# Hypothesis Testing for Categorical Variable

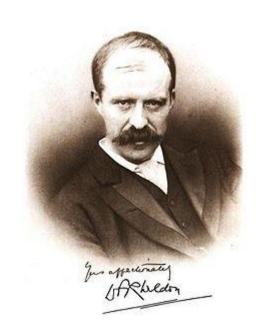
Portland State University USP 634 Data Analysis I Spring 2017

# Testing for Goodness of Fit Using Chi-Square

#### Weldon's dice

Walter Frank Raphael Weldon (1860 - 1906), was an English evolutionary biologist and a founder of biometry. He was the joint founding editor of Biometrika, with Francis Galton and Karl Pearson.

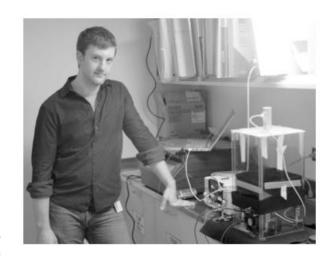
In 1894, he rolled 12 dice 26,306 times, and recorded the number of 5s or 6s (which he considered to be a success).



It was observed that 5s or 6s occurred more often than expected, and Pearson hypothesized that this was probably due to the construction of the dice. Most inexpensive dice have hollowed-out pips, and since opposite sides add to 7, the face with 6 pips is lighter than its opposing face, which has only 1 pip.

# Labby's dice

In 2009, Zacariah Labby (U of Chicago), repeated Weldon's experiment using a homemade dice-throwing, pip counting machine.



www.youtube.com/watch?v=95EErdouO2w

The rolling-imaging process took about 20 seconds per roll.

Each day there were ~150 images to process manually.

At this rate Weldon's experiment was repeated in a little more than six full days.

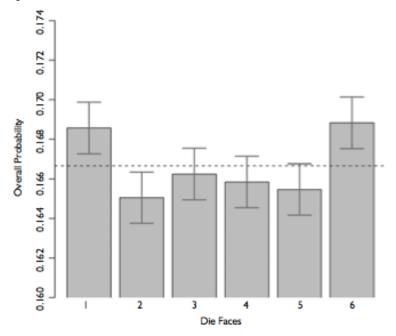
Recommended reading:

galton.uchicago.edu/about/docs/labby09dice.pdf

# Labby's dice (cont.)

Labby did not actually observe the same phenomenon that Weldon observed (higher frequency of 5s and 6s).

Automation allowed Labby to collect more data than Weldon did in 1894, instead of recording "successes" and "failures", Labby recorded the individual number of pips on each die.



### **Expected counts**

Labby rolled 12 dice 26,306 times. If each side is equally likely to come up, how many 1s, 2s, ..., 6s would he expect to have observed?

- (a)  $\frac{1}{6}$
- (b) 12 / 6
- (c) 26,306 / 6
- (d) 12 x 26,306 / 6

### **Expected counts**

Labby rolled 12 dice 26,306 times. If each side is equally likely to come up, how many 1s, 2s, ..., 6s would he expect to have observed?

- (a)  $\frac{1}{6}$
- (b) 12 / 6
- (c) 26,306 / 6
- (d)  $12 \times 26,306 / 6 = 52,612$

## **Summarizing Labby's results**

The table below shows the observed and expected counts from Labby's experiment.

Outcome	Observed	Expected
1	53,222	52,612
2	52,118	52,612
3	52,465	52,612
4	52,338	52,612
5	52,244	52,612
6	53,285	52,612
Total	315,672	315,672

Why are the expected counts the same for all outcomes but the observed counts are different? At a first glance, does there appear to be an inconsistency between the observed and expected counts?

## Setting the hypotheses

Do these data provide convincing evidence of an inconsistency between the observed and expected counts?

H<sub>0</sub>:There is no inconsistency between the observed and the expected counts. The observed counts follow the same distribution as the expected counts.

H<sub>A</sub>: There is an inconsistency between the observed and the expected counts. The observed counts <u>do not</u> follow the same distribution as the expected counts. There is a bias in which side comes up on the roll of a die.

## **Evaluating the hypotheses**

To evaluate these hypotheses, we quantify how different the observed counts are from the expected counts.

Large deviations from what would be expected based on sampling variation (chance) alone provide strong evidence for the alternative hypothesis.

This is called a goodness of fit test since we're evaluating how well the observed data fit the expected distribution.

### Anatomy of a test statistic

The general form of a test statistic is point estimate – null value SE of point estimate

This construction is based on

- identifying the difference between a point estimate and an expected value if the null hypothesis was true, and
- standardizing that difference using the standard error of the point estimate.

These two ideas will help in the construction of an appropriate test statistic for count data.

### **Chi-square statistic**

When dealing with counts and investigating how far the observed counts are from the expected counts, we use a new test statistic called the chi-square ( $\chi^2$ ) statistic.

χ<sup>2</sup> statistic

$$\chi^2 = \sum_{i=1}^k \frac{(O-E)^2}{E}$$
 where  $k = \text{total number of cells}$ 

# Calculating the chi-square statistic

Outcome	Observed	Expected	$\frac{(O-E)^2}{E}$
1	53,222	52,612	$\frac{(53,222-52,612)^2}{52,612} = 7.07$
2	52,118	52,612	$\frac{(52,118-52,612)^2}{52,612} = 4.64$
3	52,465	52,612	$\frac{(52,465-52,612)^2}{52,612} = 0.41$
4	52,338	52,612	$\frac{(52,338-52,612)^2}{52,612} = 1.43$
5	52,244	52,612	$\frac{(52,244-52,612)^2}{52,612} = 2.57$
6	53,285	52,612	$\frac{(53,285-52,612)^2}{52,612} = 8.61$
Total	315,672	315,672	24.73

# Why square?

Squaring the difference between the observed and the expected outcome does two things:

- Any standardized difference that is squared will now be positive.
- Differences that already looked unusual will become much larger after being squared.

When have we seen this before?

## The chi-square distribution

In order to determine if the  $\chi^2$  statistic we calculated is considered unusually high or not we need to first describe its distribution.

The chi-square distribution has just one parameter called degrees of freedom (df), which influences the shape, center, and spread of the distribution.

#### Remember

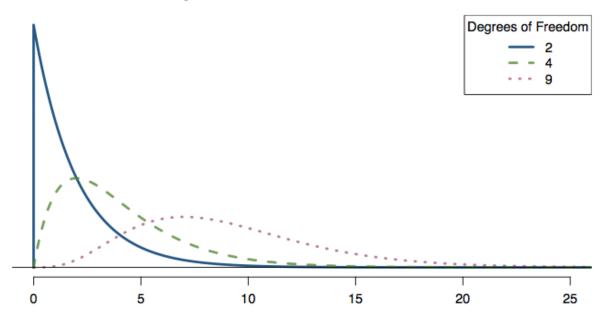
So far we've seen two other continuous distributions:

- normal distribution: unimodal and symmetric with two parameters:
   mean and standard deviation
- t distribution: unimodal and symmetric with one parameter: degrees of freedom

Unlike Normal and t distribution,  $\chi^2$  only cover the positive area (0, +inf) on the x-axis

#### **Practice**

Which of the following is false?

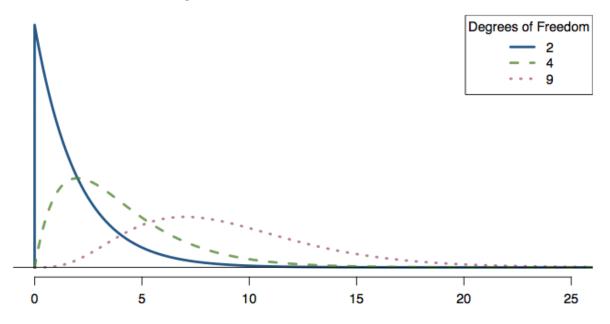


As the df increases,

- (a) the center of the  $\chi^2$  distribution increases as well
- (b) the variability of the  $\chi^2$  distribution increases as well
- (c) the shape of the  $\chi^2$  distribution becomes more skewed (less like a normal)

#### **Practice**

Which of the following is false?

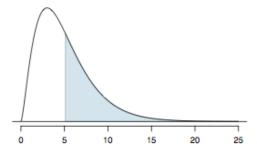


As the df increases,

- (a) the center of the  $\chi^2$  distribution increases as well
- (b) the variability of the  $\chi^2$  distribution increases as well
- (c) the shape of the  $\chi^2$  distribution becomes more skewed (less like a normal)

# Finding areas under the chi-square curve

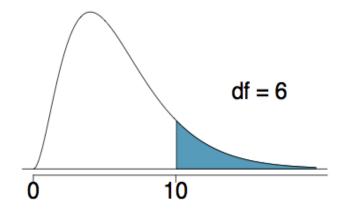
- p-value = tail area under the chi-square distribution (as usual)
- For this we can use technology, or a chi-square probability table.
- This table works a lot like the t table, but only provides upper tail values.



0.3 1.07	0.2 1.64	0.1	0.05	0.02	0.01	0.005	0.001
1.07	1.64	0.71					
		2.71	3.84	5.41	6.63	7.88	10.83
2.41	3.22	4.61	5.99	7.82	9.21	10.60	13.82
3.66	4.64	6.25	7.81	9.84	11.34	12.84	16.27
4.88	5.99	7.78	9.49	11.67	13.28	14.86	18.47
6.06	7.29	9.24	11.07	13.39	15.09	16.75	20.52
7.23	8.56	10.64	12.59	15.03	16.81	18.55	22.46
8.38	9.80	12.02	14.07	16.62	18.48	20.28	24.32
	2.41 3.66 4.88 6.06 7.23	2.41       3.22         3.66       4.64         4.88       5.99         6.06       7.29         7.23       8.56	2.41       3.22       4.61         3.66       4.64       6.25         4.88       5.99       7.78         6.06       7.29       9.24         7.23       8.56       10.64	2.41       3.22       4.61       5.99         3.66       4.64       6.25       7.81         4.88       5.99       7.78       9.49         6.06       7.29       9.24       11.07         7.23       8.56       10.64       12.59	2.41     3.22     4.61     5.99     7.82       3.66     4.64     6.25     7.81     9.84       4.88     5.99     7.78     9.49     11.67       6.06     7.29     9.24     11.07     13.39       7.23     8.56     10.64     12.59     15.03	2.41     3.22     4.61     5.99     7.82     9.21       3.66     4.64     6.25     7.81     9.84     11.34       4.88     5.99     7.78     9.49     11.67     13.28       6.06     7.29     9.24     11.07     13.39     15.09       7.23     8.56     10.64     12.59     15.03     16.81	2.41     3.22     4.61     5.99     7.82     9.21     10.60       3.66     4.64     6.25     7.81     9.84     11.34     12.84       4.88     5.99     7.78     9.49     11.67     13.28     14.86       6.06     7.29     9.24     11.07     13.39     15.09     16.75       7.23     8.56     10.64     12.59     15.03     16.81     18.55

# Finding areas under the chi-square curve (cont.)

Estimate the shaded area under the chi-square curve with df = 6.

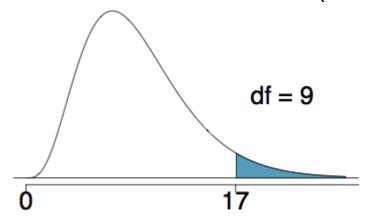


$$P(\chi^2_{df=6} > 10)$$
 is between 0.1 and 0.2

Upper tail	0.3	0.2	0.1	0.05	0.02	0.01	0.005	0.001
df 1	1.07	1.64	2.71	3.84	5.41	6.63	7.88	10.83
2	2.41	3.22	4.61	5.99	7.82	9.21	10.60	13.82
3	3.66	4.64	6.25	7.81	9.84	11.34	12.84	16.27
4	4.88	5.99	7.78	9.49	11.67	13.28	14.86	18.47
5	6.06	7.29	9.24	11.07	13.39	15.09	16.75	20.52
6	7.23	8.56	10.64	12.59	15.03	16.81	18.55	22.46
7	8.38	9.80	12.02	14.07	16.62	18.48	20.28	24.32

# Finding areas under the chi-square curve (cont.)

Estimate the shaded area (above 17) under the  $\chi^2$  curve with df = 9.

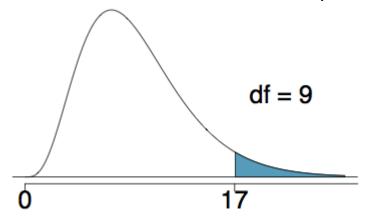


- (a) between 0.01 and 0.02
- (b) 0.02
- (c) between 0.02 and 0.05
- (d) 0.05
- (e) between 0.05 and 0.10

Upper tail	0.3	0.2	0.1	0.05	0.02	0.01	0.005	0.001
df 7	8.38	9.80	12.02	14.07	16.62	18.48	20.28	24.32
8	9.52	11.03	13.36	15.51	18.17	20.09	21.95	26.12
9	10.66	12.24	14.68	16.92	19.68	21.67	23.59	27.88
	11.78				l .			
11	12.90	14.63	17.28	19.68	22.62	24.72	26.76	31.26

# Finding areas under the chi-square curve (cont.)

Estimate the shaded area (above 17) under the  $\chi^2$  curve with df = 9.



- (a) between 0.01 and 0.02
- (b) 0.02
- (c) between 0.02 and 0.05
- (d) 0.05
- (e) between 0.05 and 0.10

Upper tail	0.3	0.2	0.1	0.05	0.02	0.01	0.005	0.001
df 7	1					18.48		
8						20.09		
9						21.67		
10	11.78	13.44	15.99	18.31	21.16	23.21	25.19	29.59
11	12.90	14.63	17.28	19.68	22.62	24.72	26.76	31.26

# Finding the tail areas using computation

While probability tables are very helpful in understanding how probability distributions work, and provide quick reference when computational resources are not available, they are somewhat archaic.

#### Using R:

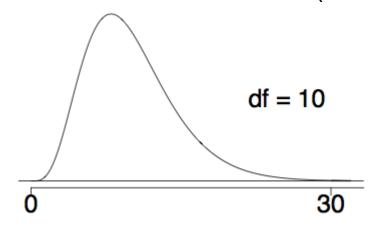
```
pchisq(q = 17, df = 9, lower.tail = FALSE) \# 0.04871598
```

#### Using a web applet:

http://bitly.com/dist\_calc

# Finding areas under the chi-square curve (one more)

Estimate the shaded area (above 30) under the  $\chi^2$  curve with df = 10.

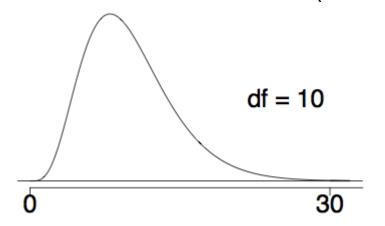


- (a) between 0.005 and 0.001
- (b) less than 0.001
- (c) greater than 0.001
- (d) greater than 0.3
- (e) cannot tell using this table

Upper	tail	0.3	0.2	0.1	0.05	0.02	0.01	0.005	0.001
df	7	8.38	9.80	12.02	14.07	16.62	18.48	20.28	24.32
	8	9.52	11.03	13.36	15.51	18.17	20.09	21.95	26.12
	9	10.66	12.24	14.68	16.92	19.68	21.67	23.59	27.88
	10	11.78	13.44	15.99	18.31	21.16	23.21	25.19	29.59
	11	12.90	14.63	17.28	19.68	22.62	24.72	26.76	31.26

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Estimate the shaded area (above 30) under the  $\chi^2$  curve with df = 10.



- (a) between 0.005 and 0.001
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- (d) greater than 0.3
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Upper tail	0.3	0.2	0.1	0.05	0.02	0.01	0.005	0.001	$\rightarrow$
df 7	8.38	9.80	12.02	14.07	16.62	18.48	20.28	24.32	]
8	9.52	11.03	13.36	15.51	18.17	20.09	21.95	26.12	
9	10.66	12.24	14.68	16.92	19.68	21.67	23.59	27.88	
10	11.78	13.44	15.99	18.31	21.16	23.21	25.19	29.59	$\rightarrow$
11	12.90	14.63	17.28	19.68	22.62	24.72	26.76	31.26	

### **Back to Labby's dice**

The research question was: Do these data provide convincing evidence of an inconsistency between the observed and expected counts?

The hypotheses were:

H<sub>0</sub>: There is no inconsistency between the observed and the expected counts. The observed counts follow the same distribution as the expected counts.

H<sub>A</sub>: There is an inconsistency between the observed and the expected counts. The observed counts <u>do not</u> follow the same distribution as the expected counts. There is a bias in which side comes up on the roll of a die.

We had calculated a test statistic of  $\chi^2 = 24.67$ .

All we need is the df and we can calculate the tail area (the p-value) and make a decision on the hypotheses.

# Degrees of freedom for a goodness of fit test

When conducting a goodness of fit test to evaluate how well the observed data follow an expected distribution, the degrees of freedom are calculated as the number of cells (k) minus 1.

$$df = k - 1$$

For dice outcomes, k = 6, therefore

$$df = 6 - 1 = 5$$

# Finding a p-value for a chi-square test

The p-value for a chi-square test is defined as the tail area above

the calculated test statistic

df = 5

use R code:

pchisq(24.67, df=5, lower.tail=FALSE)
#0.0001613338

p-value = 
$$P(\chi_{df=5}^2 > 24.67)$$
 is less than 0.001

Upper	tail	0.3	0.2	0.1	0.05	0.02	0.01	0.005	0.001	$\rightarrow$
df	1	1.07	1.64	2.71	3.84	5.41	6.63	7.88	10.83	
	2	2.41	3.22	4.61	5.99	7.82	9.21	10.60	13.82	
	3	3.66	4.64	6.25	7.81	9.84	11.34	12.84	16.27	
	4	4.88	5.99	7.78	9.49	11.67	13.28	14.86	18.47	
	5	6.06	7.29	9.24	11.07	13.39	15.09	16.75	20.52	$\rightarrow$

# Conclusion of the hypothesis test

We calculated a p-value less than 0.001. At 5% significance level, what is the conclusion of the hypothesis test?

- (a) Reject H<sub>0</sub>, the data provide convincing evidence that the dice are fair.
- (b) Reject H<sub>0</sub>, the data provide convincing evidence that the dice are biased.
- (c) Fail to reject H<sub>0</sub>, the data provide convincing evidence that the dice are fair.
- (d) Fail to reject H<sub>0</sub>, the data provide convincing evidence that the dice are biased.

# Conclusion of the hypothesis test

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- (d) Fail to reject H<sub>0</sub>, the data provide convincing evidence that the dice are biased.

#### Turns out...

The 1-6 axis is consistently shorter than the other two (2-5 and 3-4), thereby supporting the hypothesis that the faces with one and six pips are larger than the other faces.

Pearson's claim that 5s and 6s appear more often due to the carved-out pips is not supported by these data.

Dice used in casinos have flush faces, where the pips are filled in with a plastic of the same density as the surrounding material and are precisely balanced.

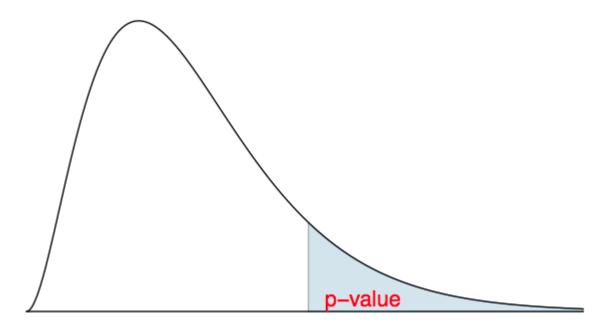




# Recap: p-value for a chi-square test

The p-value for a chi-square test is defined as the tail area above the calculated test statistic.

This is because the test statistic is always positive, and a higher test statistic means a stronger deviation from the null hypothesis.



# Conditions for the chi-square test

Independence: Each case that contributes a count to the table must be independent of all the other cases in the table.

Sample size: Each particular scenario (i.e. cell) must have at least 5 <u>expected</u> cases.

df > 1: Degrees of freedom must be greater than 1.

Failing to check conditions may unintentionally affect the test's error rates.

#### 2009 Iran Election

There was lots of talk of election fraud in the 2009 Iran election (http://news.bbc.co.uk/2/hi/middle\_east/8099115.stm). We'll compare the data from a poll conducted before the election (observed data) to the reported votes in the election to see if the two follow the same distribution.

	Observed # of	Reported % of
Candidate	voters in poll	votes in election
(1) Ahmedinajad	338	63.29%
(2) Mousavi	136	34.10%
(3) Minor candidates	30	2.61%
Total	504	100%
	<b>↓</b>	<b>↓</b>
	observed	expected
		distribution

## **Hypotheses**

What are the hypotheses for testing if the distributions of reported and polled votes are different?

H<sub>0</sub>: The observed counts from the poll follow the same distribution as the reported votes.

 $H_A$ : The observed counts from the poll do not follow the same distribution as the reported votes.

### Calculation of the test statistic

	Observed # of	Reported % of	Expected # of
Candidate	voters in poll	votes in election	votes in poll
(1) Ahmedinajad	338	63.29%	$504 \times 0.6329 = 319$
(2) Mousavi	136	34.10%	$504 \times 0.3410 = 172$
(3) Minor candidates	30	2.61%	$504 \times 0.0261 = 13$
Total	504	100%	504

$$\frac{(O_1 - E_1)^2}{E_1} = \frac{(338 - 319)^2}{319} = 1.13$$

$$\frac{(O_2 - E_2)^2}{E_2} = \frac{(136 - 172)^2}{172} = 7.53$$

$$\frac{(O_2 - E_2)^2}{E_2} = \frac{(30 - 13)^2}{13} = 22.23$$

$$\chi^2_{df=3-1=2} = 30.89$$

> pchisq(30.89, df=2, lower.tail=FALSE)

#### Conclusion

Based on these calculations what is the conclusion of the hypothesis test?

- (a) p-value is low, H<sub>0</sub> is rejected. The observed counts from the poll do <u>not</u> follow the same distribution as the reported votes.
- (b) p-value is high, H<sub>0</sub> is not rejected. The observed counts from the poll follow the same distribution as the reported votes.
- (c) p-value is low, H<sub>0</sub> is rejected. The observed counts from the poll follow the same distribution as the reported votes
- (d) p-value is low,  $H_0$  is not rejected. The observed counts from the poll do <u>not</u> follow the same distribution as the reported votes.

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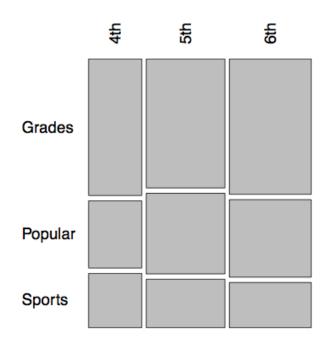
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- (d) p-value is low, H<sub>0</sub> is not rejected. The observed counts from the poll do \underline{not} follow the same distribution as the reported votes.

# **Chi-Square Test of Independence**

## Popular kids

In the dataset popular, students in grades 4-6 were asked whether good grades, athletic ability, or popularity was most important to them. A two-way table separating the students by grade and by choice of most important factor is shown below. Do these data provide evidence to suggest that goals vary by grade?

	Grades	Popular	Sports
$4^{th}$	63	31	25
$5^{th}$	88	55	33
$6^{th}$	96	55	32



## Chi-square test of independence

#### The hypotheses are:

H<sub>0</sub>: Grade and goals are independent. Goals do not vary by grade.

H<sub>A</sub>: Grade and goals are dependent. Goals vary by grade.

## Chi-square test of independence

#### The hypotheses are:

H<sub>0</sub>: Grade and goals are independent.

Goals do not vary by grade.

H<sub>A</sub>: Grade and goals are dependent.

Goals vary by grade.

The test statistic is calculated as

$$\chi_{df}^2 = \sum_{i=1}^k \frac{(O-E)^2}{E}$$
 where  $df = (R-1) \times (C-1)$ ,

where k is the number of cells, R is the number of rows, and C is the number of columns.

Note: we calculate df differently for one-way and two-way tables.

The p-value is the area under the  $\chi^2_{df}$  curve, above the calculated test statistic.

## **Expected counts in two-way tables**

$$\mathsf{Expected Count} = \frac{(\mathsf{row} \; \mathsf{total}) \times (\mathsf{column} \; \mathsf{total})}{\mathsf{table} \; \mathsf{total}}$$

	Grades	Popular	Sports	Total
$4^{th}$	63	31	25	119
$5^{th}$	88	55	33	176
$6^{th}$	96	55	32	183
Total	247	141	90	478

$$E_{row \ 1,col \ 1} = \frac{119 \times 247}{478} = 61$$
  $E_{row \ 1,col \ 2} = \frac{119 \times 141}{478} = 35$ 

## **Expected counts in two-way tables**

What is the expected count for the highlighted cell?

	Grades	Popular	Sports	Total
$4^{th}$	63	31	25	119
$5^{th}$	88	<i>55</i>	33	176
$6^{th}$	96	55	32	183
Total	247	141	90	478

- (a) 176 x 141 / 478
- (b) 119 x 141 / 478
- (c) 176 x 247 / 478
- (d) 176 x 478 / 478

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(b) 119 x 141 / 478

(c) 176 x 247 / 478

(d) 176 x 478 / 478

 $\rightarrow$  52

more than expected # of 5th graders have a goal of being popular

# Calculating the test statistic in twoway tables

Expected counts are shown in blue next to the observed counts.

	Grades	Popular	Sports	Total
$4^{th}$	63 <i>61</i>	31 <i>35</i>	25 <b>23</b>	119
$5^{th}$	88 <mark>91</mark>	55 <b>52</b>	33 <mark>33</mark>	176
$6^{th}$	96 <mark>95</mark>	55 <b>54</b>	32 <b>34</b>	183
Total	247	141	90	478

$$\chi^{2} = \sum \frac{(63-61)^{2}}{61} + \frac{(31-35)^{2}}{35} + \dots + \frac{(32-34)^{2}}{34} = 1.3121$$

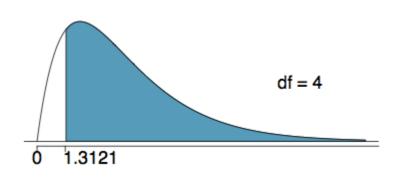
$$df = (R-1) \times (C-1) = (3-1) \times (3-1) = 2 \times 2 = 4$$

# Calculating the p-value

Which of the following is the correct p-value for this hypothesis test?

$$\chi^2_{df} = 1.3121$$





- (a) more than 0.3
- (b) between 0.3 and 0.2
- (c) between 0.2 and 0.1
- (d) between 0.1 and 0.05
- (e) less than 0.001

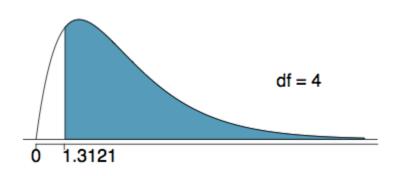
									0.001
df	1	1.07	1.64	2.71	3.84	5.41	6.63	7.88	10.83
									13.82
;	3	3.66	4.64	6.25	7.81	9.84	11.34	12.84	16.27
									18.47
	5	6.06	7.29	9.24	11.07	13.39	15.09	16.75	20.52

# Calculating the p-value

Which of the following is the correct p-value for this hypothesis test?

$$\chi^2_{df} = 1.3121$$

$$df = 4$$



#### (a) more than 0.3

- (b) between 0.3 and 0.2
- (c) between 0.2 and 0.1
- (d) between 0.1 and 0.05
- (e) less than 0.001

		I							0.001
df	1	1.07	1.64	2.71	3.84	5.41	6.63	7.88	10.83
									13.82
	3	3.66	4.64	6.25	7.81	9.84	11.34	12.84	16.27
	4	4.88	5.99	7.78	9.49	11.67	13.28	14.86	18.47
	5	6.06	7.29	9.24	11.07	13.39	15.09	16.75	20.52

#### Conclusion

Do these data provide evidence to suggest that goals vary by grade?

H<sub>0</sub>: Grade and goals are independent.

Goals do not vary by grade.

H<sub>A</sub>: Grade and goals are dependent.

Goals vary by grade.

Since the p-value is large, we fail to reject  $H_0$ . The data do not provide convincing evidence that grade and goals are dependent. It doesn't appear that goals vary by grade.

#### **Gender Discrimination**

		Pro		
		Promoted	Not Promoted	Total
Gender	Male	21	3	24
	Female	14	10	24
	Total	35	13	48

H<sub>0</sub>: Promotion and gender are independent, no gender discrimination;

H<sub>A</sub>: Promotion and gender are dependent, there is gender discrimination.

#### With R:

Table 1. Weighted sample demographics for those who reported meeting on-line and off-line and significance tests for differences between the groups

Weighted means

		weighted means	
Demographic	On-line	Off-line	Significance test
n	6,654	12,384	
Percent female	44.72	56.98	$\chi^2(1) = 127.48*$
Age (y)			
Mean	37.99 (0.22)	37.74 (0.16)	$F_{(1, 17,985)} = 0.41$
18–29	21.43%	26.40%	$\chi^2(4) = 42.94*$
30–39	40.92%	36.74%	
40-49	22.57%	19.19%	
50–64	12.02%	14.09%	
65+	3.05%	3.57%	
Ethnicity			
White/Caucasian	64.01%	69.89%	$\chi^2(4) = 176.12*$
Black/African American	6.45%	9.70%	
Hispanic	24.54%	14.92%	
Asian or Pacific Islander	2.79%	2.75%	
Other	1.28%	1.45%	
Income			
Less than \$15,000	2.39%	4.37%	$\chi^2(6) = 324.14*$
\$15,000 to \$24,999	4.08%	7.57%	
\$25,000 to \$34,999	6.01%	8.88%	
\$35,000 to \$49,999	9.67%	13.44%	
\$50,000 to \$74,999	18.41%	20.36%	
\$75,000 to \$99,999	16.29%	14.05%	
\$100,000 or more	40.50%	26.14%	
Education			
High school or less	18.24%	26.57%	$\chi^2(3) = 80.71*$
Associates or job training	17.79%	17.43%	*
College	49.26%	43.90%	
Graduate school	14.70%	12.11%	
Religious affiliation			
Catholic	23.49%	23.60%	$\chi^{2}(6) = 64.81*$
Christian/Protestant	40.02%	37.31%	70
Jewish	4.42%	2.00%	
Mormon	2.13%	2.06%	
Spiritual, but unaffiliated	13.47%	15.58%	
Athiest/No Religion	8.60%	10.50%	
Other religion	7.86%	8.95%	
Employment Status			
Used full or part time	82.84%	70.85%	$\chi^2(1) = 178.97*$
Retired	6.13%	6.84%	$\chi^{2}(1) = 1.31$
Student	8.21%	8.70%	$\chi^{2}(1) = 0.75$
Stay at home parent	18.50%	26.64%	$\chi^2(1) = 86.42*$

Because of the number of unpredicted comparisons, we set significance at \*P < 0.005. The  $\chi^2$  tests were done using a Rao-Scott Correction to account for weighting the sample. Small percentages of participants did not report ethnicity (1.2%) or Income (4.3%) so column totals do not add to 100%. Because individuals could select multiple employment categories,  $\chi^2$  tests were done for each employment status individually.

Cacioppo, et al, 2013. (Table 1), page 10137.