

No title because you have to listen to me talk

Can I make regression with fancy lingo beat Eilmer?

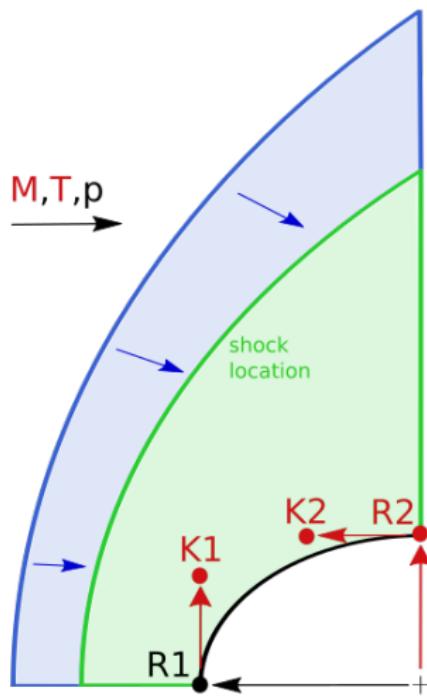
Machine Learning of Bow Shocks

Jamie Border

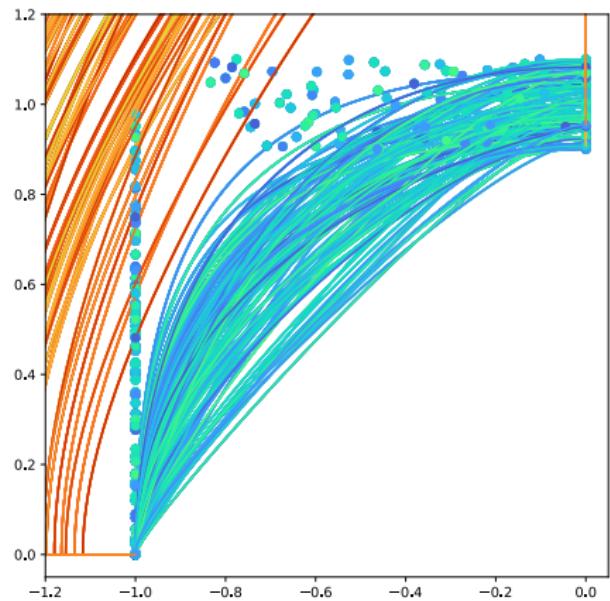
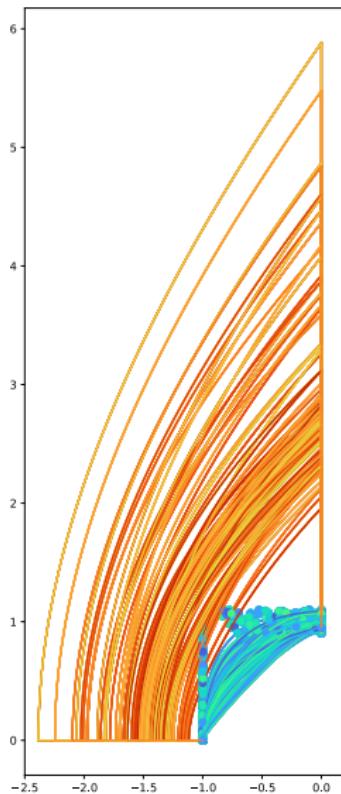
A Lightning Talk

November 18th, 2022

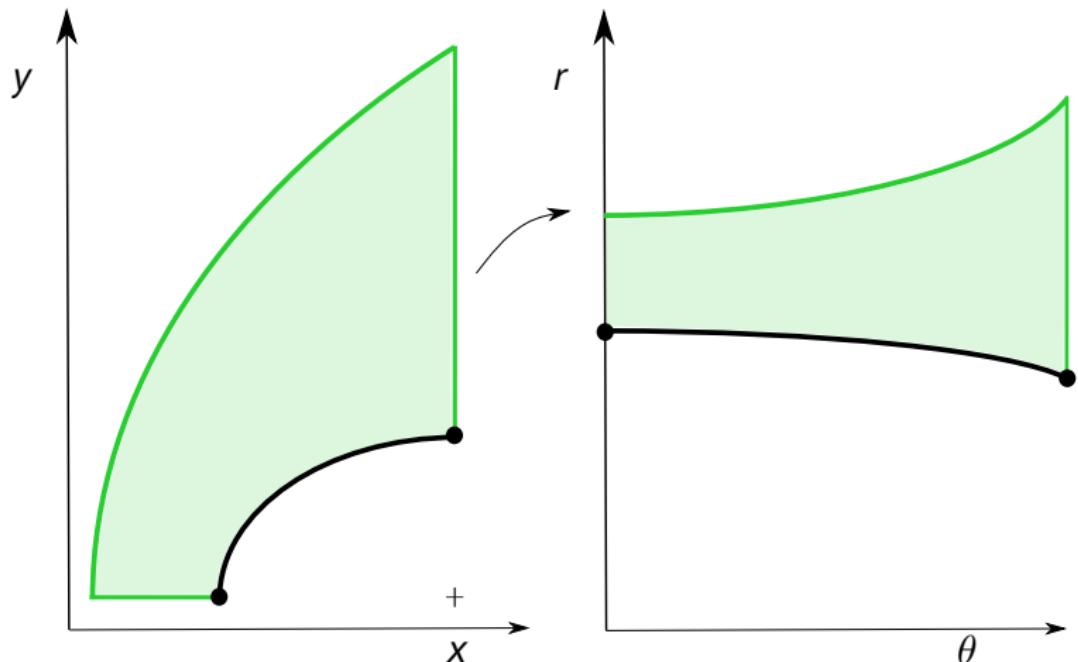
Problem definition



Randomly generated bodies and shock-fit bow shocks



Mapping from cartesian to polar coordinates



Fitting to shock data

$$r(\theta) = \sum_{k=0}^m a_k \theta^k, \quad \frac{dr(\theta)}{d\theta} = \sum_{k=1}^m k a_k \theta^{k-1}, \quad \theta = [0, \pi/2]$$

Least-squares fit,

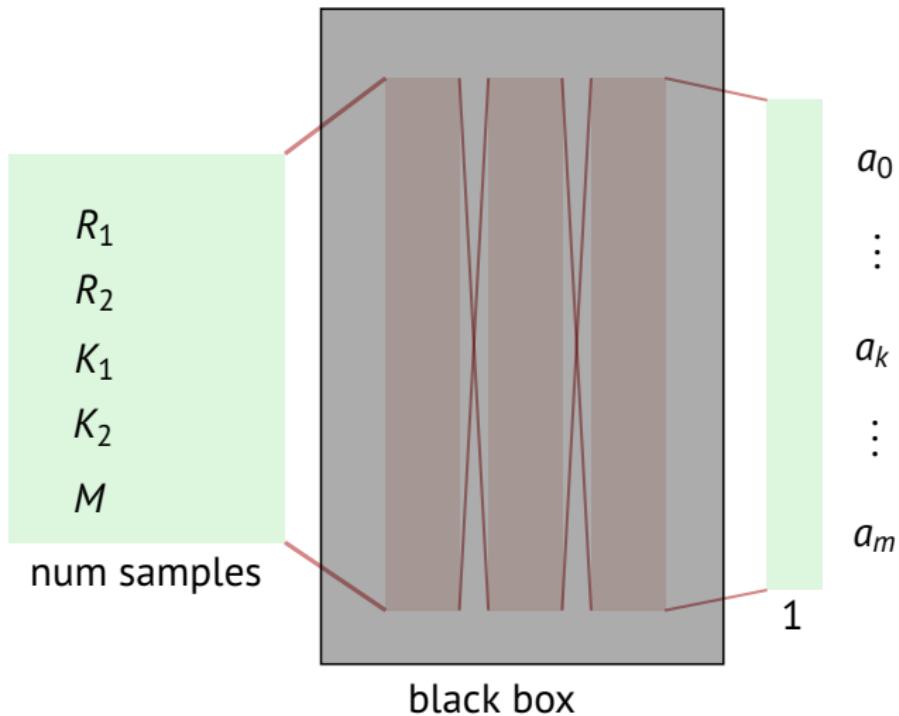
$$I = \sum_{i=1}^N \|r(\theta_i) - r_i\|^2;$$

in matrix form, solving $I = (\mathbf{Ax} - \mathbf{b})^2$, giving

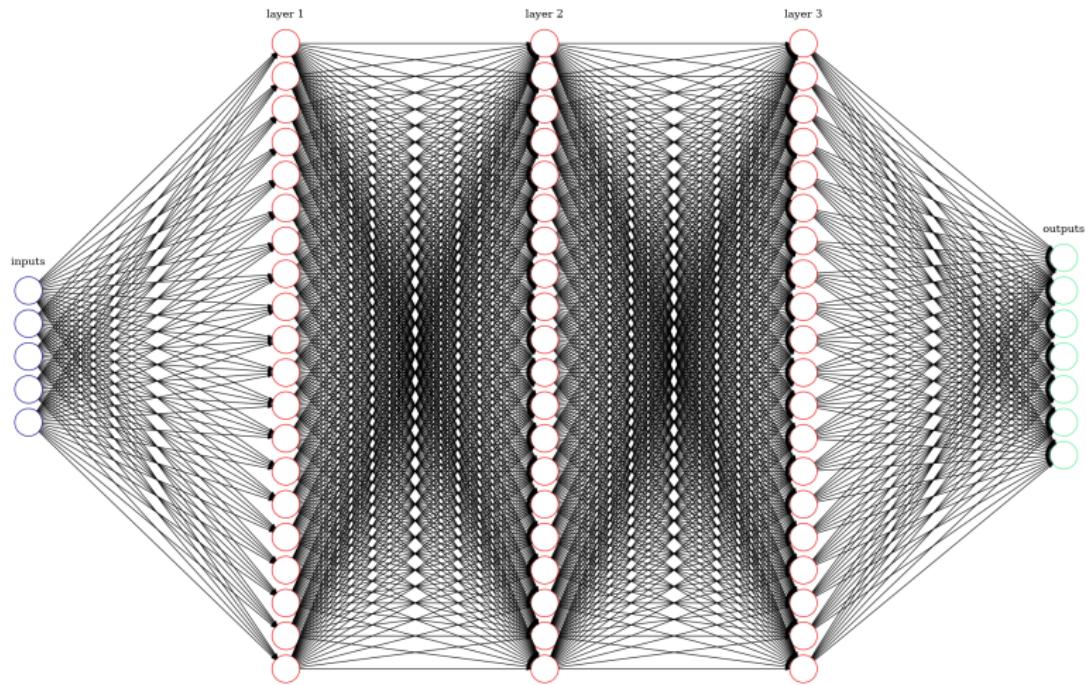
$$\mathbf{A}^T \mathbf{Ax} = \mathbf{A}^T \mathbf{b},$$

or if including gradient terms as constraints

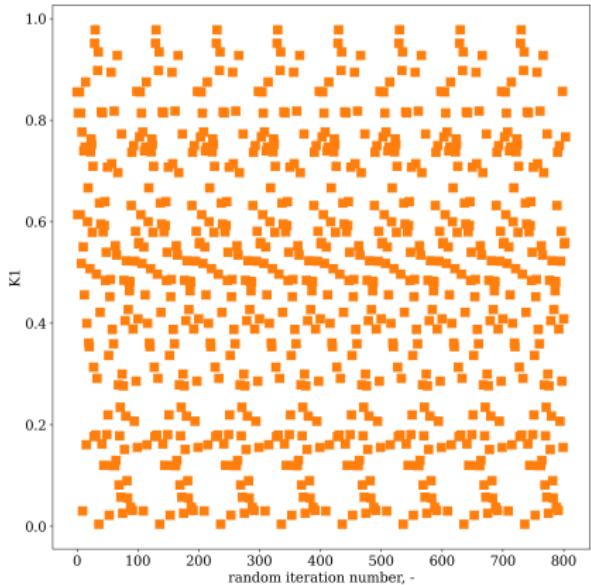
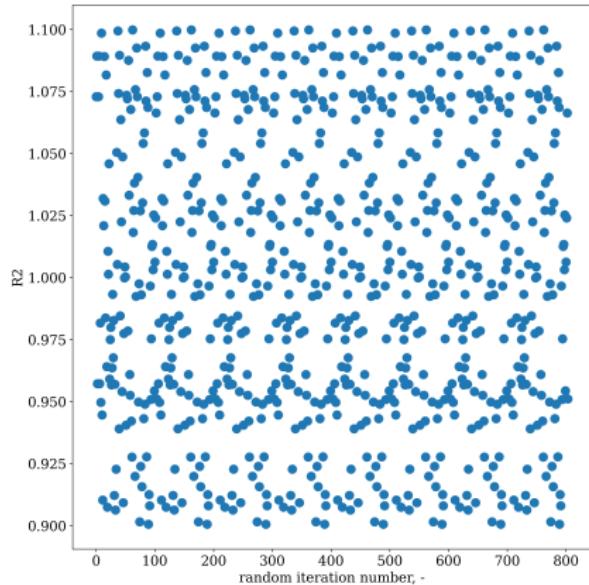
$$\begin{bmatrix} \mathbf{A}^T \mathbf{A} & \mathbf{C}^T \\ \mathbf{C} & \mathbf{0} \end{bmatrix} \begin{bmatrix} \mathbf{x} \\ \boldsymbol{\lambda} \end{bmatrix} = \begin{bmatrix} \mathbf{A}^T \mathbf{b} \\ \mathbf{d} \end{bmatrix}.$$



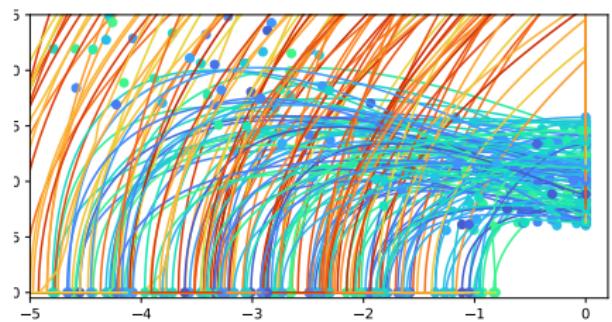
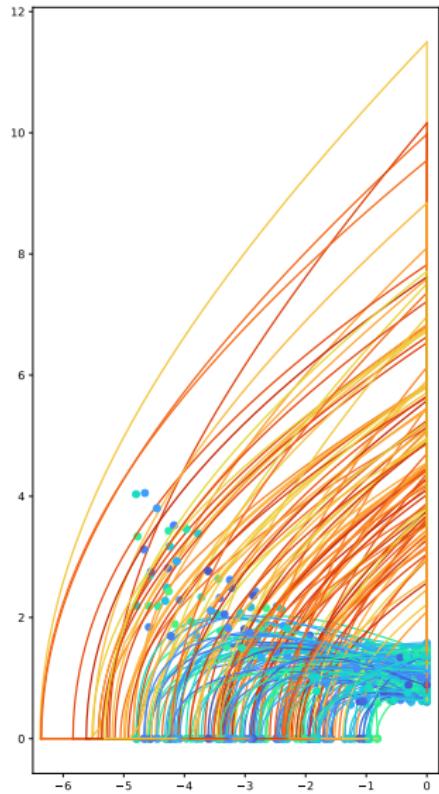
ML



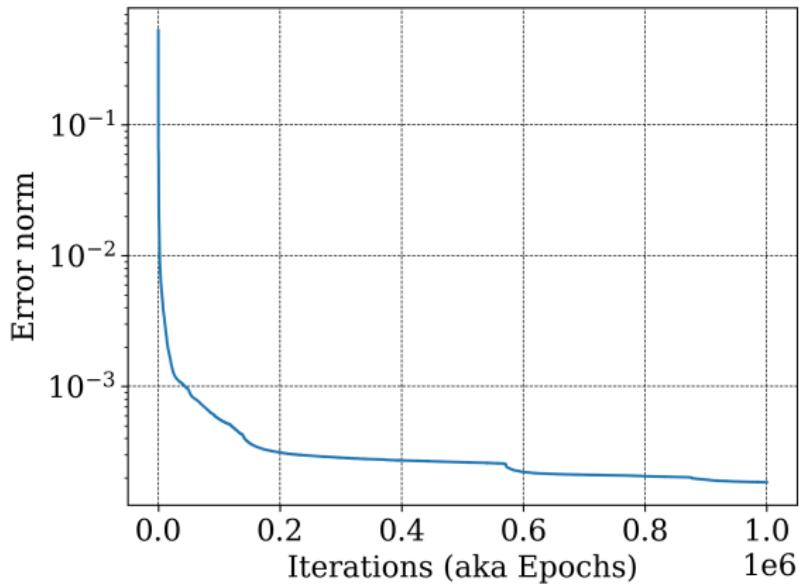
'Random' parameters



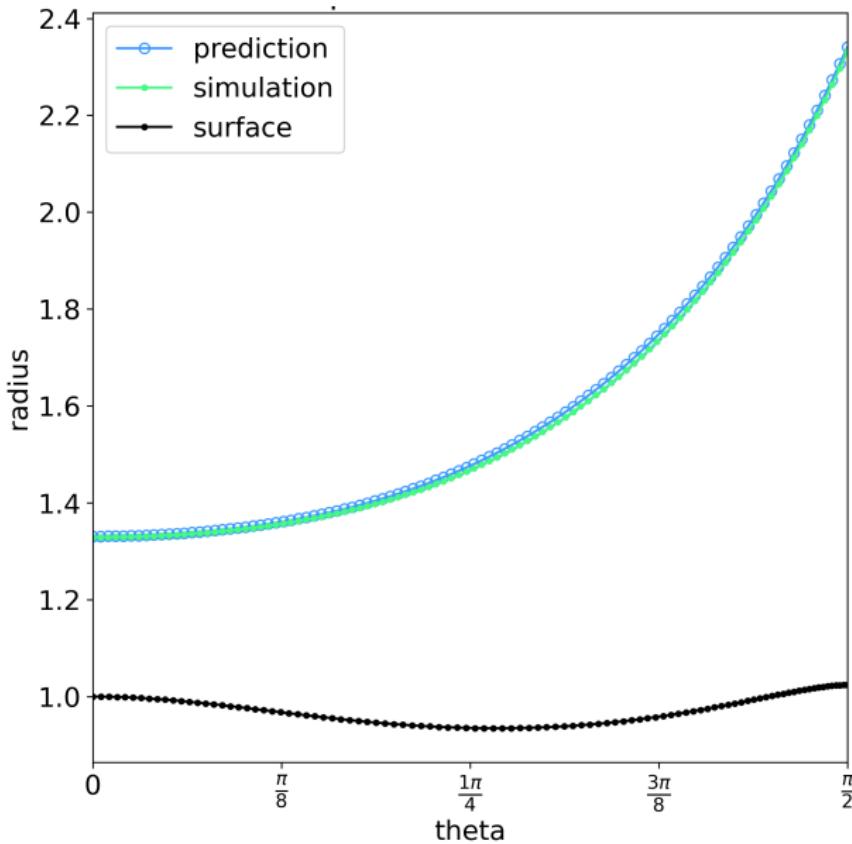
Poor randomly generated bodies and shock-fit bow shocks



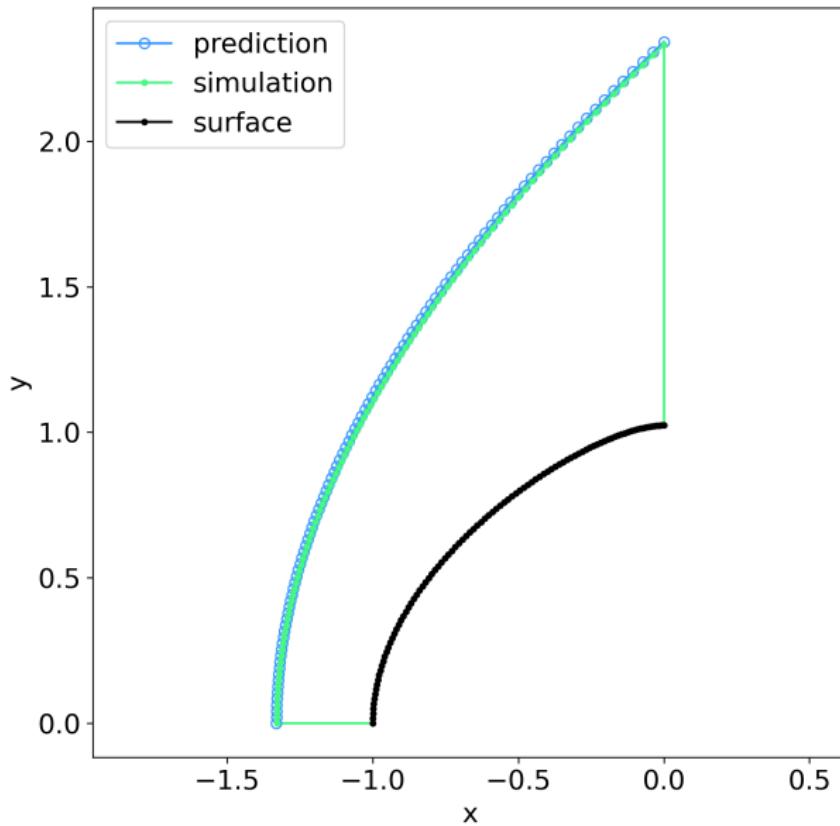
Convergence



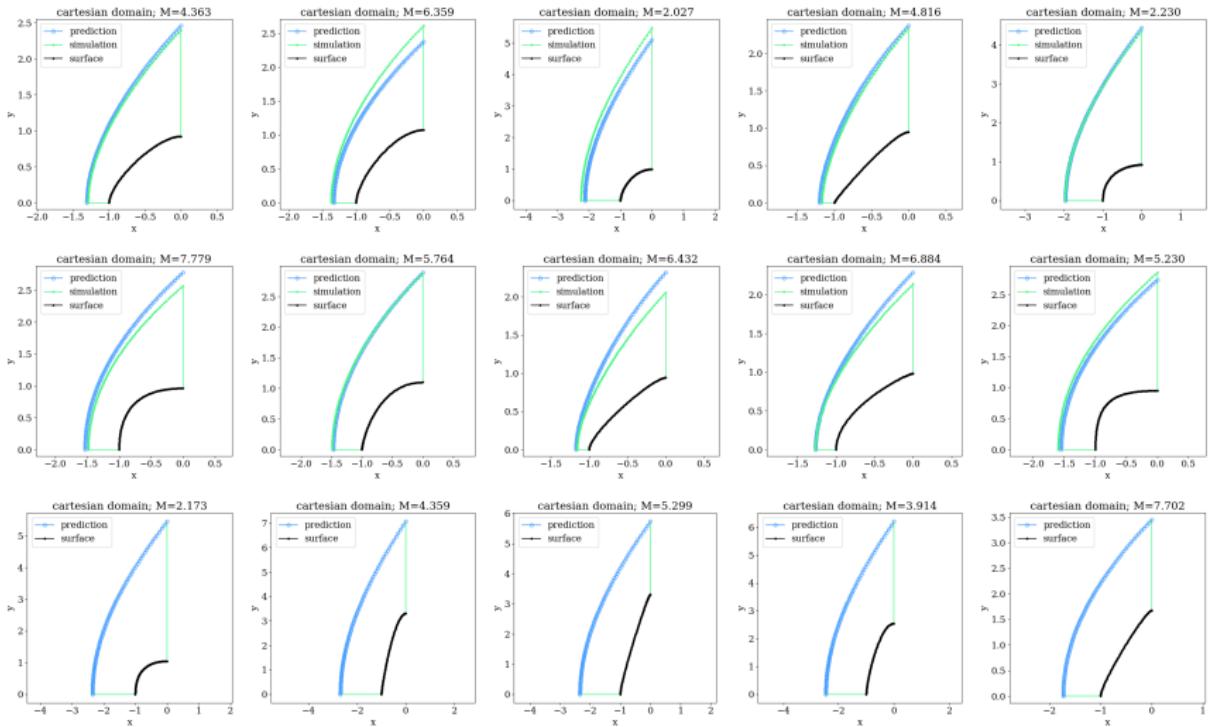
Example fit in polar coordinates



Example fit in cartesian coordinates



Test Results



Summary

“...did a thing that is known to be bad and it was bad” - known

- random data was not random
- parameters too broad for too little data
- many knobs to turn regarding data/parameter input and output
- so many knobs to turn regarding ML algorithm / structure / solution approach

Takeaways: nothing, please!