

Deep Multi-Label Learning

by

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Abstract

Deep Multi-Label Learning

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Thesis: MCom (Mathematical Statistics)

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English abstract

Uittreksel

Diep Multi-Etiket Leer

(“*Deep Multi-Label Learning*”)

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Afrikaans abstract

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Nomenclature

Constants

$$g = 9.81 \text{ m/s}^2$$

Variables

Re_D	Reynolds number (diameter)	[]
x	Coordinate	[m]
\ddot{x}	Acceleration	[m/s ²]
θ	Rotation angle	[rad]
τ	Moment	[N·m]

Vectors and Tensors

\vec{v} Physical vector, see equation ...

Subscripts

a Adiabatic
 a Coordinate

Chapter 1

Introduction

1.1 Motivation

The motivation for this thesis is two-fold:

1. Image classification is a highly relevant topic in Computer Vision, Machine Learning and Statistical Learning. It is a thoroughly researched domain and already by many regarded as a ‘solved’ problem. This progress is mainly attributed to the yearly large-scale image classification competition, *ImageNet*¹, and the development of *Convolutional Neural Networks* (CNNs). The last five winners of ImageNet all used a variant of CNNs in their solution. However, the main focus up until recently was on problems of single label classification. Therefore, the field of multi-label image classification is nowhere near the maturity level of its single-label counterpart. Multi-label classification has a wide range of applications, not only in image classification. It has been applied to problems in text categorisation, multimedia, biology, chemical data analysis, social network mining and e-learning among others. This is most likely the reason why it has seen such a rapid increase of academic publications (see Figure 1.1). However, researchers have not yet reached consensus on how to deal with many of the aspects when learning from multi-labelled data, *e.g.* dependency between labels. There are a very limited number of publications specifically dealing with multi-label classification of images, even more so while using CNNs for this task. The field can gain from an up-to-date review of the literature, more statistical perspectives on some of the challenges, additional benchmark datasets and quality empirical evaluations of the theory.
2. Deforestation is a massive global problem. It contributes to reduced biodiversity, habitat loss, climate change and other devastating effects.

¹<http://www.image-net.org/>

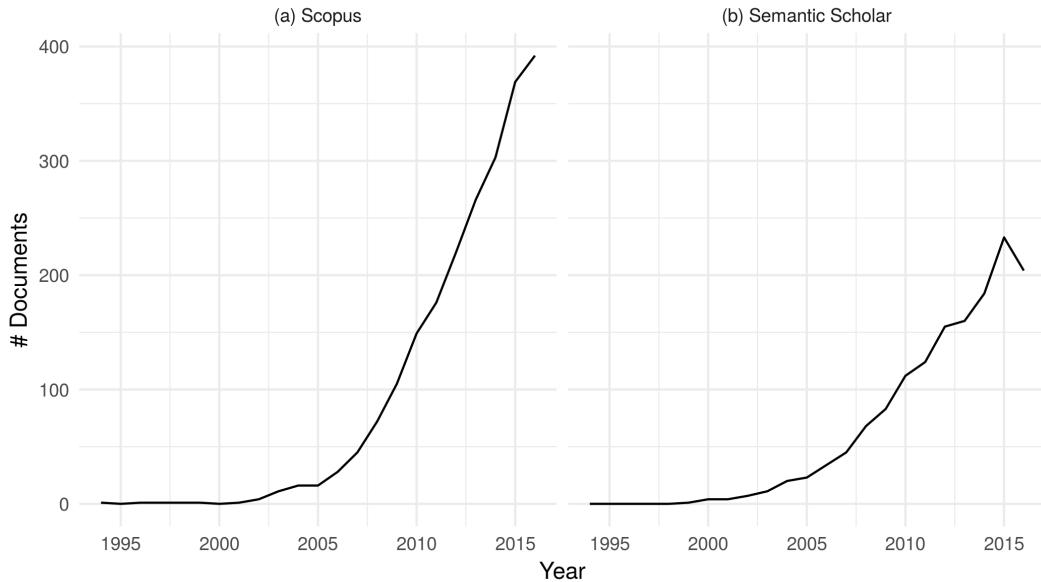


Figure 1.1: Line graphs illustrating the rise in multi-label learning publications per year for two databases. The database searches were done on 24-03-2017. The searches were not identical since they were limited to the search features of the databases. (a) The search on Scopus (cite) was for all documents (conference papers, articles, conference, articles in press, reviews, book chapters and books) in any subject area with either the words *multi-label* or *multilabel* and either the words *learning* or *classification* found in either their titles, abstracts or keywords. (b) The search on Semantic Scholar was based on machine learning principles and thus automatically decides which research documents are relevant to a specific search query. The query used was *multilabel multi-label learning classification*. The search only returns research in the computer science and neuroscience fields of study. More technical details can be found on the respective engine's websites.

It is said that the world loses an area of forest the size of 48 football fields per minute and the area most affected is in the Amazon basin (cite Kaggle). This problem can be fought more effectively by governments and local stakeholders if better data about the location of deforestation and human invasion on forests are continuously available to them - an ideal task for machine learning! Planet² and SCON³ constructed a dataset of labelled satellite images taken of the Amazon basin and released it as part of a competition on Kaggle⁴, challenging competitors to build algorithms that can automatically label these images with atmospheric

²Designer and builder of the world's largest constellation of Earth-imaging satellites - www.planet.com

³Remote sensing experts - www.sccon.com.br/eng

⁴Runs programming contests to crowd source machine learning solutions - www.kaggle.com

conditions and various classes of land use/cover⁵. Resulting algorithms will help the global community better understand where, how, and why deforestation happens all over the world - and ultimately how to respond.

1.2 Thesis Objectives

This thesis works towards building a multi-label classifier that can label satellite images of the Amazon as accurately as possible. The method thought best to achieve this goal is to:

1. Identify the most important and latest developments in the literature for: multi-label classification, image classification and *remote sensing* (analysis of satellite images).
2. Provide an extensive review and discussion of these methods and how they compare to each other.
3. Empirically evaluate and compare them on the satellite image data in order to find the best strategies for our labeling task.

Since practically every state-of-the-art solution to an image classification problem is a CNN, it is reasonable to restrict the space of possible classifiers to CNNs. This thesis should provide the reader with a clear understanding of CNNs and how to effectively apply them to a multi-label classification problem, and especially in the domain of remote sensing. The main contribution of this thesis is a review of multi-label CNNs.

update this section as progress is made with thesis.

1.3 Data

This section covers an initial introduction to the data available for the problem at hand. The elements of the data important to know before moving on will be discussed here and the rest will be addressed throughout the thesis, as it becomes relevant to the discussion. This is done here to get a better understanding of the problem before exploring the literature.

1.3.1 Image Format

The data for this task comes from a set of images (also referred to as chips). Each chip is a small excerpt from a larger image of a specific scene in the Amazon taken by satellites. The chip size in pixels is 256×256 , representing roughly 90 hectares of land, and is taken from a larger scene of 6600×2200

⁵Land cover indicates the physical land type such as forest or open water whereas land use documents how people are using the land.

pixels. All of the satellite images were taken between January 1, 2016 and February 1, 2017. The format of these images differ from the standard image format. Each image contains four spectral bands: red (R), green (G), blue (B) and near infrared (NIR), where the standard format images usually only contain R, G and B. The additional NIR colour channel is common in remote sensing⁶ applications and supposedly allows for clear distinction between water and vegetation in satellite images, for example.

Another difference between these images and the usual format is that these have pixel intensities in 16-bit digital number format as opposed to the usual 8-bit of standard RGB images. This allows the colours in the images to have a much higher range since 16-bit pixel intensities have 65536 (2^{16}) levels, compared to 256 levels of 8-bit images. This becomes useful, for example, to distinguish between very dark or very bright areas in an image. If the pixel values of a chip gets flattened out into a vector, it will be of size 262144 ($256 \times 256 \times 4$). However, CNNs take the images in their array form as input.

1.3.2 Collection and Labelling of the Images

The image collection was created by first specifying a “wish list” of scenes containing the phenomena the creators wanted to be included, in addition to a rough estimate of the number of such scenes that are necessary for a sufficient representation in the final collection. This set of scenes was then searched for manually on Planet Explorer⁷. From these scenes the 4-band chips were created. A schematic of this process can be seen in Figure 1.2. The chips were labelled manually by crowd sourcing. The utmost care was taken to get a large and well-labelled dataset, but that does not mean the labels all correspond to the ground-truth, *i.e.* the data will contain some inherent error. The creators believe that the data has a reasonable high signal to noise ratio.

Note, the training and test splits were determined by the Kaggle competition creators. The training chips are labeled but at the time of writing this, the test chips are not yet made available to competitors. Predicted labels for the test chips can be submitted to Kaggle to evaluate in terms of the F_2 -score, a metric which will be discussed in Chapter ???. This setup prevents competitors from using the test chips for training a classifier. There are 40479 training chips and 61191 test chips.

1.3.3 Class Labels

The class labels for the images can be divided into three groups: atmospheric conditions, common land cover/use phenomena and rare land cover/use phenomena.

⁶The use of satellite- or aircraft-based sensor technologies to detect and classify objects on Earth [https://en.wikipedia.org/wiki/Remote_sensing].

⁷A web based interactive map of Earth consisting of satellite images, similar to Google Earth - www.planet.com/explorer

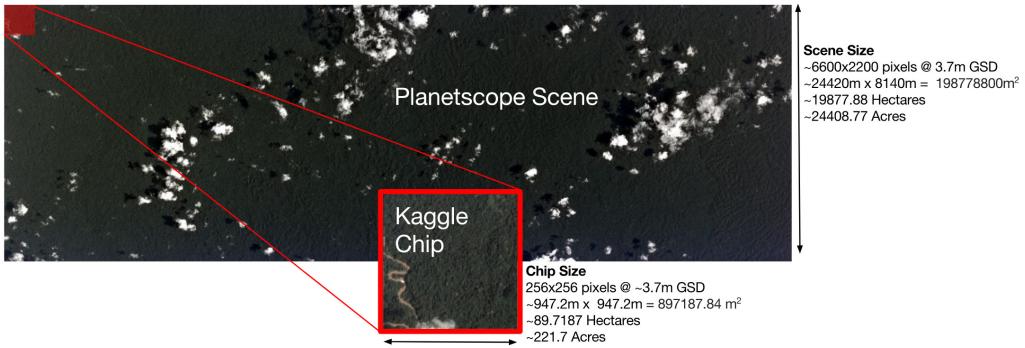


Figure 1.2: Schematic of the image collection process.

ena. In total there are 17 possible labels. Each chip will have one atmospheric label and zero or more common and rare labels. Chips that are labeled as cloudy should have no other labels.

The atmospheric condition labels are: *clear*, *haze*, *partly cloudy* and *cloudy*. They are relevant to a chip when:

- **clear:** there are no evidence of clouds.
- **haze:** clouds are visible but they are not so opaque as to obscure the ground.
- **partly cloudy:** scenes show opaque cloud cover over any portion of the image but the land cover/use phenomena are still visible.
- **cloudy:** 90% of the image is obscured with opaque cloud cover.

Examples of chips with atmospheric labels can be found in Figure 1.3. Each chip should only have one atmospheric label and therefore this classifying task simplifies to a multiclass problem. This allows for the option to break up the labeling task of all the labels into two tasks: a multiclass classification problem for the atmospheric labels and a multi-label classification problem for the land cover/use labels. This approach might save some computational time and give extra information to the multi-label learners for classifying the land cover/use labels. We will experiment with these approaches in Chapter ??.

The common land cover/use labels are: *primary*, *agriculture*, *water*, *habitation*, *road*, *cultivation* and *bare ground*. They are relevant to a chip when:

- **primary:** it is primarily consisting of rain forest (virgin forest), *i.e.* dense tree cover.
- **agriculture:** it contains any land cleared of trees that is being used for agriculture or range land.
- **water:** it contains any one of the following: rivers, reservoirs, or oxbow lakes.
- **habitation:** it contains human homes or buildings.

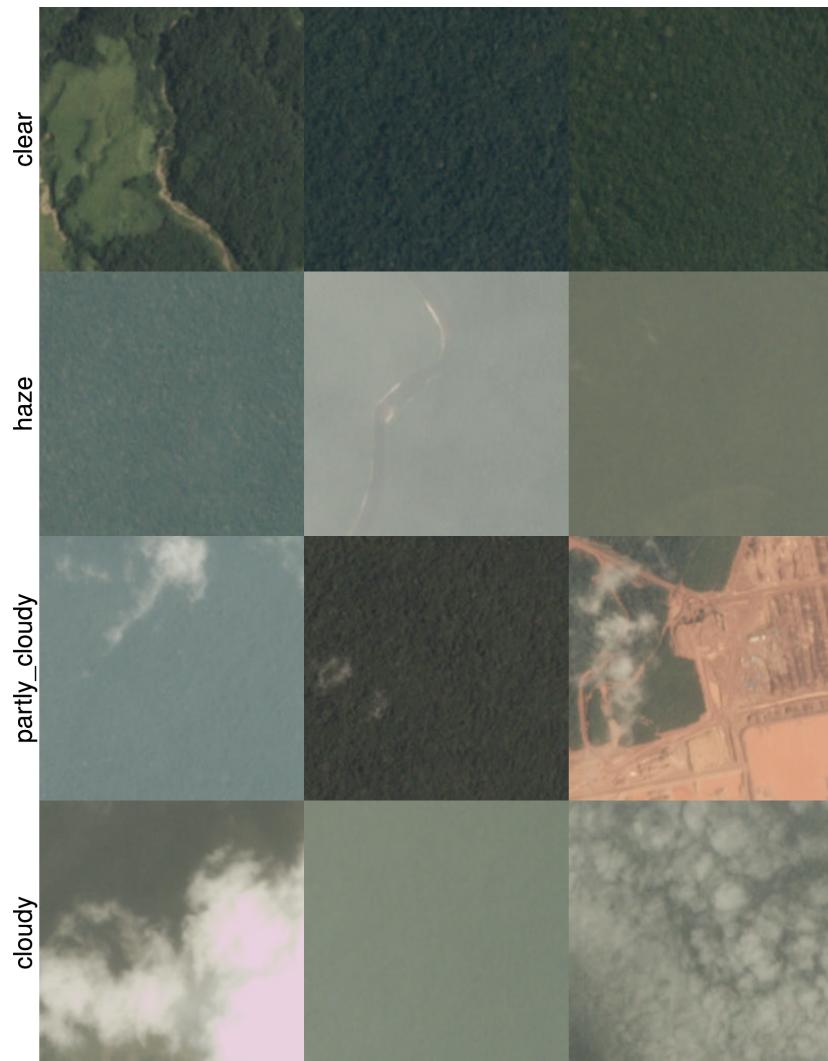


Figure 1.3: Examples of chips with atmospheric labels. These (along with all the other chips plotted throughout the thesis) are the JPEG conversions of the original 4-band, 16-bit images.

- **road:** it contains any type of road.
- **cultivation:** it shows signs of smaller-scale/informally cleared land for farming.
- **bare ground:** it contains naturally (not caused by humans) occurring tree-free areas.

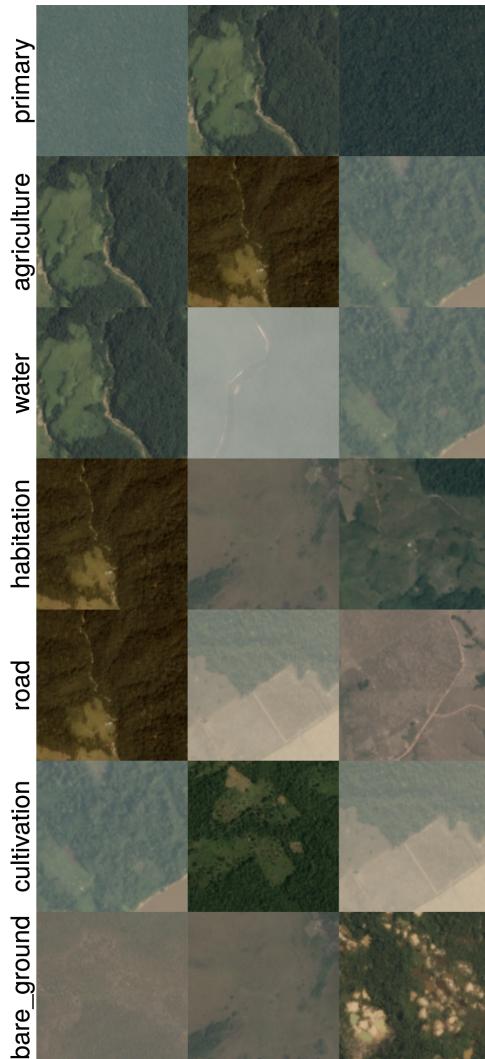


Figure 1.4: Examples of chips with common land cover/use labels.

Examples of chips with common land cover/use labels are found in Figure 1.4. According to the competition page on Kaggle, small, single-dwelling habitations are often difficult to spot but usually appear as clumps of a few pixels that are bright white. Roads sometimes look very similar to rivers and therefore these two labels might be noisy. The NIR band might give a classifier additional information to help distinguish between the two. Cultivation is a subset of

agriculture and is normally found near smaller villages, along major rivers or at the outskirts of agricultural areas. It typically covers very small areas.

The less common land cover/use labels are: *slash and burn*, *selective logging*, *blooming*, *conventional mine*, *artisinal mine* and *blow down*. Chips are tagged with these labels when:

- **slash and burn**: there are signs of the farming method that involves the cutting and burning of the forest to create a field. These look like cultivation patches with black or dark brown areas.
- **selective logging**: winding dirt roads are present adjacent to bare brown patches in otherwise primary rain forest. Selective logging is the practice of selectively removing high values tree species from the rainforest.
- **blooming**: there are signs of trees flowering. Blooming is a natural phenomena where particular species of flowering trees bloom, fruit and flower at the same time. These trees are quite big and the phenomena can be seen in the chips. They usually appear as white dots.
- **conventional mine**: it contains signs of large-scale legal mining operations.
- **artisinal mine**: it contains signs of small-scale (sometimes illegal) mining operations.
- **blow down**: there are signs of trees uprooted or broken by wind. High speed winds ($\sim 160\text{km/h}$) in the Amazon are generated when the cold dry air from the Andes settles on top of the warm moist air in the rainforest and then sinks down with incredible force, toppling larger rainforest trees. These open areas are visible from space.

Examples of chips with these less common land cover/use labels are given in Figure 1.5. These labels are more challenging to identify in the chips and since they also appear less frequently, it might be difficult for the classifier to learn these labels. The imbalance in the class distribution is apparent in Figure 1.6.

1.4 Code and Reproducibility

All of the code for this project, including the source documents, is made available at <https://github.com/jandremarais/Thesis>. The data is hosted on Kaggle at <https://www.kaggle.com/c/planet-understanding-the-amazon-from-space/data>. More instructions on how to implement the code is contained in the file named, `README.md`, in the GitHub repository.

1.5 Important Concepts and Terminology

Not surprisingly, a convolutional neural network is a type of neural network. Neural networks will be discussed in chapter 2, but there are some preliminary

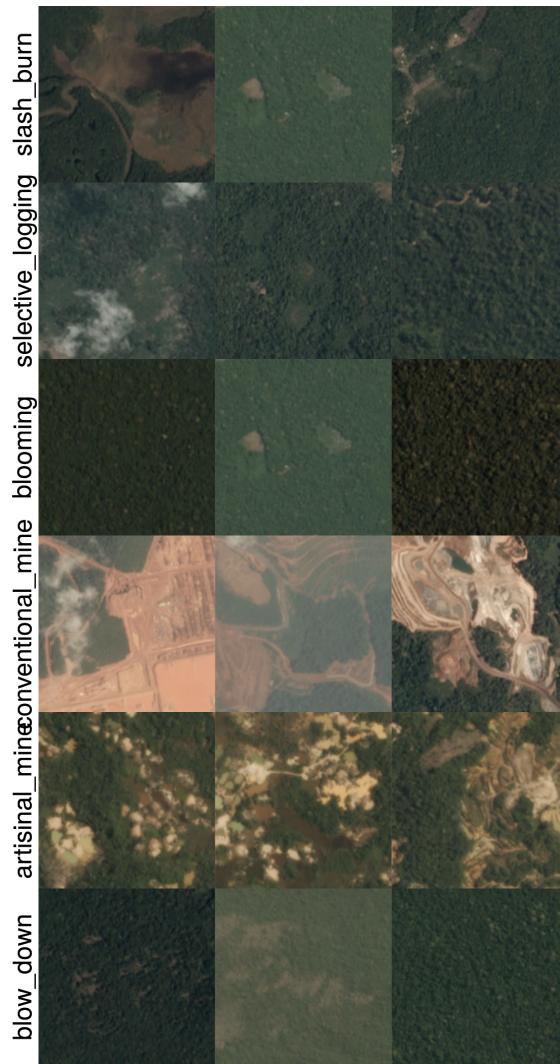


Figure 1.5: Examples of chips with less common land cover/use labels.

concepts to introduce here to ensure a better understanding of neural networks and ultimately CNNs. First, a brief introduction to the general problem of image classification is given.

1.5.1 Image Classification

There are three main tasks in computer vision (CV), namely: image classification, object detection and image segmentation. Traditional image classification is the task of assigning one label from a fixed set of categories to an input image. More recently the task has been generalised to assigning multiple labels to an input image, *i.e.* multi-label classification (MLC). First, we will only look at the single label case.

Image classification is the core of computer vision tasks and probably the

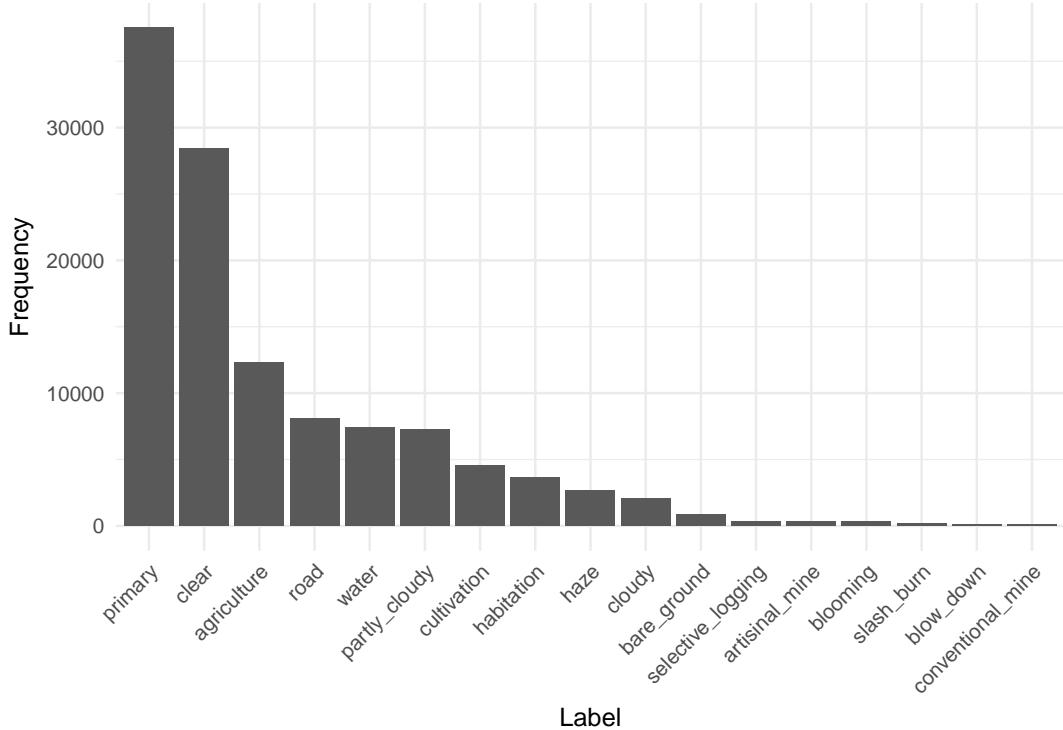


Figure 1.6: Class distribution of the labels in the training set.

most explored since it has a large variety of practical applications. It can be shown that the other two CV tasks, detection and segmentation, can be reduced to classification. Classification will be the main theme of this thesis but we will have a look at segmentation and detection later on.

show visual difference between classification, segmentation and detection.

Instead of hard coding rules on how to classify images into an image classification model, it can learn to classify images by seeing many examples of images and its corresponding labels. In this way it learns the visual appearance of each class. This is sometimes referred to as a data-driven approach. A very intuitive approach to image classification (and supervised learning in general) is called the nearest neighbour approach.

Although this approach is rarely used in practice, this description helps with the understanding of the image classification problem. The nearest neighbour classifier will take a test image, compare it to every single one of the training images, and predict its label to be the label of the closest training image. This leaves the question of how to measure the similarity between images.

An image is a grid of many small, square cells of different colors. These cells are known as pixels and one pixel represents one color. A grayscale image, 32 pixels wide and 32 pixels long, can be represented by a 32×32 matrix of

integers, where each integer represents the ‘brightness’ (intensity) of each pixel. These integers are usually in $[0, 255]$, such that the greater the integer the brighter the pixel, *i.e.* a pixel with intensity 0 is totally black and a pixel with intensity 255 is totally white. Note that a color image consists of 3 spectral bands, red, green and blue (RGB), *i.e.* the color of one pixel is determined by 3 integers each representing the intensity of the color red, green and blue, respectively.

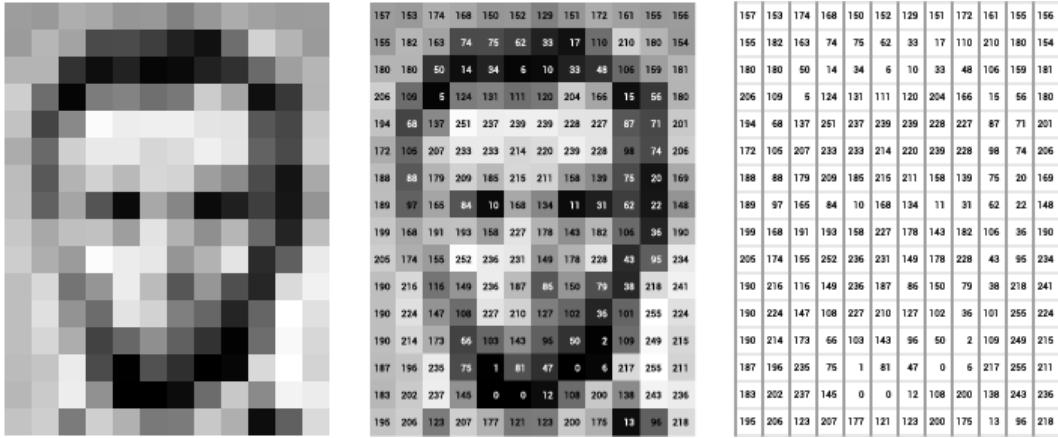


Figure 1.7: Greyscale intensities. <http://ai.stanford.edu/~syyeung/cvweb/tutorial1.html>

The (dis)similarity between two images can now be measured pixel by pixel. It is possible to represent the grayscale image mentioned above in a vector of length 32×32 . Suppose a grayscale Image 1 is flattened out to be represented by the vector $\mathbf{I}_1 = \{I_{11}, I_{12}, \dots, I_{1p}\}$ and similarly, Image 2 by \mathbf{I}_2 , where $p = 32 \times 32$. Then the dissimilarity between Image 1 and Image 2 can be calculated by the L_1 -distance:

$$d_1(\mathbf{I}_1, \mathbf{I}_2) = \sum_{j=1}^p |I_{1j} - I_{2j}|.$$

test image				training image				pixel-wise absolute value differences			
56	32	10	18	10	20	24	17	46	12	14	1
90	23	128	133	8	10	89	100	82	13	39	33
24	26	178	200	12	16	178	170	12	10	0	30
2	0	255	220	4	32	233	112	2	32	22	108

-

=

→ 456

Figure 1.8: Pixelwise difference

Now, suppose we want to predict the label of an test image a , then the nearest neighbour approach would assign the label of train image b^* to test image a if:

$$b^* = \arg \min_b d_1(\mathbf{I}_a, \mathbf{I}_b),$$

for $b = 1, 2, /dots, N$, where N is the number of training images. Of course there are other ways of measuring the dissimilarity between images. Another example would be to use the L_2 -distance:

$$d_2(\mathbf{I}_1, \mathbf{I}_2) = \sqrt{\sum_{j=1}^p (I_{1j} - I_{2j})^2}.$$

The chosen metric depends on the use case.

The nearest neighbour approach can be generalised to use more than 1 nearest neighbour when predicting the label of a test image. This approach is called the k -Nearest Neighbours (k -NN). The only difference is that, you now search for the k (instead of just 1) images with the smallest dissimilarity with the test image and then combine the labels of these k images, either through averaging or majority voting, to predict the label of the test image. Choosing the right value of k is important and is usually done by cross-validation. See Hastie ref.

The advantage of using k -NN is that it is simple and requires no time to train. Unfortunately, when it comes to test time, the algorithm needs to calculate the distance between the test image and all the other images in the training set, which is computationally very expensive. Also in [Haste ref], they show that k -NN suffers severely from the *curse of dimensionality* and that it is mostly only useful to classify lower dimensional objects. Images are very high-dimensional objects.

The dissimilarity measures discussed above are actually proven to be very poor in discriminating between images in an image classification problem. Images that are nearby in terms of the L_1 and L_2 distances are much more of a function of the general color distribution of the images, or the type of background rather than their semantic identity. Refer to the t -SNE figure.

1.5.2 Score Function

The following simple approach to image classification naturally extends to neural networks and convolutional neural networks and is therefore very important to comprehend. This approach has two major components: a score function and a loss function. The score function maps raw data (*e.g.* an image) to a set of class scores, and a loss function quantifies the agreement between the predicted class scores and the actual ground truth labels associated with the raw data. This approach can then be described as an optimization problem in which the

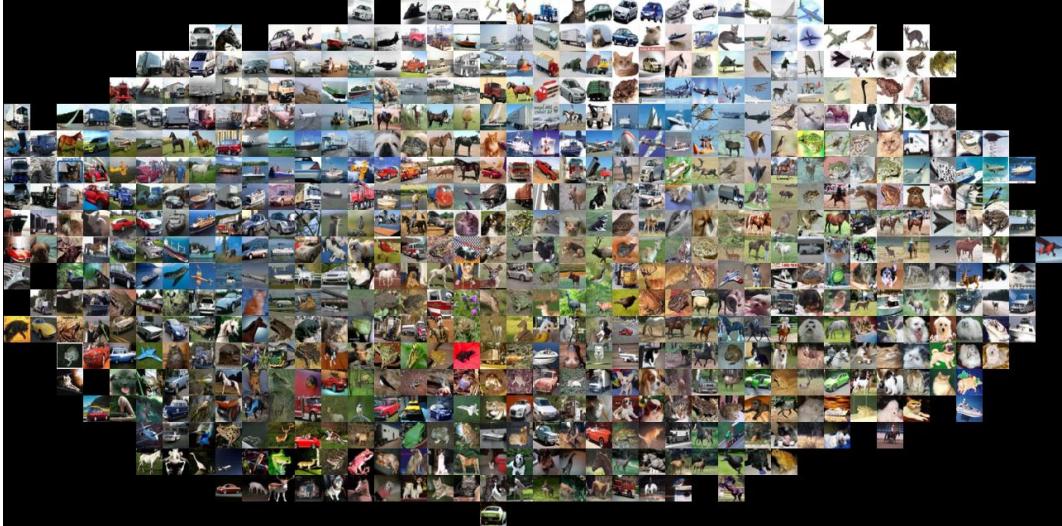


Figure 1.9: Caption

minimisation of the loss function with respect to the parameters of the score function is the main goal.

Some notation is needed to formally define this approach. Suppose we have N training images $\mathbf{x}_i \in \mathbb{R}^p$ each associated with a label $y_i \in \{1, 2, \dots, K\}$, where $i = 1, 2, \dots, N$ and K is the number of possible categories an image can belong to and p the number of pixels of each image. The score function is then defined as the function f that maps the raw image pixels to class scores:

$$f : \mathbb{R}^p \rightarrow \mathbb{R}^K.$$

The simplest possible score function is a linear mapping:

$$f(\mathbf{x}_i, W, b) = W\mathbf{x}_i + \mathbf{b}.$$

In the above equation, Image i is flattened out to be represented by a p -dimensional vector. The parameters of f are the matrix $W : K \times p$ and the vector \mathbf{b} , often called the weights and biases, respectively. These terms are comparable to the coefficient and constant terms in a statistical linear model and thus should not be confused with bias in the statistical sense.

We assume the pairs (\mathbf{x}_i, y_i) to be fixed, but we do have control over the W and \mathbf{b} terms. Our goal will be to set these in such a way so that the computed class scores for each image in the training set match the associated ground truth label as close as possible. What we have described thus far is very similar to the approach taken by convolutional neural networks, but instead the function, f , which maps the raw pixels to class scores, is much more complicated with plenty more parameters to tune.

Notice that this score function determines the score for each class as a weighted sum of the pixel values across all 3 of its spectral bands. We would

imagine that a linear classifier trained to classify, say, ships would have a weight matrix that assigns heavier weights to blue pixels on the sides of an image, which loosely corresponds to water.

If we picture the images as points in a high-dimensional space, f is a hyperplane, W determines the angle of the hyperplane and \mathbf{b} translates the hyperplane through the space. Another interpretation of this linear classifier is that each row of the weight matrix is a so-called template for the corresponding class. The linear classifier matches the input image with each of the class templates in W by calculating a dot product. A high class score would translate to a higher similarity between the input image and the class template. This interpretation is closely related to the nearest neighbour approach, but here only the test image's distance (here the negative of the inner product) to each of the K class templates are calculated instead of its distance to each of the N images in the training set.

Later on it becomes too cumbersome to keep track of two sets of parameters, W and \mathbf{b} , and therefore, for the rest of the thesis we will write the linear classifier as:

$$f(\mathbf{x}_i, W) = W\mathbf{x}_i,$$

where \mathbf{b} is now contained in the last(/first?) column of W and the last element of \mathbf{x}_i is now the constant, 1. This is the so-called bias trick.

Note that thus far we have used raw pixel values in the range of [0, 255] as input. However, in practice, it is more common to subject the input images to some preprocessing before inputting them into the score function. The benefits of this will be made clear in the optimisation section. Common preprocessing techniques are the centering and scaling of the pixels so that their values lie in the range of $[-1, 1]$. To center the input image, is to calculate a *mean image* from the training images and subtract each of its pixel values from the corresponding pixel values of each image in the training set. This is identical to zero mean centering for standard statistical learning tasks - each pixel is seen as an input feature. Scaling is done by dividing each pixel by a function of its variance across the whole training set.

1.5.3 Loss Function

To evaluate the agreement between the score function and the ground truth labels, we need a loss function. A loss function, also known as the cost function or the objective, is high when the score function does a poor job of mapping the input images to the class scores, and low when it does so accurately. There are multiple ways of defining such a loss function.

1.5.3.1 Multiclass Support Vector Machine Loss

A commonly used loss is the Multiclass Support Vector Machine (SVM) loss. In statistical learning this is more commonly known as the Hinge Loss. The SVM loss is designed in such a way that it wants the correct class for each image to have a score higher than the incorrect classes by some fixed margin Δ . More precisely, the multiclass SVM loss for the i -th example with label y_i can be given by:

$$L_i = \sum_{j \neq y_i} \max(0, s_j - s_{y_i} + \Delta),$$

where $s_j = f(x_i, W)_j$ is the score for the j -th class computed for image i . Here L_i consists of $K - 1$ components, each representing an incorrect class. A component will make no contribution to the loss if the calculated class score for the corresponding incorrect class is less than the correct class score by a margin of Δ , *i.e.* $s_{y_i} - s_j > \Delta$. It will make a positive contribution otherwise. As an example, suppose we have three predicted class scores for an image $s = [4, 5, -3]$ and that the second class is the true label. Let $\Delta = 2$. The loss computed for this image will then consist of 2 components:

$$\begin{aligned} L_i &= \max(0, 4 - 5 + 2) + \max(0, -3 - 5 + 2) \\ &= 1 + 0 \end{aligned}$$

We see that although the predicted class score for class 1 was smaller than the predicted class score for the true label, class 2, it was still within a margin of $\Delta = 2$ and therefore had a positive contribution to the loss. The predicted class score for class 3 was far lower than predicted class score for the true label and therefore did not make any contribution to the loss. In summary, the SVM loss function wants the score of the correct class to be larger than the incorrect class scores by at least Δ , if not, we will accumulate a loss.

Note that the loss is typically evaluated on a set of images and not just one, as we have described thus far. The average loss of a set with N images can be written as $L = \frac{1}{N} \sum_{i=1}^N L_i$. Another variation of the SVM loss is to replace the $\max(0, \cdot)$ term with the term, $\max(0, \cdot)^2$, which results in the squared hinge loss or the L_2 -SVM loss. This penalises violated margins more heavily and may work better in some cases. [<https://arxiv.org/abs/1306.0239>]

There is still one problem with the SVM loss described thus far. Suppose we have found a weight matrix W that correctly classifies all input images and by the correct margins, *i.e.* $L_i = 0, \forall i$, then setting the weight matrix to λW , for $\lambda > 1$ will have the same solution. This means the solution to the optimisation problem is not unique. It would make the optimisation task easier if we could remove this ambiguity. This can be done by adding a penalty term to the loss function, also known as regularisation. The most common regularisation penalty, $R(W)$, is the L_2 -norm:

$$R(W) = \sum_k \sum_l W_{k,l}^2,$$

which is simply the sum of the squared elements of the weight matrix. The full SVM loss can now be defined as:

$$L = \frac{1}{N} \sum_i L_i + \lambda R(W).$$

The two components of the loss can be called the *data loss* and the *regularisation loss*. λ determines how much regularisation should be done. If λ is large, more regularisation will take place. The value of λ is typically determined through cross-validation.

The regularisation penalty ensures a unique (or less solutions?) solution to the optimisation problem by restricting the weight parameters in size. Greater weight parameters will result in bigger loss, if everything else remain constant. Another appealing property is that penalising large weights tends to improve generalisation, because it means that no input dimension can have a very large influence on the scores all by itself.

Typically, only the weight parameters are regularised, since the bias terms do not control the strength of influence of an input dimension. However, in practice the often turns out to have a negligible effect.

To return to the value of Δ - it turns out that Δ and λ control the same trade-off and therefore we can safely set $\Delta = 1$ and only use cross-validation for determining λ . This might not seem obvious, but the key to understanding this is to realise that the weights in W have a direct influence on the class scores and therefore also on the differences between them. If all the elements in W are shrunk, all the differences in class scores will shrink and if all the elements are scaled up, the opposite will happen. Therefore, the margin Δ becomes meaningless in the sense that the weights can shrink or stretch to match Δ . Thus the only real trade-off is how large we allow the weights to be and this we specify through λ .

1.5.3.2 Softmax Classifier

The linear classifier combined with the SVM loss we call the SVM classifier. We will now look at the Softmax Classifier, which is the linear classifier combined with a different loss function. In statistics, the softmax classifier is better known as the multiclass logistic regressor. The biggest difference between the SVM classifier and the softmax classifier is that the latter gives a slightly more intuitive output in the form of normalised class probabilities, instead of the uncalibrated and less interpretable output of the SVM classifier. The loss function used for the softmax classifier is the *cross-entropy loss*:

$$\begin{aligned} L_i &= -\log \frac{e^{f_{y_i}}}{\sum_j e^{f_j}} \\ &= -f_{y_i} + \log \sum_j e^{f_j}. \end{aligned}$$

As before, the full loss is the mean of L_i over the whole dataset with an additional regularisation penalty.

To see where this loss function comes from, first consider the softmax function:

$$h_j(\mathbf{z}) = \frac{e^{z_j}}{\sum_k e^{z_k}}.$$

$h_j(\mathbf{z})$ squeezes the elements of the real-valued vector, \mathbf{z} , to fit in the range of $[0, 1]$ and that their sum always add to 1. Now, in information theory, the cross-entropy between a ‘true’ distribution p and an estimated distribution q is defined as:

$$H(p, q) = - \sum_x p(x) \log q(x).$$

Consider the case where the ‘true’ distribution, p , is a vector of zeros except at the y_i -th position, where the value is 1, and the estimated distribution, q , is the estimated class probabilities, $q = \frac{e^{f_{y_i}}}{\sum_j e^{f_j}}$. Clearly, $H(p, q)$ then simplifies to L_i . Thus the softmax classifier minimises the cross-entropy between the estimate class probabilities and the true distribution.

In the probabilistic interpretation of this classifier, we are minimising the negative log likelihood of the correct class, which can be interpreted as performing *maximum likelihood estimation* (MLE). From this view, the term $R(W)$ can be interpreted as coming from a Gaussian prior over the weight matrix, W , where instead of MLE we are performing *maximum a posteriori*.

To be clear, the softmax classifier interprets the scores computed by f to be the unnormalised log probabilities. Therefore, it undergoes the exponentiating and division (to become the normalized probabilities) before being used as input the cross-entropy loss.

Note that although we used the term ‘probabilities’ to describe the output the softmax classifier, these are not probabilities in the statistical sense. They do sum to 1 and are in the range of $[0, 1]$, but they are still technically confidence scores rather than probabilities, *i.e.* their order is interpretable but not their absolute values. The reason for this is that they depend heavily on the regularisation strength determined by λ . The higher λ is, the more uniform the probabilities become.

SVM and Softmax comparable. See <http://cs231n.github.io/linear-classify/>

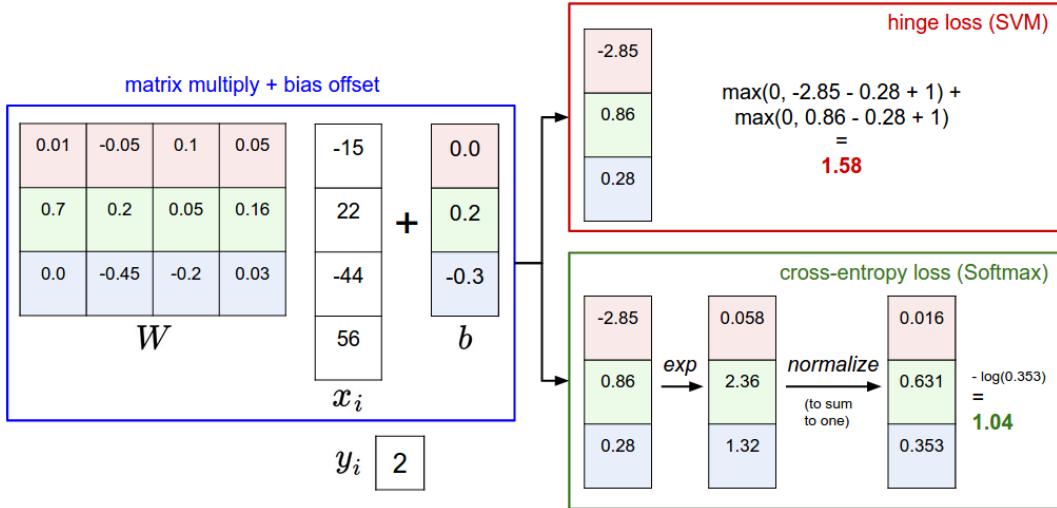


Figure 1.10: Figure to help with interp. Explain.

remember, only single label multiclass classification has been considered thus far and that some of these do not hold for multilabel classification.

1.5.4 Optimisation

From the previous sections we learned that the key components for the image classification task is the score function and the loss function. We looked at the linear mapping of raw pixel values to class scores and various loss functions, such as the hinge loss and cross-entropy loss, to evaluate the mapping against the ground truth labels. Putting all of this together, the SVM classifier can be reduced to the problem of minimising the loss:

$$L = \frac{1}{N} \sum_i \sum_{j \neq y_i} [\max(0, f(\mathbf{x}_i; W)_j - f(\mathbf{x}_i; W)_{y_i} + 1)] + \alpha R(W),$$

where $f(\mathbf{x}_i; W) = W\mathbf{x}_i$. This process of minimising the loss is also known as optimisation, which is the third key component. Optimisation is the process of finding the set of parameters W that minimise the loss function.

Once we get to convolutional neural networks, the only major difference is the use of a more complicated score function. The loss and optimisation components remain mostly unchanged.

Visualise a loss function in 2-dimensions to give idea of how it looks.
[\[http://cs231n.github.io/optimization-1/\]](http://cs231n.github.io/optimization-1/)

SVM classifier has a convex loss function. Whole research field in convex optimisation. When we get to more complex neural networks, the loss becomes non-convex.

The loss functions we use are technically non-differentiable, since there are ‘kinks’ in the loss function (gradients not define everywhere). However, the subgradient still exists and is commonly used instead. [<https://en.wikipedia.org/wiki/Subderivative>]

For this discussion on how to minimise the loss function with respect to W , we will use the SVM loss. The methods discussed may seem odd, since it is a convex optimisation problem. We only use this example for simplicity, since when we get to complex neural networks, the optimisation will not be a convex problem.

The core idea of this approach to minimise the loss with respect to W is that of iterative refinement - start with a random W and then iteratively refining it to get a lower loss. Finding the best set of weights, W is hard, but the problem of refining a specific set of weights to only be slightly better, is much easier.

A helpful analogy is that of the blindfolded hiker, who is on a hilly terrain, trying to reach the bottom. The height of the terrain represents the loss achieved. A possible strategy for the hiker to reach the bottom would be to test a step into a random direction and only take the step if it leads downhill. In optimisation terms, we can start with a random initialisation of W , generate random perturbations δW to it and if the loss at the perturbed $W + \delta W$ is lower, we will perform an update. This approach is better than a random search of W but still inefficient and computationally expensive.

It turns out that it is actually not necessary to randomly search for a good direction to move towards. The best direction can be determined mathematically. This best direction along which the weights should change corresponds to the direction of steepest descend and is related to the gradient of the loss function. In the hiking analogy, this approach roughly corresponds to feeling the slope of the hill below our feet and stepping down the direction that feels the steepest.

In one-dimensional functions, the slope is the instantaneous rate of change of the function at any specified point. The gradient is a generalisation of slope for multi-dimensional functions and is simply a vector of slopes, better known as derivatives, for each dimension in the search space. Mathematically, the expression for the derivative of a 1-dimensional function with respect to its input is:

$$\frac{df(x)}{dx} = \lim_{h \rightarrow 0} \frac{f(x + h) - f(x)}{h}.$$

When the function of interest takes a vector of numbers instead of a single number, we call the derivatives partial derivatives. The gradient is simply the vector of partial derivatives in each dimension.

There are two approaches to computing the gradient: the **numerical gradient** and the **analytic gradient**. Their pro's and con's are discussed in the following section.

1.5.4.1 Computing the Gradient Numerically

Iterate over all dimensions one by one, make a small change, h , along that dimension and calculate the partial derivative of the loss function along that dimension by seeing how much the function changed. Ideally, we want h to be as small as possible, since the mathematical formulation requires $h \rightarrow 0$. In practice it often works better to compute the numeric gradient using the centered difference formula: $\frac{f(x+h) - f(x-h)}{2h}$.

Note that the update of W should be made in the negative direction of the gradient, since we wish to decrease the loss function.

The gradient tells us the direction in which the function has the steepest rate of increase, but it does not tell us how far along this direction we should step, *i.e.* what is the value of the step size? This value is also known as the *learning rate* and we will soon learn that it is one of the most important hyperparameters of a neural network. Choosing a small step size in the direction of steepest descent will ensure consistent but slow progress. A large step in this direction may lead to a quicker descent but also has the risk of overshooting the optimal point.

The obvious downfall of this approach (in addition to that is only an approximation) is that we need to calculate the gradient in each direction/dimension. Neural networks have millions of parameters and therefore optimising them in this manner is clearly not feasible.

1.5.4.2 Computing the Gradient Analytically

The second way to compute the gradient is analytically using Calculus. A direct formula for the gradient can be derived and it also very fast to compute. This approach is more error prone to implement which is why in practice it is very common to perform a *gradient check*, which is the comparision of the analytic gradient to the numeric gradient to chech the correctness of the implementation.

By using the SVM loss for a single data point as an example:

$$L_i = \sum_{j \neq y_i} \left[\max(0, \mathbf{w}_j^T \mathbf{x}_i - \mathbf{w}_{y_i}^T \mathbf{x}_i + \Delta) \right].$$

Now, we want to differentiate the function with respect to the weights. Taking the gradient *w.r.t.* \mathbf{w}_{y_i} , gives:

$$\nabla_{\mathbf{w}_{y_i}} L_i = - \left(\sum_{j \neq y_i} \mathbb{I}(\mathbf{w}_j^T \mathbf{x}_i - \mathbf{w}_{y_i}^T \mathbf{x}_i + \Delta > 0) \right) \mathbf{x}_i,$$

where \mathbb{I} is the indicator function. This is simply the data vector scaled by the negative of the number of classes scores that did not meet the desired margin. The gradient with respect to the other rows of W where $j \neq y_i$ is:

$$\nabla_{\mathbf{w}_j} L_i = \mathbb{I}(\mathbf{w}_j^T \mathbf{x}_i - \mathbf{w}_{y_i}^T \mathbf{x}_i + \Delta > 0) \mathbf{x}_i.$$

Determining these equations are the tricky part. Once this is done, it is easy to implement the expressions and use them to perform gradient updates.

1.5.4.3 Gradient Descent

The procedure of repeatedly evaluating the gradient and then performing a parameter update is called *gradient descent*. This is by far the most common and established way of optimising neural network loss functions. Although there are some ‘bells and whistles’ to add to this algorithm, the core ideas remains the same when optimising neural networks.

One of the advantages of gradient descent is that a weight update can be made by only evaluating the gradient over a subset of the data, called *mini-batch gradient descent*. This is extremely helpful for large-scale applications, which are almost the norm for Deep Learning, since it is not necessary to compute the full loss function over the entire dataset. This leads to faster convergence and allows for the processing of large datasets that are too big to fit into a computer’s memory. A typical batch consists of 64/128/256 data points, but it depends on the computational power at hand. The gradient computed using a mini-batch is only an approximation of the gradient of the full loss. This seems to be sufficient in practice since the data points/images are correlated.

The specification of the mini-batch size is not very important and is usually determined based on memory constraints. Usually they are in powers of two, because in practice many vectorised operation implementations work faster when their inputs are sized in powers of 2. The extreme case of mini-batch gradient descent is when the batch size is selected to be 1. This is called *Stochastic Gradient Descent* (SGD). Recently, this is much less common, since it is more efficient to calculate the gradient in larger batches compared to only using one example. However, it is still widely acceptable to use the term SGD even though you are referring mini-batch gradient descent. This is actually the norm.

1.5.4.4 Backpropagation

Way of computing gradients of expressions through recursive application of the chain rule. Critical to understanding the optimisation of neural networks.

The core problem for this section is: We are given some function $f(\mathbf{x})$, where \mathbf{x} is a vector of inputs, and we are interested in computing the gradient of f at \mathbf{x} , i.e. $\nabla f(\mathbf{x})$. In our case, f corresponds to the loss function (e.g.

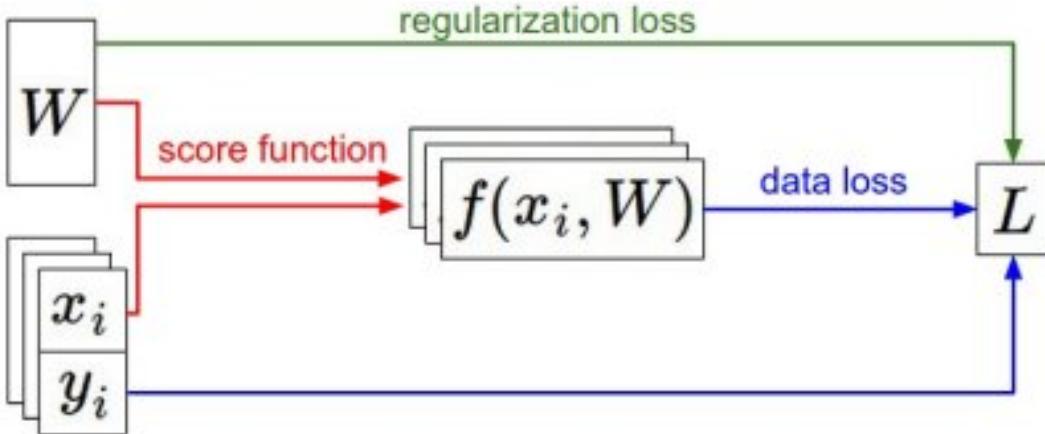


Figure 1.11: Good visual summary of data flow.

SVM loss) and the inputs \mathbf{x} will consist of the training data and the neural network weights.

Consider this simple example to introduce some of the conventions. Suppose we have the following function $f(x, y) = xy$. The partial derivative for either input is then:

$$\begin{aligned}\frac{\partial f}{\partial x} &= y, \\ \frac{\partial f}{\partial y} &= x\end{aligned}$$

These indicate the rate of change of f with respect to x and y respectively surrounding an infinitesimally small region near a particular point. For example, if $x = 2$ and $y = -5$, then $f(x, y) = -10$. The derivative on x is -5 , which tells us that if we were to increase the value of x by a tiny amount, the effect on the whole expression would be to decrease by 5 times that amount.

As used before, the vector of partial derivatives is called the gradient, ∇f . So for the previous simple example we have $\nabla f = \left[\frac{\partial f}{\partial x}, \frac{\partial f}{\partial y} \right] = [y, x]$. What follows are another two simple examples that will prove to be useful in later discussions.

For $f(x, y) = x + y$, $\nabla f = [1, 1]$, and if $f(x, y) = \max(x, y)$, then $\nabla f = [\mathbb{I}(x \geq y), \mathbb{I}(y \geq x)]$. Technically, *nabla f* for the latter function is called a subgradient, since the derivative for $\max(x, y)$ is not defined everywhere (?).

1.5.4.5 Compound Expressions with the Chain Rule

Now for the calculating of a more complicated expression, we will use the chain rule. Consider the expression $f(x, y, z) = (x + y)z$. Note that this expression can be decomposed into two expressions: $q = x + y$ and $f = qz$. From the previous simpler examples, we saw how to calculate the gradient for these

simple expression of addition and multiplication separately. But what we are really interested in is how to calculate the gradient of f w.r.t. its inputs, x, y, z . This can be done using the *chain rule*. According to the chain rule, $\frac{\partial f}{\partial x} = \frac{\partial f}{\partial q} \frac{\partial q}{\partial x}$, and similarly for $\frac{\partial f}{\partial y}$ and $\frac{\partial f}{\partial z}$. This can be viewed as the simplest form of backpropagation.

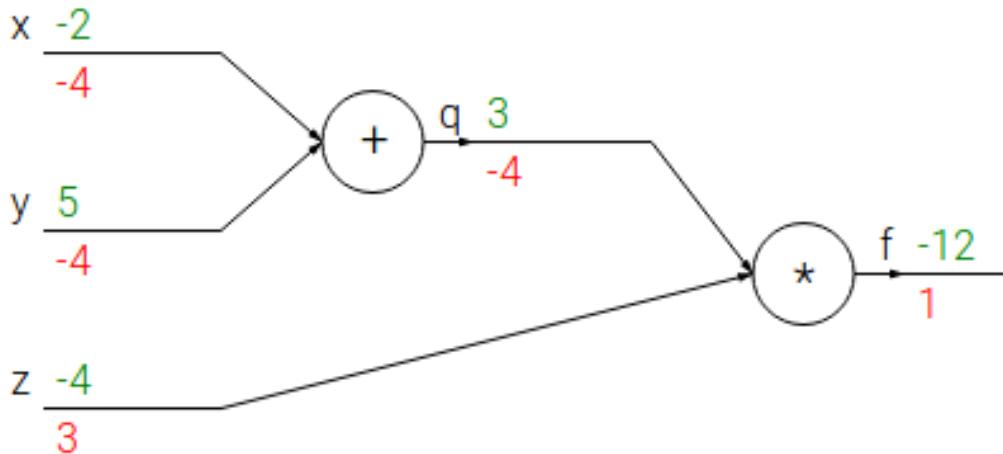


Figure 1.12: Simple circuit diagram to visualise backpropagation.

Suppose we want to compute the gradient at inputs $x = -2$, $y = 5$ and $z = -4$. First, we make a *forward pass* to compute the outputs from the given inputs, i.e. $q = 3$ and then $f = -12$. These values are shown in green in the circuit diagram. The following step is to make a *backward pass* (backpropagation), which is to start at the end and recursively apply the chain rule to compute the gradients, shown in red in the circuit diagram, all the way to the inputs of the circuit. In the example, $\frac{\partial f}{\partial f} = 1$, $\frac{\partial f}{\partial z} = 3$, $\frac{\partial f}{\partial q} = -4$, $\frac{\partial f}{\partial x} = -4$ and $\frac{\partial f}{\partial y} = -4$. The gradients can be thought of as flowing backwards through the circuit.

Each circle in the diagram can be referred to as a gate. Notice that every gate (the addition gate (+) and the multiplication gate (*)) gets some inputs and can right away compute its output value and the local gradient of its inputs with respect to its output value. This is done completely independently without being aware of any of the details of the full circuit that they are embedded in. However, during backpropagation the gate will eventually learn about the gradient of its output value on the final output of the entire circuit. According to the chain rule, the gate should take that gradient and multiply it into every gradient it normally computes for all of its inputs. Let us look at the example again to make this clear.

The (+) gate received inputs [2, -5] and computed output 3. It also computed its local gradient with respect to both of its inputs, which is 1, since it is an addition operation. The rest of the circuit computed the final value to be -12. During the backward pass, the (+) gate learns that the gradient for its output was -4. It then takes that gradient and multiplies it to all of the local gradients for its inputs, which results in -4 and -4. This implies that if x, y were to decrease (responding to their negative gradients) then the (+) gate's output would decrease, which in turn makes the (*) gate's output increase. Thus backpropagation can be thought of as gates communicating to each other through the gradient signal whether they want their outputs to increase or decrease, so as to make the final output higher.

1.5.4.6 Modularity

We introduced addition gates and multiplication gates, but any kind of differentiable function can act as a gate. We can also group multiple gates into a single gate or decompose a function into multiple gates whenever it is convenient. Consider the following expression to illustrate this:

$$f(\mathbf{w}, \mathbf{x}) = \frac{1}{1 + e^{-(w_0x_0 + w_1x_1 + w_2)}}.$$

This function is actually a common piece in a neural network, but for now we can view it as mapping from inputs \mathbf{x}, \mathbf{w} to a single number. The function is made up of multiple gates, and aside from the ones already discussed (addition, multiplication and max), they are:

$$\begin{aligned} f(x) &= \frac{1}{x} &\implies \frac{df}{dx} &= -\frac{1}{x^2} \\ f_c(x) &= c + x &\implies \frac{df}{dx} &= 1 \\ f(x) &= e^x &\implies \frac{df}{dx} &= e^x \\ f_a(x) &= ax &\implies \frac{df}{dx} &= a \end{aligned}$$

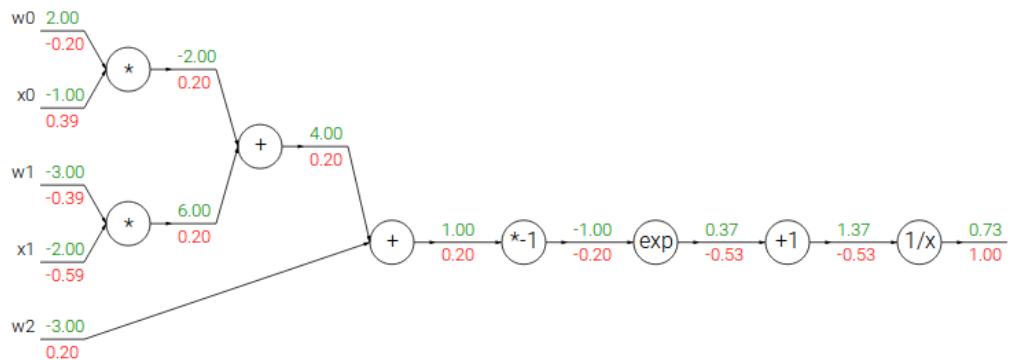
where c, a are constants. The full circuit for this expression is then:

The long chain of functions (gates) on the dot product of \mathbf{x} and \mathbf{w} is the decomposition of the *sigmoid function*:

$$\sigma(x) = \frac{1}{1 + e^{-x}}.$$

The derivative of the sigmoid function simplifies to a very convenient expression:

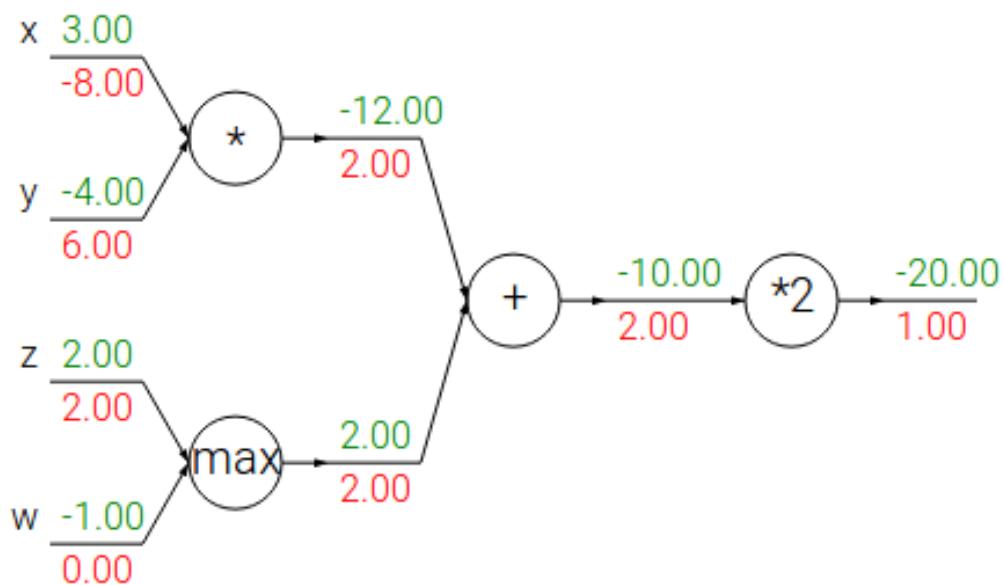
$$\frac{d\sigma(x)}{dx} = \frac{e^{-x}}{(1 + e^{-x})^2} = \left(\frac{1 + e^{-x} - 1}{1 + e^{-x}} \right) \left(\frac{1}{1 + e^{-x}} \right) = (1 - \sigma(x))\sigma(x).$$

**Figure 1.13:** Sigmoid circuit.

Therefore in any real practical application it would be very useful to group the operations of the tail chain into a single gate.

1.5.4.7 Patterns in Backward Flow

It is interesting to note that in many cases the backward-flowing gradient can be interpreted on an intuitive level. Take the three most commonly used gates in neural networks, (add, mul, max), as an example. All of them have very simple interpretations in terms of how they act during backpropagation. Consider the following example circuit:

**Figure 1.14:** example circuit for interpretation.

From the diagram above, the following patterns should be clear:

- The add gate always takes the gradient on its output and distributes it equally to all of its inputs, regardless of what their values were during the forward pass. This is because the local gradient for the add operation is always 1 for all its inputs.
- The max gate routes the gradient to exactly one of its inputs, the input that had the highest value during the forward pass. This because the local gradient for a max gate is 1 for the highest value and 0 for all other values.
- The multiply gate switches the gradients of its inputs and then multiply it by its output gradient.

Notice that if one of the inputs to the multiply gate is very small and the other is very big, then the multiply gate will do something slightly unintuitive: it will assign a relatively huge gradient to the small input and a tiny gradient to the large input. This is good to know, since in linear classifiers where the weights are multiplied by the inputs, it means that if the inputs are multiplied by a 1000, then the gradient on the weights will be 1000 times larger and you would have to lower the learning rate by that factor to compensate. This shows how important preprocessing is for the optimisation of a classifier.

The above sections were concerned with single variables, but all concepts extend in a straight-forward manner to matrix and vector operations. However, one must pay closer attention to dimensions and transpose operations.

- <http://cs231n.github.io/>

1.6 Outline

The structure of this thesis is built to mimic the workflow of fitting a supervised learning model to data. At each step, the relevant literature will be critically reviewed and discussed. Thereafter the proposed and recommended strategies will be applied to our data to see if the results match the literature and to find the best methods for our application.

In any supervised learning problem, it is essential to become familiar with the data and the task at hand before moving on to the training process. The background information of the data has already been discussed. In Chapter ?? the unique properties of multi-label data will be investigated and what steps are recommended to follow for data with certain properties. It is very important to clearly define the objective of the supervised learning task. For this thesis, prediction accuracy is more important than making inferences on the data (models also giving insight into the data is a bonus). The evaluation

metric for our task will be introduced and discussed in Chapter ?? along with other ways to evaluate multi-label classifiers.

Other things still to mention:

- basic ML strategies
- ML resampling strategies for class imbalance and error estimates
- orders of complexity
- label dependence
- input space reduction
- output space reduction
- final predictions and evaluations (maybe MDS of actual vs predicted)
- might want to include short history/timeline of ML
- might want to do a meta analysis of the literature on main topics

Chapter 2

Neural Networks

2.1 Introduction

In chapter 1 we have introduced all of the basic components for building a Neural Network. Recall the linear classifier that mapped the inputs, \mathbf{x} , to a vector of class scores, \mathbf{s} , $\mathbf{s} = W\mathbf{x}$, where W is a matrix of weights. Here W has K rows and p columns corresponding to the number of classes and size of the inputs respectively. As mentioned in chapter 1, a Neural Network has a more complicated mapping from the inputs to the class scores. An example Neural Network would instead have a mapping like, $\mathbf{s} = W_2 \max(0, W_1 \mathbf{x})$. This time, for example, W_1 could be a matrix transforming the inputs to a 100-dimensional vector, thus of size $100 \times p$. The function $\max(0, \cdot)$ introduces a non-linearity that is applied element-wise. It simply thresholds all values below zero to zero. There are several types of non-linearities that can be applied, but this is a common choice. Finally, W_2 , is a matrix of size $K \times 100$, mapping the intermediate vector to the final class scores. The key difference here is the non-linearity. If it is left out, the two matrices could be collapsed into one and therefore the predicted class scores would again be a linear function of the input. W_1, W_2 is learned through stochastic gradient descent (SGD), their gradients are derived with the chain rule and computed with backpropogation.

The above mapping is an example of a two-layer network. A three-layer neural network may look something like this:

$$\mathbf{s} = W_3 \max(0, W_2 \max(0, W_1 \mathbf{x})).$$

Now there are two non-linearities and W_1, W_2, W_3 are all parameters to be learned. Their sizes, which determine the size of the intermediate layers (vectors), are seen as hyperparameters and how they can be determined will be discussed shortly. In the next section we will show where the name, Neural Networks, come from and ...

2.2 Biological Motivation and Connections

Originally primarily inspired by the goal of modelling biological neural systems, but has since diverged and become a matter of engineering and achieving good results in Machine Learning tasks.

Coarse model of biological neural systems and how they can be modelled.

2.3 Common Activation Functions

2.3.1 Sigmoid

2.3.2 Tanh

2.3.3 ReLu

- Leaky ReLu

2.3.4 Maxout

- mention where we will discuss ELU and SELU

2.4 Architectures

Layerwise organisation, naming conventions, size

Representational power -> universal approximators.

More on size, overfitting and generalisation, regularisation

- – <https://arxiv.org/abs/1706.01350>

2.5 Setup

2.5.1 Data Preprocessing

- mean subtraction
- normalisation
- pca and whitening
- leakage

2.5.2 Weight Initialisation

- all zero
- small random
- calibrating the variances

- sparse initialisation
- initialising biases

2.5.3 Batch Normalisation

- <https://arxiv.org/abs/1502.03167>

2.5.4 Regularisation

- L1
- L2
- maxnorm
- Dropout: <http://www.cs.toronto.edu/~rsalakhu/papers/srivastava14a.pdf>, <http://papers.nips.cc/paper/4882-dropout-training-as-adaptive-regularization.pdf>
- noise in forward pass
- bias regularisation
- per layerregularisation

2.6 Loss Functions

2.6.1 Classification

2.6.2 Attrubute Classification

2.6.3 Regression

2.6.4 Structered Prediction

2.7 Learning

Process of learning the parameters and finding good hyperparameters.

- practical tips for learning

2.7.1 Monitoring

- loss function + learning rate
- train/val acc
- ration of weights

- activation per layer
- first layer viz

2.7.2 Parameter Updates

- momentum
- Nesterov
- decay
- adaptive: adagrad, rmsprop, adam
- something on cyclical?

2.7.3 Freezing Layers

- <https://arxiv.org/abs/1706.04983>

2.8 Hyperparameter Optimisation

2.9 Evaluation

2.9.1 Ensembles

- same model diff initialisations
- top models through cv
- different checkpoints
- running average of parameters
- the paper on ensembling from cyclical minima
- maybe tta
- Pseudo-Labelling and Knowledge-Distillation

Chapter 3

Convolutional Neural Networks

3.1 Introduction

3.2 ConvNet Layers

3.2.1 Convolutional Layer

3.2.2 Pooling Layer

- mixed pool: <https://pdfs.semanticscholar.org/de66/4f22dd4c7b4c15ac4a52513004aee55765ff.pdf> and <https://arxiv.org/pdf/1509.08985.pdf>, can try implementation from <https://github.com/fchollet/keras/issues/2816>
- maxout?

3.2.3 Normalisation Layer

3.2.4 Fully Connected Layer

- also option to replace with conv layer

3.3 ConvNet Architectures

3.3.1 Layer Patterns

3.3.2 Layer Sizing Patterns

3.3.3 Famous Architectures

- AlexNet
- VGG
- ResNet
- DenseNet

- Inception (?)

3.4 Visualizing CNN's

- <https://github.com/raghakot/keras-vis>
- <http://yosinski.com/deepvis>

3.4.1 Activations and First Layer Weights

3.4.2 Images with Maximum Activation

3.4.3 t-SNE Embedding

3.4.4 Occluding

- more resources: <http://cs231n.github.io/understanding-cnn/>

3.5 Transfer Learning

3.5.1 Feature Extractor

3.5.2 Fine-Tuning

3.5.3 Pretrained Models

Chapter 4

Multi-Label Convolutional Neural Networks

4.1 Introduction

First discuss the domain of MLC in general (only the aspects transferable to Deep Learning) and then move on to look at approaches of ML with ConvNets

4.2 Multi-Label Classification

4.3 Evaluation Metrics

4.4 Label Dependence

4.5 Problem Transformation Approaches

4.5.1 Binary Relevance

4.5.2 Label Powerset

4.5.3 Classifier Chains

4.6 Algorithm Adaption Approaches

4.7 Ensemble Approaches

4.7.1 Ensemble of Classifier Chains

4.7.2 Random k-Labelssets

- something on (re)sampling

4.8 Spatial Regularization Networks

- <https://arxiv.org/pdf/1702.05891.pdf>

4.9 From Single to Multi Output Paper ()

4.10 RNN-CNN paper ()

4.11 Direct binary Embedding

- <https://arxiv.org/pdf/1703.04960.pdf>

4.12 Another ML architecture

- <https://arxiv.org/pdf/1609.07982.pdf>
- replace last softmax with sigmoid
- replace last FC with maxout

- replace last pooling with spatial pyramid pooling
- other option use FCN with global max pool at end before sigmoid
- dropout only on first layers after representation (fixed VGG)
- note they also used dropout at testing and then combined for mean prediction

4.13 Is object localization for free? – Weakly-supervised learning with convolutional neural networks

- http://www.cv-foundation.org/openaccess/content_cvpr_2015/papers/Oquab_Is_Object_Localization_2015_CVPR_paper.pdf
- section on label correlations for MLC

4.14 Near Perfect Protein Multi-Label Classification with Deep Neural Networks

- <https://arxiv.org/pdf/1703.10663.pdf>
- spp layer after convolutions - not sure if it has to do with MLC

4.15 BP-MLL

- <http://citeseerx.ist.psu.edu/viewdoc/download?doi=10.1.1.130.7318&rep=rep1&type=pdf>
- description on NN and some references

4.16 ML NN for text

- <https://arxiv.org/pdf/1312.5419.pdf>

4.17 ML MT

- <http://www.cripac.ia.ac.cn/irds/People/lwang/M-MCG/Publications/2013/YH2013ICIP.pdf>
- but not much detail

4.18 ML Attention:

- <https://arxiv.org/pdf/1412.7755.pdf>

4.19 Sparsemax ML loss

- <https://arxiv.org/pdf/1602.02068.pdf>
- Other object detection

Chapter 5

Remote Sensing

- Wiki: In current usage, the term “remote sensing” generally refers to the use of satellite- or aircraft-based sensor technologies to detect and classify objects on Earth, including on the surface and in the atmosphere and oceans, based on propagated signals (e.g. electromagnetic radiation).

The idea is not to review the domain in detail, but rather to discuss the state-of-the-art Deep Learning approaches to Remote Sensing or related problems.

5.1 Multi-Label Classification Based on Low Rank Representation for Image Annotation

- (?)
- remote sensing images are easily accumulated but the labeling process is most of the infeasible.
- most applications in single-label framework.
- graph-based multi-label classification approach called Multi-Label Classification based on Low Rank Representation for image annotation (MLC-LRR) has been proposed.
- can effectively capture global label correlation.
- take advantage of limited labeled images and abundant unlabeled images
- does very well

5.2 <https://arxiv.org/pdf/1706.01171.pdf>

- recent years DL have made a breakthrough for satellite image analysis
- land cover classification
- hyperspectral image analysis

- synthetic aperture radar
- large datasets of satellite images with high quality labels are not easily available
- most works use pre trained
- use early and late fusion of rgb images and local binary patterns
- We design deep models by constructing a two-stream deep architecture where texture coded mapped images are used as a second stream and fuse it with the standard RGB stream
- only single label

5.3 Do Deep Features Generalize from Everyday Objects to Remote Sensing and Aerial Scenes Domains?

- http://www.cv-foundation.org/openaccess/content_cvpr_workshops_2015/W13/papers/Penatti_Do_Deep_Features_2015_CVPR_paper.pdf
- the use of deep learning is rapidly growing
- still no evaluation of pretrained convnets in aerial and remote sensing domains
- contribution: evaluation of the generalisation power of convnets from everyday objects to aerial and remote sensing domain, comparative evaluation of global descriptors, correlation analysis among different convnets
- also used fusing
- convnet features the best for aerial
- ACC and BIC best for Coffee Scene
- depends on intrinsic properties of data
- fusion can improve
- looks like fine tuned conv layers aswell
- only output of penultimate layer of pretrained network is used

5.4 Transferring Deep Convolutional Neural Networks for the Scene Classification of High-Resolution Remote Sensing Imagery

- <http://www.mdpi.com/2072-4292/7/11/14680/htm>
- can we transfer the successfully pre-trained CNNs to address HRRS scene classification, which is also a typical recognition task with limited amount

of training data?

- test two feature extraction from CNN: fc layer before classification, last conv layer with different scaled inputs
- also contribute comparison of pretrained convnets (vgg's, alex, caffe, places)
- lack of investigations on using CNNs for HRRS
- did not pre train convnet feature extractors
- center + corners with horizontal flips augmentation for testing. Did this to input images and averaged outputs for ultimate feature extraction (shows empirically that it helped)
- for fc features, performed better after relu
- Although the features of FC layers capture global spatial layout information, they are still fairly sensitive to global rotation and scaling, making them less suitable for HRRS scenes that greatly differ in orientation and scales.
- not sure how they used BOW on multi scale conv features
- show multi scale does better (wonder if this will be true if skip connections)
- their methods not better than googlenet + finetune
- conv features more suitable than fc, both better than low level

5.5 Land Use Classification in Remote Sensing Images by Convolutional Neural Networks

- <https://arxiv.org/pdf/1508.00092.pdf>
- pretrain nets (caffe and google) + fine tune
- compare training from scratch, fine tuning and feature vector
- for UC-Merced: fine tuning got best results and then feature vector
- better than handcrafted features
- for Brazilian coffee: from scratch and fine tune were very similar

5.6 Learning Low Dimensional Convolutional Neural Networks for High-Resolution Remote Sensing Image Retrieval

- <https://arxiv.org/pdf/1610.03023.pdf>
- Investigate how to extract deep feature representations based on convolutional neural networks (CNN) for high-resolution remote sensing image retrieval (HRRSIR)

- compare feature extraction from fc and conv from pre trained, vs training novel cnn on large scale remote sensing and then features are used.
- Nothing newer than vgg
- ambiguous results with fc layer with + without relu
- both better than handcrafted features
- feature aggregation methods used (figure out)
- the custom pretrained scheme performed better when the datasets were similar

5.7 What do We Learn by Semantic Scene Understanding for Remote Sensing imagery in CNN framework?

- <https://arxiv.org/pdf/1705.07077.pdf>
- Compared with object recognition, scene understanding not only needs to identify the targets, it should also understand the distribution of targets in a scene
- model depth acts differently on different classes
- more complex scenes require greater depth
- multi scale works better for complex scenes

5.8 Unsupervised Geometric Learning of Hyperspectral Images

- <https://arxiv.org/pdf/1704.07961.pdf>
- way of segmenting hyperspectral images without supervision

5.9 Using convolutional networks and satellite imagery to identify patterns in urban environments at a large scale

- <https://arxiv.org/pdf/1704.02965.pdf>
- good survey and resources on other land classification projects
- pretrained model on image net, fine tune on urban atlas and deepsat
- mostly urban environments
- interesting figure on how the area trained on makes a difference in accuracy on other areas
- shows bigger patch size leads to better accuracy

Chapter 6

Using Satellite Imagery for Good: Detecting Communities in Desert and Mapping Vaccination Activities

- <https://arxiv.org/pdf/1705.04451.pdf>
- interesting insight under implementation section
- better to train on own data than pretrain
- interesting method of adding more data: after n epochs test model on a set, those that were wrong are added to training (unclear on specifics)
- FCN worked better for them, batchnorm didnt
- relu did not work

Chapter 7

Solar Power Plant Detection on Multi-Spectral Satellite Imagery using Weakly-Supervised CNN with Feedback Features and m-PCNN Fusion

- <https://arxiv.org/pdf/1704.06410.pdf>
- novel architecture

Chapter 8

Hard Mixtures of Experts for Large Scale Weakly Supervised Vision

- <https://arxiv.org/pdf/1704.06363.pdf>
- MOE for MLC

8.1 To read:

- Vehicle detection in satellite images by hybrid deep convolutional neural networks,
- Unsupervised deep feature extraction for remote sensing image classification,
- Detecting man-made structures and changes in satellite imagery with a content-based information retrieval system built on self-organizing maps
- Deep learning-based classification of hyperspectral data
- Spectralspatial classification of hyperspectral data based on deep belief network,
- Multiclass feature learning for hyperspectral image classification: Sparse and hierarchical solutions
- High-resolution sar image classification via deep convolutional autoencoders
- Deep learning earth observation classification using imagenet pretrained networks

- Representation learning for contextual object and region detection in remote sensing
- Feature learning based approach for weed classification using high resolution aerial images from a digital camera mounted on a uav
- Saliency-guided unsupervised feature learning for scene classification
- Unsupervised deep feature extraction of hyperspectral image
- Deep model for classification of hyperspectral image using restricted boltzmann machine
- Unsupervised feature learning for aerial scene classification
- High-resolution remote-sensing imagery retrieval using sparse features by auto-encoder
- Visual descriptors for content-based retrieval of remote sensing images
- Classification and Segmentation of Satellite Orthoimagery Using Convolutional Neural Networks
- Convolutional Neural Network Based Automatic Object Detection on Aerial Images
- Land Use and Land Cover Classification Using Deep Learning Techniques
- Benchmarking Deep Learning Frameworks for the Classification of Very High Resolution Satellite Multispectral Data. !!!
- Learning Multi-Scale Deep Features for High-Resolution Satellite Image Classification.
- DeepSat - A Learning framework for Satellite Imagery
- https://www.cs.toronto.edu/%7Evmnih/docs/Mnih_Volodymyr_PhD_Thesis.pdf (hinton student thesis), implementation: <https://github.com/mitmul/ssai-cnn>
- Remote Sensing Image Scene Classification: Benchmark and State of the Art
- (?)
- (?)
- Semantic annotation of high-resolution remote sensing images via Gaussian process multi-instance multilabel learning
- deepsat for data: <https://github.com/trailbehind/DeepOSM>, guide at: <https://github.com/developmentseed/skynet-data>

Chapter 9

Results (/Application)

In this chapter, some of the theoretical recommendations will be evaluated empirically, with the goal to find the best approaches for this dataset. The full end-to-end workflow will be discussed and intermediate results also reported.

(Preliminary) The network will consist of two parts: a feature extraction part and a classification part. Basically a fine-tuning framework. The feauture extractor will be a popular Convolutional Neural Network (CNN) pretrained on ImageNet, *e.g.* VGG, ResNet, DenseNet, Inception. The classification part is the mapping from the extracted features to the class scores. This can be done in various ways and will be experimented with, for example: a combination of BR output and LP output, classification head for each label or Rakel output. The weights of the whole classification part will be trained on the Amazon dataset and, in some cases, the last layers of the feature extraction part.

9.1 Comparison of Pretrained Networks for Transfer Learning

- VGG16
- VGG19
- ResNet50
- DenseNet
- Inception

9.2 Experimentation with Classification Heads

- separate vs combined
- BR vs LP vs CC?
- Rakel?
- combo of BR and LP

- FCN
- spp: <https://github.com/yhenon/keras-spp>

9.3 Class Imbalance

- https://www.reddit.com/r/MachineLearning/comments/6iq5i8/d_what_are_your_favorite_ways_for_dealing_with/

9.4 Data Augmentation

- elastice transform: <https://pdfs.semanticscholar.org/7b1c/c19dec9289c66e7ab45e80e8c422735.pdf>

9.5 Pseudo-Labelling

9.6 Ensembling

Chapter 10

Things that need a place:

- challenges for image classification: (maybe in CNNs in practice)
 - <http://cs231n.github.io/classification/>
- Feature learning
- one-shot learning:
 - <https://github.com/sorenbouma/keras-oneshot>
 - https://github.com/fchollet/keras/blob/master/examples/mnist_siamese_graph.py
 - <https://sorenbouma.github.io/blog/oneshot/>
- multi-task learning:
 - <https://arxiv.org/abs/1706.05137>
- relational learning:
 - <https://arxiv.org/pdf/1706.01427.pdf>
- AutoML:
 - <https://research.googleblog.com/2017/05/using-machine-learning-to-explore.html>

Chapter 11

Conclusion

- summary
- contributions
- recommendations
- limitations
- future work

Appendices

Appendix A

Benchmark Datasets

Appendix B

Software

Bibliography