National University of Sciences & Technology School of Electrical Engineering and Computer Science Department of Basic sciences

MATH-112 Calculus-II (3+0): BSCS-6ABC Spring 2017

| Assignment 1: First order differential equations | |
|--------------------------------------------------|------------------------------|
| CLO1 | |
| Maximum Marks: 70 | Instructor: Dr. Hina M. Dutt |
| Announcement Date: 2 March 2017 | Due Date : 9 March 2017 |

Instructions:

- This is a group assignment. Each group must have 5 members.
- Write names and registration numbers of all group members on the cover page.
- Examples must be different from each other or marks will be deducted.
- Assignment must be hand written.
- Assignments must be properly bound or marks will be deducted.
- Copied assignments will be marked zero.
- CR of the class will collect all the assignments and submit to the instructor.
- Assignments are not acceptable after the deadline.

Question 1

Write three first order ordinary differential equations in each of the following case:

- i. Non-linear and non-homogeneous
- ii. Non-homogeneous and separable
- iii. Separable and exact

Question 2

Discuss homogeneity and exactness of the equation

$$y - x\frac{dy}{dx} = x + y\frac{dy}{dx}$$

and solve it by two methods.

Question 3

Determine M(x, y) so that the equation

$$M(x,y)dx + \left(xe^{xy} + 2xy + \frac{1}{x}\right)dy = 0$$

is exact.

Question 4

Solve

$$3(1+t^2)\frac{dy}{dt} = 2ty(y^3 - 1).$$

Question 5

For a series circuit containing only a resistor and an inductor, Kirchhoff's second law states the sum of the voltage drop across the inductor $(L^{dI}/_{dt})$ and the voltage drop across the resistor

(IR) is the same as the impressed voltage V(t) on the circuit, i.e. we have the following differential equation for the current I(t)

$$L\frac{dI}{dt} + RI = V(t),$$

where L and R are constants known as the inductance and the resistance, respectively. Determine I(t) if R = 6 Omega, L = 3H, V(t) = 3sint V and I(0) = 15(A).

Question 6

Suppose a small cannonball weighing 16 pounds is shot vertically upward with an initial velocity $v_0=300\frac{ft}{s}$.

- a) Suppose air resistance is ignored, determine the velocity of the cannonball at any time t.
- b) Using the result obtained in part (a), determine the height s(t) of the cannonball measured from the ground level. Determine the maximum height attained by the cannonball.
- c) Assume that air resistance is proportional to instantaneous velocity v(t). Show that in this case the maximum height attained by the cannonball is less than that in part (b), by supposing that the constant of proportionality is k=0.0025.

(The End)