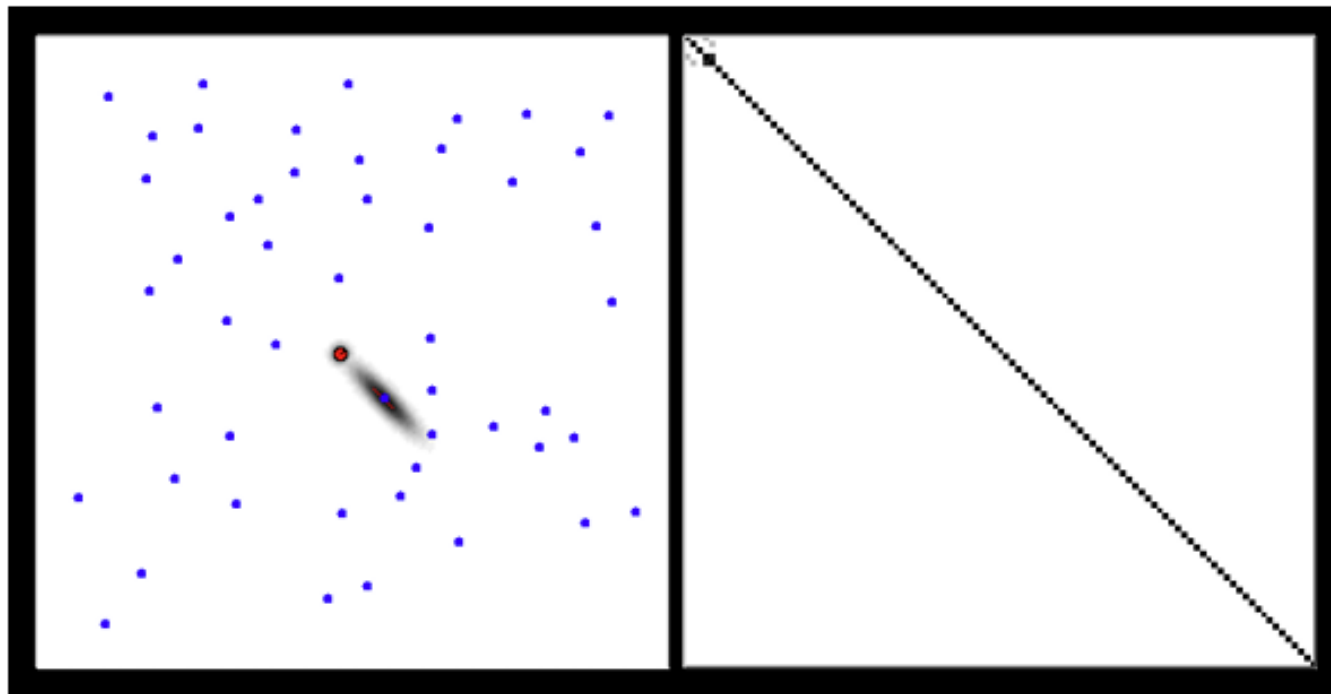
- In the limited, the landmark estimates become fully correlated



Courtesy: Dissanayake



# EKF SLAM Correlations

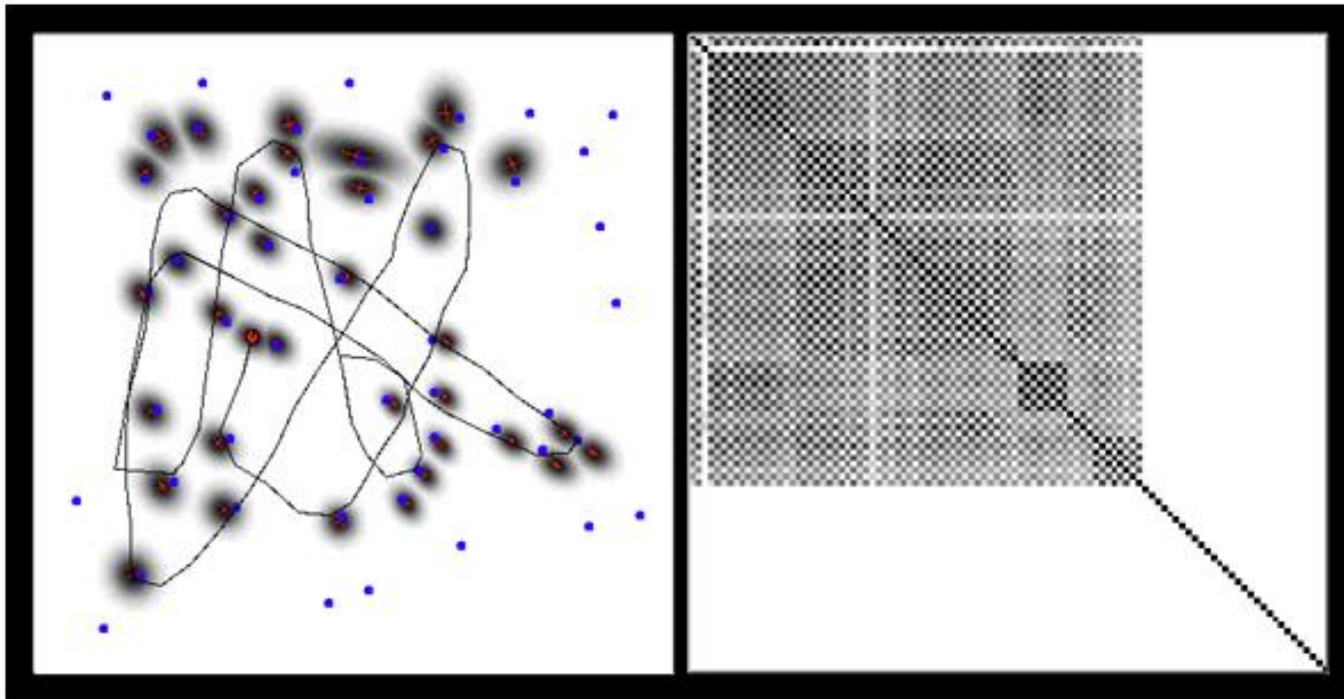


Map

Correlation matrix

(normalized covariance matrix)

# EKF SLAM Correlations

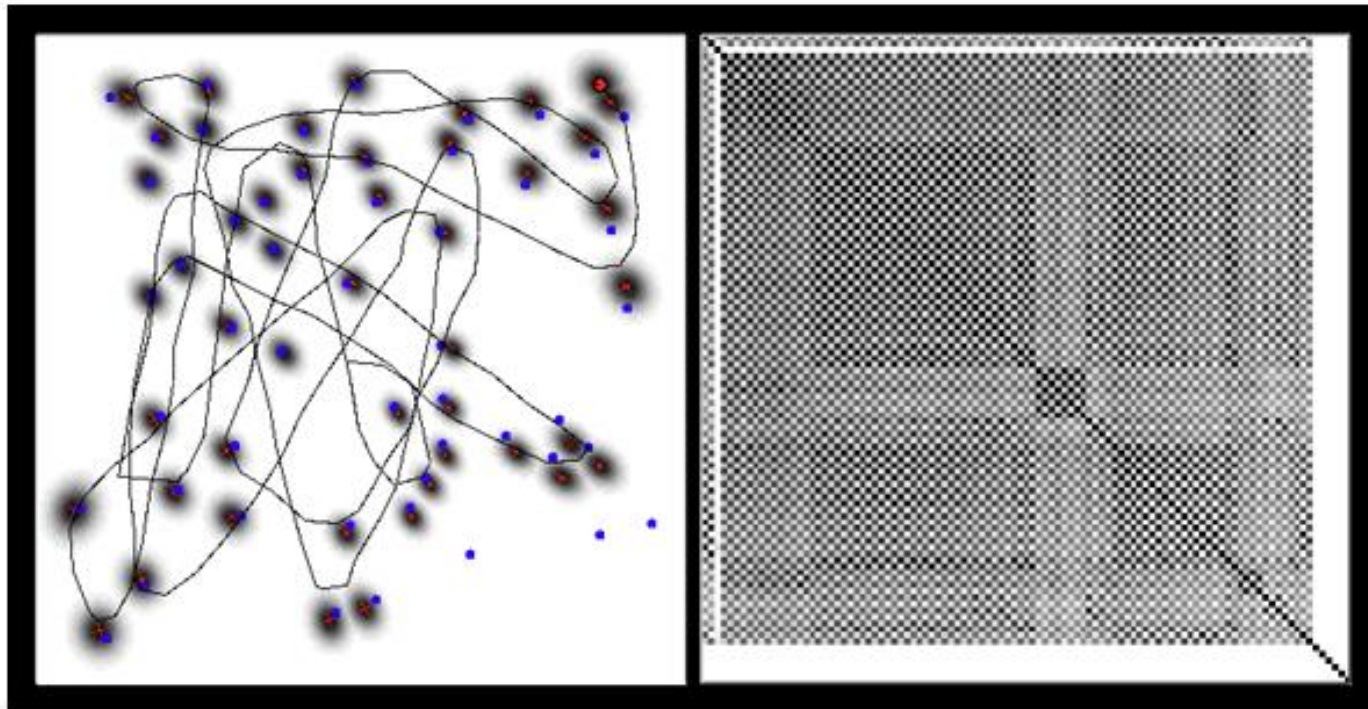


Map

Correlation matrix

# EKF SLAM Correlations

- What if I fix a location of one landmark?

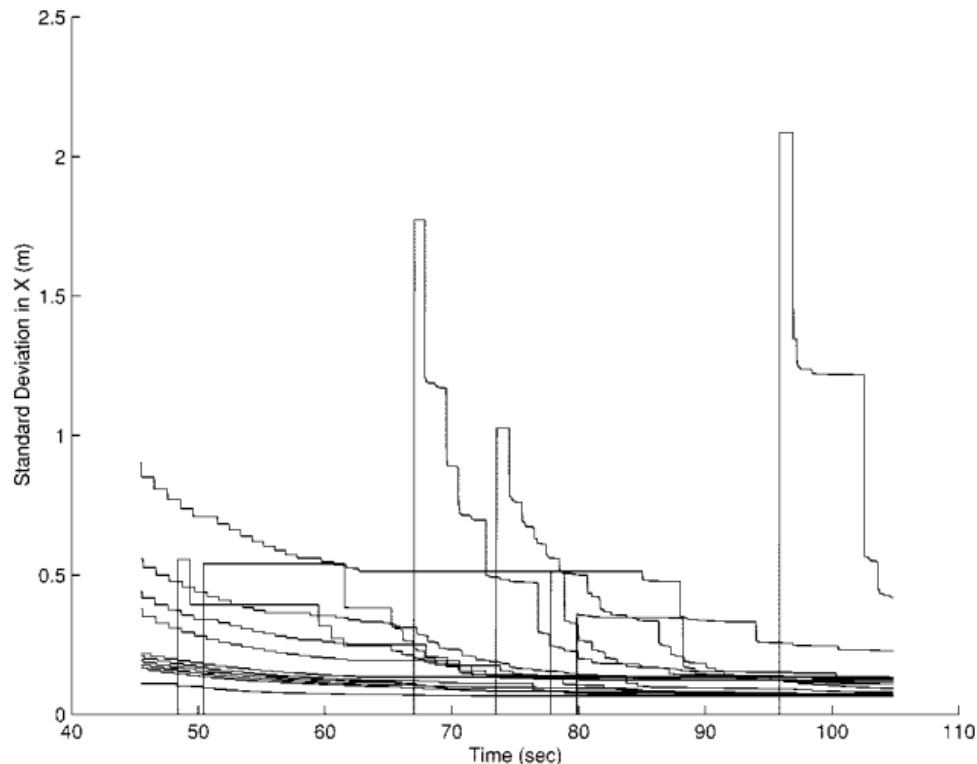


Map

Correlation matrix

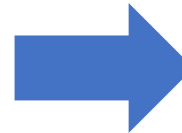
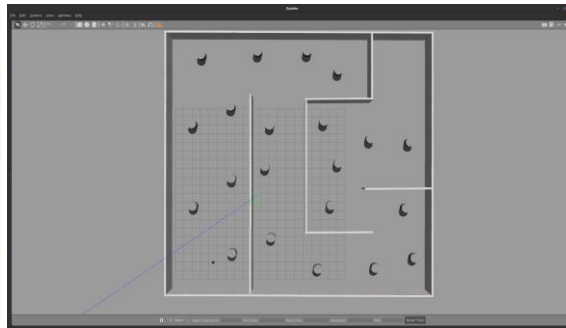
# EKF SLAM Uncertainties

- The determinant of any sub-matrix of the map covariance matrix decreases monotonically
- New landmarks are initialized with maximum uncertainty



# How to Close Loops in Urbans?

- What are the differences?



# Place Recognition

- From **small/medium-scale** environments to **large-scale**
- From **short-term** operation to **long-term**
- From **global sparse landmark** to **topological dense representations**, Lecture 6 Map Representations and Organization
- Place Recognition Today
  - LiDAR Place Recognition - Scan Context
  - Visual Place Recognition



# **LiDAR Place Recognition**



# Recap L4 - Sensors

- LiDAR - Light Detection and Ranging
- Compared to 2D Laser Scanner
  - 3D Data
  - More expensive



3 Years Ago



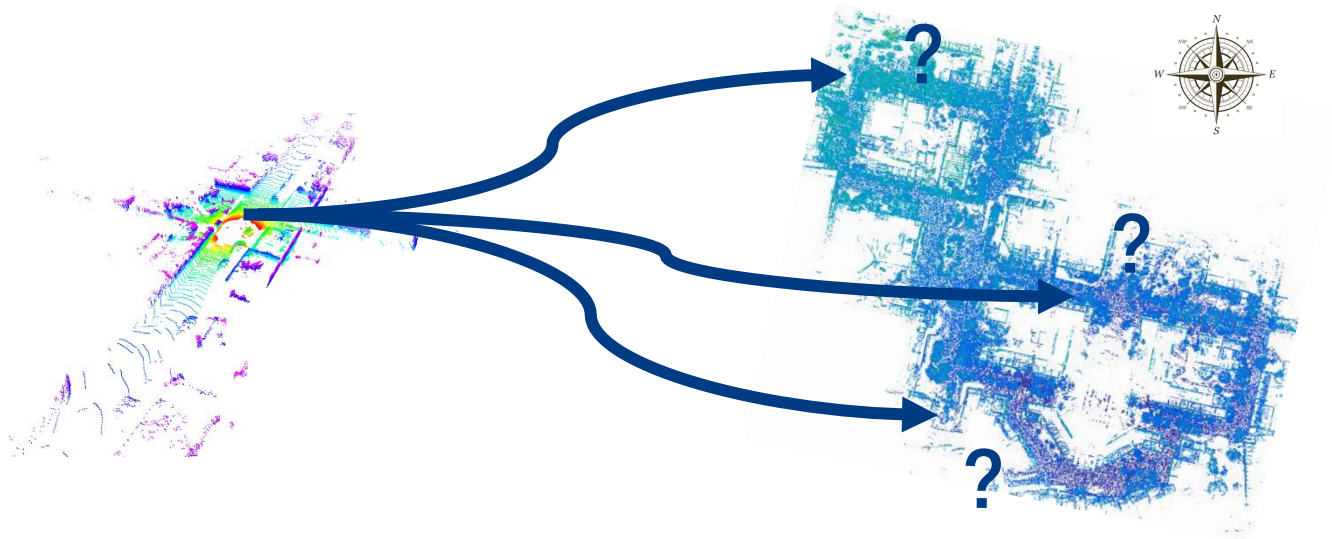
# LiDAR Place Recognition

## Robotics

- Has the robot been to this place before?
- Which point clouds were taken around the same location?

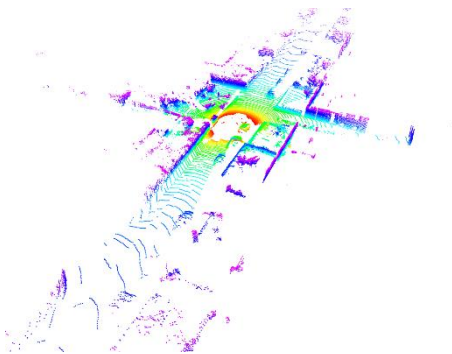
## LiDAR Point Cloud Retrieval Problem

- Have I seen this point cloud before?
- Which LiDAR scan or submap in my map database look similar to it?

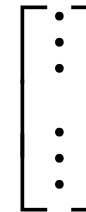
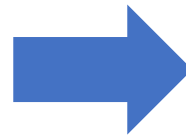


# Key Points

- Need descriptors
  - discriminative
  - low-dimension
- Need retrieval scheme
  - need similarity design
  - high efficiency
  - better provides orientation



**LiDAR Point Cloud**



**Descriptor**

# LiDAR Place Recognition

- Many approaches in recent years
- Kim G, Kim A. **Scan context: Egocentric spatial descriptor for place recognition within 3d point cloud map**. In 2018 IEEE/RSJ International Conference on Intelligent Robots and Systems (IROS) 2018 Oct 1 (pp. 4802-4809). IEEE.

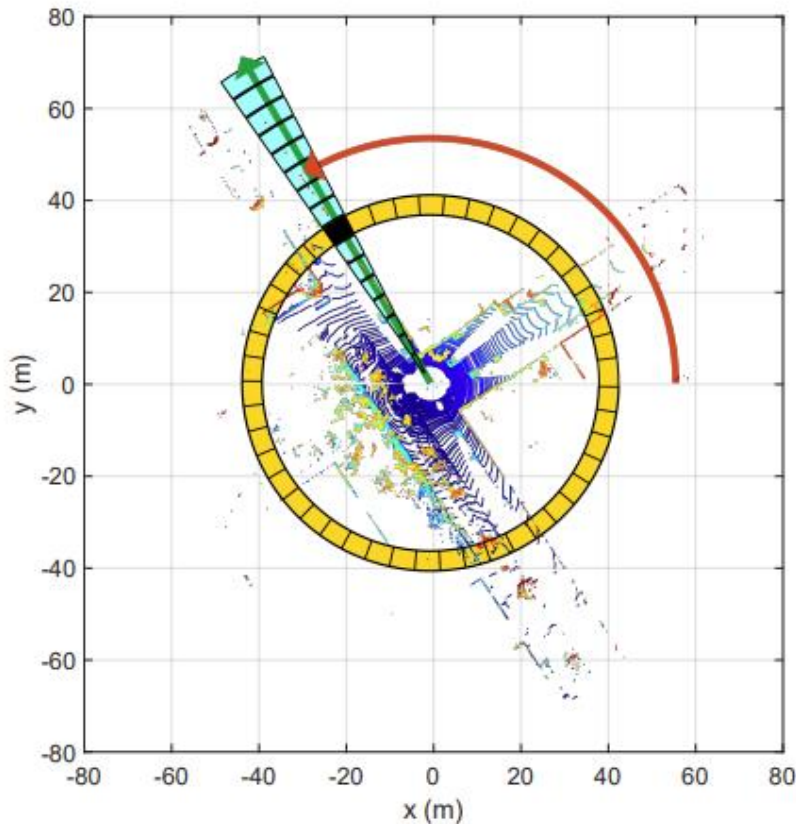
2018 IEEE/RSJ International Conference on Intelligent Robots and Systems (IROS)  
Madrid, Spain, October 1-5, 2018

## **Scan Context: Egocentric Spatial Descriptor for Place Recognition within 3D Point Cloud Map**

Giseop Kim<sup>1</sup> and Ayoung Kim<sup>1\*</sup>

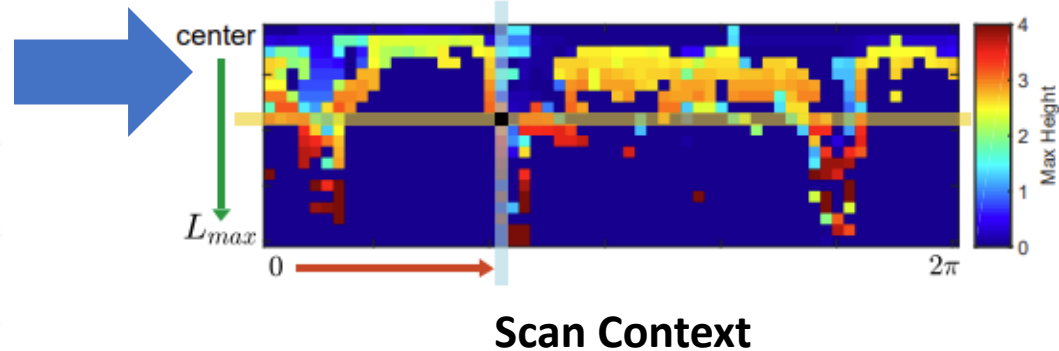
# Describe a LiDAR Point Cloud

- Encodes the highest z-value in each context pixel



$$\phi(\mathcal{P}_{ij}) = \max_{\mathbf{p} \in \mathcal{P}_{ij}} z(\mathbf{p})$$

$$I = (a_{ij}) \in \mathbb{R}^{N_r \times N_s}, a_{ij} = \phi(\mathcal{P}_{ij})$$

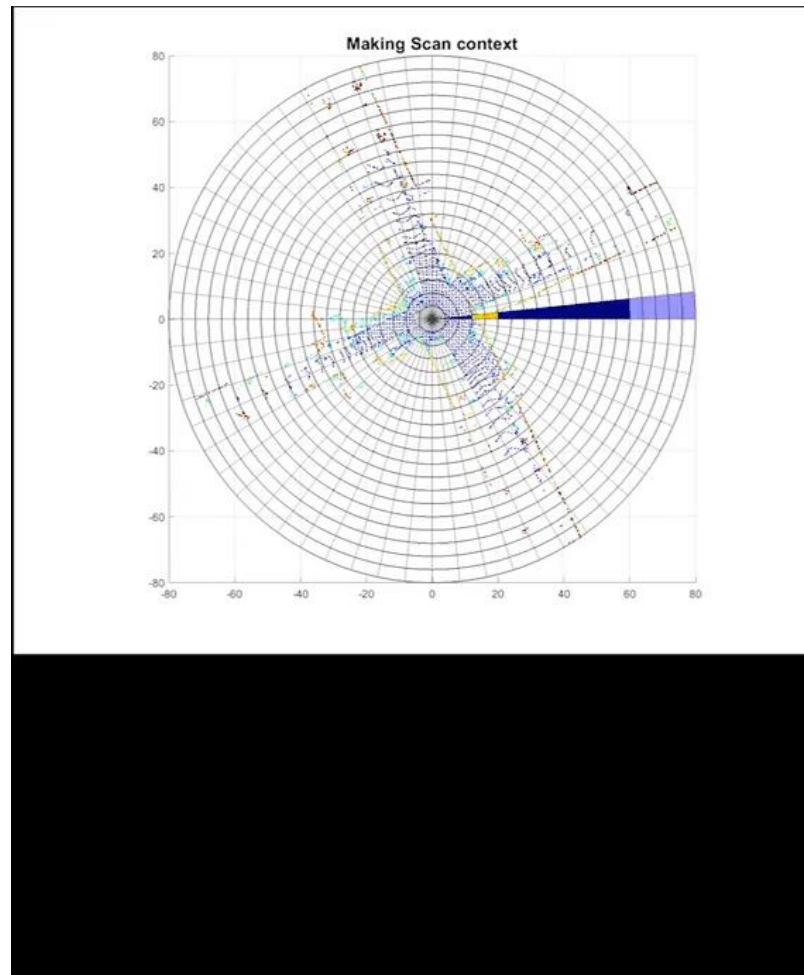


**Bin division along azimuthal and radial directions**

Courtesy: Scan Context by Kim

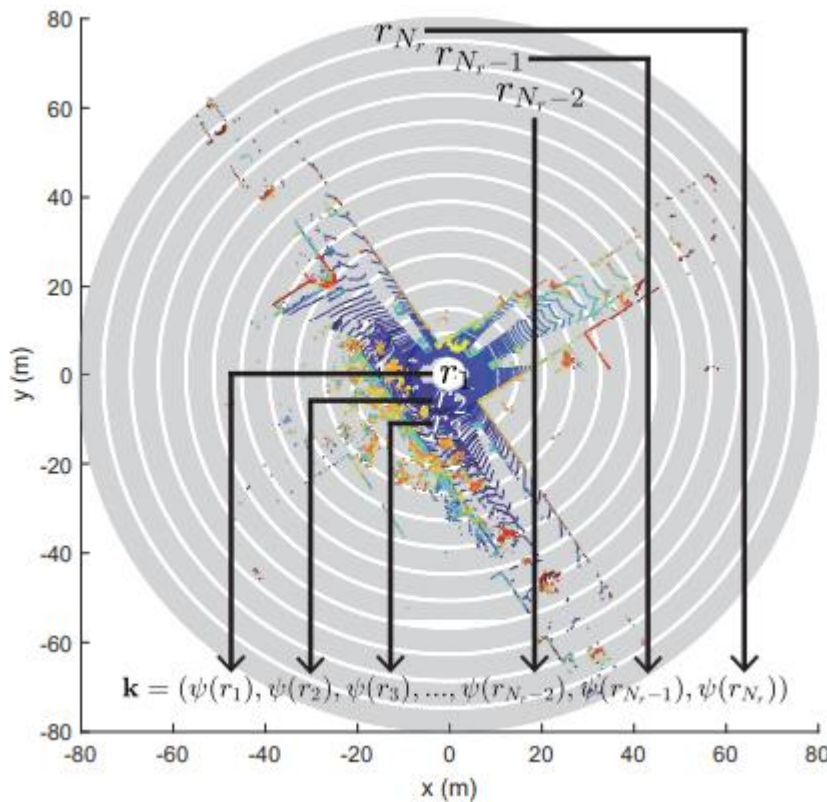
# Describe a LiDAR Point Cloud

- From the scan to the context



# Ring Key for Fast Retrieval

- From 2-Dimension to 1-Dimension
- Occupy ratio of each ring

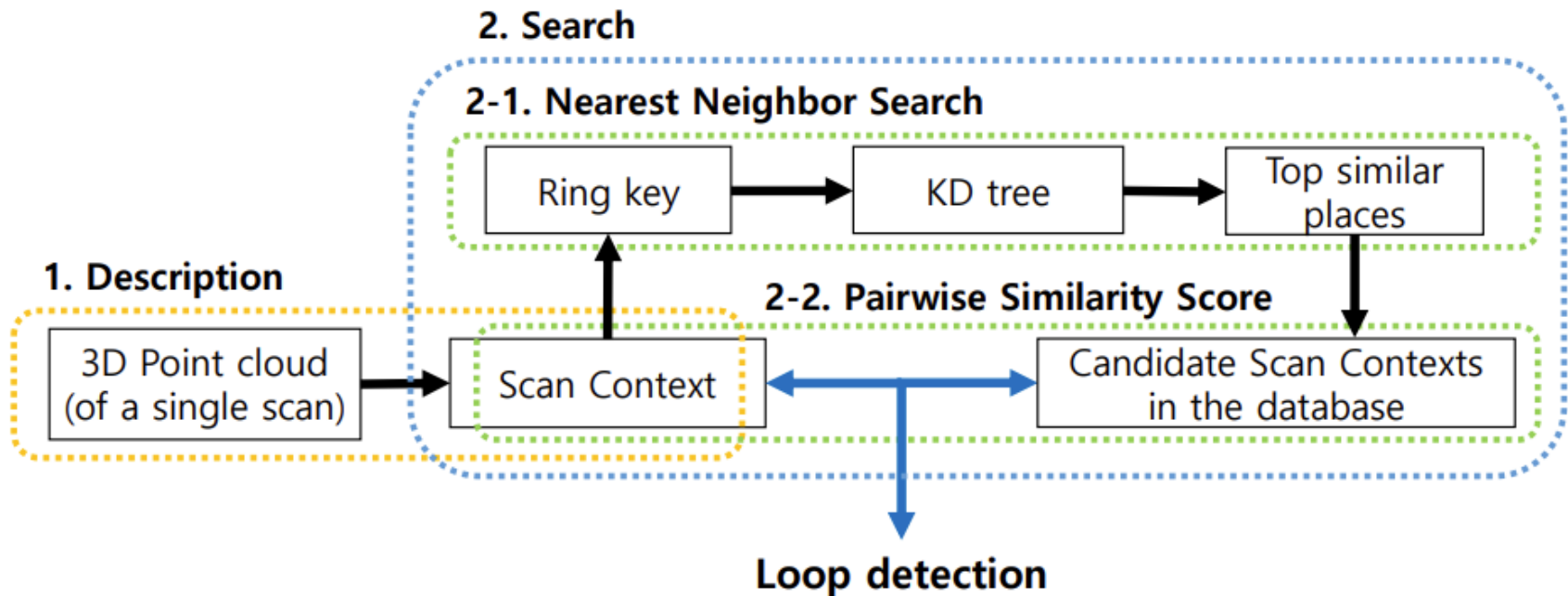


$$\mathbf{k} = (\psi(r_1), \dots, \psi(r_{N_r}))$$

$$\psi(r_i) = \frac{\|r_i\|_0}{N_s}$$

# Scan Context Framework

- First Describe, Then Search
- Framework



# Similarity Score

For a candidate, the similarity score is by

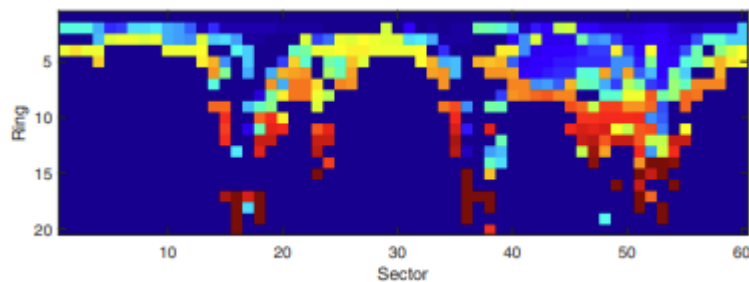
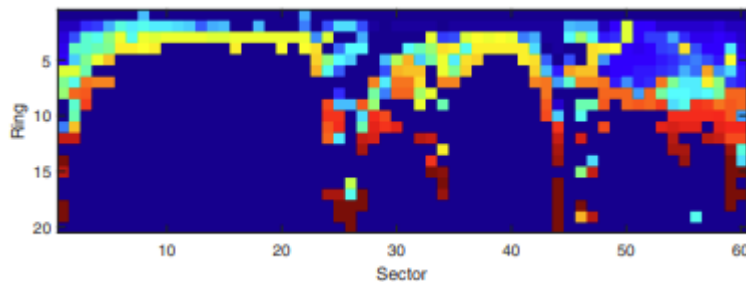
- Cosine Distance of each column in the context

$$d(I^q, I^c) = \frac{1}{N_s} \sum_{j=1}^{N_s} \left( 1 - \frac{c_j^q \cdot c_j^c}{\|c_j^q\| \|c_j^c\|} \right)$$

- Exhaustive search on the columns and find the “best” alignment

$$D(I^q, I^c) = \min_{n \in [N_s]} d(I^q, I_n^c),$$

$$n^* = \operatorname{argmin}_{n \in [N_s]} d(I^q, I_n^c).$$



**Contexts at the same location but with different orientation**



## *Scan Context*: Egocentric Spatial Descriptor for Place Recognition within 3D Point Cloud Map

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Ayoung Kim<sup>1</sup>

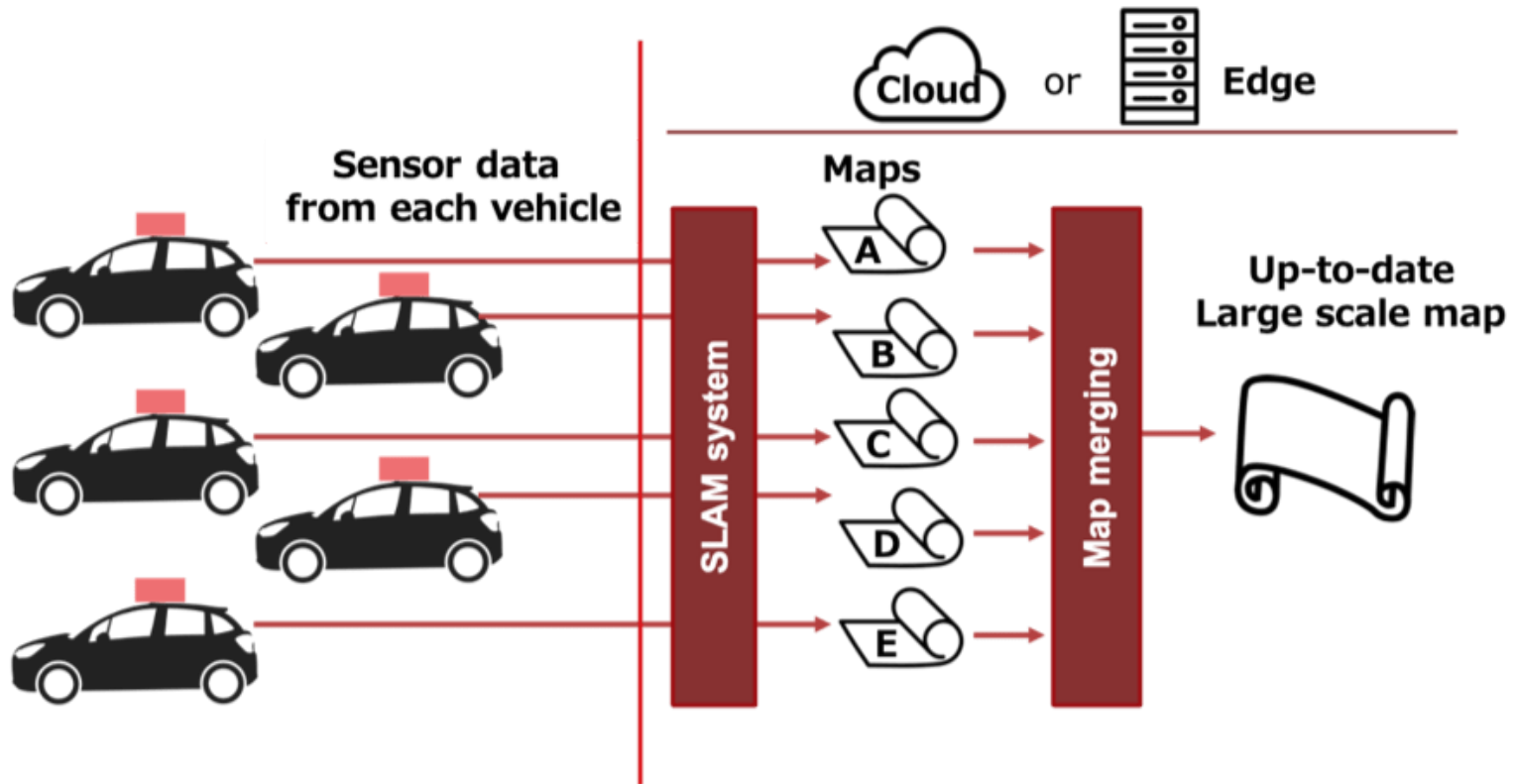
ayoungk@kaist.ac.kr

<sup>1</sup> Intelligent Robotic Autonomy and Perception (IRAP) Lab

**KAIST**

# Application of the LiDAR PR

- Large-scale LiDAR mapping in cities



# Our Work on LiDAR PR

- Yu Z, Qiao Z, Qiu L, Yin H, Shen S. Multi-Session, Localization-oriented and Lightweight LiDAR Mapping Using Semantic Lines and Planes. arXiv preprint arXiv:2307.07126. 2023 Jul 14.



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## **Multi-Session, Localization-oriented and Lightweight LiDAR Mapping Using Semantic Lines and Planes**

Zehuan Yu, Zhijian Qiao, Liuyang Qiu, Huan Yin and Shaojie Shen

# Visual Place Recognition

# Visual Place Recognition

## Robotics

- Has the robot been to this place before?
- Which ~~point clouds~~ images were taken around the same location?

## LiDAR Point Cloud Retrieval Problem

- Have I seen this ~~point cloud~~ image before?
- Which ~~LiDAR scan or submap~~ image in my map database look similar to it?



# Why so challenging?

- Much more difficult than LiDAR place recognition
  - information-rich data -> high dimensional descriptors
  - illumination change
  - view change
  - others



**Two images at the same place**

# Visual Place Recognition Survey

- Many many many approaches for VPR
- Lowry S, Sünderhauf N, Newman P, Leonard JJ, Cox D, Corke P, Milford MJ. **Visual place recognition: A survey.** *IEEE transactions on robotics*. 2015 Nov 26;32(1):1-9.

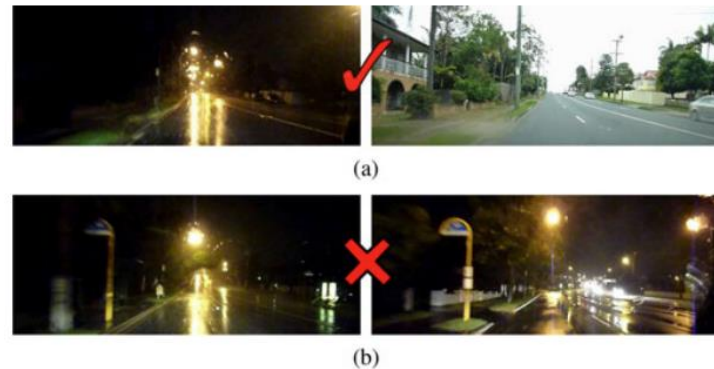
IEEE TRANSACTIONS ON ROBOTICS, VOL. 32, NO. 1, FEBRUARY 2016

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## Visual Place Recognition: A Survey

Stephanie Lowry, Niko Sünderhauf, Paul Newman, *Fellow, IEEE*, John J. Leonard, *Fellow, IEEE*, David Cox, Peter Corke, *Fellow, IEEE*, and Michael J. Milford, *Member, IEEE*

**Abstract**—Visual place recognition is a challenging problem due to the vast range of ways in which the appearance of real-world places can vary. In recent years, improvements in visual sensing capabilities, an ever-increasing focus on long-term mobile robot autonomy, and the ability to draw on state-of-the-art research in other disciplines—particularly recognition in computer vision and animal navigation in neuroscience—have all contributed to significant advances in visual place recognition systems. This paper presents a survey of the visual place recognition research landscape. We start by introducing the concepts behind place recognition—the role of place recognition in the animal kingdom, how a “place” is defined in a robotics context, and the major components of a place recognition system. Long-term robot operations have revealed that changing



1000 Kilometers Of  
Appearance-Only SLAM

FabMap 2.0

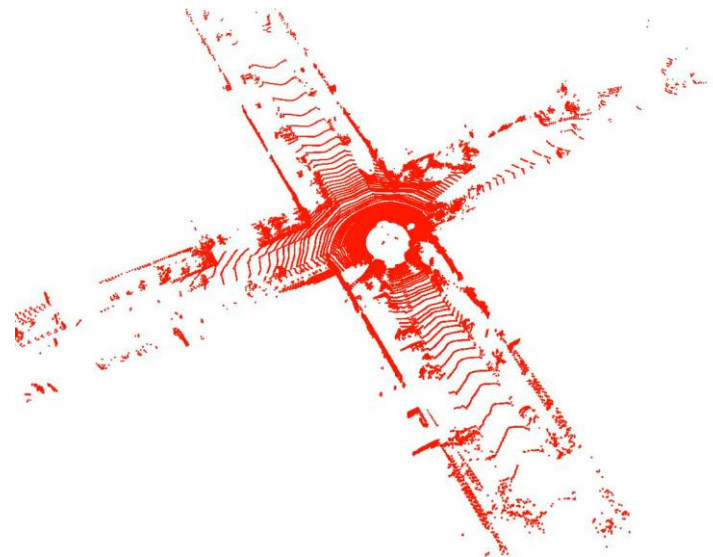


# Summary of Place Recognition

- Place recognition is a data retrieval problem
- Scan Context could handle most LiDAR place recognition cases
- Many issues for information-rich visual place recognition

For the SLAM problem

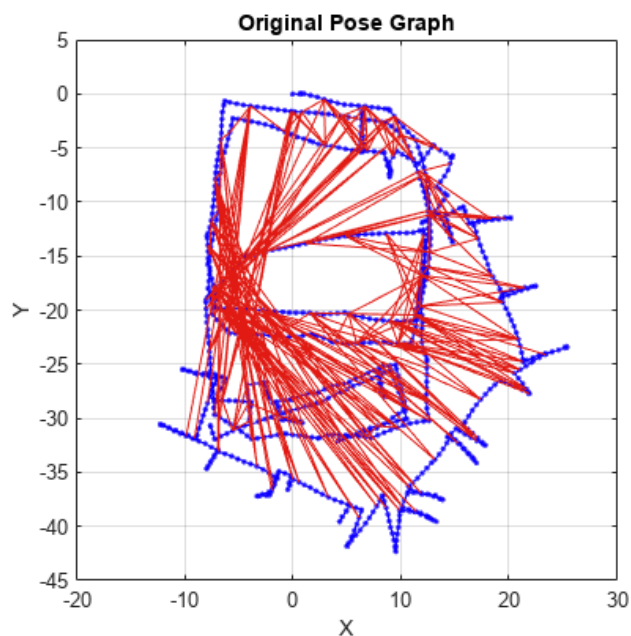
- In medium/large-scale environments, **place recognition and pose estimation** provides a **constraint** for robot poses



Pose Estimation by ICP

# Constraint

- A constraint is a relative transformation between two poses
- Can we refine the global mapping results from ICP odometry and EKF SLAM (w/o loop closing) with more constraints? (For high-precision mapping)



# Next Lecture

- Pose Graph SLAM
  - one of the state-of-the-art mapping frameworks
  - not recursive filter, a batch processing approach
  - we study a 2D dense laser-based case

