1 0 0
$$\psi_{100} = \frac{1}{\sqrt{\pi}} \left(\frac{Z}{a_0}\right)^{3/2} e^{-Zr/a_0}$$

2 0 0 $\psi_{200} = \frac{1}{4\sqrt{2\pi}} \left(\frac{Z}{a_0}\right)^{3/2} \left(2 - \frac{Zr}{a_0}\right) e^{-Zr/2a_0}$
2 1 0 $\psi_{210} = \frac{1}{4\sqrt{2\pi}} \left(\frac{Z}{a_0}\right)^{3/2} \frac{Zr}{a_0} e^{-Zr/2a_0} \cos \vartheta$
2 1 ±1 $\psi_{21\pm 1} = \frac{1}{8\sqrt{\pi}} \left(\frac{Z}{a_0}\right)^{3/2} \frac{Zr}{a_0} e^{-Zr/2a_0} \sin \vartheta e^{\pm i\varphi}$

Eigenfunktionen $\psi_{n m}(\mathbf{r}, \vartheta, \varphi)$

Ouantenzahlen Q

2

±2

m

3 0
$$\psi_{300} = \frac{1}{81\sqrt{3\pi}} \left(\frac{Z}{a_0}\right)^{3/2} \left(27 - 18\frac{Zr}{a_0} + 2\frac{Z^2r^2}{a_0^2}\right) e^{-Zr/3a_0}$$

3 1 0 $\psi_{310} = \frac{\sqrt{2}}{81\sqrt{\pi}} \left(\frac{Z}{a_0}\right)^{3/2} \left(6 - \frac{Zr}{a_0}\right) \frac{Zr}{a_0} e^{-Zr/3a_0} \cos \vartheta$

3 1 0
$$\psi_{310} = \frac{\sqrt{2}}{81\sqrt{\pi}} \left(\frac{Z}{a_0}\right)^{3/2} \left(6 - \frac{Zr}{a_0}\right) \frac{Zr}{a_0} e^{-Zr/3a_0} \cos \vartheta$$
3 1 ± 1 $\psi_{31\pm 1} = \frac{1}{81\sqrt{\pi}} \left(\frac{Z}{a_0}\right)^{3/2} \left(6 - \frac{Zr}{a_0}\right) \frac{Zr}{a_0} e^{-Zr/3a_0} \sin \vartheta e^{\pm i\varphi}$

$$81 \sqrt{\pi} \quad (a_0) \quad (a_0) \quad a_0$$

$$1 \quad \pm 1 \quad \psi_{31\pm 1} = \frac{1}{81 \sqrt{\pi}} \left(\frac{Z}{a_0}\right)^{3/2} \left(6 - \frac{Zr}{a_0}\right) \frac{Zr}{a_0} e^{-Zr/3a_0} \sin \vartheta e^{\pm i\varphi}$$

$$2 \quad 0 \quad \psi_{330} = \frac{1}{2\pi} \left(\frac{Z}{a_0}\right)^{3/2} \frac{Z^2 r^2}{a_0^2 + 2\pi^2} e^{-Zr/3a_0} (3\cos^2 \vartheta - 1)$$

$$\psi_{31\pm 1} = \frac{1}{81\sqrt{\pi}} \left(\frac{Z}{a_0}\right)^{3/2} \left(6 - \frac{Zr}{a_0}\right) \frac{Zr}{a_0} e^{-Zr/3a_0} \sin \vartheta e^{\pm i\varphi}$$

$$2 \qquad 0 \qquad \psi_{320} = \frac{1}{81\sqrt{6\pi}} \left(\frac{Z}{a_0}\right)^{3/2} \frac{Z^2 r^2}{a_0^2} e^{-Zr/3a_0} (3\cos^2 \vartheta - 1)$$

$$\psi_{320} = \frac{1}{81\sqrt{6\pi}} \left(\frac{Z}{a_0}\right)^{3/2} \frac{Z^2 r^2}{a_0^2} e^{-Zr/3a_0} (3\cos^2\vartheta - 1)$$

$$2 \qquad \pm 1 \qquad \psi_{32+1} = \frac{1}{2\pi} \left(\frac{Z}{a_0}\right)^{3/2} \frac{Z^2 r^2}{a_0^2} e^{-Zr/3a_0} \sin\vartheta \cos\vartheta e^{\pm i\varphi}$$

$$81\sqrt{6}\pi \quad (a_0) \qquad a_0^2$$

$$2 \qquad \pm 1 \qquad \psi_{32\pm 1} = \frac{1}{81\sqrt{\pi}} \left(\frac{Z}{a_0}\right)^{3/2} \frac{Z^2 r^2}{a_0^2} e^{-Zr/3a_0} \sin \vartheta \cos \vartheta e^{\pm i\varphi}$$

$$2 \qquad \pm 2 \qquad \psi_{32\pm 2} = \frac{1}{162\sqrt{\pi}} \left(\frac{Z}{a_0}\right)^{3/2} \frac{Z^2 r^2}{a_0^2} e^{-Zr/3a_0} \sin^2 \vartheta e^{\pm 2i\varphi}$$