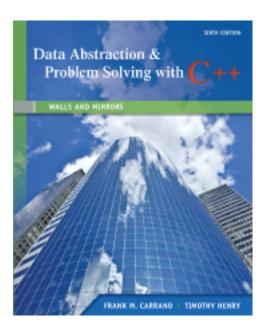
Answers to Checkpoint Questions

Data Abstraction & Problem Solving with C++

WALLS AND MIRRORS

SIXTH EDITION



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Question 1 Write specifications using UML notation for a function that computes the sum of the first five positive integers in an array of *n* arbitrary integers.

The specifications include type definitions, arguments, and preconditions and postconditions.

```
// Computes the sum of the first 5 positive integers
// in an array anArray.
// Precondition: The array anArray contains n integers, n >= 5;
// at least 5 integers in anArray are positive.
// Postcondition: Returns the sum of the first 5 positive
// integers in anArray; anArray and n are unchanged.
sumOf(in anArray: arrayType, in n: integer): integer

Another solution:
// Computes the sum of the first 5 positive integers
// in an array anArray.
// Precondition: The array anArray contains n integers.
// Postcondition: If anArray contains at least 5
// positive integers, returns their sum; otherwise, returns 0.
// anArray and n are unchanged.
sumOf(in anArray: arrayType, in n:integer): integer
```

Question 2 What is an abstract data type?

An abstract data type is a specification of data values and the operations on that data. This specification does not indicate how to store the data or how to implement the operations, and it is independent of any programming language.

Question 3 What steps should you take when designing an ADT?

- Describe the data.
- Identify the ADT's behaviors.
- Write the behaviors on a CRC card.
- Specify each operation by writing comments and UML; clearly identify assumptions.
- Refine the specifications by considering their behavior under unusual conditions.
- Write an abstract base class.

C++ Interlude 1

 ${f Question~1}$ Revise the parameterized constructor to call the base-class's constructor instead of MagicBox's constructor.

```
template < class ItemType >
MagicBox < ItemType > :: MagicBox (const ItemType & theItem) {
    PlainBox < ItemType > :: setItem(theItem);
    firstItemStored = true;
} // end constructor
```

Question 1 The following function computes the sum of the first $n \ge 1$ integers. Show how this function satisfies the properties of a recursive function.

```
/** Computes the sum of the integers from 1 through n.
@pre n > 0.
@post None.
@param n A positive integer
@return The sum 1 + 2 + . . . + n. */
int sumUpTo(int n)
{
   int sum = 0;
   if (n == 1)
       sum = 1;
   else // n > 1
       sum = n + sumUpTo(n - 1);
   return sum;
} // end sumUpTo
```

The product of n numbers is defined in terms of the product of n-1 numbers, which is a smaller problem of the same type. When n is 1, the product is anArray[0]; this occurrence is the base case. Because $n \ge 1$ initially and n decreases by 1 at each recursive call, the base case will be reached.

Question 2 Write a box trace of the function given in Checkpoint Question 1.

We trace the function with 4 as its argument (see next page).

The initial call ${\tt sumUpTo}\,(4)$ is made, and method ${\tt sumUpTo}$ begins execution:



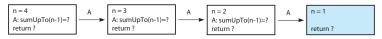
At point A a recursive call is made, and the new invocation of the method sumUpTo begins execution:



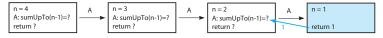
At point A a recursive call is made, and the new invocation of the method sumUpTo begins execution:



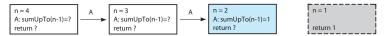
At point A a recursive call is made, and the new invocation of the method $\verb"sumUpTo"$ begins execution:



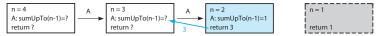
This is the base case, so this invocation of sumUpTo completes and returns a value to the caller:



The method value is returned to the calling box, which continues execution:



The current invocation of $\mathtt{sumUpTo}\,$ completes and returns a value to the caller:



The method value is returned to the calling box, which continues execution:



The current invocation of sumUpTo completes and returns a value to the caller:



The method value is returned to the calling box, which continues execution:



The current invocation of $\mbox{ sumUpTo }$ completes and returns a value to the caller:



The value 10 is returned to the initial call.

Question 3 Given an integer n > 0, write a recursive function countDown that writes the integers n, $n - 1, \ldots, 1$. *Hint:* What task can you do and what task can you ask a friend to do for you?

```
// Precondition: n > 0.
// Postcondition: Writes n, n - 1, ... , 1.
void countDown(int n)
{
   if (n > 0)
   {
      cout << n << endl;
      countDown(n-1);
   } // end if
} // end countDown</pre>
```

Question 4 In the previous definition of writeArrayBackward, why does the base case occur when the value of first exceeds the value of last?

When first > last, the array is empty. That is the base case. Since the body of the if statement is skipped in this case, no action takes place.

Question 5 Write a recursive function that computes and returns the product of the first $n \ge 1$ real numbers in an array.

```
// Precondition: anArray is an array of n real numbers, n ≥ 1.
// Postcondition: Returns the product of the n numbers in
// anArray.
double computeProduct(const double anArray[], int n),
{
   if (n == 1)
       return anArray[0];
   else
      return anArray[n - 1] * computeProduct(anArray, n - 1);
} // end computeProduct
```

Question 6 Show how the function that you wrote for the previous question satisfies the properties of a recursive function.

- 1. computeProduct calls itself.
- An array of n numbers is passed to the method. The recursive call is given a smaller array of n - 1 numbers.
- 3. anArray[0] is the base case.
- Since n ≥ 1 and the number of entries considered in anArray decreases by 1 at each recursive call, eventually the recursive call is computeProduct(anArray, 1). That is, n is 1, and the base case is reached.

Question 7 Write a recursive function that computes and returns the product of the integers in the array anArray[first..last].

Question 8 Define the recursive C++ function maxArray that returns the largest value in an array and adheres to the pseudocode just given.

Question 9 Trace the execution of the function solveTowers to solve the Towers of Hanoi problem for two disks.

The three recursive calls result in the following moves: Move a disk from A to C, from A to B, and then from C to B.

Question 10 Compute g(4, 2).

6

Question 11 Of the following recursive functions that you saw in this chapter, identify those that exhibit tail recursion: fact, writeBackward, writeBackward2, rabbit, *P* in the parade problem, getNumberOfGroups, maxArray, binarySearch, and kSmall.

writeBackward, binarySearch, and kSmall.

Question 1 What happens to the array items when the method add cannot add another entry to it, because it is already full?

Nothing.

Question 2 If a client of ArrayBag creates a bag aBag and a vector v containing five items, what happens to those items after the statement v = aBag.toVector() executes?

The memory originally allocated for v is now inaccessible. The five items in the original vector still exist but are no longer in v.

Question 3 What is an advantage and a disadvantage of calling the method getFrequencyOf from contains?

Advantage: Once getFrequencyOf works correctly, writing a correct version of contains is simple. Disadvantage: contains does more work than needed, because getFrequencyOf must check every entry in the bag. A more involved definition of contains could stop looking for the desired entry as soon as it is found.

Question 4 Revise the definition of the method contains so that it calls the method getIndexOf.

```
template<class ItemType>
bool ArrayBag<ItemType>::contains(const ItemType& anEntry) const
{
   return getIndexOf(anEntry) > -1;
} // end getCurrentSize
```

Question 5 Should we revise the specification of the method contains so that if it locates a given entry within the bag, it returns the index of that entry?

No. As a public method, contains should not provide a client with such implementation details. The client should have no expectation that a bag's entries are in an array, since they are in no particular order.

Question 6 Revise the definition of the method getIndexOf so that it does not use a boolean variable.

```
template<class ItemType>
int ArrayBag<ItemType>::getIndexOf(const ItemType& target) const
{
   int result = -1;
   int searchIndex = 0;
   // If the bag is empty, itemCount is zero, so loop is skipped
  while ((result == -1) && (searchIndex < itemCount))</pre>
      if (items[searchIndex] == target)
      {
         result = searchIndex;
      }
     else
      {
         searchIndex++;
      } // end if
   } // end while
  return result;
} // end getIndexOf
```

Question 1 Consider a linked chain of three nodes, such that each node contains a string. The first node contains "A", the second node contains "B", and the third node contains "C".

- a. Write C++ statements that create the described linked chain. Beginning with a head pointer headPtr that contains nullptr, create and attach a node for "C", then create and attach a node for "B", and finally create and attach a node for "A".
- **b.**Repeat part a, but instead create and attach nodes in the order "A", "B", "C".

```
// Part a: Create nodes for C, B, and A; insert nodes at beginning of
chain.
headPtr = new Node<ItemType>("C");
Node<ItemType>* newNodePtr = new Node<ItemType>("B");
newNodePtr->setNext(headPtr);
headPtr = newNodePtr;
newNodePtr->setNext(headPtr);
headPtr = newNodePtr;

// Part b: Create nodes for A, B, and C; insert nodes at end of chain.
headPtr = new Node<ItemType>("A");
Node<ItemType>* newNodePtr = new Node<ItemType>("B");
headPtr->setNext(newNodePtr);
Node<ItemType>* lastNodePtr = newNodePtr;
newNodePtr = new Node<ItemType>("C");
lastNodePtr->setNext(newNodePtr);
```

Question 2 Why are only a few changes necessary to reuse the code in Listing 3-2? How would you implement the changes using the "find and replace" functionality of a text editor or IDE?

Because both ArrayBag and LinkedBag are derived from BagInterface, they each implement the same methods. Moreover, BagInterface is a template that represents the data type of the entries in the bag generically with the identifier ItemType. The program in Listing 3-2 was written in this context. Thus, by replacing ArrayBag with LinkedBag in Listing 3-2, you will get a program to test the core methods of LinkedBag.

Question 3 Why is a LinkedBag object not concerned about becoming full?

Because you are able to create a new node and attach it to the linked chain each time you want to add a new entry to a bag.

Question 4 Suppose that the ADT bag had an operation that displayed its contents. Write a C++ definition for such a method for the class LinkedBag.

```
template < class ItemType>
void LinkedBag < ItemType>::displayBag() const
{
    cout << "The bag contains " << itemCount << " items:" << endl;
    Node < ItemType>* curPtr = headPtr;
    int counter = 0;
    while ((curPtr != nullptr) && (counter < itemCount))
    {
        cout << curPtr->getItem()) << " ";
        curPtr = curPtr->getNext();
        counter++;
    } // end while
    cout << endl;
} // end displayBag</pre>
```

Question 5 How many assignment operations does the method that you wrote for the previous question require?

If we count counter++ as 1 assignment, displayBag requires 2 x itemCount + 2 assignments during its execution.

Question 6 If the pointer variable curPtr becomes nullptr in the method getPointerTo, what value does the method contains return when the bag is not empty?

False.

Question 7 Trace the execution of the method contains when the bag is empty.

- contains calls getPointerTo.
- In getPointerTo,
 - found = false
 - curPtr = headPtr = nullptr
 - The while loop exits immediately.
 - The method returns nullptr.
- contains returns false.

Question 8 Revise the definition of the method getPointerTo so that the loop is controlled by a counter and the value of itemCount.

```
template<class ItemType>
Node<ItemType>* LinkedBag<ItemType>::
                getPointerTo(const ItemType& target) const
{
   bool found = false;
   Node<ItemType>* curPtr = headPtr;
   int counter = 0;
  while (!found && (counter < itemCount))</pre>
      if (target == curPtr->getItem())
         found = true;
      else
      {
         counter++;
         curPtr = curPtr->getNext();
        // end if
   }
     // end while
   return curPtr;
  // end getPointerTo
```

Question 9 What is a disadvantage of the definition of the method getPointerTo, as described in the previous question, when compared to its original definition?

If you make a mistake in the loop so that it counts incorrectly, curPtr can be set to nullptr within the body of the loop. As a result, the reference curPtr->getItem() will cause an exception.

Question 10 Why should the method getPointerTo not be made public?

Because it returns a pointer, which is an implementation detail that should be hidden from the client.

Question 11 Given the previous definition of the method remove, which entry in a bag can be deleted in the least time? Why?

The first entry. It is in the first node of the linked chain, so getPointerTo can locate it sooner than any other entry.

Question 12 Given the previous definition of the method remove, which entry in a bag takes the most time to delete? Why?

The last entry. It is in the last node of the linked chain, so getPointerTo must traverse the entire chain before locating it.

Question 13 Revise the destructor in the class LinkedBag so that it does not call clear but instead directly deletes each node of the underlying linked chain.

```
template < class ItemType>
LinkedBag < ItemType>::~LinkedBag()
{
    while (headPtr != nullptr)
    {
        Node < ItemType>* nodeToDeletePtr = headPtr;
        headPtr = headPtr->getNext();

        // Return node to the system
        nodeToDeletePtr->setNext(nullptr);
        delete nodeToDeletePtr;
    } // end while
    // headPtr is nullptr
    nodeToDeletePtr = nullptr;
    itemCount = 0;
} // end destructor
```

Question 14 Revise the method clear so that it calls a recursive method to deallocate the nodes in the chain.

```
template<class ItemType>
void LinkedBag<ItemType>::clear()
{
   deallocate(headPtr);
  headPtr = nullptr;
   itemCount = 0;
} // end clear
// Private method: Deallocates all nodes assigned to the bag
template<class ItemType>
void LinkedBag<ItemType>::deallocate(Node<ItemType>* nextNodePtr)
{
  if (nextNodePtr != nullptr)
      Node<ItemType>* nodeToDeletePtr = nextNodePtr;
      nextNodePtr = nextNodePtr->getNext();
      delete nodeToDeletePtr;
      deallocate(nextNodePtr);
  } // end if
} // end deallocate
```

Question 15 Revise the program in Listing 4-4 so that it tests first the array-based implementation and then the link-based implementation. Ensure that the program does not have a memory leak.

```
int main()
{
   BagInterface<string>* bagPtr = new ArrayBag<string>();
   cout << "Testing the Array-Based Bag:" << endl;</pre>
   cout << "The initial bag is empty." << endl;</pre>
   bagTester(bagPtr);
   delete bagPtr;
   cout << endl;</pre>
   bagPtr = new LinkedBag<string>();
   cout << "Testing the Link-Based Bag:" << endl;</pre>
   cout << "The initial bag is empty." << endl;</pre>
   bagTester(bagPtr);
   delete bagPtr;
   bagPtr = nullptr;
   cout << "All done!" << endl;</pre>
   return 0;
  // end main
}
```

With the definition of BagInterface given in Listing 1-1 of Chapter 1, both the program in Listing 4-4 and this revision will cause a warning message regarding the delete operator, because BagInterface is abstract and has a nonvirtual destructor. Despite the warning, the program will produce the desired output. To avoid the warning, you should add the following statement to the definition of BagInterface:

```
virtual ~BagInterface() {}
```

Note that this constructor has an empty method; it is not a pure virtual method.

Question 1 Consider the language of these character strings: \$, cc\$d, cccc\$dd, ccccc\$ddd, and so on. Write a recursive grammar for this language.

 $\langle aString \rangle =$ \$ | cc $\langle aString \rangle$ d

Question 2 Write the prefix expression that represents the following infix expression:

$$(a/b) * c - (d + e) * f$$

$$-*/abc*+def$$

Question 3 Write the infix expression that represents the following prefix expression:

$$--a/b+c*def$$

$$(a - b / (c + d * e)) - f$$

Question 4 Is the following string a prefix expression? +-/a b c*+d e f*g h

No.

Question 5 Write the postfix expression that represents the following infix expression:

$$(a * b - c) / d + (e - f)$$

$$ab*c-d/ef-+$$

Question 6 Trace the method isPath with the map in Figure 5-6 for the following requests. Show the recursive calls and the returns from each.

- Fly from A to B.
- Fly from A to D.
- Fly from *C* to *G*.

Fly from A to B: Stack contains A, then A B.

Fly from A to D: Stack contains A, then A B, then A B D.

Fly from C to G: Stack contains C, then C D, then C D H, then C D H G.

Question 7 Consider a Four Queens problem, which has the same rules as the Eight Queens problem but uses a 4 x 4 board. Find all solutions to this new problem by applying backtracking by hand.

The queens are in the squares indicated by the following (row, column) pairs:

Solution 1: (2, 1), (4, 2), (1, 3), (3, 4)

Question 1 If you push the letters A, B, C, and D in order onto a stack of characters and then pop them, in what order will they be deleted from the stack?

D, C, B, A.

Question 2 What do the initially empty stacks stack1 and stack2 "look like" after the following sequence of operations?

```
stack1.push(1)
                                             (stack entries are listed bottom to top)
                               stack1: 1
stack1.push(2)
                               stack1: 1 2
stack2.push(3)
                               stack2: 3
stack2.push(4)
                               stack2: 3 4
stack1.pop()
                               stack1: 1
stackTop = stack2.peek()
                               stackTop : 4
stack1.push(stackTop)
                               stack1: 1 4
stack1.push(5)
                               stack1: 1 4 5
stack2.pop()
                               stack2: 3
stack2.push(6)
                               stack2: 3 6
```

Question 3 For each of the following strings, trace the execution of the balanced-braces algorithm and show the contents of the stack at each step.

```
a. x{{yz}}}b. {x{y{{z}}}}c. {{{x}}}
```

- **a.** The stack is empty when the last close brace is encountered. When the loop ends, balancedSoFar is false.
- b. When the loop ends, the stack contains one open brace and balancedSoFar is true.
- c. When the loop ends, the stack is empty and balancedSoFar is true.

Question 4 Trace the execution of the language-recognition algorithm described in the previous section for each of the following strings, and show the contents of the stack at each step.

```
a. a$a
b. ab$ab
c. ab$a
d. ab$ba
```

(Stack contents are listed from bottom to top.)

```
a.
aStack: a
inLanguage: true
stackTop: a
aStack:
while loop exits because we are at the end of the string.
inLanguage is true and aStack is empty, so a$a is in the language.
aStack: a
aStack: a b
inLanguage: true
stackTop: b
aStack: a
ch: $
ch: a
stackTop != ch, so inLanguage is set to false.
while loop exits because inLanguage is false.
inLanguage is false, so ab$ab is not in the language.
aStack: a
aStack: a b
inLanguage: true
stackTop: b
aStack: a
ch: $
ch: a
stackTop != ch, so inLanguage is set to false.
while loop exits because inLanguage is false.
inLanguage is false, so ab$a is not in the language.
d.
aStack: a
aStack: a b
inLanguage: true
stackTop: b
aStack: a
ch: $
ch: b
stackTop == ch
stackTop: a
aStack:
ch: a
stackTop == ch
while loop exits because we are at the end of the string.
inLanguage is true and aStack is empty, so ab$ba is in the language.
```

Question 5 Evaluate the postfix expression $a \ b - c +$. Assume the following values for the identifiers: a = 7, b = 3, and c = -2. Show the status of the stack after each step.

```
(Stack contents are listed from bottom to top.)
Let aStack be the stack.
ch: a
aStack: 7
ch: b
aStack: 7 3
ch: -
operand2: 3
aStack: 7
operand1:7
aStack:
result: 7 - 3 = 4
aStack: 4
ch: c
aStack: 4 −2
ch: +
operand2: -2
aStack: 4
operand1: 4
aStack:
result: 4 + (-2) = 2
aStack: 2
The value of the expression is 2.
```

Question 6 Convert the infix expression a / b * c to postfix form. Be sure to account for left-to-right association. Show the status of the stack after each step.

```
ch: a
postfix: a
ch: /
aStack: /
ch: b
postfix: a b
ch: *
postfix: a b /
aStack:
aStack: *
ch: c
postfix: a b / c
postfix: a b / c *
aStack:
```

Question 7 Explain the significance of the precedence tests in the infix-to-postfix conversion algorithm. Why is $a \ge \text{test}$ used rather than a > test?

The precedence tests control association. The \geq test enables left-to-right association when operators have the same precedence.

Question 8 Trace the method is Path with the map in Figure 6-10 for the following requests. Show the state of the stack after each step.

```
a. Fly from A to B.
b. Fly from A to D.
c. Fly from C to G.
a. (Stack contents are listed from bottom to top.)
Push origin A onto stack and mark A as visited.
aStack: A
                                         topCity: A
aStack is not empty and topCity is not the destination, so the while loop continues.
                                         Push B onto stack and mark B as visited.
nextCity: B
aStack: AB
                                         topCity: B
aStack is not empty and topCity is the destination, so the while loop exits.
aStack is not empty, so isPath returns true.
Push origin A onto stack and mark A as visited.
aStack: A
                                         topCity: A
aStack is not empty and topCity is not the destination, so the while loop continues.
nextCity: B
                                         Push B onto stack and mark B as visited.
aStack: AB
                                         topCity: B
aStack is not empty and topCity is not the destination, so the while loop continues.
nextCity: D
                                         Push D onto stack and mark D as visited.
aStack: ABD
                                         topCity: D
aStack is not empty and topCity is the destination, so the while loop exits.
aStack is not empty, so isPath returns true.
Push origin C onto stack and mark C as visited.
aStack: C
                                         topCity: C
aStack is not empty and topCity is not the destination, so the while loop continues.
                                         Push D onto stack and mark D as visited.
nextCity: D
aStack: CD
                                         topCity: D
aStack is not empty and topCity is not the destination, so the while loop continues.
                                         Push E onto stack and mark E as visited.
nextCity: E
aStack: CDE
                                         topCity: E
aStack is not empty and topCity is not the destination, so the while loop continues.
nextCity: I
                                         Push I onto stack and mark I as visited.
aStack: CDEI
                                         topCity: I
aStack is not empty and topCity is not the destination, so the while loop exits.
```

nextCity: NO_CITY

Backtrack by popping the stack.

aStack: C D E topCity: E

aStack is not empty and topCity is not the destination, so the while loop continues.

nextCity: NO_CITY

Backtrack by popping the stack.

aStack: C D topCity: D

aStack is not empty and topCity is not the destination, so the while loop continues. nextCity: F

Push F onto stack and mark F as visited.

aStack: C D F topCity: F

aStack is not empty and topCity is not the destination, so the while loop continues. nextCity: G

Push G onto stack and mark G as visited.

aStack: CDFG topCity: G

aStack is not empty and topCity is the destination, so the while loop exits.

aStack is not empty, so isPath returns true.

Question 1 In Chapter 6, the algorithms that appear in Section 6.2 involve strings. Under what conditions would you choose an array-based implementation for the stack in these algorithms?

You would use an array-based implementation if you know the maximum string length in advance and you know that the average string length is not much shorter than the maximum length.

Question 2 Describe the changes to the previous stack implementation that are necessary to replace the fixed-size array with a resizable array.

In the header file for ArrayStack, change the declaration of items and declare a new data member maxItems:

Also, change the name of MAX_STACK to DEFAULT_CAPACITY to reflect its change in meaning. In the implementation file, add an initializer to the definition of the constructor that initializes maxItems to DEFAULT_CAPACITY. Thus, the constructor appears as follows:

```
template<class ItemType>
ArrayStack<ItemType>::ArrayStack() : top(-1), maxItems(DEFAULT_CAPACITY)
{
    // end default constructor
```

Then change the definition of the push method so that when the array—and hence the stack—becomes full, push doubles the capacity of the array instead of failing to add the item and returning false. Since the stack is never full, the following version of the push method always returns true:

```
template < class ItemType>
bool ArrayBag < ItemType > :: add(const ItemType& newEntry)
{
   bool hasRoomToAdd = (itemCount < maxItems);
   if (!hasRoomToAdd)
   {
      ItemType* oldArray = items;
      items = new ItemType[2 * maxItems];
      for (int index = 0; index < maxItems; index++)
          items[index] = oldArray[index];
      delete [ ] oldArray;
      maxItems = 2 * maxItems;
   } // end if
   // We can always add the item
   items[itemCount] = newEntry;</pre>
```

```
itemCount++;
return true;
} // end push
```

Question 3 In Chapter 6, the algorithms that appear in Section 6.2 involve strings. Under what conditions would you choose a link-based implementation?

You would use a link-based implementation if you could not predict the maximum string length in advance or if the maximum string length is much larger than the average string length. For example, if the maximum string length is 300 but the average string length is 30, a link-based implementation would use less storage on average than an array-based implementation.

Question 4 Define the exception class MemoryAllocationException and then revise the definition of the method push in the class LinkedStack so that it throws this exception if it cannot allocate a new node.

```
#include <stdexcept>
#include <string>
using namespace std:
class MemoryAllocationException: public exception
public:
  MemoryAllocationException(const string& message = "") :
                exception("The operation push cannot allocate memory: " +
                          message.c_str())
  } // end constructor
}; // end MemoryAllocationException
template<class ItemType>
bool LinkedStack<ItemType>::push(const ItemType& newItem)
                            throw(MemoryAllocationException )
{
  try
   {
      Node<ItemType>* newTopNode = new Node<ItemType>(newItem, topPtr);
      topPtr = newTopNode;
   }
  catch (bad_alloc e)
      throw MemoryAllocationException("MemoryAllocationException : " +
                                      "push() cannot allocate memory.");
   } // end try/catch
   return true:
} // end push
```

Question 1 The specifications of the ADT list do not mention the case in which two or more items have the same value. Are these specifications sufficient to cover this case, or must they be revised?

Duplicate values in an ADT list are permissible and do not affect its specifications, because its operations are by position.

Question 2 Write specifications for a list whose operations insert, remove, getEntry, and setEntry always act at the end of the list.

Specify is Empty and getLength as you would for the ADT list given in this chapter.

+insert(newEntry: ItemType): boolean
Task: Inserts an entry at the end of this list.

Input: newEntry is the new entry.

Output: True if the insertion is successful; otherwise false.

+remove(): boolean

Task: Removes the entry at the end of a list.

Output: True if the removal is successful; otherwise false.

+getEntry(): ItemType

Task: Retrieves the item at the end of a list.

Output: The desired entry.

+setEntry(newEntry: ItemType): void

Task: Replaces the entry at the end of a list with the given entry.

Input: newEntry is the replacement entry.

Output: None.

Question 3 Write a pseudocode function swap(aList, i, j) that interchanges the items currently in positions i and j of a list. Define the function in terms of the ADT list operations, so that it is independent of any particular implementation of the list. Assume that the list, in fact, has items at positions i and j. What impact does this assumption have on your solution?

```
// Swaps the ith and jth items in the list aList.
swap(aList: List, i: integer, j: integer): void
  // Copy the ith and jth items.
  ithItem = aList.getEntry(i)
  jthItem = aList.retrieve(j)
  // Replace the ith item with the jth item.
  aList.remove(i)
  aList.insert(i, jthItem)
  // Replace the jth item with the ith item.
  aList.remove(j)
  aList.insert(j, ithItem)
```

Notice that the order of operations is important because when you remove an entry, the remaining entries are renumbered. If you did not assume that the entries at positions i and j existed, you would have to check that each operation was successful.

Question 4 What grocery list results from the following sequence of ADT list operations?

```
aList = a new empty list
aList.insert(1, "butter")
aList.insert(1, "eggs")
aList.insert(1, "milk")
milk
eggs
butter
```

Question 5 Suppose that myList is a list that contains the five objects a b c d e.

- a. What does myList contain after executing myList.insert(5, w)?
- b. Starting with the original five entries, what does myList contain after executing myList.insert(6, w)?
- **c.** Which of the operations in parts a and b of this question require entries in the array to shift?
- **a.** a b c d w e **b.** a b c d e w
- **c.** The insertion in part *a*.

Question 1 Given a nonempty list that is an instance of ArrayList, at what position does an insertion of a new entry require the fewest operations? Explain.

For a list of n entries, an insertion at position n + 1 does not require any other entry to move. Therefore, as long as the array items can accommodate an additional entry, an insertion at position n + 1 requires the fewest operations.

Question 2 Describe an implementation of the method insert for ArrayList that places the entry in position 1 in the last element of the array, the entry in position 2 in the next-to-last element, and so on.

If the array items has maxItems elements, items [maxItems - 1] contains the entry at position 1, items [maxItems - 2] contains the entry at position 2, and items [maxItems - n] contains the entry at position n. Suppose that this entry at position n is the last one in the list. That is, the list contains n items. To insert a new entry at position k, where k < n, you create room for the new entry in the array items by shifting the entries at lower-numbered indices (higher-numbered positions) toward the beginning of the array. That is, prior to adding a new entry at position k, you copy the entry in items[i] to items[i - 1] for values of i ranging from maxItems - n up to maxItems - k.

Question 3 How does the original version of insert given previously compare with the one described in Question 2 with respect to the number of operations required?

Except for more involved index computations, there is no difference in the effort required for these two approaches.

Question 4 Although the method remove cannot remove an entry from an empty list, it does not explicitly check for one. How does this method avoid an attempted deletion from an empty list?

The boolean expression (position >= 1) && (position <= itemCount) will be false when itemCount is zero, regardless of the value of position. Therefore, the boolean variable ableToRemove is false, and so the method does not do anything more than return false.

Question 5 Given a nonempty list that is an instance of LinkedList, at what position does an insertion of a new entry require the fewest operations? Explain.

An insertion at position 1 of the list is implemented as an insertion at the beginning of the linked chain. This insertion can be accomplished without a search of the chain for the desired position. Therefore, it requires the fewest operations.

Question 6 In the previous method insert, the second if statement tests the value of newPosition. Should the boolean expression it tests be isEmpty() || (newPosition == 1)? Explain.

Although you could test for an empty list, such a test is not necessary. When a list is empty, itemCount is zero. The only acceptable position for an insertion is 1, because the boolean expression (newPosition >= 1) && (newPosition <= itemCount + 1) will be true. Therefore, the body of the first if statement will execute, and the insertion into the empty list will occur correctly.

Question 7 How does the insert method enforce the precondition of getNodeAt?

getNodeAt's precondition is (position >= 1) && (position <= itemCount). Before insert invokes getNodeAt, the boolean expression (newPosition >= 1) && (newPosition <= itemCount + 1) must be true. The call getNodeAt(newPosition - 1) occurs only if newPosition > 1 and sets position to newPosition - 1. Therefore, position >= 1 is true. Further, since newPosition <= itemCount + 1, newPosition - 1 <= itemCount, which implies that position <= itemCount.

Question 8 The link-based implementation of the method clear contains the following loop:

```
while (!isEmpty())
  remove(1);
```

a. Can you correctly replace the loop with

```
for (int position = getLength(); position >= 1; position--)
  remove(1);
```

- **b.** Does your answer to part *a* differ if you replace remove(1) with remove(position)?
- \mathbf{c} . Do your answers to parts a and b differ if you replace the for statement with

```
for (int position = 1; position <= getLength(); position++)</pre>
```

- a. Yes.
- **b.** This replacement is still correct. We remove the last entry from the list without renumbering the remaining entries.
- c. Whether this for statement is correct depends on how the compiler makes the comparison. If position is compared to the original value of getLength(), the loop will cycle the correct number of times. Repeatedly executing remove(1) will work. However, repeatedly executing remove(position) will not work because entries are renumbered after each iteration. For example, after the first entry is removed, the second entry becomes the first entry, but position is set to 2. This new first entry is never removed. If position is compared to the current value of getLength() at each iteration, the loop will exit before the entire list is emptied.

Question 9 Revise the destructor in the class LinkedList so that it directly deletes each node of the underlying linked chain without calling either clear or remove.

```
template < class ItemType>
LinkedList < ItemType>::~LinkedList()
{
    while (headPtr != nullptr)
    {
        Node < ItemType>* nodeToDeletePtr = headPtr;
        headPtr = headPtr->getNext();

        // Return node to the system
        nodeToDeletePtr->setNext(nullptr);
        delete nodeToDeletePtr;
    } // end while
    // headPtr is nullptr
    nodeToDeletePtr = nullptr;
    itemCount = 0;
} // end destructor
```

Question 10 Using recursion, revise the destructor in the class LinkedList so that it deletes each node of the underlying linked chain.

```
template<class ItemType>
LinkedList<ItemType>::~LinkedList()
{
   deallocate(headPtr);
  headPtr = nullptr;
   itemCount = 0;
  // end destructor
// Private method: Deallocates all nodes assigned to the bag
template<class ItemType>
void LinkedList<ItemType>::deallocate(Node<ItemType>* nextNodePtr)
{
   if (nextNodePtr != nullptr)
      Node<ItemType>* nodeToDeletePtr = nextNodePtr;
      nextNodePtr = nextNodePtr->getNext();
      delete nodeToDeletePtr;
      deallocate(nextNodePtr);
  } // end if
} // end deallocate
```

Question 1 How many comparisons of array items do the following loops contain?

```
for (j = 1; j <= n - 1; j++)
{
    i = j + 1;
    do
    {
        if (theArray[i] < theArray[j])
            swap(theArray[i], theArray[j]);
        i++;
    } while (i <= n);
}</pre>
```

```
(n-1) + (n-2) + \dots + 1 = n \times (n-1) / 2
```

Question 2 Repeat Question 1, replacing the statement i = j + 1 with i = j.

```
n + (n-1) + \dots + 2 = n \times (n+1) / 2 - 1
```

Question 3 What order is an algorithm that has as a growth-rate function

```
a. 8 \times n^3 - 9 \times n
```

b.
$$7 \times \log_2 n + 20$$

c. $7 \times \log_2 n + n$

a. $O(n^3)$; **b.** $O(\log n)$; **c.** O(n)

Question 4 Consider a sequential search of *n* data items.

- **a.** If the data items are sorted into ascending order, how can you determine that your desired item is not in the data collection without always making *n* comparisons?
- **b.** What is the order of the sequential search algorithm when the desired item is not in the data collection? Do this for both sorted and unsorted data, and consider the best, average, and worst cases.
- **c.** Show that if the sequential search algorithm finds the desired item in the data collection, the algorithm's order does not depend upon whether or not the data items are sorted.
- **a.** You can stop searching as soon as the target is less than an entry, because you will have passed the point where the target would have occurred if it was in the data collection.
- **b.** Sorted data using the scheme just described in the answer to part a: Best case: O(1); average case: O(n); worst case: O(n).

Unsorted data: O(n) in all cases.

Question 1 Trace the selection sort as it sorts the following array into ascending order:

20 80 40 25 60 30

At each pass, the selected element is bold; the sorted elements are blue.

20	80	40	25	60	30
20	30	40	25	60	80
20	30	40	25	60	80
20	30	25	40	60	80
20	25	30	40	60	80
20	25	30	40	60	80
20	25	30	40	60	80

Question 2 Repeat the previous question, but instead sort the array into descending order.

Find the smallest instead of the largest entry at each pass.

20	80	40	25	60	30
30	80	40	25	60	20
30	80	40	60	25	20
60	80	40	30	25	20
60	80	40	30	25	20
80	60	40	30	25	20
80	60	40	30	25	20

Question 3 Trace the bubble sort as it sorts the following array into ascending order:

25 30 20 80 40 60.

Pass 1:							Pass 2:						
	25	30	20	80	40	60		25	20	30	40	60	80
	25	30	20	80	40	60		20	25	30	40	60	80
	25	20	30	80	40	60		20	25	30	40	60	80
	25	20	30	80	40	60		20	25	30	40	60	80
	25	20	30	40	80	60		20	25	30	40	60	80
	25	20	30	40	60	80							

Pass 3: There are no exchanges, so the algorithm will terminate.

Question 4 Repeat the previous question, but instead sort the array into descending order.

We can move either the smallest entries to the end of the array or the largest entries to the beginning of the array. The following trace uses the former strategy:

Pass 1:							Pass 2:						
	25	30	20	80	40	60		30	25	80	40	60	20
	30	25	20	80	40	60		30	25	80	40	60	20
	30	25	20	80	40	60		30	80	25	40	60	20
	30	25	80	20	40	60		30	80	40	25	60	20
	30	25	80	40	20	60		30	80	40	60	25	20
	30	25	80	40	60	20							
Pass 3:							Pass 4:						
	30	80	40	60	25	20		80	40	60	30	25	20
	80	30	40	60	25	20		80	40	60	30	25	20
	80	40	30	60	25	20		80	60	40	30	25	20
	80	40	60	30	25	20							

Pass 5: There are no exchanges, so the algorithm will terminate.

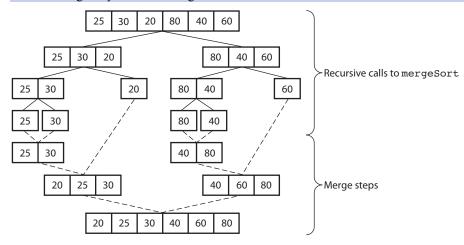
Question 5 Trace the insertion sort as it sorts the array in Checkpoint Question 3 into ascending order.

```
25
     30
          20
                80
                     40
                          60
25
     30
          20
                80
                     40
                          60
25
     20
          30
                80
                     40
                          60
25
     20
          30
                80
                     40
                          60
25
     20
          30
                40
                     80
                          60
25
     20
          30
                40
                     60
                          80
```

Question 6 Repeat the previous question, but instead sort the array into descending order.

```
25
     30
           20
                80
                      40
                           60
30
     25
           20
                80
                      40
                           60
30
     25
           20
                80
                      40
                           60
80
     30
           25
                20
                      40
                           60
80
     40
           30
                25
                      20
                           60
80
     60
           40
                30
                      25
                           20
```

Question 7 By drawing a diagram like the one shown in Figure 11-6, trace the merge sort as it sorts the following array into ascending order: 25 30 20 80 40 60.



Question 8 Show that the merge sort algorithm satisfies the four criteria of recursion that Chapter 2 describes.

- 1. Merge sort sorts an array by using a merge sort to sort each half of the array.
- 2. Sorting half of an array is a smaller problem than sorting the entire array.
- 3. An array of one element is the base case.
- 4. By halving an array and repeatedly halving the halves, you must reach array segments of one element each—that is, the base case.

Question 9 Trace the quick sort's partitioning algorithm as it partitions the following array:

38 16 40 39 12 27

```
38
     16
           40
                 39
                      12
                                  Identify first, middle, and last entries
27
                39
                                  Sort first, middle, and last entries; choose 38 as pivot
     16
           38
                      12
                            40
27
     16
           12
                39
                      38
                            40
                                  Position pivot
27
     16
           12
                 39
                      38
                            40
                                  indexFromLeft = 3, indexFromRight = 2
27
     16
           12
                 38
                                  Interchange the pivot and theArray[3]
```

Question 10 Suppose that you sort a large array of integers by using a merge sort. Next you use a binary search to determine whether a given integer occurs in the array. Finally, you display all of the integers in the sorted array.

- **a.** Which algorithm is faster, in general: the merge sort or the binary search? Explain in terms of Big O notation.
- **b.** Which algorithm is faster, in general: the binary search or displaying the integers? Explain in terms of Big O notation.
- a. A binary search is $O(\log n)$, so it is faster than a merge sort, which is $O(n \log n)$.
- b. A binary search is $O(\log n)$, so it is faster than displaying the array, which is O(n).

Question 11 Trace the radix sort as it sorts the following array into ascending order:

3812 1600 4012 3934 1234 2724 3333 5432

```
3812 1600 4012 3934 1234 2724 3333 5432
                                                       The original array
(1600) (3812, 4012, 5432) (3333) (3934, 1234, 2724)
                                                       Group by rightmost digit
1600 3812 4012 5432 3333 3934 1234 2724
                                                       Combine
(1600) (3812, 4012) (2724) (5432, 3333, 3934, 1234)
                                                       Group by third digit
1600 3812 4012 2724 5432 3333 3934 1234
                                                       Combine
(4012) (1234) (3333) (5432) (1600) (2724) (3812) (3934)
                                                       Group by second digit
4012 1234 3333 5432 1600 2724 3812 3934
                                                       Combine
(1234, 1600) (2724) (3333, 3812, 3934) (4012) (5432)
                                                       Group by first digit
1234 1600 2724 3333 3812 3934 4012 5432
                                                       Combine; the array is now sorted
```

Question 1 The specifications of the ADT sorted list do not mention the case in which two or more items have the same value. Are these specifications sufficient to cover this case, or must they be revised?

Duplicate values in an ADT sorted list are permissible and do not affect its specifications. Both removeSorted and getPosition deal with the first or only occurrences of the specified value; remove and getEntry are by position. Although insertSorted does not specify where the insertion will occur, duplicate values will be at adjacent positions.

Question 2 Write specifications for the operation insertSorted when the sorted list must not contain duplicate entries.

Task: Inserts an entry into this sorted list in its proper order so that the list remains sorted. Input: newEntry is the new entry and is not in the sorted list already.

Output: Throws an exception (PrecondViolatedExcep) if newEntry already is in the sorted list.

Question 3 Suppose that wordListPtr points to an unsorted list of words. Using the operations of the ADT list and the ADT sorted list, create a sorted list of these words.

Question 4 Assuming that the sorted list you created in the previous question is not empty, write C++ statements that

- a. Display the last entry in the sorted list.
- **b.** Add the sorted list's first entry to the sorted list again.
- a.cout << sortedWordListPtr->getEntry(numberOfWords) << endl;</pre>
- b. sortedWordListPtr->insertSorted(sortedWordListPtr->getEntry(1));

Question 5 In the while statement of the method getNodeBefore, how important is the order of the two boolean expressions that the operator && joins? Explain.

The order of the boolean expressions is important. If the given entry—anEntry—is larger than any of the current entries in the sorted list, curPtr will become nullptr after it is compared to the list's last entry. The while statement will then evaluate the expression

```
(curPtr != nullptr) && (anEntry > curPtr->getItem())
```

Because curPtr is nullptr, curPtr != nullptr will be false and curPtr->getItem() will not execute due to short-circuit evaluation. If the boolean expression had been

```
(anEntry > curPtr->getItem()) && (curPtr != nullptr)
```

curPtr->getItem() would execute and since curPtr is nullptr, an exception would occur.

Question 6 What does getNodeBefore return if the sorted list is empty? How can you use this fact to simplify the implementation of the method insertSorted given previously?

If the sorted list is empty, headPtr is nullptr. The while loop exits immediately, and the method returns nullptr—the current value of prevPtr. Because of this fact, you can replace the if statement in the method insertSorted with

```
if (prevPtr == nullptr)
```

Question 7 Suppose that you use the previous method insertSorted to add an entry to a sorted list. If the entry is already in the list, where in the list will the method insert it? Before the first occurrence of the entry, after the last occurrence of the entry, or somewhere else?

Before the first occurrence of the entry.

Question 8 What would be the answer to the previous question if you changed > to >= in the while statement of the method getNodeBefore?

After the last occurrence of the entry.

Question 9 Define the method getPosition for the class SortedListHasA.

Question 10 Repeat Checkpoint Question 7 using the method insertSorted of the class SortedListHasA.

Before the first occurrence of the entry, assuming that getPosition is defined as in Checkpoint Question 9.

Question 11 Can a client of SortedListHasA invoke the method insert of the ADT list? Explain.

No. SortedListHasA is derived from SortedListInterface, which does not declare insert. Moreover, the underlying list in SortedListHasA is private. A client of SortedListHasA has no access to this list.

Question 12 Define the method removeSorted for the class SortedListHasA.

```
template < class ItemType>
bool SortedListHasA < ItemType>::removeSorted(const ItemType& anEntry)
{
   bool ableToDelete = false;
   if (!isEmpty())
   {
      int position = getPosition(anEntry);
      ableToDelete = position > 0;
      if (ableToDelete)
      {
        ableToDelete = listPtr->remove(position);
      } // end if
   } // end if
   return ableToDelete;
} // end removeSorted
```

Question 13 Suppose that instead of using LinkedList in the implementation of SortedListHasA, you used ArrayList. What Big O would describe the performance of the method getPosition?

The method getEntry is always an O(1) operation. The loop in getPosition is therefore O(n) in the worst case, and so getPosition is O(n) when the list has an array-based implementation.

Question 14 Give an advantage and a disadvantage of using containment in the implementation of the class SortedListHasA.

Advantage: It is easier to write because the underlying list does most of the work and has been debugged.

Disadvantage: It is less efficient than an implementation that does not call and is not restricted to the methods of the ADT list.

Question 15 What would have happened if you preceded the call to insert in the method insertSorted by this->instead of LinkedList<ItemType>::? Explain.

The call this->insert(newPosition, newEntry) would call the overriding version of insert, which SortedListIsA defines, instead of LinkedList's method insert.

Question 1 If you add the letters A, B, C, and D in sequence to a queue of characters and then remove them, in what order will they leave the queue?

A, B, C, D.

Question 2 What do the initially empty queues queue1 and queue2 "look like" after the following sequence of operations? Compare these results with Checkpoint Question 2 in Chapter 6.

```
queue1.enqueue(1)
                                  queue1: 1
                                                 (Queue entries are listed front to back)
                                             2
queue1.enqueue(2)
                                  queue1: 1
queue2.enqueue(3)
                                  queue2: 3
queue2.enqueue(4)
                                  queue2: 3
queue1.dequeue()
                                  queue1: 2
queueFront = queue2.peekFront() queueFront = 3
queue1.enqueue(queueFront)
                                  queue1: 2 3
                                  queue1: 2
queue1.enqueue(5)
                                             3
queue2.dequeue()
                                  queue2: 4
                                             6
queue2.enqueue(6)
                                  queue2: 4
```

Question 3 Trace the palindrome-recognition algorithm described in this section for each of the following strings of characters:

a. abcda

b. radar

a. When the for loop ends, the stack and queue are as follows:

```
Stack: a b c d a \leftarrow top
Queue: a b c d a \leftarrow back
```

The a at the top of the stack matches the a at the front of the queue. After removing the a from both containers, the d at the top of the stack does not match the b at the front of the queue, so the string is not a palindrome.

b. When the for loop ends, the stack and queue are as follows:

```
Stack: r a d a r \leftarrow top
Queue: r a d a r \leftarrow back
```

The letters that you remove from the stack and the queue are the same, so the string is a palindrome.

Question 4 Improve the palindrome-recognition algorithm described in this section by adding the first length / 2 characters to the queue and then pushing the remaining characters onto the stack.

```
isPalindrome(someString: string): boolean
  // Create an empty queue and an empty stack
  aQueue = a new empty queue
  aStack = a new empty stack
  // Add the first half of the string to the queue
  length = length of someString
  halfLength = length / 2
  for (i = 1 through halfLength)
     nextChar = i^{th} character of someString
     aQueue.enqueue(nextChar)
  }
  // Add the rest of the string to the stack
  for (i = halfLength + 1 through length)
     nextChar = i^{th} character of someString
     aStack.push(nextChar)
  }
  // Compare the queue characters with the stack characters
  charactersAreEqual = true
  while (aQueue is not empty and charactersAreEqual)
     queueFront = aQueue.peekFront()
     stackTop = aStack.peek()
     if (queueFront equals stackTop)
         aQueue.dequeue()
        aStack.pop()
     }
     else
         charactersAreEqual = false
  return charactersAreEqual
```

Question 5 In the bank simulation problem, why is it impractical to read the entire input file and create a list of all the arrival and departure events before the simulation begins?

You cannot generate a departure event for a given arrival event independently of other events. So to read the file of arrival events and generate departure events, you would need to perform the same computations that the simulation performs.

Question 6 Complete the hand trace of the bank-line simulation that Figure 13-8 began. Show the state of the queue and the event list at each step.

The only missing portion is to indicate that at time 35 the last customer leaves the bank, the bank queue is empty, and the event list is empty.

Question 7 For each of the following situations, which of these ADTs (1 through 6) would be most appropriate? (1) a queue; (2) a stack; (3) a list; (4) a sorted list; (5) a priority queue; (6) none of these

- a. The customers at a deli counter who take numbers to mark their turn 1
- **b.** An alphabetic list of names
- **c.** Integers that need to be sorted 3
- **d.** The boxes in a box trace of a recursive function
- e. A grocery list ordered by the occurrence of the items in the store
- **f.** The items on a cash register tape 1 or 3
- g. A word processor that allows you to correct typing errors by using the Backspace key 2
- **h.** A program that uses backtracking
- i. A list of ideas in chronological order 1, 3, or 5
- j. Airplanes that stack above a busy airport, waiting to land 1 or 5
- **k.** People who are put on hold when they call for customer service 1
- **l.** An employer who fires the most recently hired person

Question 1 Why is a tail pointer desirable when you use a chain of linked nodes to implement a queue?

Because additions to a queue occur at its end, you would want to add nodes to the end of the linked chain. The tail pointer enables you to make such additions efficiently. With only a head pointer, you would have to traverse the entire chain each time you wanted to add to the end of the chain.

Question 2 If you use a circular chain that has only a tail pointer, as Figure 14-3 illustrates, how do you access the data in the first node?

First, you get a pointer to the first node by executing the following statement:

```
Node<ItemType>* frontPtr = backPtr->getNext();
```

Then the data in the first node is frontPtr->getItem().

Question 3 If the ADT queue had a method clear that removed all entries from a queue, what would its definition be in the previous link-based implementation?

A method clear could repeatedly call dequeue until the queue is empty. One such definition follows:

```
template<class ItemType>
void LinkedQueue<ItemType>::clear()
{
   while (!isEmpty())
        dequeue();
} // end clear
```

However, since dequeue is a boolean-valued method, you could replace the previous while loop with the following one:

```
while (dequeue())
{}
```

Question 4 Suppose that we change the naive array-based implementation of a queue pictured in Figure 14-7 so that the back of the queue is in items[0]. Although repeated removals from the front would no longer cause rightward drift, what other problem would this implementation cause?

Additions to the queue, which will be at its back, will require that all entries curently in the queue shift one array location toward the array's end.

Question 5 If the ADT queue had a method clear that removed all entries from a queue, what would its definition be in the previous array-based implementation?

```
template<class ItemType>
void ArrayQueue<ItemType>::clear()
{
   front = 0;
   back = MAX_QUQUE - 1;
   count = 0;
} // end clear
```

Question 6 Define the method peek for the sorted list implementation of the ADT priority queue.

```
template<class ItemType>
ItemType SL_PriorityQueue<ItemType>::peek() const
throw(PrecondViolatedExcep)
{
   if (isEmpty())
       throw PrecondViolatedExcep("peekFront() called with empty queue.");

   // Priority queue is not empty; return highest-priority item;
   // it is at the end of the sorted list
   return slistPtr->getEntry(slistPtr->getLength());
} // end peek
```

Question 1 What kind of tree is the tree in Figure 15-1a?

A general tree.

Question 2 Repeat the previous question, but use the tree in Figure 15-3c instead.

A binary tree.

Question 3 Given the tree in Figure 15-3c, what node or nodes are

- **a.** Ancestors of *b*?
- **b.** Descendants of x?
- c. Leaves?
- $\mathbf{a} \cdot -$ and \mathbf{x} .
- b. , c, a, b.
- **c.** a, b, c.

Question 4 Given the tree in Figure 15-4, what node or nodes are

- **a.** The tree's root?
- **b.** Parents?
- **c.** Children of the parents in part b of this question?
- d. Siblings?
- a. Jane.
- b. Jane, Bob, Tom.
- c. Bob and Tom are children of Jane. Alan and Ellen are children of Bob. Nancy and Wendy are children of Tom.
- d. Bob and Tom are siblings, Alan and Ellen are siblings, Nancy and Wendy are siblings.

Question 5 What are the levels of all nodes in the trees in parts b, c, and d of Figure 15-5?

```
Figure 15-5b: Level 1: A; Level 2: B, C; Level 3: D, E; Level 4: F; Level 5: G. Figure 15-5c: Level 1: A; Level 2: B; Level 3: C; Level 4: D; Level 5: E; Level 6: F; Level 7: G. Figure 15-5d: Level 1: A; Level 2: B; Level 3: C; Level 4: D; Level 5: E; Level 6: F; Level 7: G.
```

Question 6 What is the height of the tree in Figure 15-4?

3.

Question 7 Consider the binary trees in Figure 15-8. a. Which are complete? **b.** Which are full? c. Which are balanced? d. Which have minimum height? e. Which have maximum height? **a.** b, c, d, e. **b.** e. **c.** b, c, d, e. **d.** b, c, d, e. **e.** a. **Question 8** What are the preorder, inorder, and postorder traversals of the binary trees in parts a, b, and *c* of Figure 15-5? Figure 15-5a: Preorder: A, B, D, E, C, F, G; Inorder: D, B, E, A, F, C, G; Postorder: D, E, B, F, G, C, A. Figure 15-5b: Preorder: A, B, D, F, G, E, C; Inorder: G, F, D, B, E, A, C; Postorder: G, F, D, E, B, C, A. Figure 15-5c: Preorder: A, B, C, D, E, F, G; Inorder: A, C, E, G, F, D, B; Postorder: G, F, E, D, C, B, A. **Question 9** Show that each tree in Figures 15-13 and 15-14 is a binary search tree. Jane is larger than all of the data in its left subtree and Figure 15-13: smaller than all of the data in its right subtree. Bob is larger than Allan in its left subtree and smaller than Elisa in its right subtree. Tom is larger than Nancy in its left subtree and smaller than Wendy in its right subtree. Jane is larger than all of the data in its left subtree and Figure 15-14a: smaller than all of the data in its right subtree. Bob is larger than Allan in its left subtree and smaller than Elisa in its right subtree. Nancy is smaller than all of the data in its right subtree. Tom is smaller than Wendy in its right subtree.

Figure 15-14b:	Alan is smaller than all of the data in its right subtree.		
1.50.0	Bob is smaller than all of the data in its right subtree.		
	Elisa is smaller than all of the data in its right subtree.		
	Jane is smaller than all of the data in its right subtree.		
	Nancy is smaller than all of the data in its right subtree.		
	Tom is smaller than Wendy in its right subtree.		
Figure 15-14c:	Tom is larger than all of the data in its left subtree and smaller than Wendy in its right subtree.		
	Jane is larger than all of the data in its left subtree and smaller than Nancy in its right subtree.		
	Bob is larger than Allan in its left subtree and smaller than Elisa in its right subtree.		

Question 10 Show that the inorder traversals of each binary search tree in Figures 15-13 and 15-14 are the same.

Figure 15-13: Beginning at Jane, the root, the traversal takes the following steps: inorder(Jane), inorder(Bob), inorder(Alan), inorder(<empty>), return, **Visit Alan**, inorder(<empty>), return, **Visit Bob**, inorder(Elisa), inorder(<empty>), return, **Visit Elisa**, inorder(<empty>), return, return, **Visit Jane**, inorder(Tom), inorder(Nancy), inorder(<empty>), return, **Visit Nancy**, inorder(<empty>), return, return, **Visit Tom**, inorder(Wendy), inorder(<empty>), return, **Visit Wendy**, inorder(<empty>), return, return, return, return, return.

Figure 15-14a: Beginning at Jane, the root, the traversal takes the following steps: inorder(Jane), inorder(Bob), inorder(Alan), inorder(<empty>), return, **Visit Alan**, inorder(<empty>), return, **Visit Bob**, inorder(Elisa), inorder(<empty>), return, **Visit Elisa**, inorder(<empty>), return, return, return, **Visit Jane**, inorder(Nancy), inorder(<empty>), return, **Visit Nancy**, inorder(Tom), inorder(<empty>), return, **Visit Tom**, inorder(Wendy), inorder(<empty>), return, **Visit Wendy**, inorder(<empty>), return, return, return, return.

The inorder traversals of Figures 15-14b and 15-14c are like the previous ones.

Question 11 What are the preorder and postorder traversals of each binary search tree in Figures 15-13 and 15-14? Are the preorder traversals the same? Are the postorder traversals the same?

Figure 15-13: Preorder: Jane, Bob, Alan, Elisa, Tom, Nancy, Wendy; Postorder: Alan, Elisa, Bob, Nancy, Wendy, Tom, Jane.

Figure 15-14a: Preorder: Jane, Bob, Alan, Elisa, Nancy, Tom, Wendy; Postorder: Alan, Elisa, Bob, Wendy, Tom, Nancy, Jane.

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Figure 15-14b: Preorder: Alan, Bob, Elisa, Jane, Nancy, Tom, Wendy;

Postorder: Wendy, Tom, Nancy, Jane, Elisa, Bob, Alan.

Figure 15-14c: Preorder: Tom, Jane, Bob, Alan, Elisa, Nancy, Wendy;

Postorder: Alan, Elisa, Bob, Nancy, Jane, Wendy, Tom.

No two traversals are the same.

Question 12 Using the tree in Figure 15-14c, trace the algorithm that searches a binary search tree for

a. Elisa

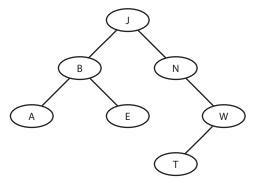
b. Kyle

In each case, list the nodes in the order in which the search visits them.

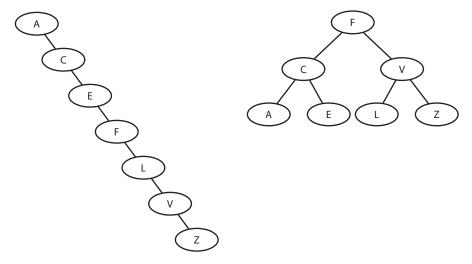
a. Tom, Jane, Bob, Elisa.

b. Tom, Jane, Nancy.

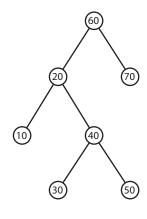
Question 13 Beginning with an empty binary search tree, what binary search tree is formed when you insert the following letters in the order given? J, N, B, A, W, E, T



Question 14 Arrange nodes that contain the letters A, C, E, F, L, V, and Z into two binary search trees: one that has maximum height and one that has minimum height.



Question 1 Represent the binary tree in Figure 15-18 of Chapter 15 with an array.



		tree		
	item	leftChild	rightChild	root
0	60	1	2	0
1	20	3	4	free
2	70	-1	-1	7
3	10	-1	-1	
4	40	5	6	
5	30	-1	-1	
6	50	-1	-1	
7	?	-1	8	
8	?	-1	9	
•	•	•	•	Free list
•	•	•	•	
•	•	•	•	

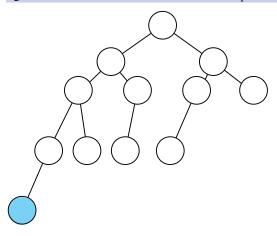
Question 2 What are the definitions of the public method getNumberOfNodes and the protected helper method getNumberOfNodesHelper?

Question 3 What is the definition of the public method setRootData?

```
template < class ItemType>
void BinaryNodeTree < ItemType>::setRootData(const ItemType& newItem)
{
   if (isEmpty())
     rootPtr = new BinaryNode < ItemType>(newItem, nullptr, nullptr);
   else
     rootPtr->setItem(newItem);
} // end setRootData
```

Question 4 What is the definition of the public method getRootData? Recall that this method has a precondition.

Question 5 Where would a new node be placed next in the binary tree shown in Figure 16-3?



Question 6 Define the protected method postorder.

```
template < class ItemType>
void BinaryNodeTree < ItemType>::
postorder(void visit(ItemType&), BinaryNode < ItemType>* treePtr) const
{
    if (treePtr != nullptr)
    {
        postorder(visit, treePtr->getLeftChildPtr());
        postorder(visit, treePtr->getRightChildPtr());
        ItemType theItem = treePtr->getItem();
        visit(theItem);
    } // end if
} // end postorder
```

Question 7 Starting with an empty binary search tree, in what order should you insert items to get the binary search tree in Figure 15-18 of Chapter 15?

60, 20, 10, 40, 30, 50, 70 is one of several possible orders. (This order results from a preorder traversal of the tree.)

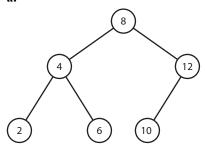
Question 8 Given the binary search tree in Figure 15-18 of Chapter 15, trace the removal algorithms when removing each of the following values from the tree. Begin with the original tree each time.

- **a.** 70
- **b.** 20
- **c.** 60
- **a.** The call to removeValue begins at the root and locates 70 in the root's right child. This child is passed to removeNode, which removes the child from the tree because it is a leaf.
- **b.** The call to removeValue begins at the root and locates 20 in the root's left child. This child is passed to removeNode, which determines that it has two children. The inorder successor of 20 is 30, and occurs in a leaf. 30 replaces 20 in the left child of the root, and the leaf that contained 30 originally is removed from the tree.
- c. The call to removeValue begins at the root and locates 60 in the root itself. The root is passed to removeNode, which determines that it has two children. The inorder successor of 60 is 70, and occurs in a leaf. 70 replaces 60 in the root, and the leaf that contained 70 originally is removed from the tree.

Question 9 Consider the pseudocode operation readTree.

- **a.** What binary search tree results when you execute **readTree** with a file of the six integers 2, 4, 6, 8, 10, 12?
- **b.** Is the resulting tree's height a minimum? Is the tree complete? Is it full?

9

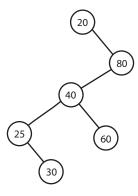


b. The tree has minimum height and is complete but not full.

 $\label{eq:Question 10} \textbf{Question 10} \text{ Trace the tree sort algorithm as it sorts the following array into ascending order:}$

20 80 40 25 60 30.

Inserting the array entries into a binary search tree produces the following tree:

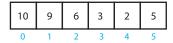


An inorder traversal of this tree results in the sorted array.

Question 1 Is the full binary tree in Figure 16-16 of Chapter 16 a heap? Why?

No, the tree is not a maxheap or a minheap. The root 30 is neither the largest nor the smallest value in the tree. Each of the root's children is neither the largest nor the smallest value in its subtree.

Question 2 What array represents the maxheap shown in Figure 17-1a?



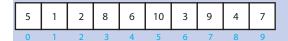
Question 3 What array represents the minheap shown in Figure 17-1b?

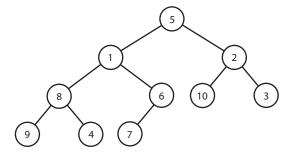


Question 4 What criterion can you use to tell whether the node in items[i] is a leaf?

To see whether the node in items[i] is a leaf, we need to test whether its children either exist or contain node values. These children are in items[2 * i + 1] and items[2 * i + 2]. Suppose that size is the array's length. The node in items[i] is a leaf if 2 * i + 1 is greater than size. If 2 * i + 1 is less than or equal to size, we must assume that sentinel values are within the unused array locations—that is, those locations after the last one used by the heap. Then if a sentinel value is in items[2 * i + 1], items[i] is a leaf.

Question 5 What complete binary tree does the following array represent?





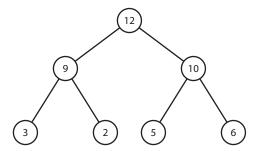
Question 6 Does the array in the previous question represent a heap?

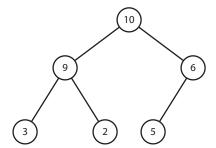
No.

Question 7 Is the full binary tree in Figure 16-16 of Chapter 16 a semiheap?

No.

Question 8 Consider the maxheap in Figure 17-1a. Draw the heap after you insert 12 and then remove 12.

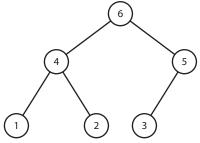




Question 9 What does the initially empty heap myHeap contain after the following sequence of pseudocode operations?

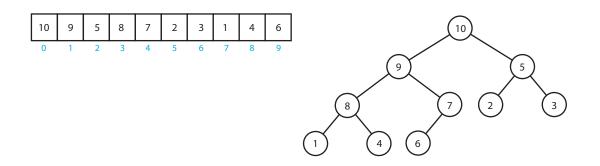
```
myHeap.add(2)
myHeap.add(3)
myHeap.add(4)
myHeap.add(1)
myHeap.add(9)
myHeap.remove()
myHeap.add(7)
myHeap.add(6)
myHeap.remove()
myHeap.add(6)
myHeap.add(5)
```

The array that represents the heap is 7 5 6 4 3 2.



Question 10 Execute the following pseudocode statements on the array shown in Checkpoint Question 5.

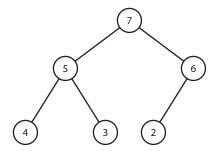
```
for (index = n - 1 down to 0)
heapRebuild(index)
```



Question 11 Consider a heap-based implementation of the ADT priority queue. What does the underlying heap contain after the following sequence of pseudocode operations, assuming that pQueue is an initially empty priority queue?

```
pQueue.add(5)
pQueue.add(9)
pQueue.add(6)
pQueue.add(7)
pQueue.add(3)
pQueue.add(4)
pQueue.remove()
pQueue.add(9)
pQueue.add(2)
pQueue.remove()
```

The array that represents the heap is 7 5 6 4 3 2.



Question 12 Trace the heap sort as it sorts the following array into ascending order:

25 30 20 80 40 60.

```
25 30 20 80 40 60 Original array 80 40 60 30 25 20 Initial rebuild to form a heap 20 40 60 30 25 80 After swapping 20 and 80 60 40 20 30 25 80 rebuild(0, anArray, 5) 25 40 20 30 60 80 After swapping 25 and 60 40 30 20 25 60 80 rebuild(0, anArray, 4) 25 30 20 40 60 80 After swapping 25 and 40 30 25 20 40 60 80 rebuild(0, anArray, 3) 20 25 30 40 60 80 After swapping 20 and 30 25 20 30 40 60 80 rebuild(0, anArray, 2) 20 25 30 40 60 80 After swapping 20 and 25 20 25 30 40 60 80 Sorted array
```

Question 1 Using the ADT dictionary operations, write pseudocode for a replace function at the client level that replaces the dictionary item whose search key is x with another item whose search key is also x.

Question 2 Explain how the while loop in the previous definition of the method add locates the insertion point for the new entry in the array items.

The loop compares the given search key with the search key of the entries in the array items. The search begins at the last entry in the array and progresses toward the beginning of the array. If the search key of the current entry is greater than the given search key, the entry is moved to the next higher location in the array. As soon as an entry is considered whose search key either matches or is less than the given search key, the new entry is inserted into the array at the array location just beyond that of the current entry. This location is available for use, because it either is vacant or its former entry was moved to the next higher location by this loop.

Question 3 Why is short-circuit evaluation important in the while loop of the previous definition of the method add?

Short-circuit evaluation ensures that the value of index is greater than zero when it is used in the expression items[index - 1]. If the value of index is zero or smaller, short-circuit evaluation prevents the execution of the second part of the boolean expression—that is, searchKey < items[index-1].getKey()—thereby avoiding an illegal index for the array items.

Question 4 We mentioned that the remove method calls the private method findEntryIndex to locate the entry to remove. Assuming that the entry is located, what does remove need to do after it gets the index of this entry?

If itemIndex is the index of the entry to remove, the remove method must shift the entries after items[itemIndex] by one position toward the beginning of the array. That is, it must execute the assignment items[i] = items[i + 1] for values of i that range from itemIndex to itemCount -2. After these shifts, remove must decrease the value of itemCount by 1.

Question 5 What is the definition of the method traverse for ArrayDictionary?

```
template < class KeyType, class ItemType>
void ArrayDictionary < KeyType, ItemType>::traverse(void visit(ItemType&))
const
{
    // The array items is sorted; simply traverse the array.
    for (int index = 0; index < itemCount; index++)
    {
        ItemType currentItem = items[index].getItem();
        visit(currentItem);
    } // end for
} // end traverse</pre>
```

Question 6 Write the pseudocode for the remove operation when linear probing is used to implement the hash table.

```
// Removes a specific entry from the dictionary, given its search key.
// Returns true if the operation was successful, or false otherwise.
remove(searchKey: KeyType): boolean
index = getHashIndex(searchKey)
Search the probe sequence that begins at hashTable[index] for searchKey
if (searchKey is found)
{
    Flag entry as removed // No need to actually remove the entry
    itemCount--
    return true
}
else
    return false
```

Question 7 What is the probe sequence that double hashing uses when

```
h_1(key) = key \mod 11, h_2(key) = 7 - (key \mod 7), and key = 19?

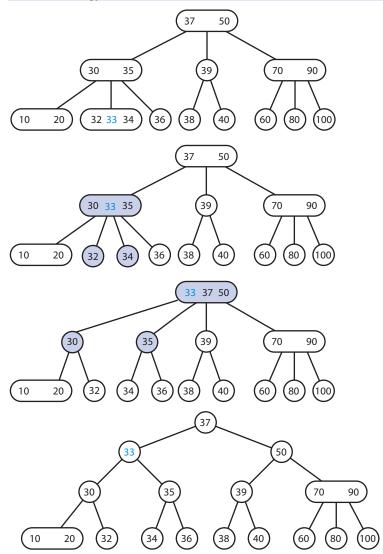
h_1(19) = 8 and h_2(19) = 2. Thus, the probe sequence is 8, 10, 1, 3, 5, 7, 9, 0, 2, 4, 6.
```

Question 8 If $h(x) = x \mod 7$ and separate chaining resolves collisions, what does the hash table look like after the following insertions occur: 8, 10, 24, 15, 32, 17? Assume that each item contains only a search key.

$$h(8) = 1$$
, $h(10) = 3$, $h(24) = 3$, $h(15) = 1$, $h(32) = 4$, $h(17) = 3$.

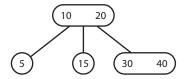
hashTable[1] \rightarrow 15 \rightarrow hashTable[2 \rightarrow nullptr hashTable[3] \rightarrow 17 \rightarrow 24 \rightarrow hashTable[4] \rightarrow

Question 1 To be sure that you fully understand the insertion algorithm, insert 32 into the 2-3 tree in Figure 19-11. The result should be the tree shown in Figure 19-6b. Once again, compare this tree with the binary search tree in Figure 19-6a and notice the dramatic advantage of the 2-3 tree's insertion strategy.

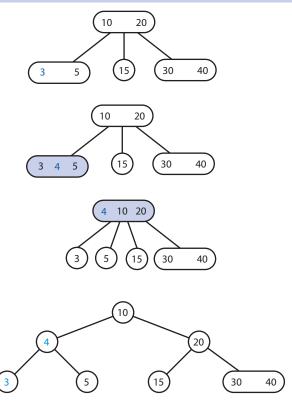


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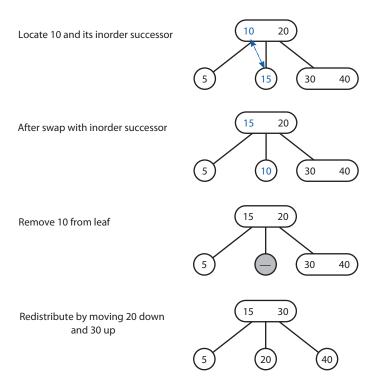
Question 2 What is the result of inserting 5, 40, 10, 20, 15, and 30—in the order given—into an initially empty 2-3 tree? Note that insertion of one item into an empty 2-3 tree will create a single node that contains the inserted item.



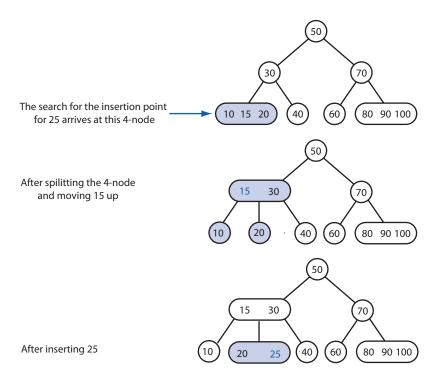
Question 3 What is the result of inserting 3 and 4 into the 2-3 tree that you created in the previous question?



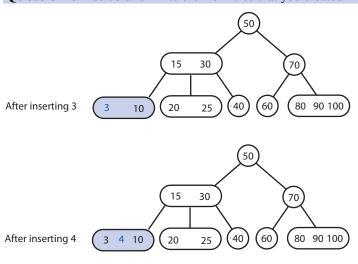
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Question 5 Insert 25 into the 2-3-4 tree in Figure 19-27b.



Question 6 Insert 3 and 4 into the 2-3-4 tree that you created in the previous question.

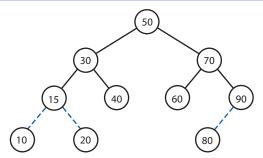


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Question 7 Why does a node in a red-black tree require less memory than a node in a 2-3-4 tree?

Each node in a red-black tree requires memory for two pointers and two pointer colors. These pointers and pointer colors require no more memory than the four pointers in a node in a 2-3-4 tree. In addition, a node in a red-black tree requires memory for only one data item, whereas a node in a 2-3-4 tree requires memory for three data items.

Question 8 What red-black tree represents the 2-3-4 tree in Figure 19-27a?



Question 1 Describe the graphs in Figure 20-32. For example, are they directed? Connected? Complete? Weighted?

Figure 20-32a is directed and connected. Figure 20-32b is undirected and connected. Neither graph is weighted.

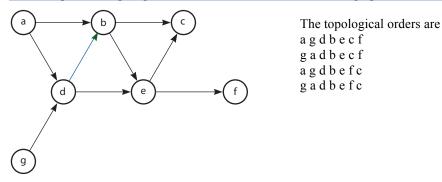
Question 2 Use the depth-first strategy and the breadth-first strategy to traverse the graph in Figure 20-32a, beginning with vertex 0. List the vertices in the order in which each traversal visits them.

DFS: 0, 1, 2, 4, 3; BFS: 0, 1, 2, 3, 4.

Question 3 Write the adjacency matrix for the graph in Figure 20-32a.

	0		2		4
0	0 0 0 0 1	1	0	0	0
1	0	0	1	1	0
2	0	0	0	0	1
3	0	1	0	0	0
4	1	0	0	0	0

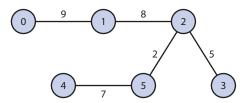
Question 4 Add an edge to the directed graph in Figure 20-14 that runs from vertex d to vertex b. Write all possible topological orders for the vertices in this new graph.



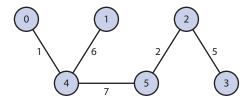
Question 5 Is it possible for a connected undirected graph with five vertices and four edges to contain a simple cycle? Explain.

No. See Observation 2 in Section 20.4.2.

Question 6 Draw the DFS spanning tree whose root is vertex 0 for the graph in Figure 20-33.



Question 7 Draw the minimum spanning tree whose root is vertex 0 for the graph in Figure 20-33.



Question 8 What are the shortest paths from vertex 0 to each vertex of the graph in Figure 20- 24a? (Note the weights of these paths in Figure 20-25.)

Path from 0 to 1 [0, 4, 2, 1] has weight 7.

Path from 0 to 2 [0, 4, 2] has weight 5.

Path from 0 to 3 [0, 4, 2, 3] has weight 8.

Path from 0 to 4 [0, 4] has weight 4.

Question 1 Consider two files of 1,600 employee records each. The records in each file are organized into sixteen 100-record blocks. One file is sequential access and the other is direct access. Describe how you would append one record to the end of each file.

Sequential access file: Copy the original file file1 into another file file2. Write on file2 a new block containing the desired record and 99 blank records. Copy file2 to the original file file1. **Direct access file:** Create a new block containing the desired record and 99 blank records. Write the new block to the file as the 17th block.

Question 2 Trace externalMergesort with an external file of 16 blocks. Assume that the arrays in1, in2, and out are each one block long. List the calls to the various functions in the order in which they occur.

```
externalMergesort(unsortedFileName, sortedFileName)
// This call to externalMergesort results in the following actions:
  Associate unsortedFileName with the file variable inFile
  Associate sortedFileName with the file variable outFile
  blocksort(inFile, tempFile1, numBlocks)
  // Records in each block are now sorted; numBlocks is 16
  mergeFile(tempFile1, tempFile2, 1, 16)
  // This call to mergeFile makes the following calls to mergeRuns:
     mergeRuns(tempFile1, tempFile2, 1, 1)
     mergeRuns(tempFile1, tempFile2, 3, 1)
     mergeRuns(tempFile1, tempFile2, 5, 1)
     mergeRuns(tempFile1, tempFile2, 7, 1)
     mergeRuns(tempFile1, tempFile2, 9, 1)
     mergeRuns(tempFile1, tempFile2, 11, 1)
     mergeRuns(tempFile1, tempFile2, 13, 1)
     mergeRuns(tempFile1, tempFile2, 15, 1)
  mergeFile(tempFile2, tempFile1, 2, 16)
  // This call to mergeFile makes the following calls to mergeRuns:
     mergeRuns(tempFile2, tempFile1, 1, 2)
     mergeRuns(tempFile2, tempFile1, 5, 2)
     mergeRuns(tempFile2, tempFile1, 9, 2)
```

```
mergeRuns(tempFile2, tempFile1, 13, 2)
mergeFile(tempFile1, tempFile2, 4, 16)
// This call to mergeFile makes the following calls to mergeRuns:
    mergeRuns(tempFile1, tempFile2, 1, 4)
    mergeRuns(tempFile1, tempFile2, 9, 4)

mergeFile(tempFile2, tempFile1, 8, 16)
// This call to mergeFile makes the following calls to mergeRuns:
    mergeRuns(tempFile2, tempFile1, 1, 8)
copyFile(tempFile1, outFile)
```

Question 3 Trace the retrieval algorithm for an indexed external file when the search key is less than all keys in the index. Assume that the index file stores the index records sequentially, sorted by their search keys, and contains 20 blocks of 50 records each. Also assume that the data file contains 100 blocks, and that each block contains 10 employee records. List the calls to the various functions in the order in which they occur.

```
getItem(indexFile[1..20], dataFile, searchKey)
buf.readBlock(indexFile[1..20], 10)
getItem(indexFile[1..9], dataFile, searchKey)
buf.readBlock(indexFile[1..9], 5)
getItem(indexFile[1..4], dataFile, searchKey)
buf.readBlock(indexFile[1..4], 2)
getItem(indexFile[1..1], dataFile, searchKey)
buf.readBlock(indexFile[1..1], 1)
throw NotFoundException
```

Question 4 Repeat Checkpoint Question 3, but this time assume that the search key equals the key in record 26 of block 12 of the index. Also assume that record 26 of the index points to block 98 of the data file.

```
getItem(indexFile[1..20], dataFile, searchKey)
buf.readBlock(indexFile[1..20], 10)
getItem(tIndex[11..20], dataFile, searchKey)
buf.readBlock(indexFile[11..20], 15)
getItem(tIndex[11..14], dataFile, searchKey)
buf.readBlock(indexFile[11..14], 12)
j = 26
blockNum = 98
data.readBlock(dataFile, 98)
Find data record data.getRecord(k) whose search key equals searchKey
return data.getRecord(k)
```