Cyberdyne runs a production line with 8 machines M1 to M8. The products that go on this line require processing by all 8 machines in sequence (i.e. starting on M1 then processing on M2 and onwards through the rest of the machines until they finish processing on M8) but the time that each product requires on each machines varies. The company has received an order for 30 jobs (see table 1 - an Excel copy is also available on Blackboard).

0b. import liblaries

```
In [144]: import numpy as np
import pandas as pd
import matplotlib.pyplot as plt
from pulp import *
```

0a. load data

```
In [145]: jobs = pd.read_csv('Jobs.csv')
```

In [146]: jobs.set_index('Job')

Out[146]:

	Time on M_1	Time on M_2	Time on M_3	Time on M_4	Time on M_5	Time on M_6	Time on M_7	Time on M_8
Job								
1	9	3	6	10	8	5	3	2
2	2	4	4	1	1	5	5	3
3	5	9	8	2	9	8	1	10
4	3	5	10	6	8	9	1	2
5	2	2	7	9	7	8	8	1
6	1	5	7	6	6	5	2	10
7	8	1	2	1	6	6	4	2
8	9	3	2	4	6	3	6	10
9	4	4	2	3	7	7	10	8
10	1	4	3	2	3	10	9	6
11	2	8	8	8	3	4	7	10
12	6	8	10	8	10	3	6	7
13	6	2	7	1	10	1	10	7
14	9	7	5	4	8	1	2	2
15	3	1	10	4	10	2	8	3
16	9	2	1	1	4	3	7	4
17	7	1	7	6	6	3	6	7
18	8	5	5	10	5	9	2	4
19	6	1	6	1	1	7	5	2
20	7	1	5	9	7	1	8	2
21	2	8	5	2	3	4	6	10
22	1	8	9	9	7	1	10	8
23	10	3	3	10	6	7	2	4
24	7	1	6	2	4	4	9	2

	Time on M_1	Time on M_2	Time on M_3	Time on M_4	Time on M_5	Time on M_6	Time on M_7	Time on M_8
Job								
25	5	8	9	6	10	2	5	4
26	9	3	5	1	8	6	9	1
27	1	9	5	9	7	1	7	1
28	9	8	3	3	4	8	10	4
29	2	4	7	3	3	1	10	1
30	6	10	9	1	10	1	4	5

1. Create a computer tool to calculate the time of the end of the final job on the las machine, given a sorted list of jobs. Assume that jobs cannot overtake one another in the line.

In [147]: sorted_list_of_jobs = range(0,30)

```
In [215]: def total time(list of jobs):
              \# [0,3,1,2]
              time passed = 0
              n = 8 # number of machines
              all jobs finished = False
              job stage = np.zeros(len(list of jobs), dtype=int)
              job time left = np.zeros(len(list of jobs), dtype=int)
              is job busy = np.zeros(len(list of jobs), dtype=bool)
              machine time left = np.zeros(n, dtype=int) # specifies how much left for the job
              machine job number = np.zeros(n, dtype=int) # specifies which job INDEX from list of jobs is being executed
              is machine busy = np.zeros(8, dtype=bool)
              while not all jobs finished:
                  # iterate through machines to fill them with jobs
                  for ind in range(0,n):
                      # add appropraite amount of time to machines time left
                      if not is machine busy[ind] and machine job number[ind] != -1:
                          # get ind of next job
                          next job = machine job number[ind]
                          # check wether next job is busy
                          if not is_job_busy[next_job] and job_stage[next_job] == ind:
                              job stage[next job] += 1
                              is job busy[next job] = True
                              machine job number[ind] += 1
                              job_time_left[next_job] += jobs.iloc[list_of_jobs[next_job],ind+1]
                              machine time left[ind] += jobs.iloc[list of jobs[next job],ind+1]
                                print("Machine: " + str(ind) + " - " + str(machine_job number[ind]))
                              # if machine took its last item then tell it not to take any more
```

```
if machine job number[ind] >= len(list of jobs):
                    machine job number[ind] = -1
     print("----") # this indicates that one unit time passed
   # decrement all machines in machines time left by 1
    time passed += 1
   machine time left = np.where(machine time left < 1, machine time left, machine time left - 1)
    job time left = np.where(job time left < 1, job time left, job time left - 1)</pre>
   # update which machines are ready to take new jobs
   is machine busy = [machine != 0 for machine in machine time left]
   is job busy = [job != 0 for job in job time left]
   # all iobs finished
    all jobs finished = all(job == 8 and busy == False for job in job stage for busy in is job busy)
    # stop if your program enters infinite loop
   if (time passed > 400):
       all jobs finished = True
return time passed
```

```
In [216]: time = total_time(list(sorted_list_of_jobs))
print("Time for this sequence: " + str(time))
```

Time for this sequence: 256

2. Use the sum of time that the job requires on all machines as a heuristic. Order the jobs in an ascending and descending order and calculate the total makespan of the resulting job sequence (the time that it takes to complete all 8 processes on all jobs).

```
In [217]: jobs_2 = jobs.copy()
    jobs_2['total_time'] = jobs_2[jobs_2.columns[1:]].sum(axis=1)

    jobs_2_ascending = jobs_2.sort_values(by ='total_time', kind='mergesort')
    jobs_2_descending = jobs_2.sort_values(by ='total_time', ascending=False, kind='mergesort')

    jobs_heuristic_ascending = jobs_2_ascending.index.to_series().values
    jobs_heuristic_descending = jobs_2_descending.index.to_series().values

In [218]:    time_ascending = total_time(jobs_heuristic_ascending)
    print("Time_for_ASCENDING_sequence: " + str(time_ascending))
    print("Time_for_DESCENDING_sequence: " + str(time_descending))

Time_for_ASCENDING_sequence: 262
Time_for_DESCENDING_sequence: 267
```

3. Use the sum of the time of the first four jobs and the sum of the time of the last four jobs and use Johnson's rule 1 to schedule the jobs. Compute the makespan and compare with the previous ones.

create sequence of jobs according to johnson's rule

```
In [226]: jobs johnsons = np.zeros(30, dtype=int)
          first ind = 0
          last ind = 29
          for index, row in jobs_3_johnsons.iterrows():
              if row['lowest'] == row['first four m']:
                  jobs johnsons[first ind] = index
                  first ind += 1
              if row['lowest'] == row['last four m']:
                  jobs johnsons[last ind] = index
                  last ind -= 1
In [227]: time johnsons = total time(jobs johnsons)
          print("Time for JOHNSON'S sequence: " + str(time johnsons))
```

Time for JOHNSON'S sequence: 243

4. Use a metaheuristic method to find a good schedule and compare with the results of the previous sections

Genetic algorithm

1) initialisation

2) iteration

```
In [261]: import random
          random.seed(a=100) # set seed value, such that your psudo-random generated numbers are reproducible
          # function used to create child from two parents
          def breed(parent1, parent2):
              child = []
              childP1 = []
              childP2 = []
              geneA = int(random.random() * len(parent1))
              geneB = int(random.random() * len(parent1))
              startGene = min(geneA, geneB)
              endGene = max(geneA, geneB)
              for i in range(startGene, endGene):
                   childP1.append(parent1[i])
              childP2 = [item for item in parent2 if item not in childP1]
               child = childP1 + childP2
              return child
          def mutate(individual, mutationRate):
              for swapped in range(len(individual)):
                   if(random.random() < mutationRate):</pre>
                       swapWith = int(random.random() * len(individual))
                       job1 = individual[swapped]
                       job2 = individual[swapWith]
                       individual[swapped] = job2
                       individual[swapWith] = job1
              return individual
          # above functions are adapted from:
          # https://towardsdatascience.com/evolution-of-a-salesman-a-complete-genetic-algorithm-tutorial-for-python-6fe5d2b3ca35
```

```
In [262]: results = np.zeros(len(list of sequences), dtype=int)
          n = 0 # variabel for termination condition
          min_time_old = None
          min time = None
          iteration = 1
          while n < 10:
              print("----- ITERATION " + str(iteration) + " -----")
              iteration += 1
              i = 0
              # update termination condition
              if min time == min time old:
                  n += 1
              else:
                  n = 0
              min time old = min time
              # ASSSES FITNESS
              for seq in list of sequences:
                  results[i] = total time(seq)
                  print(str(i) + ": " + str(results[i]))
                  i += 1
              results sorted = np.sort(results)
              # SELECT PARENTS
              # choose 4 parents from 5 best samples
              parents top = np.random.choice(results sorted[:5], size=4, replace=False)
              # choose 2 parents from other 5 samples
              parents bottom = np.random.choice(results sorted[5:], size=2, replace=False)
              # combine all 6 parents into a single array
              parents = np.concatenate((parents_top, parents_bottom))
              # form 3 random couples
              parents_perm = np.random.permutation(parents)
```

```
couples = [[i,j] for i,j in zip(parents_perm[:3], parents_perm[3:])]
    # get sequences from fitness values
    couples_sequences = [ [list_of_sequences[results.tolist().index(x)], list_of_sequences[results.tolist().index(y)]
1 for x, y in couples]
    # GET CHILDREN
    children 1 = [breed(p1, p2) for p1, p2 in couples sequences] # get 1st children from each couple
    children 2 = [breed(p1, p2) for p1, p2 in couples sequences] # get 2nd children from each couple
    children = np.concatenate((children 1, children 2))
    # MUTATE CHILDREN
   for i in range(len(children)):
        children[i] = mutate(children[i], 0.2)
   # GET NEW POPULATION (get new -> list of sequences)
   list of sequences = np.concatenate(([list of sequences[results.tolist().index(x)] for x in results sorted[:4]], ch
ildren))
   min time = results sorted[0]
print()
print("Best time: " + str(min time))
print("The best sequence is: " + str(list of sequences[results.tolist().index(min time)]))
```

----- ITERATION 1 -----0: 256 1: 262 2: 267 3: 243 4: 243 5: 250 6: 265 7: 245 8: 258 9: 271 ----- ITERATION 2 -----0: 243 1: 243 2: 245 3: 250 4: 247 5: 252 6: 241 7: 261 8: 253 9: 258 ----- ITERATION 3 -----0: 241 1: 243 2: 243 3: 245 4: 253 5: 256 6: 240 7: 247 8: 274 9: 247 ----- ITERATION 4 -----0: 240 1: 241 2: 243 3: 243 4: 254 5: 266 6: 249

```
7: 238
8: 262
9: 253
----- ITERATION 5 -----
0: 238
1: 240
2: 241
3: 243
4: 240
5: 252
6: 242
7: 252
8: 249
9: 241
----- ITERATION 6 -----
0: 238
1: 240
2: 240
3: 241
4: 241
5: 238
6: 245
7: 245
8: 245
9: 237
----- ITERATION 7 -----
0: 237
1: 238
2: 238
3: 240
4: 241
5: 234
6: 263
7: 242
8: 264
9: 226
----- ITERATION 8 -----
0: 226
1: 234
2: 237
3: 238
4: 233
```

```
5: 242
6: 254
7: 258
8: 252
9: 247
----- ITERATION 9 -----
0: 226
1: 233
2: 234
3: 237
4: 252
5: 236
6: 246
7: 260
8: 239
9: 258
----- ITERATION 10 -----
0: 226
1: 233
2: 234
3: 236
4: 259
5: 229
6: 242
7: 256
8: 244
9: 246
----- ITERATION 11 -----
0: 226
1: 229
2: 233
3: 234
4: 253
5: 252
6: 262
7: 242
8: 233
9: 247
----- ITERATION 12 -----
0: 226
1: 229
2: 233
```

```
3: 233
4: 259
5: 231
6: 236
7: 238
8: 253
9: 243
----- ITERATION 13 -----
0: 226
1: 229
2: 231
3: 233
4: 237
5: 243
6: 248
7: 248
8: 256
9: 258
----- ITERATION 14 -----
0: 226
1: 229
2: 231
3: 233
4: 230
5: 276
6: 247
7: 251
8: 238
9: 258
----- ITERATION 15 -----
0: 226
1: 229
2: 230
3: 231
4: 258
5: 236
6: 254
7: 248
8: 251
9: 248
----- ITERATION 16 -----
0: 226
```

```
1: 229
2: 230
3: 231
4: 257
5: 273
6: 233
7: 255
8: 258
9: 242
----- ITERATION 17 -----
0: 226
1: 229
2: 230
3: 231
4: 258
5: 260
6: 246
7: 247
8: 249
9: 250
----- ITERATION 18 -----
0: 226
1: 229
2: 230
3: 231
4: 238
5: 247
6: 257
7: 249
8: 253
9: 245
Best time: 226
The best sequence is: [23 8 1 9 12 4 11 14 17 27 5 15 20 24 6 21 19 18 7 28 25 2 10 0
 29 3 22 26 16 13]
```

Tabu algorithm

file:///C:/Users/XPS/Downloads/week_16.html

```
In [264]: # to be added
```

Particle swarm optimisation

```
In [263]: # to be added
```

5. Create a mathematical programming model for the problem and try to optimally solve it. If completed, compare the solution to the previous sections.

```
In [265]: # to be added
In []:
```