

Untitled

Jamie Ash

2022-12-09

Question 1. Prove each of the following. In each case, you should create a bijection between the two sets. Briefly justify that your function are in fact bijections.

- (a) $\{\heartsuit, \clubsuit, \spadesuit\} = \{\circ, \square, \triangle\}$
- (b) $\mathbb{N} = \{\text{oddnaturalnumbers}\}$
- (c) $A \times \{1\} = A$, where A is any set.

Question 2. Let F denote the set of all functions from \mathbb{N} to $\{0, 1\}$.

- (a) Describe at least three functions in the set F .
- (b) Prove that $|F| = |P(\mathbb{N})|$.

Use multiplicative rule to show $|F| = 2^{|\mathbb{N}|}$. *Note: a function with the same input and same output is an equal function. so there's $2 \times 2 \times 2 \times \dots \times n$ where n is the last natural number.

elements in $\mathbb{N} = \{1, 2, 3, \dots, n\}$
options for each element = $\{(0, 1)_1, (0, 1)_2, (0, 1)_3, \dots, (0, 1)_n\}$