

Coordinates

$$Co : (\frac{1}{3}, \frac{2}{3}, \frac{1}{6}), (1, 1, \frac{1}{2}), (\frac{2}{3}, \frac{1}{3}, \frac{5}{6})$$

$$O : (0, 0, \frac{23959}{100000}), (\frac{2}{3}, \frac{1}{3}, \frac{3}{32}), (\frac{2}{3}, \frac{1}{3}, \frac{14323}{25000}), (\frac{1}{3}, \frac{2}{3}, \frac{10677}{25000}), (\frac{1}{3}, \frac{2}{3}, \frac{29}{32}), (0, 0, \frac{76041}{100000})$$

$$Li : (0, 0, 0), (\frac{2}{3}, \frac{1}{3}, \frac{1}{3}), (\frac{1}{3}, \frac{2}{3}, \frac{2}{3})$$

$$\begin{aligned} Reflections : & (0, 0, 1), (0, 0, 2), (0, 0, 3), (0, 0, 4), (1, 0, 0), (1, 0, 1), \\ & (1, 0, 2), (1, 0, 3), (2, 1, 0), (1, 1, 1), (1, 1, 2), (1, 1, 3), \\ & (2, 0, 0), (2, 0, 1), (2, 0, 2), (2, 0, 3), (2, 1, 0), (2, 1, 1), \\ & (2, 1, 2), (2, 1, 3), (3, 0, 0), (3, 0, 1), (3, 0, 2) \end{aligned}$$

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$$\begin{aligned} F_{hkl} = & f_{Co}(e^{2\pi i(\frac{h}{3} + \frac{2k}{3} + \frac{l}{6})} + e^{2\pi i(h+k+\frac{l}{2})} + e^{2\pi i(\frac{2h}{3} + \frac{k}{3} + \frac{5l}{6})}) \\ & + f_O(e^{2\pi i(0+0+\frac{23959l}{100000})} + e^{2\pi i(\frac{2h}{3} + \frac{k}{3} + \frac{3l}{32})} + e^{2\pi i(\frac{2h}{3} + \frac{k}{3} + \frac{14323l}{25000})} + e^{2\pi i(\frac{h}{3} + \frac{2k}{3} + \frac{10677l}{25000})} \\ & + e^{2\pi i(\frac{h}{3} + \frac{2k}{3} + \frac{29l}{32})} + e^{2\pi i(0+0+\frac{76041l}{100000})}) \\ & + f_{Li}(e^{2\pi i(0+0+0)} + e^{2\pi i(\frac{2h}{3} + \frac{k}{3} + \frac{l}{3})} + e^{2\pi i(\frac{h}{3} + \frac{2k}{3} + \frac{2l}{3})}) \\ = & f_{Co}(e^{2\pi i(\frac{h}{3} + \frac{2k}{3} + \frac{l}{6})} + e^{2\pi i(h+k+\frac{l}{2})} + e^{2\pi i(\frac{2h}{3} + \frac{k}{3} + \frac{5l}{6})}) \\ & + f_O(e^{2\pi i(\frac{23959l}{100000})} + e^{2\pi i(\frac{2h}{3} + \frac{k}{3} + \frac{3l}{32})} + e^{2\pi i(\frac{2h}{3} + \frac{k}{3} + \frac{14323l}{25000})} + e^{2\pi i(\frac{h}{3} + \frac{2k}{3} + \frac{10677l}{25000})} \\ & + e^{2\pi i(\frac{h}{3} + \frac{2k}{3} + \frac{29l}{32})} + e^{2\pi i(\frac{76041l}{100000})}) \\ & + f_{Li}(e^{2\pi i(0)} + e^{2\pi i(\frac{2h}{3} + \frac{k}{3} + \frac{l}{3})} + e^{2\pi i(\frac{h}{3} + \frac{2k}{3} + \frac{2l}{3})}) \end{aligned}$$

$$\begin{aligned}
F_{001} &= f_{Co}(e^{2\pi i(\frac{0}{3} + \frac{2.0}{3} + \frac{1}{6})} + e^{2\pi i(0+0+\frac{1}{2})} + e^{2\pi i(\frac{2.0}{3} + \frac{0}{3} + \frac{5.1}{6})}) \\
&\quad + f_O(e^{2\pi i(0+0+\frac{23959.1}{100000})} + e^{2\pi i(\frac{2.0}{3} + \frac{0}{3} + \frac{3.1}{32})} + e^{2\pi i(\frac{2.0}{3} + \frac{0}{3} + \frac{14323.1}{25000})} + e^{2\pi i(\frac{0}{3} + \frac{2.0}{3} + \frac{10677.1}{25000})}) \\
&\quad + e^{2\pi i(\frac{0}{3} + \frac{2.0}{3} + \frac{29.1}{32})} + e^{2\pi i(0+0+\frac{76041.1}{100000})}) \\
&\quad + f_{Li}(e^{2\pi i(0+0+0)} + e^{2\pi i(\frac{2.0}{3} + \frac{0}{3} + \frac{1}{3})} + e^{2\pi i(\frac{0}{3} + \frac{2.0}{3} + \frac{2.1}{3})}) \\
&= f_{Co}(e^{2\pi i(\frac{0}{3} + \frac{2.0}{3} + \frac{1}{6})} + e^{2\pi i(0+0+\frac{1}{2})} + e^{2\pi i(\frac{2.0}{3} + \frac{0}{3} + \frac{5.1}{6})}) \\
&\quad + f_O(e^{2\pi i(\frac{23959.1}{100000})} + e^{2\pi i(\frac{2.0}{3} + \frac{0}{3} + \frac{3.1}{32})} + e^{2\pi i(\frac{2.0}{3} + \frac{0}{3} + \frac{14323.1}{25000})} + e^{2\pi i(\frac{0}{3} + \frac{2.0}{3} + \frac{10677.1}{25000})}) \\
&\quad + e^{2\pi i(\frac{0}{3} + \frac{2.0}{3} + \frac{29.1}{32})} + e^{2\pi i(\frac{76041.1}{100000})}) \\
&\quad + f_{Li}(e^{2\pi i(0)} + e^{2\pi i(\frac{2.0}{3} + \frac{0}{3} + \frac{1}{3})} + e^{2\pi i(\frac{0}{3} + \frac{2.0}{3} + \frac{2.1}{3})}) \\
&= f_{Co}(e^{2\pi i(\frac{1}{6})} + e^{2\pi i(\frac{1}{2})} + e^{2\pi i(\frac{5}{6})}) \\
&\quad + f_O(e^{2\pi i(\frac{23959}{100000})} + e^{2\pi i(\frac{3}{32})} + e^{2\pi i(\frac{14323}{25000})} + e^{2\pi i(\frac{10677}{25000})}) \\
&\quad + e^{2\pi i(\frac{29}{32})} + e^{2\pi i(\frac{76041}{100000})}) \\
&\quad + f_{Li}(e^{2\pi i(0)} + e^{2\pi i(\frac{1}{3})} + e^{2\pi i(\frac{2}{3})}) \\
&= f_{Co}([0.5 + (0.86603)i] + -1 + [0.5 + (-0.86603)i]) \\
&\quad + f_O([0.06536 + (0.99786)i] + [0.83147 + (0.55557)i] \\
&\quad + [-0.89686 + (-0.44231)i] + [-0.89686 + (0.44231)i] \\
&\quad + [0.83147 + (-0.55557)i] + [0.06536 + (-0.99786)i]) \\
&\quad + f_{Li}(1 + [-0.5 + (0.86603)i] + [-0.5 + (-0.86603)i]) \\
&= 6.506960965675657e - 05f_O
\end{aligned}$$

$$\begin{aligned}
F_{002} &= f_{Co}(e^{2\pi i(\frac{0}{3} + \frac{2.0}{3} + \frac{2}{6})} + e^{2\pi i(0+0+\frac{2}{2})} + e^{2\pi i(\frac{2.0}{3} + \frac{0}{3} + \frac{5.2}{6})}) \\
&\quad + f_O(e^{2\pi i(0+0+\frac{23959.2}{100000})} + e^{2\pi i(\frac{2.0}{3} + \frac{0}{3} + \frac{3.2}{32})} + e^{2\pi i(\frac{2.0}{3} + \frac{0}{3} + \frac{14323.2}{25000})} + e^{2\pi i(\frac{0}{3} + \frac{2.0}{3} + \frac{10677.2}{25000})}) \\
&\quad + e^{2\pi i(\frac{0}{3} + \frac{2.0}{3} + \frac{29.2}{32})} + e^{2\pi i(0+0+\frac{76041.2}{100000})}) \\
&\quad + f_{Li}(e^{2\pi i(0+0+0)} + e^{2\pi i(\frac{2.0}{3} + \frac{0}{3} + \frac{2}{3})} + e^{2\pi i(\frac{0}{3} + \frac{2.0}{3} + \frac{2.2}{3})}) \\
&= f_{Co}(e^{2\pi i(\frac{0}{3} + \frac{2.0}{3} + \frac{2}{6})} + e^{2\pi i(0+0+\frac{2}{2})} + e^{2\pi i(\frac{2.0}{3} + \frac{0}{3} + \frac{5.2}{6})}) \\
&\quad + f_O(e^{2\pi i(\frac{23959.2}{100000})} + e^{2\pi i(\frac{2.0}{3} + \frac{0}{3} + \frac{3.2}{32})} + e^{2\pi i(\frac{2.0}{3} + \frac{0}{3} + \frac{14323.2}{25000})} + e^{2\pi i(\frac{0}{3} + \frac{2.0}{3} + \frac{10677.2}{25000})}) \\
&\quad + e^{2\pi i(\frac{0}{3} + \frac{2.0}{3} + \frac{29.2}{32})} + e^{2\pi i(\frac{76041.2}{100000})}) \\
&\quad + f_{Li}(e^{2\pi i(0)} + e^{2\pi i(\frac{2.0}{3} + \frac{0}{3} + \frac{2}{3})} + e^{2\pi i(\frac{0}{3} + \frac{2.0}{3} + \frac{2.2}{3})}) \\
&= f_{Co}(e^{2\pi i(\frac{1}{3})} + e^{2\pi i(1)} + e^{2\pi i(\frac{5}{3})}) \\
&\quad + f_O(e^{2\pi i(\frac{23959}{50000})} + e^{2\pi i(\frac{3}{16})} + e^{2\pi i(\frac{14323}{12500})} + e^{2\pi i(\frac{10677}{12500})}) \\
&\quad + e^{2\pi i(\frac{29}{16})} + e^{2\pi i(\frac{76041}{50000})}) \\
&\quad + f_{Li}(e^{2\pi i(0)} + e^{2\pi i(\frac{2}{3})} + e^{2\pi i(\frac{4}{3})}) \\
&= f_{Co}([-0.5 + (0.86603)i] + 1 + [-0.5 + (-0.86603)i]) \\
&\quad + f_O([-0.99146 + (0.13044)i] + [0.38268 + (0.92388)i] \\
&\quad + [0.60873 + (0.79338)i] + [0.60873 + (-0.79338)i] \\
&\quad + [0.38268 + (-0.92388)i] + [-0.99146 + (-0.13044)i]) \\
&\quad + f_{Li}(1 + [-0.5 + (-0.86603)i] + [-0.5 + (0.86603)i]) \\
&= 8.83277971748253e - 05f_O
\end{aligned}$$

$$\begin{aligned}
F_{003} &= f_{Co}(e^{2\pi i(\frac{0}{3} + \frac{2.0}{3} + \frac{3}{6})} + e^{2\pi i(0+0+\frac{3}{2})} + e^{2\pi i(\frac{2.0}{3} + \frac{0}{3} + \frac{5.3}{6})}) \\
&\quad + f_O(e^{2\pi i(0+0+\frac{23959.3}{100000})} + e^{2\pi i(\frac{2.0}{3} + \frac{0}{3} + \frac{3.3}{32})} + e^{2\pi i(\frac{2.0}{3} + \frac{0}{3} + \frac{14323.3}{25000})} + e^{2\pi i(\frac{0}{3} + \frac{2.0}{3} + \frac{10677.3}{25000})}) \\
&\quad + e^{2\pi i(\frac{0}{3} + \frac{2.0}{3} + \frac{29.3}{32})} + e^{2\pi i(0+0+\frac{76041.3}{100000})}) \\
&\quad + f_{Li}(e^{2\pi i(0+0+0)} + e^{2\pi i(\frac{2.0}{3} + \frac{0}{3} + \frac{3}{3})} + e^{2\pi i(\frac{0}{3} + \frac{2.0}{3} + \frac{2.3}{3})}) \\
&= f_{Co}(e^{2\pi i(\frac{0}{3} + \frac{2.0}{3} + \frac{3}{6})} + e^{2\pi i(0+0+\frac{3}{2})} + e^{2\pi i(\frac{2.0}{3} + \frac{0}{3} + \frac{5.3}{6})}) \\
&\quad + f_O(e^{2\pi i(\frac{23959.3}{100000})} + e^{2\pi i(\frac{2.0}{3} + \frac{0}{3} + \frac{3.3}{32})} + e^{2\pi i(\frac{2.0}{3} + \frac{0}{3} + \frac{14323.3}{25000})} + e^{2\pi i(\frac{0}{3} + \frac{2.0}{3} + \frac{10677.3}{25000})}) \\
&\quad + e^{2\pi i(\frac{0}{3} + \frac{2.0}{3} + \frac{29.3}{32})} + e^{2\pi i(\frac{76041.3}{100000})}) \\
&\quad + f_{Li}(e^{2\pi i(0)} + e^{2\pi i(\frac{2.0}{3} + \frac{0}{3} + \frac{3}{3})} + e^{2\pi i(\frac{0}{3} + \frac{2.0}{3} + \frac{2.3}{3})}) \\
&= f_{Co}(e^{2\pi i(\frac{1}{2})} + e^{2\pi i(\frac{3}{2})} + e^{2\pi i(\frac{5}{2})}) \\
&\quad + f_O(e^{2\pi i(\frac{71877}{100000})} + e^{2\pi i(\frac{9}{32})} + e^{2\pi i(\frac{42969}{25000})} + e^{2\pi i(\frac{32031}{25000})}) \\
&\quad + e^{2\pi i(\frac{87}{32})} + e^{2\pi i(\frac{2.2812}{1})}) \\
&\quad + f_{Li}(e^{2\pi i(0)} + e^{2\pi i(1)} + e^{2\pi i(2)}) \\
&= f_{Co}(-1 + -1 + -1) \\
&\quad + f_O([-0.19497 + (-0.98081)i] + [-0.19509 + (0.98079)i] \\
&\quad + [-0.19503 + (-0.9808)i] + [-0.19503 + (0.9808)i] \\
&\quad + [-0.19509 + (-0.98079)i] + [-0.19497 + (0.98081)i]) \\
&\quad + f_{Li}(1 + 1 + 1) \\
&= 3f_{Co} - 1.1701721809067713f_O + 3f_{Li}
\end{aligned}$$

$$\begin{aligned}
F_{004} &= f_{Co}(e^{2\pi i(\frac{0}{3} + \frac{2.0}{3} + \frac{4}{6})} + e^{2\pi i(0+0+\frac{4}{2})} + e^{2\pi i(\frac{2.0}{3} + \frac{0}{3} + \frac{5.4}{6})}) \\
&\quad + f_O(e^{2\pi i(0+0+\frac{23959.4}{100000})} + e^{2\pi i(\frac{2.0}{3} + \frac{0}{3} + \frac{3.4}{32})} + e^{2\pi i(\frac{2.0}{3} + \frac{0}{3} + \frac{14323.4}{25000})} + e^{2\pi i(\frac{0}{3} + \frac{2.0}{3} + \frac{10677.4}{25000})}) \\
&\quad + e^{2\pi i(\frac{0}{3} + \frac{2.0}{3} + \frac{29.4}{32})} + e^{2\pi i(0+0+\frac{76041.4}{100000})}) \\
&\quad + f_{Li}(e^{2\pi i(0+0+0)} + e^{2\pi i(\frac{2.0}{3} + \frac{0}{3} + \frac{4}{3})} + e^{2\pi i(\frac{0}{3} + \frac{2.0}{3} + \frac{2.4}{3})}) \\
&= f_{Co}(e^{2\pi i(\frac{0}{3} + \frac{2.0}{3} + \frac{4}{6})} + e^{2\pi i(0+0+\frac{4}{2})} + e^{2\pi i(\frac{2.0}{3} + \frac{0}{3} + \frac{5.4}{6})}) \\
&\quad + f_O(e^{2\pi i(\frac{23959.4}{100000})} + e^{2\pi i(\frac{2.0}{3} + \frac{0}{3} + \frac{3.4}{32})} + e^{2\pi i(\frac{2.0}{3} + \frac{0}{3} + \frac{14323.4}{25000})} + e^{2\pi i(\frac{0}{3} + \frac{2.0}{3} + \frac{10677.4}{25000})}) \\
&\quad + e^{2\pi i(\frac{0}{3} + \frac{2.0}{3} + \frac{29.4}{32})} + e^{2\pi i(\frac{76041.4}{100000})}) \\
&\quad + f_{Li}(e^{2\pi i(0)} + e^{2\pi i(\frac{2.0}{3} + \frac{0}{3} + \frac{4}{3})} + e^{2\pi i(\frac{0}{3} + \frac{2.0}{3} + \frac{2.4}{3})}) \\
&= f_{Co}(e^{2\pi i(\frac{2}{3})} + e^{2\pi i(2)} + e^{2\pi i(\frac{10}{3})}) \\
&\quad + f_O(e^{2\pi i(\frac{23959}{25000})} + e^{2\pi i(\frac{3}{8})} + e^{2\pi i(\frac{14323}{6250})} + e^{2\pi i(\frac{10677}{6250})}) \\
&\quad + e^{2\pi i(\frac{29}{8})} + e^{2\pi i(\frac{76041}{25000})}) \\
&\quad + f_{Li}(e^{2\pi i(0)} + e^{2\pi i(\frac{4}{3})} + e^{2\pi i(\frac{8}{3})}) \\
&= f_{Co}([-0.5 + (-0.86603)i] + 1 + [-0.5 + (0.86603)i]) \\
&\quad + f_O([0.96597 + (-0.25866)i] + [-0.70711 + (0.70711)i] \\
&\quad + [-0.2589 + (0.9659)i] + [-0.2589 + (-0.9659)i] \\
&\quad + [-0.70711 + (-0.70711)i] + [0.96597 + (0.25866)i]) \\
&\quad + f_{Li}(1 + [-0.5 + (0.86603)i] + [-0.5 + (-0.86603)i]) \\
&= 7.513663179392616e - 05 f_O
\end{aligned}$$

$$\begin{aligned}
F_{100} &= f_{Co}(e^{2\pi i(\frac{1}{3} + \frac{2.0}{3} + \frac{0}{6})} + e^{2\pi i(1+0+\frac{0}{2})} + e^{2\pi i(\frac{2.1}{3} + \frac{0}{3} + \frac{5.0}{6})}) \\
&\quad + f_O(e^{2\pi i(0+0+\frac{23959.0}{100000})} + e^{2\pi i(\frac{2.1}{3} + \frac{0}{3} + \frac{3.0}{32})} + e^{2\pi i(\frac{2.1}{3} + \frac{0}{3} + \frac{14323.0}{25000})} + e^{2\pi i(\frac{1}{3} + \frac{2.0}{3} + \frac{10677.0}{25000})}) \\
&\quad + e^{2\pi i(\frac{1}{3} + \frac{2.0}{3} + \frac{29.0}{32})} + e^{2\pi i(0+0+\frac{76041.0}{100000})}) \\
&\quad + f_{Li}(e^{2\pi i(0+0+0)} + e^{2\pi i(\frac{2.1}{3} + \frac{0}{3} + \frac{0}{3})} + e^{2\pi i(\frac{1}{3} + \frac{2.0}{3} + \frac{2.0}{3})}) \\
&= f_{Co}(e^{2\pi i(\frac{1}{3} + \frac{2.0}{3} + \frac{0}{6})} + e^{2\pi i(1+0+\frac{0}{2})} + e^{2\pi i(\frac{2.1}{3} + \frac{0}{3} + \frac{5.0}{6})}) \\
&\quad + f_O(e^{2\pi i(\frac{23959.0}{100000})} + e^{2\pi i(\frac{2.1}{3} + \frac{0}{3} + \frac{3.0}{32})} + e^{2\pi i(\frac{2.1}{3} + \frac{0}{3} + \frac{14323.0}{25000})} + e^{2\pi i(\frac{1}{3} + \frac{2.0}{3} + \frac{10677.0}{25000})}) \\
&\quad + e^{2\pi i(\frac{1}{3} + \frac{2.0}{3} + \frac{29.0}{32})} + e^{2\pi i(\frac{76041.0}{100000})}) \\
&\quad + f_{Li}(e^{2\pi i(0)} + e^{2\pi i(\frac{2.1}{3} + \frac{0}{3} + \frac{0}{3})} + e^{2\pi i(\frac{1}{3} + \frac{2.0}{3} + \frac{2.0}{3})}) \\
&= f_{Co}(e^{2\pi i(\frac{1}{3})} + e^{2\pi i(1)} + e^{2\pi i(\frac{2}{3})}) \\
&\quad + f_O(e^{2\pi i(0)} + e^{2\pi i(\frac{2}{3})} + e^{2\pi i(\frac{2}{3})} + e^{2\pi i(\frac{1}{3})}) \\
&\quad + e^{2\pi i(\frac{1}{3})} + e^{2\pi i(0)}) \\
&\quad + f_{Li}(e^{2\pi i(0)} + e^{2\pi i(\frac{2}{3})} + e^{2\pi i(\frac{1}{3})}) \\
&= f_{Co}([-0.5 + (0.86603)i] + 1 + [-0.5 + (-0.86603)i]) \\
&\quad + f_O(1 + [-0.5 + (-0.86603)i] + [-0.5 + (-0.86603)i] \\
&\quad + [-0.5 + (0.86603)i] + [-0.5 + (0.86603)i] \\
&\quad + 1) \\
&\quad + f_{Li}(1 + [-0.5 + (-0.86603)i] + [-0.5 + (0.86603)i]) \\
&= 0(ForbiddenReflection)
\end{aligned}$$

$$\begin{aligned}
F_{101} &= f_{Co}(e^{2\pi i(\frac{1}{3} + \frac{2 \cdot 0}{3} + \frac{1}{6})} + e^{2\pi i(1+0+\frac{1}{2})} + e^{2\pi i(\frac{2 \cdot 1}{3} + \frac{0}{3} + \frac{5 \cdot 1}{6})}) \\
&\quad + f_O(e^{2\pi i(0+0+\frac{23959 \cdot 1}{100000})} + e^{2\pi i(\frac{2 \cdot 1}{3} + \frac{0}{3} + \frac{3 \cdot 1}{32})} + e^{2\pi i(\frac{2 \cdot 1}{3} + \frac{0}{3} + \frac{14323 \cdot 1}{25000})} + e^{2\pi i(\frac{1}{3} + \frac{2 \cdot 0}{3} + \frac{10677 \cdot 1}{25000})}) \\
&\quad + e^{2\pi i(\frac{1}{3} + \frac{2 \cdot 0}{3} + \frac{29 \cdot 1}{32})} + e^{2\pi i(0+0+\frac{76041 \cdot 1}{100000})}) \\
&\quad + f_{Li}(e^{2\pi i(0+0+0)} + e^{2\pi i(\frac{2 \cdot 1}{3} + \frac{0}{3} + \frac{1}{3})} + e^{2\pi i(\frac{1}{3} + \frac{2 \cdot 0}{3} + \frac{2 \cdot 1}{3})}) \\
&= f_{Co}(e^{2\pi i(\frac{1}{3} + \frac{2 \cdot 0}{3} + \frac{1}{6})} + e^{2\pi i(1+0+\frac{1}{2})} + e^{2\pi i(\frac{2 \cdot 1}{3} + \frac{0}{3} + \frac{5 \cdot 1}{6})}) \\
&\quad + f_O(e^{2\pi i(\frac{23959 \cdot 1}{100000})} + e^{2\pi i(\frac{2 \cdot 1}{3} + \frac{0}{3} + \frac{3 \cdot 1}{32})} + e^{2\pi i(\frac{2 \cdot 1}{3} + \frac{0}{3} + \frac{14323 \cdot 1}{25000})} + e^{2\pi i(\frac{1}{3} + \frac{2 \cdot 0}{3} + \frac{10677 \cdot 1}{25000})}) \\
&\quad + e^{2\pi i(\frac{1}{3} + \frac{2 \cdot 0}{3} + \frac{29 \cdot 1}{32})} + e^{2\pi i(\frac{76041 \cdot 1}{100000})}) \\
&\quad + f_{Li}(e^{2\pi i(0)} + e^{2\pi i(\frac{2 \cdot 1}{3} + \frac{0}{3} + \frac{1}{3})} + e^{2\pi i(\frac{1}{3} + \frac{2 \cdot 0}{3} + \frac{2 \cdot 1}{3})}) \\
&= f_{Co}(e^{2\pi i(\frac{1}{2})} + e^{2\pi i(\frac{3}{2})} + e^{2\pi i(\frac{3}{2})}) \\
&\quad + f_O(e^{2\pi i(\frac{23959}{100000})} + e^{2\pi i(\frac{73}{96})} + e^{2\pi i(\frac{92969}{75000})} + e^{2\pi i(\frac{57031}{75000})}) \\
&\quad + e^{2\pi i(\frac{119}{96})} + e^{2\pi i(\frac{76041}{100000})}) \\
&\quad + f_{Li}(e^{2\pi i(0)} + e^{2\pi i(1)} + e^{2\pi i(1)}) \\
&= f_{Co}(-1 + -1 + -1) \\
&\quad + f_O([0.06536 + (0.99786)i] + [0.0654 + (-0.99786)i] \\
&\quad + [0.06538 + (0.99786)i] + [0.06538 + (-0.99786)i] \\
&\quad + [0.0654 + (0.99786)i] + [0.06536 + (-0.99786)i]) \\
&\quad + f_{Li}(1 + 1 + 1) \\
&= 3f_{Co} + 0.3922933805869383f_O + 3f_{Li}
\end{aligned}$$

$$\begin{aligned}
F_{102} &= f_{Co}(e^{2\pi i(\frac{1}{3} + \frac{2.0}{3} + \frac{2}{6})} + e^{2\pi i(1+0+\frac{2}{2})} + e^{2\pi i(\frac{2.1}{3} + \frac{0}{3} + \frac{5.2}{6})}) \\
&\quad + f_O(e^{2\pi i(0+0+\frac{23959.2}{100000})} + e^{2\pi i(\frac{2.1}{3} + \frac{0}{3} + \frac{3.2}{32})} + e^{2\pi i(\frac{2.1}{3} + \frac{0}{3} + \frac{14323.2}{25000})} + e^{2\pi i(\frac{1}{3} + \frac{2.0}{3} + \frac{10677.2}{25000})}) \\
&\quad + e^{2\pi i(\frac{1}{3} + \frac{2.0}{3} + \frac{29.2}{32})} + e^{2\pi i(0+0+\frac{76041.2}{100000})}) \\
&\quad + f_{Li}(e^{2\pi i(0+0+0)} + e^{2\pi i(\frac{2.1}{3} + \frac{0}{3} + \frac{2}{3})} + e^{2\pi i(\frac{1}{3} + \frac{2.0}{3} + \frac{2.2}{3})}) \\
&= f_{Co}(e^{2\pi i(\frac{1}{3} + \frac{2.0}{3} + \frac{2}{6})} + e^{2\pi i(1+0+\frac{2}{2})} + e^{2\pi i(\frac{2.1}{3} + \frac{0}{3} + \frac{5.2}{6})}) \\
&\quad + f_O(e^{2\pi i(\frac{23959.2}{100000})} + e^{2\pi i(\frac{2.1}{3} + \frac{0}{3} + \frac{3.2}{32})} + e^{2\pi i(\frac{2.1}{3} + \frac{0}{3} + \frac{14323.2}{25000})} + e^{2\pi i(\frac{1}{3} + \frac{2.0}{3} + \frac{10677.2}{25000})}) \\
&\quad + e^{2\pi i(\frac{1}{3} + \frac{2.0}{3} + \frac{29.2}{32})} + e^{2\pi i(\frac{76041.2}{100000})}) \\
&\quad + f_{Li}(e^{2\pi i(0)} + e^{2\pi i(\frac{2.1}{3} + \frac{0}{3} + \frac{2}{3})} + e^{2\pi i(\frac{1}{3} + \frac{2.0}{3} + \frac{2.2}{3})}) \\
&= f_{Co}(e^{2\pi i(\frac{2}{3})} + e^{2\pi i(2)} + e^{2\pi i(\frac{7}{3})}) \\
&\quad + f_O(e^{2\pi i(\frac{23959}{50000})} + e^{2\pi i(\frac{41}{48})} + e^{2\pi i(\frac{67969}{37500})} + e^{2\pi i(\frac{44531}{37500})}) \\
&\quad + e^{2\pi i(\frac{103}{48})} + e^{2\pi i(\frac{76041}{50000})}) \\
&\quad + f_{Li}(e^{2\pi i(0)} + e^{2\pi i(\frac{4}{3})} + e^{2\pi i(\frac{5}{3})}) \\
&= f_{Co}([-0.5 + (-0.86603)i] + 1 + [-0.5 + (0.86603)i]) \\
&\quad + f_O([-0.99146 + (0.13044)i] + [0.60876 + (-0.79335)i] \\
&\quad + [0.38272 + (-0.92386)i] + [0.38272 + (0.92386)i] \\
&\quad + [0.60876 + (0.79335)i] + [-0.99146 + (-0.13044)i]) \\
&\quad + f_{Li}(1 + [-0.5 + (0.86603)i] + [-0.5 + (-0.86603)i]) \\
&= 5.553516419576354e - 05 f_O
\end{aligned}$$

$$\begin{aligned}
F_{103} &= f_{Co}(e^{2\pi i(\frac{1}{3} + \frac{2.0}{3} + \frac{3}{6})} + e^{2\pi i(1+0+\frac{3}{2})} + e^{2\pi i(\frac{2.1}{3} + \frac{0}{3} + \frac{5.3}{6})}) \\
&\quad + f_O(e^{2\pi i(0+0+\frac{23959.3}{100000})} + e^{2\pi i(\frac{2.1}{3} + \frac{0}{3} + \frac{3.3}{32})} + e^{2\pi i(\frac{2.1}{3} + \frac{0}{3} + \frac{14323.3}{25000})} + e^{2\pi i(\frac{1}{3} + \frac{2.0}{3} + \frac{10677.3}{25000})}) \\
&\quad + e^{2\pi i(\frac{1}{3} + \frac{2.0}{3} + \frac{29.3}{32})} + e^{2\pi i(0+0+\frac{76041.3}{100000})}) \\
&\quad + f_{Li}(e^{2\pi i(0+0+0)} + e^{2\pi i(\frac{2.1}{3} + \frac{0}{3} + \frac{3}{3})} + e^{2\pi i(\frac{1}{3} + \frac{2.0}{3} + \frac{2.3}{3})}) \\
&= f_{Co}(e^{2\pi i(\frac{1}{3} + \frac{2.0}{3} + \frac{3}{6})} + e^{2\pi i(1+0+\frac{3}{2})} + e^{2\pi i(\frac{2.1}{3} + \frac{0}{3} + \frac{5.3}{6})}) \\
&\quad + f_O(e^{2\pi i(\frac{23959.3}{100000})} + e^{2\pi i(\frac{2.1}{3} + \frac{0}{3} + \frac{3.3}{32})} + e^{2\pi i(\frac{2.1}{3} + \frac{0}{3} + \frac{14323.3}{25000})} + e^{2\pi i(\frac{1}{3} + \frac{2.0}{3} + \frac{10677.3}{25000})}) \\
&\quad + e^{2\pi i(\frac{1}{3} + \frac{2.0}{3} + \frac{29.3}{32})} + e^{2\pi i(\frac{76041.3}{100000})}) \\
&\quad + f_{Li}(e^{2\pi i(0)} + e^{2\pi i(\frac{2.1}{3} + \frac{0}{3} + \frac{3}{3})} + e^{2\pi i(\frac{1}{3} + \frac{2.0}{3} + \frac{2.3}{3})}) \\
&= f_{Co}(e^{2\pi i(\frac{5}{6})} + e^{2\pi i(\frac{5}{2})} + e^{2\pi i(\frac{19}{6})}) \\
&\quad + f_O(e^{2\pi i(\frac{71877}{100000})} + e^{2\pi i(\frac{91}{96})} + e^{2\pi i(\frac{2.3854}{1})} + e^{2\pi i(\frac{1.6146}{1})}) \\
&\quad + e^{2\pi i(\frac{293}{96})} + e^{2\pi i(\frac{2.2812}{1})}) \\
&\quad + f_{Li}(e^{2\pi i(0)} + e^{2\pi i(\frac{5}{3})} + e^{2\pi i(\frac{7}{3})}) \\
&= f_{Co}([0.5 + (-0.86603)i] + -1 + [0.5 + (0.86603)i]) \\
&\quad + f_O([-0.19497 + (-0.98081)i] + [0.94693 + (-0.32144)i] \\
&\quad + [-0.75188 + (0.6593)i] + [-0.75188 + (-0.6593)i] \\
&\quad + [0.94693 + (0.32144)i] + [-0.19497 + (0.98081)i]) \\
&\quad + f_{Li}(1 + [-0.5 + (-0.86603)i] + [-0.5 + (0.86603)i]) \\
&= 0.00016364843607136192f_O
\end{aligned}$$

$$\begin{aligned}
F_{210} &= f_{Co}(e^{2\pi i(\frac{2}{3} + \frac{2 \cdot 1}{3} + \frac{0}{6})} + e^{2\pi i(2+1+\frac{0}{2})} + e^{2\pi i(\frac{2 \cdot 2}{3} + \frac{1}{3} + \frac{5 \cdot 0}{6})}) \\
&\quad + f_O(e^{2\pi i(0+0+\frac{23959 \cdot 0}{100000})} + e^{2\pi i(\frac{2 \cdot 2}{3} + \frac{1}{3} + \frac{3 \cdot 0}{32})} + e^{2\pi i(\frac{2 \cdot 2}{3} + \frac{1}{3} + \frac{14323 \cdot 0}{25000})} + e^{2\pi i(\frac{2}{3} + \frac{2 \cdot 1}{3} + \frac{10677 \cdot 0}{25000})}) \\
&\quad + e^{2\pi i(\frac{2}{3} + \frac{2 \cdot 1}{3} + \frac{29 \cdot 0}{32})} + e^{2\pi i(0+0+\frac{76041 \cdot 0}{100000})}) \\
&\quad + f_{Li}(e^{2\pi i(0+0+0)} + e^{2\pi i(\frac{2 \cdot 2}{3} + \frac{1}{3} + \frac{0}{3})} + e^{2\pi i(\frac{2}{3} + \frac{2 \cdot 1}{3} + \frac{2 \cdot 0}{3})}) \\
&= f_{Co}(e^{2\pi i(\frac{2}{3} + \frac{2 \cdot 1}{3} + \frac{0}{6})} + e^{2\pi i(2+1+\frac{0}{2})} + e^{2\pi i(\frac{2 \cdot 2}{3} + \frac{1}{3} + \frac{5 \cdot 0}{6})}) \\
&\quad + f_O(e^{2\pi i(\frac{23959 \cdot 0}{100000})} + e^{2\pi i(\frac{2 \cdot 2}{3} + \frac{1}{3} + \frac{3 \cdot 0}{32})} + e^{2\pi i(\frac{2 \cdot 2}{3} + \frac{1}{3} + \frac{14323 \cdot 0}{25000})} + e^{2\pi i(\frac{2}{3} + \frac{2 \cdot 1}{3} + \frac{10677 \cdot 0}{25000})}) \\
&\quad + e^{2\pi i(\frac{2}{3} + \frac{2 \cdot 1}{3} + \frac{29 \cdot 0}{32})} + e^{2\pi i(\frac{76041 \cdot 0}{100000})}) \\
&\quad + f_{Li}(e^{2\pi i(0)} + e^{2\pi i(\frac{2 \cdot 2}{3} + \frac{1}{3} + \frac{0}{3})} + e^{2\pi i(\frac{2}{3} + \frac{2 \cdot 1}{3} + \frac{2 \cdot 0}{3})}) \\
&= f_{Co}(e^{2\pi i(\frac{4}{3})} + e^{2\pi i(3)} + e^{2\pi i(\frac{5}{3})}) \\
&\quad + f_O(e^{2\pi i(0)} + e^{2\pi i(\frac{5}{3})} + e^{2\pi i(\frac{5}{3})} + e^{2\pi i(\frac{4}{3})}) \\
&\quad + e^{2\pi i(\frac{4}{3})} + e^{2\pi i(0)}) \\
&\quad + f_{Li}(e^{2\pi i(0)} + e^{2\pi i(\frac{5}{3})} + e^{2\pi i(\frac{4}{3})}) \\
&= f_{Co}([-0.5 + (0.86603)i] + 1 + [-0.5 + (-0.86603)i]) \\
&\quad + f_O(1 + [-0.5 + (-0.86603)i] + [-0.5 + (-0.86603)i] \\
&\quad + [-0.5 + (0.86603)i] + [-0.5 + (0.86603)i] \\
&\quad + 1) \\
&\quad + f_{Li}(1 + [-0.5 + (-0.86603)i] + [-0.5 + (0.86603)i]) \\
&= 0(ForbiddenReflection)
\end{aligned}$$

$$\begin{aligned}
F_{111} &= f_{Co}(e^{2\pi i(\frac{1}{3} + \frac{2 \cdot 1}{3} + \frac{1}{6})} + e^{2\pi i(1+1+\frac{1}{2})} + e^{2\pi i(\frac{2 \cdot 1}{3} + \frac{1}{3} + \frac{5 \cdot 1}{6})}) \\
&\quad + f_O(e^{2\pi i(0+0+\frac{23959 \cdot 1}{100000})} + e^{2\pi i(\frac{2 \cdot 1}{3} + \frac{1}{3} + \frac{3 \cdot 1}{32})} + e^{2\pi i(\frac{2 \cdot 1}{3} + \frac{1}{3} + \frac{14323 \cdot 1}{25000})} + e^{2\pi i(\frac{1}{3} + \frac{2 \cdot 1}{3} + \frac{10677 \cdot 1}{25000})}) \\
&\quad + e^{2\pi i(\frac{1}{3} + \frac{2 \cdot 1}{3} + \frac{29 \cdot 1}{32})} + e^{2\pi i(0+0+\frac{76041 \cdot 1}{100000})}) \\
&\quad + f_{Li}(e^{2\pi i(0+0+0)} + e^{2\pi i(\frac{2 \cdot 1}{3} + \frac{1}{3} + \frac{1}{3})} + e^{2\pi i(\frac{1}{3} + \frac{2 \cdot 1}{3} + \frac{2 \cdot 1}{3})}) \\
&= f_{Co}(e^{2\pi i(\frac{1}{3} + \frac{2 \cdot 1}{3} + \frac{1}{6})} + e^{2\pi i(1+1+\frac{1}{2})} + e^{2\pi i(\frac{2 \cdot 1}{3} + \frac{1}{3} + \frac{5 \cdot 1}{6})}) \\
&\quad + f_O(e^{2\pi i(\frac{23959 \cdot 1}{100000})} + e^{2\pi i(\frac{2 \cdot 1}{3} + \frac{1}{3} + \frac{3 \cdot 1}{32})} + e^{2\pi i(\frac{2 \cdot 1}{3} + \frac{1}{3} + \frac{14323 \cdot 1}{25000})} + e^{2\pi i(\frac{1}{3} + \frac{2 \cdot 1}{3} + \frac{10677 \cdot 1}{25000})}) \\
&\quad + e^{2\pi i(\frac{1}{3} + \frac{2 \cdot 1}{3} + \frac{29 \cdot 1}{32})} + e^{2\pi i(\frac{76041 \cdot 1}{100000})}) \\
&\quad + f_{Li}(e^{2\pi i(0)} + e^{2\pi i(\frac{2 \cdot 1}{3} + \frac{1}{3} + \frac{1}{3})} + e^{2\pi i(\frac{1}{3} + \frac{2 \cdot 1}{3} + \frac{2 \cdot 1}{3})}) \\
&= f_{Co}(e^{2\pi i(\frac{7}{6})} + e^{2\pi i(\frac{5}{2})} + e^{2\pi i(\frac{11}{6})}) \\
&\quad + f_O(e^{2\pi i(\frac{23959}{100000})} + e^{2\pi i(\frac{35}{32})} + e^{2\pi i(\frac{39323}{25000})} + e^{2\pi i(\frac{35677}{25000})}) \\
&\quad + e^{2\pi i(\frac{61}{32})} + e^{2\pi i(\frac{76041}{100000})}) \\
&\quad + f_{Li}(e^{2\pi i(0)} + e^{2\pi i(\frac{4}{3})} + e^{2\pi i(\frac{5}{3})}) \\
&= f_{Co}([0.5 + (0.86603)i] + -1 + [0.5 + (-0.86603)i]) \\
&\quad + f_O([0.06536 + (0.99786)i] + [0.83147 + (0.55557)i] \\
&\quad + [-0.89686 + (-0.44231)i] + [-0.89686 + (0.44231)i] \\
&\quad + [0.83147 + (-0.55557)i] + [0.06536 + (-0.99786)i]) \\
&\quad + f_{Li}(1 + [-0.5 + (0.86603)i] + [-0.5 + (-0.86603)i]) \\
&= 6.506960965786679e - 05 f_O
\end{aligned}$$

$$\begin{aligned}
F_{112} &= f_{Co}(e^{2\pi i(\frac{1}{3} + \frac{2}{3} + \frac{2}{6})} + e^{2\pi i(1+1+\frac{2}{2})} + e^{2\pi i(\frac{2}{3} + \frac{1}{3} + \frac{5}{6})}) \\
&\quad + f_O(e^{2\pi i(0+0+\frac{23959 \cdot 2}{100000})} + e^{2\pi i(\frac{2}{3} + \frac{1}{3} + \frac{3 \cdot 2}{32})} + e^{2\pi i(\frac{2}{3} + \frac{1}{3} + \frac{14323 \cdot 2}{25000})} + e^{2\pi i(\frac{1}{3} + \frac{2}{3} + \frac{10677 \cdot 2}{25000})} \\
&\quad + e^{2\pi i(\frac{1}{3} + \frac{2}{3} + \frac{29 \cdot 2}{32})} + e^{2\pi i(0+0+\frac{76041 \cdot 2}{100000})}) \\
&\quad + f_{Li}(e^{2\pi i(0+0+0)} + e^{2\pi i(\frac{2}{3} + \frac{1}{3} + \frac{2}{3})} + e^{2\pi i(\frac{1}{3} + \frac{2}{3} + \frac{2}{3})}) \\
&= f_{Co}(e^{2\pi i(\frac{1}{3} + \frac{2}{3} + \frac{2}{6})} + e^{2\pi i(1+1+\frac{2}{2})} + e^{2\pi i(\frac{2}{3} + \frac{1}{3} + \frac{5}{6})}) \\
&\quad + f_O(e^{2\pi i(\frac{23959 \cdot 2}{100000})} + e^{2\pi i(\frac{2}{3} + \frac{1}{3} + \frac{3 \cdot 2}{32})} + e^{2\pi i(\frac{2}{3} + \frac{1}{3} + \frac{14323 \cdot 2}{25000})} + e^{2\pi i(\frac{1}{3} + \frac{2}{3} + \frac{10677 \cdot 2}{25000})} \\
&\quad + e^{2\pi i(\frac{1}{3} + \frac{2}{3} + \frac{29 \cdot 2}{32})} + e^{2\pi i(\frac{76041 \cdot 2}{100000})}) \\
&\quad + f_{Li}(e^{2\pi i(0)} + e^{2\pi i(\frac{2}{3} + \frac{1}{3} + \frac{2}{3})} + e^{2\pi i(\frac{1}{3} + \frac{2}{3} + \frac{2}{3})}) \\
&= f_{Co}(e^{2\pi i(\frac{4}{3})} + e^{2\pi i(3)} + e^{2\pi i(\frac{8}{3})}) \\
&\quad + f_O(e^{2\pi i(\frac{23959}{50000})} + e^{2\pi i(\frac{19}{16})} + e^{2\pi i(\frac{26823}{12500})} + e^{2\pi i(\frac{23177}{12500})} \\
&\quad + e^{2\pi i(\frac{45}{16})} + e^{2\pi i(\frac{76041}{50000})}) \\
&\quad + f_{Li}(e^{2\pi i(0)} + e^{2\pi i(\frac{5}{3})} + e^{2\pi i(\frac{7}{3})}) \\
&= f_{Co}([-0.5 + (0.86603)i] + 1 + [-0.5 + (-0.86603)i]) \\
&\quad + f_O([-0.99146 + (0.13044)i] + [0.38268 + (0.92388)i] \\
&\quad + [0.60873 + (0.79338)i] + [0.60873 + (-0.79338)i] \\
&\quad + [0.38268 + (-0.92388)i] + [-0.99146 + (-0.13044)i]) \\
&\quad + f_{Li}(1 + [-0.5 + (-0.86603)i] + [-0.5 + (0.86603)i]) \\
&= 8.832779717460326e - 05 f_O
\end{aligned}$$

$$\begin{aligned}
F_{113} &= f_{Co}(e^{2\pi i(\frac{1}{3} + \frac{2 \cdot 1}{3} + \frac{3}{6})} + e^{2\pi i(1+1+\frac{3}{2})} + e^{2\pi i(\frac{2 \cdot 1}{3} + \frac{1}{3} + \frac{5 \cdot 3}{6})}) \\
&\quad + f_O(e^{2\pi i(0+0+\frac{23959 \cdot 3}{100000})} + e^{2\pi i(\frac{2 \cdot 1}{3} + \frac{1}{3} + \frac{3 \cdot 3}{32})} + e^{2\pi i(\frac{2 \cdot 1}{3} + \frac{1}{3} + \frac{14323 \cdot 3}{25000})} + e^{2\pi i(\frac{1}{3} + \frac{2 \cdot 1}{3} + \frac{10677 \cdot 3}{25000})}) \\
&\quad + e^{2\pi i(\frac{1}{3} + \frac{2 \cdot 1}{3} + \frac{29 \cdot 3}{32})} + e^{2\pi i(0+0+\frac{76041 \cdot 3}{100000})}) \\
&\quad + f_{Li}(e^{2\pi i(0+0+0)} + e^{2\pi i(\frac{2 \cdot 1}{3} + \frac{1}{3} + \frac{3}{3})} + e^{2\pi i(\frac{1}{3} + \frac{2 \cdot 1}{3} + \frac{2 \cdot 3}{3})}) \\
&= f_{Co}(e^{2\pi i(\frac{1}{3} + \frac{2 \cdot 1}{3} + \frac{3}{6})} + e^{2\pi i(1+1+\frac{3}{2})} + e^{2\pi i(\frac{2 \cdot 1}{3} + \frac{1}{3} + \frac{5 \cdot 3}{6})}) \\
&\quad + f_O(e^{2\pi i(\frac{23959 \cdot 3}{100000})} + e^{2\pi i(\frac{2 \cdot 1}{3} + \frac{1}{3} + \frac{3 \cdot 3}{32})} + e^{2\pi i(\frac{2 \cdot 1}{3} + \frac{1}{3} + \frac{14323 \cdot 3}{25000})} + e^{2\pi i(\frac{1}{3} + \frac{2 \cdot 1}{3} + \frac{10677 \cdot 3}{25000})}) \\
&\quad + e^{2\pi i(\frac{1}{3} + \frac{2 \cdot 1}{3} + \frac{29 \cdot 3}{32})} + e^{2\pi i(\frac{76041 \cdot 3}{100000})}) \\
&\quad + f_{Li}(e^{2\pi i(0)} + e^{2\pi i(\frac{2 \cdot 1}{3} + \frac{1}{3} + \frac{3}{3})} + e^{2\pi i(\frac{1}{3} + \frac{2 \cdot 1}{3} + \frac{2 \cdot 3}{3})}) \\
&= f_{Co}(e^{2\pi i(\frac{3}{2})} + e^{2\pi i(\frac{7}{2})} + e^{2\pi i(\frac{7}{2})}) \\
&\quad + f_O(e^{2\pi i(\frac{71877}{100000})} + e^{2\pi i(\frac{41}{32})} + e^{2\pi i(\frac{67969}{25000})} + e^{2\pi i(\frac{57031}{25000})}) \\
&\quad + e^{2\pi i(\frac{119}{32})} + e^{2\pi i(\frac{2 \cdot 2812}{1})}) \\
&\quad + f_{Li}(e^{2\pi i(0)} + e^{2\pi i(2)} + e^{2\pi i(3)}) \\
&= f_{Co}(-1 + -1 + -1) \\
&\quad + f_O([-0.19497 + (-0.98081)i] + [-0.19509 + (0.98079)i] \\
&\quad + [-0.19503 + (-0.9808)i] + [-0.19503 + (0.9808)i] \\
&\quad + [-0.19509 + (-0.98079)i] + [-0.19497 + (0.98081)i]) \\
&\quad + f_{Li}(1 + 1 + 1) \\
&= 3f_{Co} - 1.1701721809067727f_O + 3f_{Li}
\end{aligned}$$

$$\begin{aligned}
F_{200} &= f_{Co}(e^{2\pi i(\frac{2}{3} + \frac{2.0}{3} + \frac{0}{6})} + e^{2\pi i(2+0+\frac{0}{2})} + e^{2\pi i(\frac{2.2}{3} + \frac{0}{3} + \frac{5.0}{6})}) \\
&\quad + f_O(e^{2\pi i(0+0+\frac{23959.0}{100000})} + e^{2\pi i(\frac{2.2}{3} + \frac{0}{3} + \frac{3.0}{32})} + e^{2\pi i(\frac{2.2}{3} + \frac{0}{3} + \frac{14323.0}{25000})} + e^{2\pi i(\frac{2}{3} + \frac{2.0}{3} + \frac{10677.0}{25000})}) \\
&\quad + e^{2\pi i(\frac{2}{3} + \frac{2.0}{3} + \frac{29.0}{32})} + e^{2\pi i(0+0+\frac{76041.0}{100000})}) \\
&\quad + f_{Li}(e^{2\pi i(0+0+0)} + e^{2\pi i(\frac{2.2}{3} + \frac{0}{3} + \frac{0}{3})} + e^{2\pi i(\frac{2}{3} + \frac{2.0}{3} + \frac{2.0}{3})}) \\
&= f_{Co}(e^{2\pi i(\frac{2}{3} + \frac{2.0}{3} + \frac{0}{6})} + e^{2\pi i(2+0+\frac{0}{2})} + e^{2\pi i(\frac{2.2}{3} + \frac{0}{3} + \frac{5.0}{6})}) \\
&\quad + f_O(e^{2\pi i(\frac{23959.0}{100000})} + e^{2\pi i(\frac{2.2}{3} + \frac{0}{3} + \frac{3.0}{32})} + e^{2\pi i(\frac{2.2}{3} + \frac{0}{3} + \frac{14323.0}{25000})} + e^{2\pi i(\frac{2}{3} + \frac{2.0}{3} + \frac{10677.0}{25000})}) \\
&\quad + e^{2\pi i(\frac{2}{3} + \frac{2.0}{3} + \frac{29.0}{32})} + e^{2\pi i(\frac{76041.0}{100000})}) \\
&\quad + f_{Li}(e^{2\pi i(0)} + e^{2\pi i(\frac{2.2}{3} + \frac{0}{3} + \frac{0}{3})} + e^{2\pi i(\frac{2}{3} + \frac{2.0}{3} + \frac{2.0}{3})}) \\
&= f_{Co}(e^{2\pi i(\frac{2}{3})} + e^{2\pi i(2)} + e^{2\pi i(\frac{4}{3})}) \\
&\quad + f_O(e^{2\pi i(0)} + e^{2\pi i(\frac{4}{3})} + e^{2\pi i(\frac{4}{3})} + e^{2\pi i(\frac{2}{3})}) \\
&\quad + e^{2\pi i(\frac{2}{3})} + e^{2\pi i(0)}) \\
&\quad + f_{Li}(e^{2\pi i(0)} + e^{2\pi i(\frac{4}{3})} + e^{2\pi i(\frac{2}{3})}) \\
&= f_{Co}([-0.5 + (-0.86603)i] + 1 + [-0.5 + (0.86603)i]) \\
&\quad + f_O(1 + [-0.5 + (0.86603)i] + [-0.5 + (0.86603)i] \\
&\quad + [-0.5 + (-0.86603)i] + [-0.5 + (-0.86603)i] \\
&\quad + 1) \\
&\quad + f_{Li}(1 + [-0.5 + (0.86603)i] + [-0.5 + (-0.86603)i]) \\
&= 0(ForbiddenReflection)
\end{aligned}$$

$$\begin{aligned}
F_{201} &= f_{Co}(e^{2\pi i(\frac{2}{3} + \frac{2.0}{3} + \frac{1}{6})} + e^{2\pi i(2+0+\frac{1}{2})} + e^{2\pi i(\frac{2.2}{3} + \frac{0}{3} + \frac{5.1}{6})}) \\
&\quad + f_O(e^{2\pi i(0+0+\frac{23959.1}{100000})} + e^{2\pi i(\frac{2.2}{3} + \frac{0}{3} + \frac{3.1}{32})} + e^{2\pi i(\frac{2.2}{3} + \frac{0}{3} + \frac{14323.1}{25000})} + e^{2\pi i(\frac{2}{3} + \frac{2.0}{3} + \frac{10677.1}{25000})}) \\
&\quad + e^{2\pi i(\frac{2}{3} + \frac{2.0}{3} + \frac{29.1}{32})} + e^{2\pi i(0+0+\frac{76041.1}{100000})}) \\
&\quad + f_{Li}(e^{2\pi i(0+0+0)} + e^{2\pi i(\frac{2.2}{3} + \frac{0}{3} + \frac{1}{3})} + e^{2\pi i(\frac{2}{3} + \frac{2.0}{3} + \frac{2.1}{3})}) \\
&= f_{Co}(e^{2\pi i(\frac{2}{3} + \frac{2.0}{3} + \frac{1}{6})} + e^{2\pi i(2+0+\frac{1}{2})} + e^{2\pi i(\frac{2.2}{3} + \frac{0}{3} + \frac{5.1}{6})}) \\
&\quad + f_O(e^{2\pi i(\frac{23959.1}{100000})} + e^{2\pi i(\frac{2.2}{3} + \frac{0}{3} + \frac{3.1}{32})} + e^{2\pi i(\frac{2.2}{3} + \frac{0}{3} + \frac{14323.1}{25000})} + e^{2\pi i(\frac{2}{3} + \frac{2.0}{3} + \frac{10677.1}{25000})}) \\
&\quad + e^{2\pi i(\frac{2}{3} + \frac{2.0}{3} + \frac{29.1}{32})} + e^{2\pi i(\frac{76041.1}{100000})}) \\
&\quad + f_{Li}(e^{2\pi i(0)} + e^{2\pi i(\frac{2.2}{3} + \frac{0}{3} + \frac{1}{3})} + e^{2\pi i(\frac{2}{3} + \frac{2.0}{3} + \frac{2.1}{3})}) \\
&= f_{Co}(e^{2\pi i(\frac{5}{6})} + e^{2\pi i(\frac{5}{2})} + e^{2\pi i(\frac{13}{6})}) \\
&\quad + f_O(e^{2\pi i(\frac{23959}{100000})} + e^{2\pi i(\frac{137}{96})} + e^{2\pi i(\frac{1.9063}{1})} + e^{2\pi i(\frac{82031}{75000})}) \\
&\quad + e^{2\pi i(\frac{151}{96})} + e^{2\pi i(\frac{76041}{100000})}) \\
&\quad + f_{Li}(e^{2\pi i(0)} + e^{2\pi i(\frac{5}{3})} + e^{2\pi i(\frac{4}{3})}) \\
&= f_{Co}([0.5 + (-0.86603)i] + -1 + [0.5 + (0.86603)i]) \\
&\quad + f_O([0.06536 + (0.99786)i] + [-0.89687 + (0.44229)i] \\
&\quad + [0.83148 + (-0.55555)i] + [0.83148 + (0.55555)i] \\
&\quad + [-0.89687 + (-0.44229)i] + [0.06536 + (-0.99786)i]) \\
&\quad + f_{Li}(1 + [-0.5 + (-0.86603)i] + [-0.5 + (0.86603)i]) \\
&= 6.0325241624095693e - 05 f_O
\end{aligned}$$

$$\begin{aligned}
F_{202} &= f_{Co}(e^{2\pi i(\frac{2}{3} + \frac{2.0}{3} + \frac{2}{6})} + e^{2\pi i(2+0+\frac{2}{2})} + e^{2\pi i(\frac{2.2}{3} + \frac{0}{3} + \frac{5.2}{6})}) \\
&\quad + f_O(e^{2\pi i(0+0+\frac{23959.2}{100000})} + e^{2\pi i(\frac{2.2}{3} + \frac{0}{3} + \frac{3.2}{32})} + e^{2\pi i(\frac{2.2}{3} + \frac{0}{3} + \frac{14323.2}{25000})} + e^{2\pi i(\frac{2}{3} + \frac{2.0}{3} + \frac{10677.2}{25000})} \\
&\quad + e^{2\pi i(\frac{2}{3} + \frac{2.0}{3} + \frac{29.2}{32})} + e^{2\pi i(0+0+\frac{76041.2}{100000})}) \\
&\quad + f_{Li}(e^{2\pi i(0+0+0)} + e^{2\pi i(\frac{2.2}{3} + \frac{0}{3} + \frac{2}{3})} + e^{2\pi i(\frac{2}{3} + \frac{2.0}{3} + \frac{2.2}{3})}) \\
&= f_{Co}(e^{2\pi i(\frac{2}{3} + \frac{2.0}{3} + \frac{2}{6})} + e^{2\pi i(2+0+\frac{2}{2})} + e^{2\pi i(\frac{2.2}{3} + \frac{0}{3} + \frac{5.2}{6})}) \\
&\quad + f_O(e^{2\pi i(\frac{23959.2}{100000})} + e^{2\pi i(\frac{2.2}{3} + \frac{0}{3} + \frac{3.2}{32})} + e^{2\pi i(\frac{2.2}{3} + \frac{0}{3} + \frac{14323.2}{25000})} + e^{2\pi i(\frac{2}{3} + \frac{2.0}{3} + \frac{10677.2}{25000})} \\
&\quad + e^{2\pi i(\frac{2}{3} + \frac{2.0}{3} + \frac{29.2}{32})} + e^{2\pi i(\frac{76041.2}{100000})}) \\
&\quad + f_{Li}(e^{2\pi i(0)} + e^{2\pi i(\frac{2.2}{3} + \frac{0}{3} + \frac{2}{3})} + e^{2\pi i(\frac{2}{3} + \frac{2.0}{3} + \frac{2.2}{3})}) \\
&= f_{Co}(e^{2\pi i(1)} + e^{2\pi i(3)} + e^{2\pi i(3)}) \\
&\quad + f_O(e^{2\pi i(\frac{23959}{50000})} + e^{2\pi i(\frac{73}{48})} + e^{2\pi i(\frac{92969}{37500})} + e^{2\pi i(\frac{57031}{37500})} \\
&\quad + e^{2\pi i(\frac{119}{48})} + e^{2\pi i(\frac{76041}{50000})}) \\
&\quad + f_{Li}(e^{2\pi i(0)} + e^{2\pi i(2)} + e^{2\pi i(2)}) \\
&= f_{Co}(1 + 1 + 1) \\
&\quad + f_O([-0.99146 + (0.13044)i] + [-0.99144 + (-0.13053)i] \\
&\quad + [-0.99145 + (0.13048)i] + [-0.99145 + (-0.13048)i] \\
&\quad + [-0.99144 + (0.13053)i] + [-0.99146 + (-0.13044)i]) \\
&\quad + f_{Li}(1 + 1 + 1) \\
&= 3f_{Co} - 5.948701964355033f_O + 3f_{Li}
\end{aligned}$$

$$\begin{aligned}
F_{203} &= f_{Co}(e^{2\pi i(\frac{2}{3} + \frac{2.0}{3} + \frac{3}{6})} + e^{2\pi i(2+0+\frac{3}{2})} + e^{2\pi i(\frac{2.2}{3} + \frac{0}{3} + \frac{5.3}{6})}) \\
&\quad + f_O(e^{2\pi i(0+0+\frac{23959.3}{100000})} + e^{2\pi i(\frac{2.2}{3} + \frac{0}{3} + \frac{3.3}{32})} + e^{2\pi i(\frac{2.2}{3} + \frac{0}{3} + \frac{14323.3}{25000})} + e^{2\pi i(\frac{2}{3} + \frac{2.0}{3} + \frac{10677.3}{25000})}) \\
&\quad + e^{2\pi i(\frac{2}{3} + \frac{2.0}{3} + \frac{29.3}{32})} + e^{2\pi i(0+0+\frac{76041.3}{100000})}) \\
&\quad + f_{Li}(e^{2\pi i(0+0+0)} + e^{2\pi i(\frac{2.2}{3} + \frac{0}{3} + \frac{3}{3})} + e^{2\pi i(\frac{2}{3} + \frac{2.0}{3} + \frac{2.3}{3})}) \\
&= f_{Co}(e^{2\pi i(\frac{2}{3} + \frac{2.0}{3} + \frac{3}{6})} + e^{2\pi i(2+0+\frac{3}{2})} + e^{2\pi i(\frac{2.2}{3} + \frac{0}{3} + \frac{5.3}{6})}) \\
&\quad + f_O(e^{2\pi i(\frac{23959.3}{100000})} + e^{2\pi i(\frac{2.2}{3} + \frac{0}{3} + \frac{3.3}{32})} + e^{2\pi i(\frac{2.2}{3} + \frac{0}{3} + \frac{14323.3}{25000})} + e^{2\pi i(\frac{2}{3} + \frac{2.0}{3} + \frac{10677.3}{25000})}) \\
&\quad + e^{2\pi i(\frac{2}{3} + \frac{2.0}{3} + \frac{29.3}{32})} + e^{2\pi i(\frac{76041.3}{100000})}) \\
&\quad + f_{Li}(e^{2\pi i(0)} + e^{2\pi i(\frac{2.2}{3} + \frac{0}{3} + \frac{3}{3})} + e^{2\pi i(\frac{2}{3} + \frac{2.0}{3} + \frac{2.3}{3})}) \\
&= f_{Co}(e^{2\pi i(\frac{7}{6})} + e^{2\pi i(\frac{7}{2})} + e^{2\pi i(\frac{23}{6})}) \\
&\quad + f_O(e^{2\pi i(\frac{71877}{100000})} + e^{2\pi i(\frac{155}{96})} + e^{2\pi i(\frac{3.0521}{1})} + e^{2\pi i(\frac{1.9479}{1})}) \\
&\quad + e^{2\pi i(\frac{325}{96})} + e^{2\pi i(\frac{2.2812}{1})}) \\
&\quad + f_{Li}(e^{2\pi i(0)} + e^{2\pi i(\frac{7}{3})} + e^{2\pi i(\frac{8}{3})}) \\
&= f_{Co}([0.5 + (0.86603)i] + -1 + [0.5 + (-0.86603)i]) \\
&\quad + f_O([-0.19497 + (-0.98081)i] + [-0.75184 + (-0.65935)i] \\
&\quad + [0.94691 + (0.3215)i] + [0.94691 + (-0.3215)i] \\
&\quad + [-0.75184 + (0.65935)i] + [-0.19497 + (0.98081)i]) \\
&\quad + f_{Li}(1 + [-0.5 + (0.86603)i] + [-0.5 + (-0.86603)i]) \\
&= 0.00020610429381390238f_O
\end{aligned}$$

$$\begin{aligned}
F_{210} &= f_{Co}(e^{2\pi i(\frac{2}{3} + \frac{2 \cdot 1}{3} + \frac{0}{6})} + e^{2\pi i(2+1+\frac{0}{2})} + e^{2\pi i(\frac{2 \cdot 2}{3} + \frac{1}{3} + \frac{5 \cdot 0}{6})}) \\
&\quad + f_O(e^{2\pi i(0+0+\frac{23959 \cdot 0}{100000})} + e^{2\pi i(\frac{2 \cdot 2}{3} + \frac{1}{3} + \frac{3 \cdot 0}{32})} + e^{2\pi i(\frac{2 \cdot 2}{3} + \frac{1}{3} + \frac{14323 \cdot 0}{25000})} + e^{2\pi i(\frac{2}{3} + \frac{2 \cdot 1}{3} + \frac{10677 \cdot 0}{25000})}) \\
&\quad + e^{2\pi i(\frac{2}{3} + \frac{2 \cdot 1}{3} + \frac{29 \cdot 0}{32})} + e^{2\pi i(0+0+\frac{76041 \cdot 0}{100000})}) \\
&\quad + f_{Li}(e^{2\pi i(0+0+0)} + e^{2\pi i(\frac{2 \cdot 2}{3} + \frac{1}{3} + \frac{0}{3})} + e^{2\pi i(\frac{2}{3} + \frac{2 \cdot 1}{3} + \frac{2 \cdot 0}{3})}) \\
&= f_{Co}(e^{2\pi i(\frac{2}{3} + \frac{2 \cdot 1}{3} + \frac{0}{6})} + e^{2\pi i(2+1+\frac{0}{2})} + e^{2\pi i(\frac{2 \cdot 2}{3} + \frac{1}{3} + \frac{5 \cdot 0}{6})}) \\
&\quad + f_O(e^{2\pi i(\frac{23959 \cdot 0}{100000})} + e^{2\pi i(\frac{2 \cdot 2}{3} + \frac{1}{3} + \frac{3 \cdot 0}{32})} + e^{2\pi i(\frac{2 \cdot 2}{3} + \frac{1}{3} + \frac{14323 \cdot 0}{25000})} + e^{2\pi i(\frac{2}{3} + \frac{2 \cdot 1}{3} + \frac{10677 \cdot 0}{25000})}) \\
&\quad + e^{2\pi i(\frac{2}{3} + \frac{2 \cdot 1}{3} + \frac{29 \cdot 0}{32})} + e^{2\pi i(\frac{76041 \cdot 0}{100000})}) \\
&\quad + f_{Li}(e^{2\pi i(0)} + e^{2\pi i(\frac{2 \cdot 2}{3} + \frac{1}{3} + \frac{0}{3})} + e^{2\pi i(\frac{2}{3} + \frac{2 \cdot 1}{3} + \frac{2 \cdot 0}{3})}) \\
&= f_{Co}(e^{2\pi i(\frac{4}{3})} + e^{2\pi i(3)} + e^{2\pi i(\frac{5}{3})}) \\
&\quad + f_O(e^{2\pi i(0)} + e^{2\pi i(\frac{5}{3})} + e^{2\pi i(\frac{5}{3})} + e^{2\pi i(\frac{4}{3})}) \\
&\quad + e^{2\pi i(\frac{4}{3})} + e^{2\pi i(0)}) \\
&\quad + f_{Li}(e^{2\pi i(0)} + e^{2\pi i(\frac{5}{3})} + e^{2\pi i(\frac{4}{3})}) \\
&= f_{Co}([-0.5 + (0.86603)i] + 1 + [-0.5 + (-0.86603)i]) \\
&\quad + f_O(1 + [-0.5 + (-0.86603)i] + [-0.5 + (-0.86603)i] \\
&\quad + [-0.5 + (0.86603)i] + [-0.5 + (0.86603)i] \\
&\quad + 1) \\
&\quad + f_{Li}(1 + [-0.5 + (-0.86603)i] + [-0.5 + (0.86603)i]) \\
&= 0(ForbiddenReflection)
\end{aligned}$$

$$\begin{aligned}
F_{211} &= f_{Co}(e^{2\pi i(\frac{2}{3} + \frac{2 \cdot 1}{3} + \frac{1}{6})} + e^{2\pi i(2+1+\frac{1}{2})} + e^{2\pi i(\frac{2 \cdot 2}{3} + \frac{1}{3} + \frac{5 \cdot 1}{6})}) \\
&\quad + f_O(e^{2\pi i(0+0+\frac{23959 \cdot 1}{100000})} + e^{2\pi i(\frac{2 \cdot 2}{3} + \frac{1}{3} + \frac{3 \cdot 1}{32})} + e^{2\pi i(\frac{2 \cdot 2}{3} + \frac{1}{3} + \frac{14323 \cdot 1}{25000})} + e^{2\pi i(\frac{2}{3} + \frac{2 \cdot 1}{3} + \frac{10677 \cdot 1}{25000})}) \\
&\quad + e^{2\pi i(\frac{2}{3} + \frac{2 \cdot 1}{3} + \frac{29 \cdot 1}{32})} + e^{2\pi i(0+0+\frac{76041 \cdot 1}{100000})}) \\
&\quad + f_{Li}(e^{2\pi i(0+0+0)} + e^{2\pi i(\frac{2 \cdot 2}{3} + \frac{1}{3} + \frac{1}{3})} + e^{2\pi i(\frac{2}{3} + \frac{2 \cdot 1}{3} + \frac{2 \cdot 1}{3})}) \\
&= f_{Co}(e^{2\pi i(\frac{2}{3} + \frac{2 \cdot 1}{3} + \frac{1}{6})} + e^{2\pi i(2+1+\frac{1}{2})} + e^{2\pi i(\frac{2 \cdot 2}{3} + \frac{1}{3} + \frac{5 \cdot 1}{6})}) \\
&\quad + f_O(e^{2\pi i(\frac{23959 \cdot 1}{100000})} + e^{2\pi i(\frac{2 \cdot 2}{3} + \frac{1}{3} + \frac{3 \cdot 1}{32})} + e^{2\pi i(\frac{2 \cdot 2}{3} + \frac{1}{3} + \frac{14323 \cdot 1}{25000})} + e^{2\pi i(\frac{2}{3} + \frac{2 \cdot 1}{3} + \frac{10677 \cdot 1}{25000})}) \\
&\quad + e^{2\pi i(\frac{2}{3} + \frac{2 \cdot 1}{3} + \frac{29 \cdot 1}{32})} + e^{2\pi i(\frac{76041 \cdot 1}{100000})}) \\
&\quad + f_{Li}(e^{2\pi i(0)} + e^{2\pi i(\frac{2 \cdot 2}{3} + \frac{1}{3} + \frac{1}{3})} + e^{2\pi i(\frac{2}{3} + \frac{2 \cdot 1}{3} + \frac{2 \cdot 1}{3})}) \\
&= f_{Co}(e^{2\pi i(\frac{3}{2})} + e^{2\pi i(\frac{7}{2})} + e^{2\pi i(\frac{5}{2})}) \\
&\quad + f_O(e^{2\pi i(\frac{23959}{100000})} + e^{2\pi i(\frac{169}{96})} + e^{2\pi i(\frac{2 \cdot 2396}{1})} + e^{2\pi i(\frac{1 \cdot 7604}{1})}) \\
&\quad + e^{2\pi i(\frac{215}{96})} + e^{2\pi i(\frac{76041}{100000})}) \\
&\quad + f_{Li}(e^{2\pi i(0)} + e^{2\pi i(\frac{2}{1})} + e^{2\pi i(2)}) \\
&= f_{Co}(-1 + -1 + -1) \\
&\quad + f_O([0.06536 + (0.99786)i] + [0.0654 + (-0.99786)i] \\
&\quad + [0.06538 + (0.99786)i] + [0.06538 + (-0.99786)i] \\
&\quad + [0.0654 + (0.99786)i] + [0.06536 + (-0.99786)i]) \\
&\quad + f_{Li}(1 + 1 + 1) \\
&= 3f_{Co} + 0.39229338058693924f_O + 3f_{Li}
\end{aligned}$$

$$\begin{aligned}
F_{212} &= f_{Co}(e^{2\pi i(\frac{2}{3} + \frac{2}{3} + \frac{2}{6})} + e^{2\pi i(2+1+\frac{2}{2})} + e^{2\pi i(\frac{2}{3} + \frac{1}{3} + \frac{5}{6})}) \\
&\quad + f_O(e^{2\pi i(0+0+\frac{23959 \cdot 2}{100000})} + e^{2\pi i(\frac{2}{3} + \frac{1}{3} + \frac{3 \cdot 2}{32})} + e^{2\pi i(\frac{2}{3} + \frac{1}{3} + \frac{14323 \cdot 2}{25000})} + e^{2\pi i(\frac{2}{3} + \frac{2}{3} + \frac{10677 \cdot 2}{25000})} \\
&\quad + e^{2\pi i(\frac{2}{3} + \frac{2}{3} + \frac{29 \cdot 2}{32})} + e^{2\pi i(0+0+\frac{76041 \cdot 2}{100000})}) \\
&\quad + f_{Li}(e^{2\pi i(0+0+0)} + e^{2\pi i(\frac{2}{3} + \frac{1}{3} + \frac{2}{3})} + e^{2\pi i(\frac{2}{3} + \frac{2}{3} + \frac{2}{3})}) \\
&= f_{Co}(e^{2\pi i(\frac{2}{3} + \frac{2}{3} + \frac{2}{6})} + e^{2\pi i(2+1+\frac{2}{2})} + e^{2\pi i(\frac{2}{3} + \frac{1}{3} + \frac{5}{6})}) \\
&\quad + f_O(e^{2\pi i(\frac{23959 \cdot 2}{100000})} + e^{2\pi i(\frac{2}{3} + \frac{1}{3} + \frac{3 \cdot 2}{32})} + e^{2\pi i(\frac{2}{3} + \frac{1}{3} + \frac{14323 \cdot 2}{25000})} + e^{2\pi i(\frac{2}{3} + \frac{2}{3} + \frac{10677 \cdot 2}{25000})} \\
&\quad + e^{2\pi i(\frac{2}{3} + \frac{2}{3} + \frac{29 \cdot 2}{32})} + e^{2\pi i(\frac{76041 \cdot 2}{100000})}) \\
&\quad + f_{Li}(e^{2\pi i(0)} + e^{2\pi i(\frac{2}{3} + \frac{1}{3} + \frac{2}{3})} + e^{2\pi i(\frac{2}{3} + \frac{2}{3} + \frac{2}{3})}) \\
&= f_{Co}(e^{2\pi i(\frac{5}{3})} + e^{2\pi i(4)} + e^{2\pi i(\frac{10}{3})}) \\
&\quad + f_O(e^{2\pi i(\frac{23959}{50000})} + e^{2\pi i(\frac{89}{48})} + e^{2\pi i(\frac{2 \cdot 8125}{1})} + e^{2\pi i(\frac{82031}{37500})} \\
&\quad + e^{2\pi i(\frac{151}{48})} + e^{2\pi i(\frac{76041}{50000})}) \\
&\quad + f_{Li}(e^{2\pi i(0)} + e^{2\pi i(\frac{7}{3})} + e^{2\pi i(\frac{8}{3})}) \\
&= f_{Co}([-0.5 + (-0.86603)i] + 1 + [-0.5 + (0.86603)i]) \\
&\quad + f_O([-0.99146 + (0.13044)i] + [0.60876 + (-0.79335)i] \\
&\quad + [0.38272 + (-0.92386)i] + [0.38272 + (0.92386)i] \\
&\quad + [0.60876 + (0.79335)i] + [-0.99146 + (-0.13044)i]) \\
&\quad + f_{Li}(1 + [-0.5 + (0.86603)i] + [-0.5 + (-0.86603)i]) \\
&= 5.5535164196429676e - 05 f_O
\end{aligned}$$

$$\begin{aligned}
F_{213} &= f_{Co}(e^{2\pi i(\frac{2}{3} + \frac{2 \cdot 1}{3} + \frac{3}{6})} + e^{2\pi i(2+1+\frac{3}{2})} + e^{2\pi i(\frac{2 \cdot 2}{3} + \frac{1}{3} + \frac{5 \cdot 3}{6})}) \\
&\quad + f_O(e^{2\pi i(0+0+\frac{23959 \cdot 3}{100000})} + e^{2\pi i(\frac{2 \cdot 2}{3} + \frac{1}{3} + \frac{3 \cdot 3}{32})} + e^{2\pi i(\frac{2 \cdot 2}{3} + \frac{1}{3} + \frac{14323 \cdot 3}{25000})} + e^{2\pi i(\frac{2}{3} + \frac{2 \cdot 1}{3} + \frac{10677 \cdot 3}{25000})}) \\
&\quad + e^{2\pi i(\frac{2}{3} + \frac{2 \cdot 1}{3} + \frac{29 \cdot 3}{32})} + e^{2\pi i(0+0+\frac{76041 \cdot 3}{100000})}) \\
&\quad + f_{Li}(e^{2\pi i(0+0+0)} + e^{2\pi i(\frac{2 \cdot 2}{3} + \frac{1}{3} + \frac{3}{3})} + e^{2\pi i(\frac{2}{3} + \frac{2 \cdot 1}{3} + \frac{2 \cdot 3}{3})}) \\
&= f_{Co}(e^{2\pi i(\frac{2}{3} + \frac{2 \cdot 1}{3} + \frac{3}{6})} + e^{2\pi i(2+1+\frac{3}{2})} + e^{2\pi i(\frac{2 \cdot 2}{3} + \frac{1}{3} + \frac{5 \cdot 3}{6})}) \\
&\quad + f_O(e^{2\pi i(\frac{23959 \cdot 3}{100000})} + e^{2\pi i(\frac{2 \cdot 2}{3} + \frac{1}{3} + \frac{3 \cdot 3}{32})} + e^{2\pi i(\frac{2 \cdot 2}{3} + \frac{1}{3} + \frac{14323 \cdot 3}{25000})} + e^{2\pi i(\frac{2}{3} + \frac{2 \cdot 1}{3} + \frac{10677 \cdot 3}{25000})}) \\
&\quad + e^{2\pi i(\frac{2}{3} + \frac{2 \cdot 1}{3} + \frac{29 \cdot 3}{32})} + e^{2\pi i(\frac{76041 \cdot 3}{100000})}) \\
&\quad + f_{Li}(e^{2\pi i(0)} + e^{2\pi i(\frac{2 \cdot 2}{3} + \frac{1}{3} + \frac{3}{3})} + e^{2\pi i(\frac{2}{3} + \frac{2 \cdot 1}{3} + \frac{2 \cdot 3}{3})}) \\
&= f_{Co}(e^{2\pi i(\frac{11}{6})} + e^{2\pi i(\frac{9}{2})} + e^{2\pi i(\frac{25}{6})}) \\
&\quad + f_O(e^{2\pi i(\frac{71877}{100000})} + e^{2\pi i(\frac{187}{96})} + e^{2\pi i(\frac{3 \cdot 3854}{1})} + e^{2\pi i(\frac{2 \cdot 6146}{1})}) \\
&\quad + e^{2\pi i(\frac{389}{96})} + e^{2\pi i(\frac{2 \cdot 2812}{1})}) \\
&\quad + f_{Li}(e^{2\pi i(0)} + e^{2\pi i(\frac{8}{3})} + e^{2\pi i(\frac{10}{3})}) \\
&= f_{Co}([0.5 + (-0.86603)i] + -1 + [0.5 + (0.86603)i]) \\
&\quad + f_O([-0.19497 + (-0.98081)i] + [0.94693 + (-0.32144)i] \\
&\quad + [-0.75188 + (0.6593)i] + [-0.75188 + (-0.6593)i] \\
&\quad + [0.94693 + (0.32144)i] + [-0.19497 + (0.98081)i]) \\
&\quad + f_{Li}(1 + [-0.5 + (-0.86603)i] + [-0.5 + (0.86603)i]) \\
&= 0.00016364843607136192f_O
\end{aligned}$$

$$\begin{aligned}
F_{300} &= f_{Co}(e^{2\pi i(\frac{3}{3}+\frac{2.0}{3}+\frac{0}{6})} + e^{2\pi i(3+0+\frac{0}{2})} + e^{2\pi i(\frac{2.3}{3}+\frac{0}{3}+\frac{5.0}{6})}) \\
&\quad + f_O(e^{2\pi i(0+0+\frac{23959.0}{100000})} + e^{2\pi i(\frac{2.3}{3}+\frac{0}{3}+\frac{3.0}{32})} + e^{2\pi i(\frac{2.3}{3}+\frac{0}{3}+\frac{14323.0}{25000})} + e^{2\pi i(\frac{3}{3}+\frac{2.0}{3}+\frac{10677.0}{25000})}) \\
&\quad + e^{2\pi i(\frac{3}{3}+\frac{2.0}{3}+\frac{29.0}{32})} + e^{2\pi i(0+0+\frac{76041.0}{100000})}) \\
&\quad + f_{Li}(e^{2\pi i(0+0+0)} + e^{2\pi i(\frac{2.3}{3}+\frac{0}{3}+\frac{0}{3})} + e^{2\pi i(\frac{3}{3}+\frac{2.0}{3}+\frac{2.0}{3})}) \\
&= f_{Co}(e^{2\pi i(\frac{3}{3}+\frac{2.0}{3}+\frac{0}{6})} + e^{2\pi i(3+0+\frac{0}{2})} + e^{2\pi i(\frac{2.3}{3}+\frac{0}{3}+\frac{5.0}{6})}) \\
&\quad + f_O(e^{2\pi i(\frac{23959.0}{100000})} + e^{2\pi i(\frac{2.3}{3}+\frac{0}{3}+\frac{3.0}{32})} + e^{2\pi i(\frac{2.3}{3}+\frac{0}{3}+\frac{14323.0}{25000})} + e^{2\pi i(\frac{3}{3}+\frac{2.0}{3}+\frac{10677.0}{25000})}) \\
&\quad + e^{2\pi i(\frac{3}{3}+\frac{2.0}{3}+\frac{29.0}{32})} + e^{2\pi i(\frac{76041.0}{100000})}) \\
&\quad + f_{Li}(e^{2\pi i(0)} + e^{2\pi i(\frac{2.3}{3}+\frac{0}{3}+\frac{0}{3})} + e^{2\pi i(\frac{3}{3}+\frac{2.0}{3}+\frac{2.0}{3})}) \\
&= f_{Co}(e^{2\pi i(1)} + e^{2\pi i(3)} + e^{2\pi i(2)}) \\
&\quad + f_O(e^{2\pi i(0)} + e^{2\pi i(2)} + e^{2\pi i(2)} + e^{2\pi i(1)}) \\
&\quad + e^{2\pi i(1)} + e^{2\pi i(0)}) \\
&\quad + f_{Li}(e^{2\pi i(0)} + e^{2\pi i(2)} + e^{2\pi i(1)}) \\
&= f_{Co}(1+1+1) \\
&\quad + f_O(1+1+1+1+1+1) \\
&\quad + f_{Li}(1+1+1) \\
&= 3f_{Co} + 6f_O + 3f_{Li}
\end{aligned}$$

$$\begin{aligned}
F_{301} &= f_{Co}(e^{2\pi i(\frac{3}{3} + \frac{2.0}{3} + \frac{1}{6})} + e^{2\pi i(3+0+\frac{1}{2})} + e^{2\pi i(\frac{2.3}{3} + \frac{0}{3} + \frac{5.1}{6})}) \\
&\quad + f_O(e^{2\pi i(0+0+\frac{23959.1}{100000})} + e^{2\pi i(\frac{2.3}{3} + \frac{0}{3} + \frac{3.1}{32})} + e^{2\pi i(\frac{2.3}{3} + \frac{0}{3} + \frac{14323.1}{25000})} + e^{2\pi i(\frac{3}{3} + \frac{2.0}{3} + \frac{10677.1}{25000})}) \\
&\quad + e^{2\pi i(\frac{3}{3} + \frac{2.0}{3} + \frac{29.1}{32})} + e^{2\pi i(0+0+\frac{76041.1}{100000})}) \\
&\quad + f_{Li}(e^{2\pi i(0+0+0)} + e^{2\pi i(\frac{2.3}{3} + \frac{0}{3} + \frac{1}{3})} + e^{2\pi i(\frac{3}{3} + \frac{2.0}{3} + \frac{2.1}{3})}) \\
&= f_{Co}(e^{2\pi i(\frac{3}{3} + \frac{2.0}{3} + \frac{1}{6})} + e^{2\pi i(3+0+\frac{1}{2})} + e^{2\pi i(\frac{2.3}{3} + \frac{0}{3} + \frac{5.1}{6})}) \\
&\quad + f_O(e^{2\pi i(\frac{23959.1}{100000})} + e^{2\pi i(\frac{2.3}{3} + \frac{0}{3} + \frac{3.1}{32})} + e^{2\pi i(\frac{2.3}{3} + \frac{0}{3} + \frac{14323.1}{25000})} + e^{2\pi i(\frac{3}{3} + \frac{2.0}{3} + \frac{10677.1}{25000})}) \\
&\quad + e^{2\pi i(\frac{3}{3} + \frac{2.0}{3} + \frac{29.1}{32})} + e^{2\pi i(\frac{76041.1}{100000})}) \\
&\quad + f_{Li}(e^{2\pi i(0)} + e^{2\pi i(\frac{2.3}{3} + \frac{0}{3} + \frac{1}{3})} + e^{2\pi i(\frac{3}{3} + \frac{2.0}{3} + \frac{2.1}{3})}) \\
&= f_{Co}(e^{2\pi i(\frac{7}{6})} + e^{2\pi i(\frac{7}{2})} + e^{2\pi i(\frac{17}{6})}) \\
&\quad + f_O(e^{2\pi i(\frac{23959}{100000})} + e^{2\pi i(\frac{67}{32})} + e^{2\pi i(\frac{64323}{25000})} + e^{2\pi i(\frac{35677}{25000})}) \\
&\quad + e^{2\pi i(\frac{61}{32})} + e^{2\pi i(\frac{76041}{100000})}) \\
&\quad + f_{Li}(e^{2\pi i(0)} + e^{2\pi i(\frac{7}{3})} + e^{2\pi i(\frac{5}{3})}) \\
&= f_{Co}([0.5 + (0.86603)i] + -1 + [0.5 + (-0.86603)i]) \\
&\quad + f_O([0.06536 + (0.99786)i] + [0.83147 + (0.55557)i] \\
&\quad + [-0.89686 + (-0.44231)i] + [-0.89686 + (0.44231)i] \\
&\quad + [0.83147 + (-0.55557)i] + [0.06536 + (-0.99786)i]) \\
&\quad + f_{Li}(1 + [-0.5 + (0.86603)i] + [-0.5 + (-0.86603)i]) \\
&= 6.506960965775577e - 05f_O
\end{aligned}$$

$$\begin{aligned}
F_{302} &= f_{Co}(e^{2\pi i(\frac{3}{3} + \frac{2.0}{3} + \frac{2}{6})} + e^{2\pi i(3+0+\frac{2}{2})} + e^{2\pi i(\frac{2.3}{3} + \frac{0}{3} + \frac{5.2}{6})}) \\
&\quad + f_O(e^{2\pi i(0+0+\frac{23959.2}{100000})} + e^{2\pi i(\frac{2.3}{3} + \frac{0}{3} + \frac{3.2}{32})} + e^{2\pi i(\frac{2.3}{3} + \frac{0}{3} + \frac{14323.2}{25000})} + e^{2\pi i(\frac{3}{3} + \frac{2.0}{3} + \frac{10677.2}{25000})} \\
&\quad + e^{2\pi i(\frac{3}{3} + \frac{2.0}{3} + \frac{29.2}{32})} + e^{2\pi i(0+0+\frac{76041.2}{100000})}) \\
&\quad + f_{Li}(e^{2\pi i(0+0+0)} + e^{2\pi i(\frac{2.3}{3} + \frac{0}{3} + \frac{2}{3})} + e^{2\pi i(\frac{3}{3} + \frac{2.0}{3} + \frac{2.2}{3})}) \\
&= f_{Co}(e^{2\pi i(\frac{3}{3} + \frac{2.0}{3} + \frac{2}{6})} + e^{2\pi i(3+0+\frac{2}{2})} + e^{2\pi i(\frac{2.3}{3} + \frac{0}{3} + \frac{5.2}{6})}) \\
&\quad + f_O(e^{2\pi i(\frac{23959.2}{100000})} + e^{2\pi i(\frac{2.3}{3} + \frac{0}{3} + \frac{3.2}{32})} + e^{2\pi i(\frac{2.3}{3} + \frac{0}{3} + \frac{14323.2}{25000})} + e^{2\pi i(\frac{3}{3} + \frac{2.0}{3} + \frac{10677.2}{25000})} \\
&\quad + e^{2\pi i(\frac{3}{3} + \frac{2.0}{3} + \frac{29.2}{32})} + e^{2\pi i(\frac{76041.2}{100000})}) \\
&\quad + f_{Li}(e^{2\pi i(0)} + e^{2\pi i(\frac{2.3}{3} + \frac{0}{3} + \frac{2}{3})} + e^{2\pi i(\frac{3}{3} + \frac{2.0}{3} + \frac{2.2}{3})}) \\
&= f_{Co}(e^{2\pi i(\frac{4}{3})} + e^{2\pi i(4)} + e^{2\pi i(\frac{11}{3})}) \\
&\quad + f_O(e^{2\pi i(\frac{23959}{50000})} + e^{2\pi i(\frac{35}{16})} + e^{2\pi i(\frac{39323}{12500})} + e^{2\pi i(\frac{23177}{12500})} \\
&\quad + e^{2\pi i(\frac{45}{16})} + e^{2\pi i(\frac{76041}{50000})}) \\
&\quad + f_{Li}(e^{2\pi i(0)} + e^{2\pi i(\frac{8}{3})} + e^{2\pi i(\frac{7}{3})}) \\
&= f_{Co}([-0.5 + (0.86603)i] + 1 + [-0.5 + (-0.86603)i]) \\
&\quad + f_O([-0.99146 + (0.13044)i] + [0.38268 + (0.92388)i] \\
&\quad + [0.60873 + (0.79338)i] + [0.60873 + (-0.79338)i] \\
&\quad + [0.38268 + (-0.92388)i] + [-0.99146 + (-0.13044)i]) \\
&\quad + f_{Li}(1 + [-0.5 + (-0.86603)i] + [-0.5 + (0.86603)i]) \\
&= 8.83277971728269e - 05f_O
\end{aligned}$$
