

# TDDD08 – Tutorial 3

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1. Determine which of the following pairs of terms that are unifiable, and provide the most general unifier (mgu) in case there is one:

1.  $p(f(X), X, f(Y))$  and  $p(Y, f(Z), Z)$
2.  $p(f(X), f(Y), X)$  and  $p(Z, Z, W)$
3.  $p(X1, X2, X3)$  and  $p(f(X2, X2), f(X3, X3), a)$
4.  $[X, f(X) | X]$  and  $[Z, Y, Z]$

2. Draw the SLD-tree for the program below and the query `member(X, [a, b])`.

```
member(X, [X|_]).  
member(X, [_|L]) :- member(X, L).
```

3. Define the following relations on lists by means of Prolog programs. The predicates `member/2`, `append/3` and `dif/2`, may be used, if required. (`dif(X, Y)` is a “right” implementation of inequality in Prolog.)

- `longer(Xs, Ys)` — the list `Xs` has more elements than the list `Ys`. Do this without computing the length of a list. (It is simpler.)
- `append(A, B, C, ABC)` — the list `ABC` is the result of appending `A`, `B` and `C`.
- `notmember(X, Xs)` — `Xs` does not contain `X` as an element.
- Relations named `replace1`, `replace`, `replaceall`, describing replacing element  $E$  by  $EE$  in a list: replacing exactly one occurrence of  $E$ , any number of occurrences, and all occurrences.

4. Consider the following definite program P:

```

p(X) :- r(X), p(X).
q(f(X), X).
r(a).
r(Y) :- q(Y, X), r(X).

```

What are the constants, function symbols and predicate symbols of the program? What is the Herbrand universe  $\mathbf{U}_P$ , and the Herbrand base? Which of the following Herbrand interpretations are models of P?

- $I_1 = \{q(f(x), x) \mid x \in U_P\}$
- $I_2 = I_1 \cup \{r(f^{2n}(a)) \mid n \geq 0\}$
- $I_3 = I_1 \cup \{r(f^n(a)) \mid n \geq 0\}$
- $I_4 = I_1 \cup \{p(a)\} \cup \{r(f^n(a)) \mid n \geq 0\}$

Is any of them the least Herbrand model  $\mathbf{M}_P$  of  $P$ ?

5. Consider the immediate consequence operator  $T_P$ . Prove that  $I$  is a Herbrand model of  $P$  if and only if  $T_P(I) \subseteq I$ .

6. Formulate the completeness theorem of SLD-resolution and give an example of a definite program  $P$  and a definite query  $A$  such that  $P \models A\theta$ , but there is no computed answer substitution  $\sigma$  such that  $A\sigma = A\theta$ .