8/12/24, 11:56 AM Assignment 4

Assignment 4

Question 1

```
In [5]: import numpy as np
             import random
            def hits(N):
                  black_hits = 0
purple_hits = 0
                   green hits = 0
                  blue_hits = 0
red_hits = 0
                  out_hits = 0
                   for i in range(N):
                      x = random.uniform(-1, 1)
y = random.uniform(-1, 1)
                        r = np.sqrt(x**2 + y**2)
                        if r <= 0.1:
                        black_hits += 1
elif r <= 0.3:</pre>
                        purple_hits += 1
elif r <= 0.5:
    green_hits += 1
elif r <= 0.7:
    blue_hits += 1</pre>
                        elif r <= 1.0:
                        red_hits += 1
else:
                              out_hits += 1
                   # Probabilities
                  # Probabilities
total_hits = black_hits + purple_hits + green_hits + blue_hits + red_hits + out_hits
black_prob = black_hits / total_hits
purple_prob = purple_hits / total_hits
green_prob = green_hits / total_hits
blue_prob = blue_hits / total_hits
red_prob = red_hits / total_hits
                  return black_prob, purple_prob, green_prob, blue_prob, red_prob
            \verb|black_prob|, purple_prob|, green_prob|, blue_prob|, red_prob| = \verb|hits(N_sims)|
            print("Probability of hitting each section:")
            print("Black:", black_prob)
print("Burple:", purple_prob)
print("Green:", green_prob)
print("Blue:", blue_prob)
print("Red:", red_prob)
            probabilities = [black_prob, purple_prob, green_prob, blue_prob, red_prob]
scores = [1, 2, 3, 4, 5]
            probabilities = [black_prob, purple_prob, green_prob, blue_prob, red_prob]
            probabilities = np.array(probabilities)
probabilities /= probabilities.sum()
            hit = np.random.choice(scores, size=N, p=probabilities)
            print(f"The Long-term average score per shot is : {average_score:.2f}")
           Probability of hitting each section: Black: 0.008
           Purple: 0.06375
           Green: 0.12635
Blue: 0.187
           Red: 0.4022
The Long-term average score per shot is : 4.16
```

Question 2

```
In [6]: import numpy as np

#iterations and daily prob
iterations = 17000
prob more_than_4 = 0.4

#over 4 bikes sold prob
num_bikes_probabilities = [0.4, 0.35, 0.2, 0.05]
num_bikes_sold = [5, 6, 7, 8]

#model prob
model_probabilities = [0.45, 0.35, 0.15, 0.05]
model_bonuses = [10, 15, 25, 30]

#simulation
total_bonus = 0

for _ in range(iterations):
    if np.random.rand() < prob_more_than_4:
        # Determine the number of bikes sold
        num_bikes = np.random.choice(num_bikes_sold, p=num_bikes_probabilities)

    # Calculate the bonus for each bike sold
    for _ in range(num_bikes):</pre>
```

Question 3

```
In [3]: import numpy as np
              start_age = 24
end_age = 60
years = end_age - start_age
              initial_salary = 55000
              contribution_rate = 0.09 #both
              avg_salary_raise = 0.0283
std_salary_raise = 0.0072
              investment allocation = {
                     "A": 0.50,
"B": 0.25,
"C": 0.25
              investment_returns = {
    "A": {"mean": 0.0691, "std": 0.1289},
    "B": {"mean": 0.0894, "std": 0.1521},
    "C": {"mean": 0.0988, "std": 0.1714}
              final balances = []
               for _ in range(iterations):
    salary = initial_salary
    balance = 0
                     for year in range(years):
    annual_contribution = salary * contribution_rate
                            for investment, allocation in investment_allocation.items():
    contribution = annual_contribution * allocation
    annual_return = np.random.normal(investment_returns[investment]["mean"], investment_returns[investment]["std"])
    balance += contribution * (1 + annual_return)
                            salary_raise = np.random.normal(avg_salary_raise, std_salary_raise)
salary *= (1 + salary_raise)
                     final_balances.append(balance)
              expected_final_balance = np.mean(final_balances)
print(f"Expected 401(k) Balance at Age 60: ${expected_final_balance:.2f}")
            Expected 401(k) Balance at Age 60: $327461.79
```

Question 4

```
In [7]: import random
              #parameters
             values = [12, 16, 22, 8]
weights = [4, 5, 7, 3]
capacity = 140
             max_quantity = 10
num_items = len(values)
             def greedy_heuristic(values, weights, capacity, max_quantity):
                    value weight ratio = [(values[i] / weights[i], i) for i in range(len(values))]
                    value_weight_ratio.sort(reverse=True, key=lambda x: x[0])
                    total_weight = 0
                    solution = [0] * num_items
                   for ratio, i in value_weight_ratio:
    if total_weight < capacity:
        max_add = min(max_quantity, (capacity - total_weight) // weights[i])
        solution[i] = max_add
        total_value += max_add * values[i]
        total_weight += max_add * weights[i]</pre>
                   return total_value, solution
             def random_restart_heuristic(values, weights, capacity, max_quantity, n_iterations):
    best_value = 0
                   best_solution = None
                   for _ in range(n_iterations):
    random_values = values[:]
    random.shuffle(random_values)
    total_value, solution = greedy_heuristic(random_values, weights, capacity, max_quantity)
    if total_value > best_value:
        best_value = total_value
                                 best_solution = solution
                    return best_value, best_solution
```

```
#solve
n_iterations = 17000
best_value, best_solution = random_restart_heuristic(values, weights, capacity, max_quantity, n_iterations)
print(f"Best Value: {best_value}")
print(f"Best Solution: {best_solution}")
Best Value: 516
Best Solution: [10, 10, 2, 10]
```

Question 5

```
In [5]: import numpy as np
                 # Define the objective function and the constraint
                 def objective_function(x):
return 12 * x[0] + 16 * x[1] + 22 * x[2] + 8 * x[3]
                 def constraint(x):
                          return 4 * x[0] + 5 * x[1] + 7 * x[2] + 3 * x[3]
                # Simulated Annealing parameters
initial_temperature = 1000
cooling_rate = 0.95
iterations = 1000
                 min_temperature = 1e-5
                # Initial solution (randomLy generated within the bounds)
x_current = np.random.randint(0, 11, 4)
best_solution = x_current.copy()
best_value = objective_function(x_current)
                 # Simulated Annealing process
temperature = initial_temperature
                 for i in range(iterations):

# Generate a neighbor solution by modifying one of the variables
                         x_new = x_current.copy()
index = np.random.randint(0, 4)
                          x\_new[index] = np.clip(x\_new[index] + np.random.choice([-1, 1]), \ 0, \ 10) 
                          # Ensure the new solution satisfies the constraint
                        if constraint(x_new) <= 140:
    new_value = objective_function(x_new)</pre>
                                 # cutcute the acceptance proons
if new_value > best_value:
   best_value = new_value
   x_current = x_new.copy()
else:
                                         delta = new_value - best_value
acceptance_probability = np.exp(delta / temperature)
if np.random.rand() < acceptance_probability:
    x_current = X_new.copy()
                          # Cool down the temperature
                         temperature = max(temperature * cooling_rate, min_temperature)
                                 print(f"Iteration \ \{i\}: \ Best \ Value = \{best\_value\}, \ Best \ Solution = \{best\_solution\}")
                # Final result
print(f"\nFinal Solution: {best_solution}")
print(f"Final Objective Value: {best_value}")
              Iteration 0: Best Value = 358, Best Solution = [ 1 10 7 4]
Iteration 100: Best Value = 380, Best Solution = [ 1 10 8 4]
Iteration 200: Best Value = 380, Best Solution = [ 1 10 8 4]
Iteration 300: Best Value = 380, Best Solution = [ 1 10 8 4]
Iteration 400: Best Value = 380, Best Solution = [ 1 10 8 4]
Iteration 500: Best Value = 380, Best Solution = [ 1 10 8 4]
              Tteration 600: Best Value = 380, Best Solution = [ 1 10 8 4]
Tteration 700: Best Value = 380, Best Solution = [ 1 10 8 4]
Tteration 700: Best Value = 380, Best Solution = [ 1 10 8 4]
Tteration 800: Best Value = 380, Best Solution = [ 1 10 8 4]
Tteration 900: Best Value = 380, Best Solution = [ 1 10 8 4]
              Final Solution: [ 1 10 8 4]
Final Objective Value: 380
```