

- \vec{n}_1, \vec{n}_2 sec binarias de excitaciones
- $\vec{e}_{12} = \vec{n}_1 + \vec{n}_2$
- $d = w(\vec{e}_{12}) = d_H(\vec{n}_1, \vec{n}_2)$

$$\hat{X}_{12} = \text{tr}_{N \setminus L} (|\vec{n}_1\rangle \langle \vec{n}_2|)$$

$$\text{si } d > L \Rightarrow \hat{X}_{12} = 0$$

$$\mathcal{C} = \{ \vec{x}^{(1)}, \vec{x}^{(2)}, \dots, \vec{x}^{(2^K)} \} \quad \vec{x} \in \{0, 1\}^n$$

$$R = \frac{k}{n} \Rightarrow \text{tasa del código} \quad |\mathcal{C}| = 2^{nR}$$

$$\mathcal{H}_\mathcal{C} = \text{Span} (|\vec{x}^{(1)}\rangle, |\vec{x}^{(2)}\rangle, \dots, |\vec{x}^{(2^K)}\rangle)$$

$$|\mathcal{H}_\mathcal{C}| = 2^{nR}$$

$$(n, k)$$

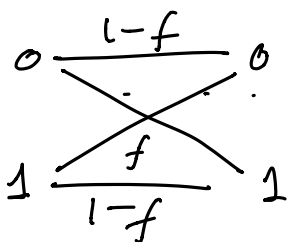
Códigos de distancia mínima d_{\min}

$$\forall \vec{x}^{(i)}, \vec{x}^{(j)} : d_H(\vec{x}^{(i)}, \vec{x}^{(j)}) \geq d_{\min}$$

$$(n, k, d)$$

$$R = k/n$$

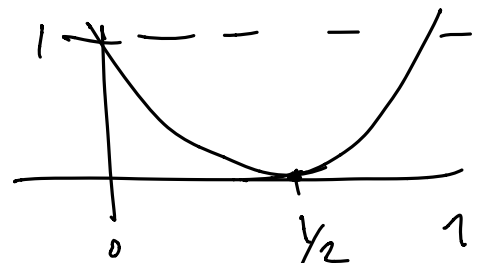
$$f = d/n$$

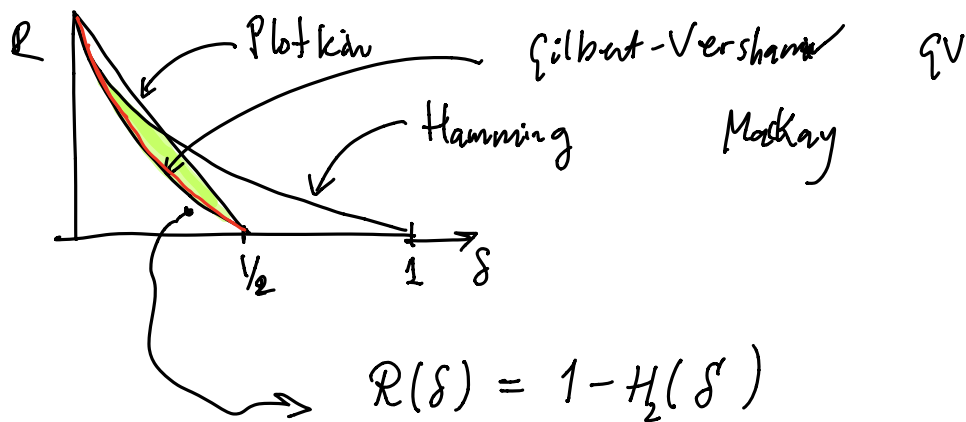


$$R = 1 - H_2(f)$$

$$\langle e \rangle = nf$$

$$\frac{\langle e \rangle}{n} = f$$





L tamaño de la subcadena $\rightarrow \ell = L/N$

Existen espacios \mathcal{H}_c con $\dim |\mathcal{H}_c| \approx 2^{N(1-H_2(\ell))}$
 $N(1-H_2(\ell))$ bits

$$|\psi\rangle = \sum_{\vec{n} \in \mathcal{C}} \psi(\vec{n}) |\vec{n}\rangle$$

$$\rho_L(\psi) = \text{tr}_{N-L}(|\psi\rangle\langle\psi|) = \sum_{\vec{n}} |\psi(\vec{n})|^2 |\vec{n}\rangle\langle\vec{n}|$$

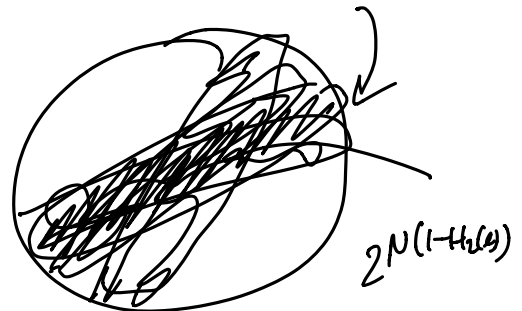
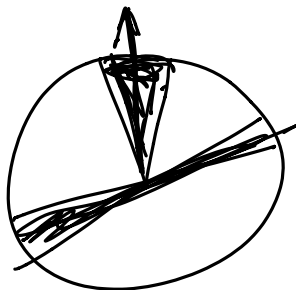
exact

(n, k, ℓ)
 $d' \leq \ell$

$$\frac{d\rho_L}{dt} = 0$$

$$\ell = 0.04$$

$$2^N ??$$



$$\epsilon = E/N$$

$$S(\epsilon)$$

$$NS(\epsilon)$$

$$2$$

$$2^{NS(\epsilon)(1-H_2(\ell))}$$

$$2^{NS(\epsilon^*) (1-H_2(L))} \sim \sum_{\epsilon} 2^{NS(\epsilon) (1-H_2(L))}$$

Preguntas Interesantes:

1) si: $S(L) = \bigcup_{\substack{\mathcal{C} \text{ código} \\ \text{de } \delta > L}} \mathcal{H}_{\mathcal{C}}$

\mathcal{C} código
de $\delta > L$

$$r = \lim_{n \rightarrow \infty} \frac{\log_2 S(L)}{n} = ?$$

2) si $\mathcal{H}_{\mathcal{C}}$ código típico de familia
en $\delta > L$, y $\epsilon = E/n$

(R, δ, ϵ)

$$R = S(\epsilon) (1-H_2(L)) ?$$

$$\vec{e} = \vec{n}_1 + \vec{n}_2$$

$$p(e_i=1) = \frac{1}{(1 + \cosh(\beta \epsilon_i))^2}$$

$$p(e_i=0) = \frac{1}{(1 + \sinh(\beta \epsilon_i))^2}$$

$$\frac{1}{(e^{\beta} + 1)^2} + \frac{1}{(e^{-\beta} + 1)^2}$$

$$\langle d \rangle = \sum_{\epsilon} \frac{1}{1 + \cosh(\beta \epsilon_i)} = N \int_{-\infty}^{\infty} \frac{1}{2\pi (1 + \cosh(\beta \epsilon(\omega)))} d\omega$$

$\epsilon(\omega) = \omega(\omega) - \omega_0$

$$\langle d^2 \rangle = N \oint \frac{d\Omega}{2\pi} \frac{1}{(\quad)} \frac{1}{(\quad)}$$

$$l < \langle d \rangle \pm \sqrt{\langle d^2 \rangle}$$

$$|\psi\rangle = \sum \psi_i |\vec{n}\rangle$$

$$\hbar \omega_{\psi} (|\psi\rangle \langle \psi|) = \omega_S + \dots$$

$$|d < L|$$

$$L=8$$

BASE:

$$\begin{matrix} x_1 & y_1 & x_3 & x_4 & x & y & x & y \\ \color{red}{1} & \color{blue}{0} & \color{red}{1} & \color{blue}{1} & \color{red}{1} & \color{red}{0} & \color{red}{1} & \color{red}{0} \end{matrix}$$

$$\gamma(101110100, 10001010)$$

$$x_1 y_2 x_3 = \frac{1}{3!} x_{[1} y_2 x_{3]}$$

$$X = \sum f(\vec{x}, \vec{v}) \gamma(\vec{x}, \vec{v})$$

$$\gamma(\vec{a}) = [\gamma_{a_1} \gamma_{a_2} \gamma_{a_3} \dots \gamma_{a_p}]$$

$$\gamma_{a_i} = O_{a_i j} \tilde{\gamma}_j$$

$$\begin{matrix} & \tilde{1} & \tilde{2} & \tilde{3} \\ \begin{matrix} \cdot 1 \\ \cdot 2 \\ 3 \end{matrix} & \begin{bmatrix} \cancel{O_{11}} & \cancel{O_{12}} & \cancel{O_{13}} \\ \cancel{O_{21}} & \cancel{O_{22}} & \cancel{O_{23}} \\ \cancel{O_{31}} & \cancel{O_{32}} & \cancel{O_{33}} \end{bmatrix} \end{matrix}$$

$$\gamma(\vec{a}) = \det(O|_{\vec{a} \vec{x}}) \gamma_{\vec{x}}$$

$$\frac{1}{2!} [\gamma_1, \gamma_2]$$

$$\frac{1}{2!} [\gamma_1, \gamma_2] = \textcircled{2} \frac{1}{2} [\tilde{\gamma}_1, \tilde{\gamma}_2] + \dots$$

$$\sum_{\vec{x}} O_{\vec{x} \vec{x}'} O_{\vec{x}''} = \det [(O \Pi O^T) |_{\vec{x} \vec{x}''}]$$

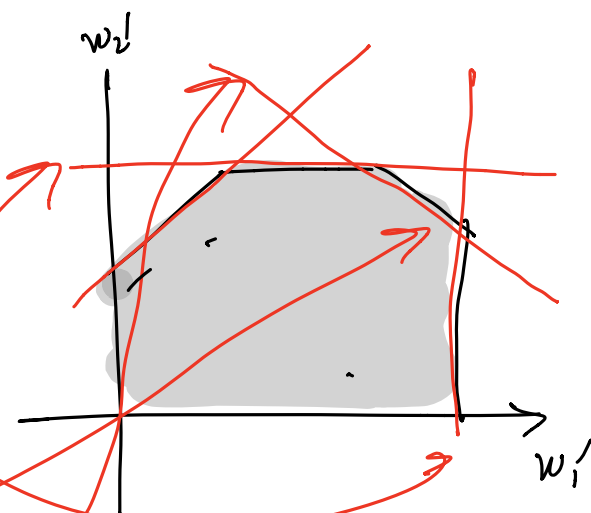
$$\begin{array}{lcl}
 & \xrightarrow{\quad d \quad} & \xrightarrow{\quad n-d \quad} \\
 & \boxed{} & \\
 \vec{x}' & \boxed{w_1' \quad w_2'} & \rightarrow w_x' = w_1' + w_2' \\
 \vec{x}' + \vec{e} = \vec{y}' & \boxed{d - w_1' \quad w_2'} & \rightarrow w_y' = d - w_1' + w_2' \\
 \vec{x}'' & \boxed{w_1'' \quad w_2''} & \rightarrow w_x'' = w_1'' + w_2'' \\
 \vec{y}'' & \boxed{d - w_1'' \quad w_2''} & \rightarrow w_y'' = d - w_1'' + w_2''
 \end{array}$$

$$\left[\begin{array}{c|c} O_x & \\ \hline & O_y \end{array} \right]$$

$$\boxed{w_1'' = w_1' \quad \text{if} \quad w_2'' = w_2'}$$

$$\left[\sum_{w_1', w_2'}^* \binom{d}{w_1'}^2 \binom{n-d}{w_2'}^2 \right]$$

$$\begin{aligned}
 0 &\leq w_1' \leq d \\
 0 &\leq w_2' \leq n-d \\
 0 &\leq w_1' + w_2' \leq l \\
 0 &\leq d - w_1' + w_2' \leq l
 \end{aligned}$$



$$\leq \left| \sqrt{\frac{2}{N}} \right|$$

$$\sum |O_{\vec{x}\vec{x}}| |\beta_{\vec{x}\vec{x}}|$$

$$W_x = \begin{bmatrix} \sqrt{\frac{2}{N}} & - & - \\ & - & - \\ & & - \\ & & & - \\ & & & & - \end{bmatrix}$$

Hadamard

$$W_x^* W_x$$

$$\left[\left(\sqrt{\frac{2}{N}} \right) \sqrt{W_x} \right] W_x$$

$$\|X_{12}\|_2^2 = \frac{1}{2^L} \sum_{w_1', w_2'}^* \binom{d}{w_1'}^2 \binom{n-d}{w_2'}^2 \left[\frac{2}{N} (w_1' + w_2') \right]^{\binom{w_1' + w_2'}{2}} \left[\frac{2}{N} (d - w_1' + w_2') \right]^{\binom{d - w_1' + w_2'}{2}}$$

$$\leq Q^n f(\delta, l)$$

$$f(\delta, l) = \max_{\mathcal{R}} \dots$$

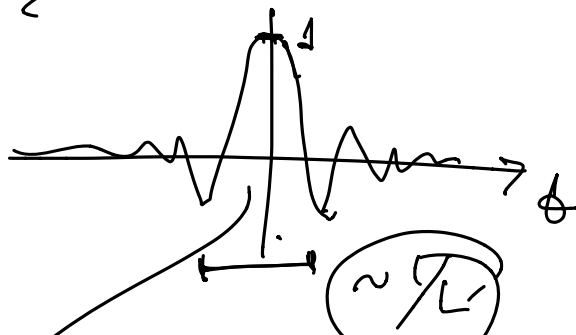
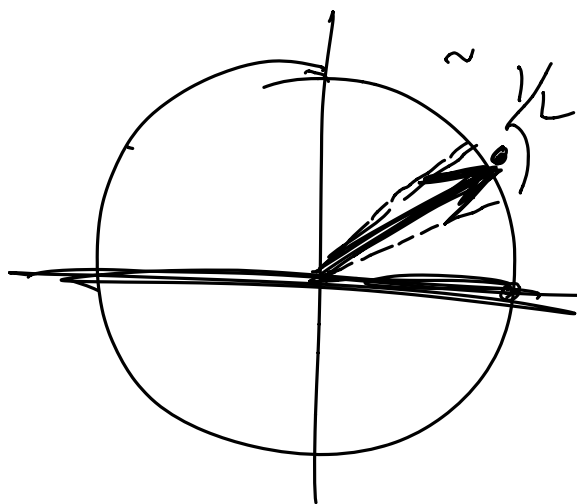
$$\begin{aligned} &= 2\delta H_2\left(\frac{\bar{w}_1'}{\delta}\right) + 2(1-\delta) H_2\left(\frac{\bar{w}_2'}{\delta}\right) + (\bar{w}_1' + \bar{w}_2') \log(2(\bar{w}_1' + \bar{w}_2')) \\ &\quad + (\delta - \bar{w}_1' + \bar{w}_2') \log(2(\delta - \bar{w}_1' + \bar{w}_2')) \\ &\quad - l \log 2 \end{aligned}$$

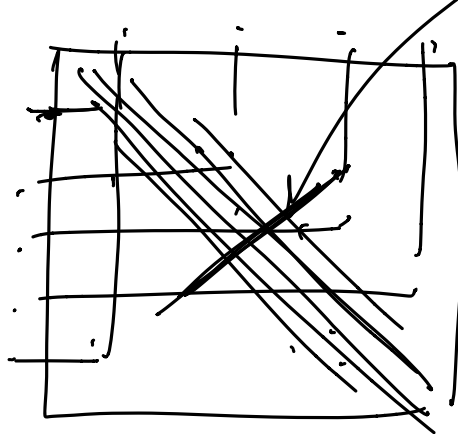
$$u^{(k)}(x) = \sqrt{\frac{2}{N}} \cos(\Theta_k x)$$

$$a_{jk} = \sum_{x=\frac{L-1}{2}}^{L-1/2} u^{(j)}(x) u^{(k)}(x)$$

$$= \frac{L}{N} \left[f_L(\theta_k - \theta_l) + f_L(\theta_k + \theta_l) \right]$$

$$f_L(\theta) = \frac{\sin(\theta L/2)}{L \sin(\theta/2)}$$





$$[0 \pi \ 0^T]$$

