

Functional Dependency

Given
 $A \rightarrow B, C$
 $D \rightarrow C$
 $E \rightarrow D$
 $B, E \rightarrow C$

Closure
 $\{A, E\}^+ = \{A, B, C, D, E\}$ ← **Superkey** (because the closure contains all keys)
Key is when none of the subsets are superkey

Armstrong's Axiom: 1
Reflexivity

Axiom: 2
Augmentation
 - For any attribute sets X, Y, Z
 o If $X \rightarrow Y$, then $X, Z \rightarrow Y, Z$

Axiom: 3
Transitivity
 - For any attribute sets X, Y, Z
 o If $X \rightarrow Y$, and $Y \rightarrow Z$, then $X \rightarrow Z$

DCNF: For all non-trivial $X \rightarrow B$, X must be a superkey

Split again!
 - BookInfo(title, genre, price)
 o FD: title \rightarrow genre, price **in BCNF**
 - BookAuthor(author, title) **in BCNF**

BCNF Example

Books(author, gender, title, genre, price)
 - author \rightarrow gender
 - title \rightarrow genre, price

Key?
 $\{author, title\}$

Is BCNF?
 No, bc the left hand side of both FDs are not superkey

Split!

Split Books using author \rightarrow gender
 - **Author**(author, gender)
 o FD: author \rightarrow gender **in BCNF**
 - **Books2**(author, title, genre, price)
 o FD: title \rightarrow genre, price **not in BCNF**

SQL



MovieID	MovieName
1	Star Wars
2	Sholay
3	The Italian Job

MovieID	CinemaName	RunForDays
2	Naz Cinema	101
5	Apollo Theater	45

Cross Join

MovieID	MovieName	MovieID	CinemaName	RunForDays
1	Star Wars	2	Naz Cinema	101
1	Star Wars	5	Apollo Theater	45
2	Sholay	2	Naz Cinema	101
2	Sholay	5	Apollo Theater	45
3	The Italian Job	2	Naz Cinema	101
3	The Italian Job	5	Apollo Theater	45

Inner

MovieID	MovieName	MovieID	CinemaName	RunForDays
2	Sholay	2	Naz Cinema	101

Left Inner

MovieID	MovieName	MovieID	CinemaName	RunForDays
1	Star Wars	NULL	NULL	NULL
2	Sholay	2	Naz Cinema	101
3	The Italian Job	NULL	NULL	NULL

Full outer

MovieID	MovieName	MovieID	CinemaName	RunForDays
1	Star Wars	NULL	NULL	NULL
2	Sholay	2	Naz Cinema	101
3	The Italian Job	NULL	NULL	NULL
NULL	NULL	5	Apollo Theater	45

Sample queries

for each country the population of the most populated city, only for countries with at least 10 cities

```
SELECT C.Name, MAX(T.Population)
FROM City as T, Country as C
WHERE T.CountryCode = C.Code
GROUP BY C.Name
HAVING COUNT(T.ID) >= 10
```

Get all countries in Europe that have all cities with <1m population

```
SELECT C.Name
FROM Country C
WHERE C.Continent = 'Europe'
AND NOT EXISTS (SELECT *
FROM City T
WHERE T.Population > 1000000
AND T.CountryCode = C.Code);
```

Inserting into Table

```
INSERT INTO Users (email, bio, country)
VALUES (
  "email@gmail.com",
  "Student",
  "US"
)
```

← OR →

```
INSERT INTO Users (email, bio, country)
VALUES
  ("email@gmail.com", "Student", "US")
  ("email@hotmail.com", "Teacher", "CA")
  ("email@apple.com", "a long string...", "CN")
```

Row Number, Find longest sequence

```
WITH num AS
  (SELECT A, (A-row_number()) OVER (ORDER BY A ASC)) AS B FROM R)
SELECT COUNT(*) AS len
FROM num
GROUP BY B
ORDER BY len DESC
```

View

```
CREATE VIEW SomeViewName AS
-- Standard query
```

Buffer Manager

Clock

- When a frame is considered:

- If pin count > 0, increment current
- If referenced = 1, set to 0 and increment
- If referenced = 0 and pin count = 0, choose the page
- Each frame has a **referenced bit** that is set to 1 when pin count becomes 0
- A **current** variable points to a frame

LRU

- Uses a queue of pointers to frames that have pin **count = 0**
- A page request uses frames only from the head of the queue
- When the pin count of a frame goes to 0, it is added to the end of the queue

access time = **rotational delay** + **seek time** + **transfer time**

$$\begin{aligned} 7200 \text{ RPM} &= 4.17 \text{ ms Rotational delay} \\ 4 \text{ KB} / 210 \text{ MB/s} &= 0.019 \text{ ms Transfer time} \\ 4.17 + 0.019 + 9 &= 13.1 \text{ ms} \leftarrow \text{Total time} \\ 4 \text{ KB} / 13.1 \text{ ms} &= 0.3 \text{ MB/s I/O Rate} \end{aligned}$$

Relational Algebra

SELECTION

$\sigma_C(R)$

UNION

$R_1 \cup R_2$

PROJECTION

$\pi_{A_1, A_2, \dots, A_n}(R)$

- Outputs all tuples in R_1 or R_2
- Both relations must have the same schema
- Output schema: same as input

CROSS-PRODUCT

$R_1 \times R_2$

- Matches each tuple in R_1 with each tuple in R_2
- Input schema: $R_1(A_1, \dots, A_n), R_2(B_1, \dots, B_m)$
- Output schema: $R(A_1, \dots, A_n, B_1, \dots, B_m)$
- **CANNOT** have the same named columns

NATURAL JOIN

$R_1 \bowtie R_2$

- Equi-join on all the common fields
- The output schema has one copy of each common attribute

JOIN (THETA JOIN)

$R_1 \bowtie_{\theta} R_2 = \sigma_{\theta}(R_1 \times R_2)$

- Cross-product followed by a selection
- θ can be any boolean-valued condition
- Might have less tuples than the cross-product

DIFFERENCE

$R_1 - R_2$

- Outputs all tuples in R_1 and **not in** R_2
- Both relations must have the same schema
- Output schema: same as input

DIVISION

R_1 / R_2

- Suppose $R_1(A, B)$ and $R_2(B)$
- The output contains all values **a** such that for every tuple **(b)** in R_2 , tuple **(a, b)** is in R_1
- Output schema: $R(A)$

How to derive

$$\pi_A(R) = \pi_A((\pi_A(R) \times R) - R)$$

$$\begin{array}{cc|c} \frac{A}{a_1} & \frac{B}{b_1} & \frac{B_2}{b_1} \\ a_1 & b_2 & \\ a_1 & b_3 & \\ a_2 & b_1 & \end{array} \quad \frac{A/B_2}{a_1} = \frac{A}{a_2}$$

- Article(artid, title, confid, numpages)
- Conference(confid, name, year, location)
- Author(artid, pid)
- Person(pid, name, affiliation)

Name of people affiliated with UW who submitted an article in 2019

$\pi_{name}(\sigma_{affiliation='UW-Madison'}(Person) \bowtie Author \bowtie Article \bowtie \pi_{confid}(\sigma_{year=2019}(Conference)))$

Output the names of the people who coauthored an article with 'John Doe'. Be careful: a person cannot be coauthor with herself!

$\pi_{name}(\sigma_{name='JohnDoe'}(Person) \bowtie Author \bowtie \rho_{pid \rightarrow oid}(Author) \bowtie \rho_{pid \rightarrow oid, name \rightarrow oname} \sigma_{name \neq 'JohnDoe'}(Author))$