

Program verification

Big area in practice (google, meta, ...). All sorts of fancy logics, important one: separation logic.
For this course: the foundation for all program logic:

HOARE LOGIC : examples, proof rules, theoretical results (relative completeness)

{} precondition ★ assertions

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y := 0
z := 1
while y * x do
    y := y + 1;
    z := z * y;
    
```

] W

{z = x!} postcondition, if the program terminates, then $z = x!$. Zato za precondition ne rabimo $\{x \neq 0\}$

Hoare logic is compositional - the proof rules follow the syntactic structure of the program.

$$\frac{\{ \Phi \} C_1 \{ \Theta \} \quad \{ \Theta \} C_2 \{ \Psi \}}{\{ \Phi \} C_1 ; C_2 \{ \Psi \}}$$

$$\frac{\{ \mathcal{I} \} C \{ \mathcal{I} \}}{\{ \mathcal{I} \} \text{while } \Theta \text{ do } C \{ \mathcal{I} \wedge \neg \Theta \}}$$

; \mathcal{I} is called the INVARIANT

Consequence rule:

$$\frac{\{ \Phi' \} C \{ \Psi' \}}{\{ \Phi \} C \{ \Psi \}} \quad \begin{array}{l} \text{SIDE CONDITIONS} \\ (\Phi \rightarrow \Phi') \quad (\Psi' \rightarrow \Psi) \end{array}$$

Assignment:

$$\frac{}{\{ \Psi[e/x] \} x := e \{ \Psi \}}$$

$$\star \frac{\{ z * (y+1) = (y+1)!, y+1 \neq 0 \} y := y+1 \{ z * y = y!, y \neq 0 \}}{} \quad \text{SIDE CONDITIONS}$$

$$\frac{\{ z = y!, y \neq 0, y \neq x \} y := y+1 \{ z * y = y!, y \neq 0 \} \quad \{ z * y = y!, y \neq 0 \} z := z * y \{ z = y!, y \neq 0 \}}{} \quad \text{SIDE CONDITIONS}$$

$$\frac{\{ z = y!, y \neq 0, y \neq x \} y := y+1 ; z := z * y \{ z = y!, y \neq 0 \}}{} \quad \text{SIDE CONDITIONS}$$

$$\{ z = y! \wedge y \neq 0 \} W \{ z = y! \wedge y \neq 0 \wedge y = x \}$$

$$\{ \{ y := 0; z := 1 \} \{ y = 0 \wedge z = 1 \} \}$$

$$\{ y = 0 \wedge z = 1 \} W \{ z = x! \}$$

$$\{ \{ y := 0; z := 1 \} W \{ z = x! \} \}$$

$$\star y = 0 \wedge z = 1 \rightarrow z = y! \wedge y \neq 0 \quad \checkmark \quad \left. \begin{array}{l} \text{SIDE} \\ \text{CONDITIONS} \end{array} \right\}$$

$$z = y! \wedge y \neq 0 \wedge y = x \rightarrow z = x! \quad \checkmark$$

Prosojnice

$$\star z = y! \wedge y \neq 0 \wedge y \neq x \rightarrow z * (y+1) = (y+1)! \wedge y+1 \neq 0$$