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CS 441 - HW1: Instance-based Methods

Complete the sections below. You do not need to fill out the checklist.

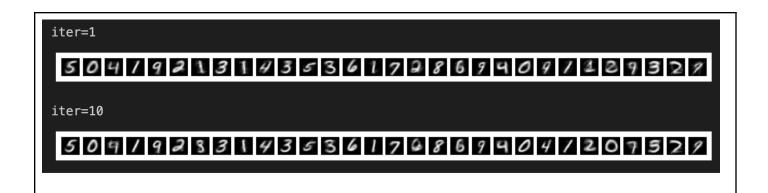
Total	Points A	vailable	[]/145
1.	Retrieva	al, K-means, 1-NN on MNIST	
	a.	Retrieval	[]/5
	b.	K-means	[]/15
	C.	1-NN	[]/10
2.	Make it	fast	
	a.	K-means plot	[]/15
	b.	1-NN error plots	[]/8
	C.	1-NN time plots	[]/7
	d.	Most confused label	[]/5
3.	Temper	ature Regression	
	a.	RMSE Tables	[]/20
4.	Concep	tual questions	[]/15
5.	Stretch	Goals	
	a.	Evaluate effect of K for MNIST	[]/15
	b.	Evaluate effect of K for Temp Reg.	[]/15
	C.	Compare Kmeans more iterations vs. restarts	[]/15

1. Retrieval, K-means, 1-NN on MNIST

a. What index is returned for x_test[1]?

28882

b. Paste the display of clusters after the 1st and 10th iteration for K=30.

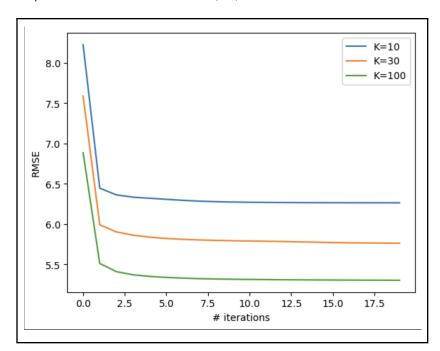


c. Error rate for first 100 test samples, using first 10,000 training samples (x.x)

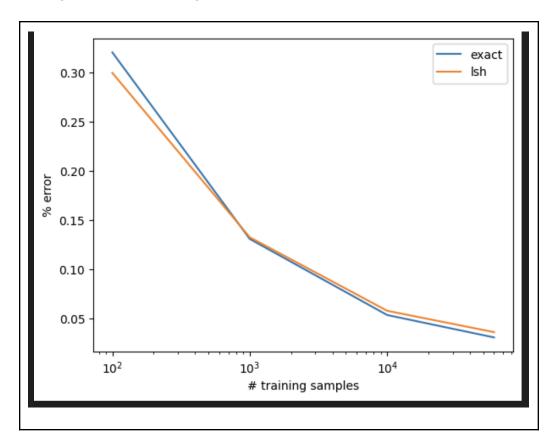
8.0%

2. Make it fast

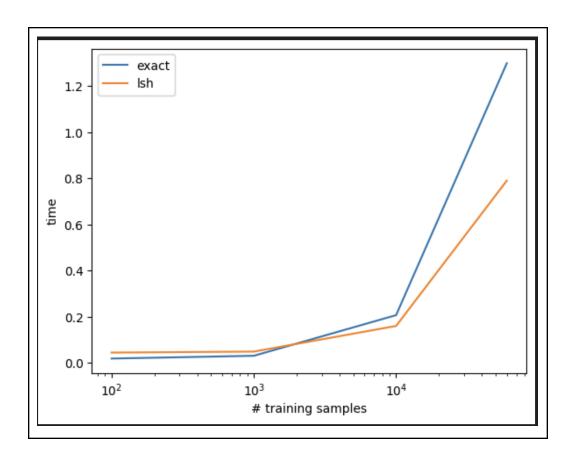
a. KMeans plot of RMSE vs iterations for K=10, 30, 100



b. Nearest neighbor error vs training size plot



c. Nearest neighbor time vs training size plot



d. What label is most commonly confused with '2'?

3. Temperature Regression

a. Table of RMSE for KNN with K=5 (x.xx)

	KNN (K=5)
Original Features	3.249
Normalized Features	2.977

4. Test your understanding

Fill in the letter corresponding to the answer. If you're not sure, you can sometimes run small experiments to check.

1. Is K-means guaranteed to decrease RMSE between nearest cluster and samples at each iteration until convergence?

	b				
2. If you increase K, is K-means e.a. Guaranteedb. Expected but not guararc. Not expected		uaranteed	to achieve I	ower RMSI	Ξ?
 3. In K-NN regression, for training be predicted for any query? a. Min(y) b. Mean(y) c. Can't be determined 	labels y, wh	at is the low	vest target v	value that c	an possibly
 Would you expect the "training or classification? Training error is Higher Lower It's problem-dependent 		-			N for
5. Would you expect the test error regression?a. Higherb. Lowerc. It's problem-dependent	for 1-NN to	be higher o	or lower than	n for 3-NN 1	for
5. Stretch Goals (optional)a. Select best K parameter for K-NN MNIST classification in K=1, 3, 5, 11, 25. (x.xx)					
Validation Set Performance	K=1	K=3	K=5	K=11	K=25
Validation Got i Chomianoc	1'` '		5		

a. Yesb. No

|--|

Best K:

3

Test % error (x.xx)

2.959%

b. Select best K parameter for K-NN temperature regression in K=1, 3, 5, 11, 25. (x.xx)

Validation Set RMSE	K=1	K=3	K=5	K=11	K=25
Original Features	5.99	5.07	4.81	4.635	4.48
Normalized Features	4.96	4.08	3.78	3.629	3.54

Best Setting (K, feature type):

K=25, Original Features

Test RMSE (x.xx)

3.04

c. Kmeans, MNIST: compare average and standard deviation RMSE based on number of iterations and number of restarts

(4 digit precision)

K=30	RMSE avg	RMSE std
20 iterations, 1 restart	5.819	0.00
4 iterations, 5 restarts	5.775	0.00
50 iterations, 1 restart	5.789	0.00
10 iterations, 5 restarts	5.769	0.00

Acknowledgments / Attribution

List any outside sources for code or ideas or "None". None

CS441: Applied ML - HW 1

Parts 1-2: MNIST

Include all the code for generating MNIST results below

```
In [ ]: # initialization code
        import numpy as np
         from tensorflow import keras
         from keras.datasets import mnist
         # from tensorflow import keras
        %matplotlib inline
         from matplotlib import pyplot as plt
         from scipy import stats
        def load mnist():
           Loads, reshapes, and normalizes the data
           (x_train, y_train), (x_test, y_test) = mnist.load_data() # loads MNIST dat
           x_{train} = np.reshape(x_{train}, (len(x_{train}), 28*28)) # reformat to 768-d
           x_{\text{test}} = \text{np.reshape}(x_{\text{test}}, (\text{len}(x_{\text{test}}), 28*28))
           maxval = x_train.max()
           x_train = x_train/maxval # normalize values to range from 0 to 1
           x \text{ test} = x \text{ test/maxval}
           return (x_train, y_train), (x_test, y_test)
         def display_mnist(x, subplot_rows=1, subplot_cols=1):
           Displays one or more examples in a row or a grid
           if subplot_rows>1 or subplot_cols>1:
             fig, ax = plt.subplots(subplot_rows, subplot_cols, figsize=(15,15))
             for i in np.arange(len(x)):
               ax[i].imshow(np.reshape(x[i], (28,28)), cmap='gray')
               ax[i].axis('off')
           else:
               plt.imshow(np.reshape(x, (28,28)), cmap='gray')
               plt.axis('off')
           plt.show()
```

```
In []: # example of using MNIST load and display functions
   (x_train, y_train), (x_test, y_test) = load_mnist()
   display_mnist(x_train[:10],1,10)
   print('Total size: train={}, test ={}'.format(len(x_train), len(x_test)))
```



Total size: train=60000, test =10000

1. Retrieval, Clustering, and NN Classification

```
In [ ]: # Retrieval
        import math
        def get_nearest(X_query, X):
          ''' Return the index of the sample in X that is closest to X_query accordi
              to L2 distance '''
          # TO DO
          mindis = math.inf
          n = X.shape[0]
          res = -1
          for i in range(n):
            dis = np.linalg.norm(X[i]-X_query)
            if dis<mindis:</pre>
              mindis = dis
              res = i
          if res>=0:
            return res
          else:
            print("error happens!")
        # print(x train.shape)
        # print(x_test.shape)
        j = get_nearest(x_test[0], x_train)
        print(j)
        j = get_nearest(x_test[1], x_train)
        print(j)
       53843
       28882
In [ ]: # K-means
        def kmeans(X, K, niter=10):
          Starting with the first K samples in X as cluster centers, iteratively ass
          point to the nearest cluster and compute the mean of each cluster.
          Input: X[i] is the ith sample, K is the number of clusters, niter is the r
          Output: K cluster centers
          1.1.1
          # TO DO -- add code to display cluster centers at each iteration also
          centers = np.copy(X[:K])
          for i in range(niter):
            choice = np.array([get_nearest(x, centers) for x in X])
            for j in range(K):
              centers[j] = np.mean(X[choice==j],axis=0)
            if i==0 or i==9:
              print(f"iter={i+1}")
              display_mnist(centers,1,30)
          return centers
        K=30
        centers = kmeans(x_train[:1000], K)
       iter=1
```

504192131435361728694091129328

iter=10

509192331435361768694041207521

incorrect rate: 8%

2. Make it fast

```
In []: # install libraries you need for part 2
!apt install libomp-dev
!pip install faiss-cpu
import faiss
import time
```

The operation couldn't be completed. Unable to locate a Java Runtime that su pports apt.

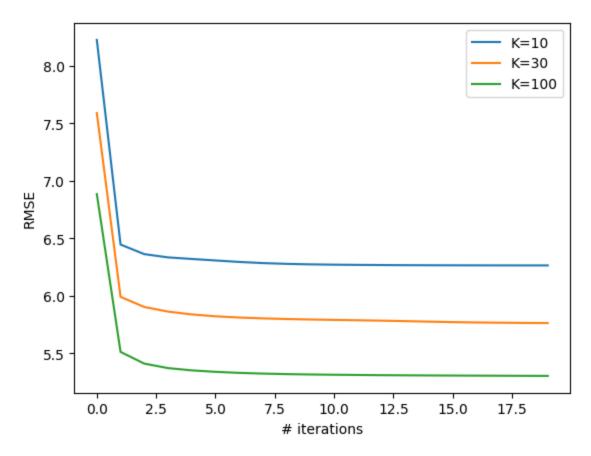
Please visit http://www.java.com for information on installing Java.

Requirement already satisfied: faiss-cpu in /Users/janghl/anaconda3/envs/am l/lib/python3.10/site-packages (1.7.4)

```
In [ ]: # retrieval
        # TO DO (check that you're using FAISS correctly)
        def fast_nearest(X_query, X, K=1, LSH=False):
          if not LSH:
            index = faiss.IndexFlatL2(x_train.shape[1]) # set for exact search
          else:
            dim = X.shape[1]
            index = faiss.IndexLSH(dim, dim)
          index.add(X) # add the data
          dist, idx = index.search(X guery, K) # returns index and sq err for each s
          return np.array(dist), np.array(idx)
        dist, idx = fast_nearest(x_test, x_train)
        print(idx[0])
        print(idx[1])
       [53843]
       [28882]
In [ ]: # K-means
```

def kmeans_fast(X, K, niter=10):

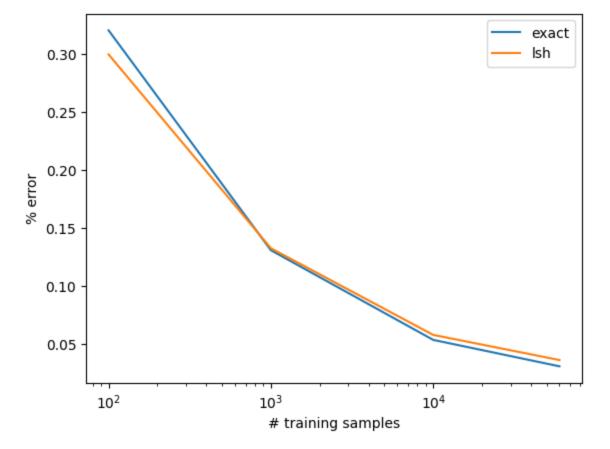
Starting with the first K samples in X as cluster centers, iteratively ass point to the nearest cluster using faiss and compute the mean of each clus Input: X[i] is the ith sample, K is the number of clusters, niter is the r Output: K cluster centers # TO DO (you can base this on part 1, but use FAISS for search) # if you include display code, you need to re-organize the plotting code b rmse = []centers = np.copy(X[:K]) for i in range(niter): dist, idx = fast nearest(X, centers) choice = np.array(idx).reshape(idx.shape[0]) rmse.append(np.sqrt(np.sum(dist)/dist.shape[0])) for j in range(K): centers[j] = np.mean(X[choice==j],axis=0) return centers, rmse K=10 centers, rmse = kmeans_fast(x_train, K, niter=20) plt.plot(np.arange(len(rmse)), rmse, label='K=10') centers, rmse = kmeans_fast(x_train, K, niter=20) plt.plot(np.arange(len(rmse)), rmse, label='K=30') K=100 centers, rmse = kmeans_fast(x_train, K, niter=20) plt.plot(np.arange(len(rmse)), rmse, label='K=100') plt.legend(), plt.ylabel('RMSE'), plt.xlabel('# iterations') plt.show()

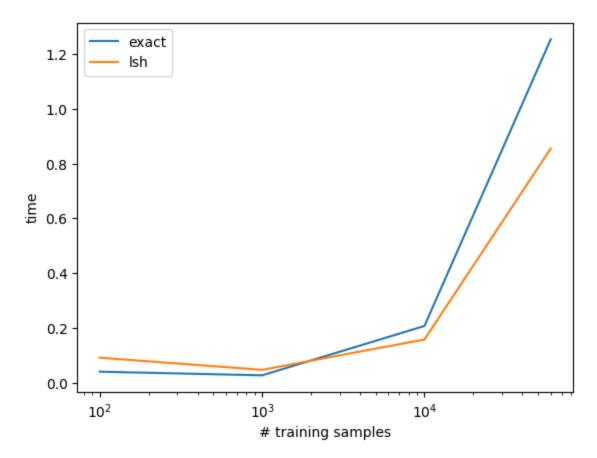


```
In [ ]: # 1-NN
        nsample = [100, 1000, 10000, 60000]
        # TO DO
        def ONN(x_train, x_test, s, LSH):
          begin = time.time()
          train = x_train[:s]
          right = 0
          if LSH:
            dim = x_{test.shape}[1]
            index = faiss.IndexLSH(dim, dim)
          else:
            index = faiss.IndexFlatL2(x_test.shape[1])
          index.add(train)
          dist, idx = index.search(x_test,1) # returns index and sq err for each san
          idx = np.array(idx).reshape(idx.shape[0])
          for i in range(len(x_test)):
            if y_test[i] == y_train[idx[i]]:
               right += 1
          acc = right/len(x_test)
          end = time.time()
          timing = end-begin
          return acc, timing
        acc exact = []
        acc_lsh = []
        timing_exact = []
        timing_lsh = []
```

```
for s in nsample:
    acc_exact_elem, timing_exact_elem = ONN(x_train, x_test, s, LSH=False)
    acc_lsh_elem, timing_lsh_elem = ONN(x_train, x_test, s, LSH=True)
    acc_exact.append(1-acc_exact_elem)
    acc_lsh.append(1-acc_lsh_elem)
    timing_exact.append(timing_exact_elem)
    timing_lsh.append(timing_lsh_elem)

plt.semilogx(nsample, acc_exact, label='exact')
plt.semilogx(nsample, acc_lsh, label='lsh')
plt.legend(), plt.ylabel('% error'), plt.xlabel('# training samples')
plt.semilogx(nsample, timing_exact, label='exact')
plt.semilogx(nsample, timing_lsh, label='lsh')
plt.legend(), plt.ylabel('time'), plt.xlabel('# training samples')
plt.show()
```





```
In [ ]: # Confusion matrix
         from sklearn import metrics
         # TO DO
         index = faiss.IndexFlatL2(x_test.shape[1])
         index.add(train)
         dist, idx = index.search(x_test,1) # returns index and sq err for each sampl
         idx = np.array(idx).reshape(idx.shape[0])
         metrics.confusion_matrix(y_test, y_train[idx])
Out[]: array([[ 971,
                                                  0,
                                                                4,
                                                                        1,
                                                                               1,
                                                                                      0],
                              1,
                                     1,
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                       9,
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                                                                        8,
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                                     3,
                                                          4,
                                                                                   941]])
                       6,
                              6,
                                            7,
                                                  20,
                                                                1,
                                                                       17,
```

Part 3: Temperature Regression

Include all your code used for part 2 in this section.

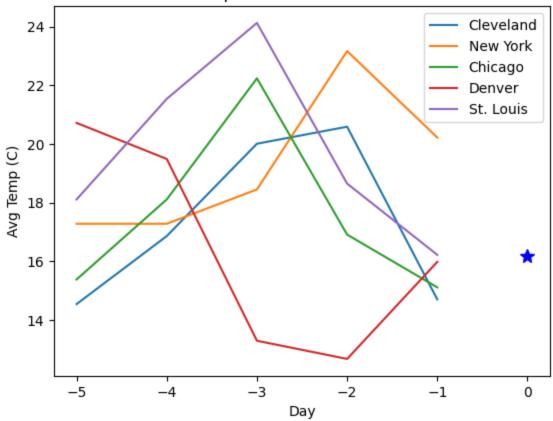
```
In []: import numpy as np
# from google.colab import drive
%matplotlib inline
```

from matplotlib import pyplot as plt

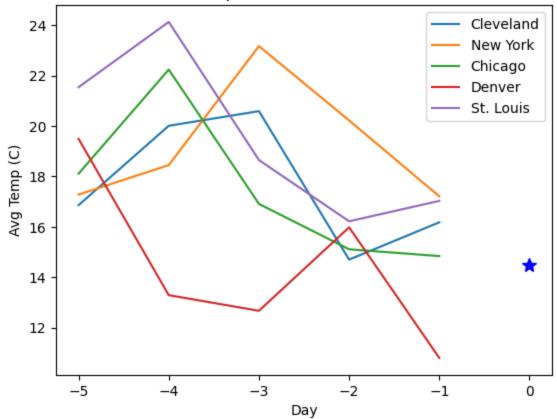
```
from sklearn.linear model import Ridge
        from sklearn.linear model import Lasso
        # load data (modify to match your data directory or comment)
        def load temp data():
          # drive.mount('/content/drive')
          # datadir = "/content/drive/My Drive/CS441/24SP/hw1/"
          datadir = "./"
          T = np.load(datadir + 'temperature_data.npz')
          x_train, y_train, x_val, y_val, x_test, y_test, dates_train, dates_val, dates_val
          T['x_train'], T['y_train'], T['x_val'], T['y_val'], T['x_test'], T['y_test
           return (x_train, y_train, x_val, y_val, x_test, y_test, dates_train, dates
        # plot one data point for listed cities and target date
        def plot_temps(x, y, cities, feature_to_city, feature_to_day, target_date):
          nc = len(cities)
          ndays = 5
          xplot = np.array([-5, -4, -3, -2, -1])
          yplot = np.zeros((nc,ndays))
          for f in np.arange(len(x)):
             for c in np.arange(nc):
               if cities[c] == feature to city[f]:
                 yplot[feature_to_day[f]+ndays,c] = x[f]
          plt.plot(xplot,yplot)
          plt.legend(cities)
          plt.plot(0, y, 'b*', markersize=10)
          plt.title('Predict Temp for Cleveland on ' + target date)
          plt.xlabel('Day')
          plt.ylabel('Avg Temp (C)')
          plt.show()
In [ ]: # load data
         (x_train, y_train, x_val, y_val, x_test, y_test, dates_train, dates_val, dat
         ''' Data format:
               x_train, y_train: features and target value for each training sample (
               x_val, y_val: features and target value for each validation sample (us
               x_test, y_test: features and target value for each test sample (used t
               dates_xxx: date of the target value for the corresponding sample
               feature to city: maps from a feature number to the city
               feature_to_day: maps from a feature number to a day relative to the ta
               Note: 361 is the temperature of Cleveland on the previous day
        1.1.1
        f = 361
        print('Feature {}: city = {}, day= {}'.format(f, feature to city[f], feature
        baseline_rmse = np.sqrt(np.mean((y_val[1:]-y_val[:-1])**2)) # root mean squa
        print('Baseline - prediction using previous day: RMSE={}'.format(baseline_rm
        # plot first two x/y for val
        plot_temps(x_val[0], y_val[0], ['Cleveland', 'New York', 'Chicago', 'Denver'
plot_temps(x_val[1], y_val[1], ['Cleveland', 'New York', 'Chicago', 'Denver'
       Feature 361: city = Cleveland, day= -1
```

Baseline - prediction using previous day: RMSE=3.460601246750482

Predict Temp for Cleveland on 2018-09-27



Predict Temp for Cleveland on 2018-09-28



```
In []: # K-NN Regression
        import copy
        def regress KNN(X trn, y trn, X tst, K=1):
          Predict the target value for each data point in X_tst using a
          K-nearest neighbor regressor based on (X_trn, y_trn), with L2 distance.
          Input: X trn[i] is the ith training data. y trn[i] is the ith training lab
          Output: return y pred, where y pred[i] is the predicted ith test value
          1.1.1
          # TO DO
          dist, idx = fast_nearest(x_test, x_train, K=K)
          y pred = np.zeros(shape=X tst.shape[0])
          for i in range(len(X tst)):
            points = []
            for j in idx[i]:
              points.append(y_trn[j])
              y_pred[i] = np.mean(points)
          return y pred
        def normalize features(x, y, fnum):
          ''' Normalize the features in x and y.
              For each data sample i:
                x2[i] = x[i]-x[i,fnum]
                y2[i] = y[i]-x[i,fnum]
          111
          # TO DO
          x2 = np.zeros like(x)
          y2 = np.zeros like(y)
          xsub = np.array(np.copy(x[:,fnum]))
          for i in range(x.shape[1]):
            x2[:,i] = x[:,i] - xsub
          y2 = y - xsub
          return x2, y2
        # KNN with original features
        # TO DO
        y_predict = regress_KNN(x_train, y_train, x_test, K=5)
        # print(f"y_predict: {y_val.shape}\nx_test: {x_val.shape}")
        print(f"rmse when K=5: {np.sqrt(np.mean((y test-y predict)**2))}")
        # KNN with normalized features
        fnum = 361 # previous day temp in Cleveland
        # TO DO
        x_train_new, y_train_new = normalize_features(x_train, y_train, fnum)
        x test new, y test new = normalize features(x test, y test, fnum)
        y predict new = regress KNN(x \text{ train new, } y \text{ train new, } x \text{ test new, } K=5)
        print(f"rmse when K=5: {np.sqrt(np.mean((y_test_new-y_predict_new)**2))}")
```

rmse when K=5: 3.249556245363484 rmse when K=5: 2.9770334300836487

Part 5: Stretch Goals

Include all your code used for part 5 in this section. You can copy-paste code from parts 1-3 if it is re-usable.

```
In [ ]: # Stretch: KNN classification (Select K)
        # find the prediction for a set
        def calc_pred(valid, dist, idx, y_train, K):
          pred = np.zeros(valid.shape[0])
          for i in range(valid.shape[0]):
            count = {}
            distance = {}
            for j in range(K):
                                           #for each of K points, p is predicted numb
              p = y_train[idx[i][j]]
              d = dist[i][j]
              if p in distance:
                 distance[p] += d
                 distance[p] = d
              if p in count:
                 count[p] += 1
              else:
                count[p] = 1
            maxnum = -math.inf
                                     #find all candidates with highest votes
            candidate = []
            for c in count:
              if count[c]>maxnum:
                maxnum = count[c]
                 candidate = [c]
              elif count[c]==maxnum:
                 candidate.append(c)
            mindist = math.inf
            result = -1
            for can in candidate:
              if distance[can]<mindist:</pre>
                 result = can
            pred[i] = result
          return pred
        def KNN_classification(x_train, y_train, K):
          train = x_train[:50000]
          valid = x_{train}[50000:]
          answer = y train[50000:]
          dist, idx = fast_nearest(valid, train, K=K)
          correct = 0
          pred = calc_pred(valid, dist, idx, y_train, K)
          for i in range(len(valid)):
            if pred[i] == answer[i]:
              correct += 1
```

```
print(f"incorrect rate for K={K}: {100*(1-correct/len(valid))}%")
        (x_train, y_train), (x_test, y_test) = load_mnist()
        hyperparameter = [1, 3, 5, 11, 25]
        for K in hyperparameter:
          KNN_classification(x_train, y_train, K)
        # Perform K=3 on the test set
        best K = 3
        dist, idx = fast nearest(x test, x train, K=best K)
        correct = 0
        pred = calc_pred(x_test, dist, idx, y_train, best_K)
        for i in range(len(x test)):
          if pred[i] == y test[i]:
            correct += 1
        print(f"incorrect rate for K={best_K}: {100*(1-correct/len(x_test))}%")
       incorrect rate for K=1: 2.880000000000005%
       incorrect rate for K=3: 2.8200000000000003%
       incorrect rate for K=5: 2.949999999999997%
       incorrect rate for K=11: 3.1499999999999972%
       incorrect rate for K=25: 3.879999999999946%
       incorrect rate for K=3: 2.959999999999996%
In [ ]: # Stretch: KNN regression (Select K)
        (x_train, y_train, x_val, y_val, x_test, y_test, dates_train, dates_val, dat
        # K-NN Regression
        hyperparameter = [1, 3, 5, 11, 25]
        for K in hyperparameter:
          # KNN with original features
          y predict = regress KNN(x train, y train, x val, K=K)
          print(f"rmse when K={K}: {np.sqrt(np.mean((y_val-y_predict)**2))}")
          # KNN with normalized features
          fnum = 361 # previous day temp in Cleveland
          x_train_new, y_train_new = normalize_features(x_train, y_train, fnum)
          x_val_new, y_val_new = normalize_features(x_val, y_val, fnum)
          y predict new = regress KNN(x train new, y train new, x val new, K=K)
          print(f"(normalized)rmse when K={K}: {np.sqrt(np.mean((y_val_new-y_predict
       rmse when K=1: 5.994830467058024
       (normalized) rmse when K=1: 4.962816257477145
       rmse when K=3: 5.0719820622291065
       (normalized) rmse when K=3: 4.081979762608333
       rmse when K=5: 4.814445285619017
       (normalized) rmse when K=5: 3.7840627858326146
       rmse when K=11: 4.635825782051689
       (normalized) rmse when K=11: 3.6293441508410265
       rmse when K=25: 4.482832870675747
       (normalized) rmse when K=25: 3.544085254919383
```

```
In [ ]: # Best on test set
        y_predict = regress_KNN(x_train, y_train, x_test, K=25)
        print(f"rmse when K={K}: {np.sqrt(np.mean((y test-y predict)**2))}")
       rmse when K=25: 3.041778206247129
In [ ]: # Stretch: K-means (more iters vs redos)
        def test(niter, nredo):
          kmeans = faiss.Kmeans(x_train.shape[1], 30, niter=niter, nredo=nredo, seed
          kmeans.train(x train)
          dist, idx = kmeans.index.search(x train, 1)
          rmse = np.sqrt(np.sum(dist) / x_train.shape[0])
          return rmse
        (x_train, y_train), (x_test, y_test) = load_mnist()
        first trail multiple = []
        first_trail_single = []
        second trail multiple = []
        second trail single = []
        for i in range(5):
          first trail multiple.append(test(10,5))
          first trail single.append(test(50,1))
          second_trail_multiple.append(test(4,5))
          second trail single.append(test(20,1))
        print(f"for first_trail_multiple: mean={np.mean(first_trail_multiple)}, std=
        print(f"for first trail single: mean={np.mean(first trail single)}, std={np.
        print(f"for second_trail_multiple: mean={np.mean(second trail multiple)}, st
        print(f"for second trail single: mean={np.mean(second trail single)}, std={r
       for first trail multiple: mean=5.789932893969209, std=0.0
       for first trail single: mean=5.769123994738427, std=0.0
       for second_trail_multiple: mean=5.819028949632977, std=0.0
       for second trail single: mean=5.775398976117003, std=0.0
In []: # from https://gist.github.com/jonathanagustin/b67b97ef12c53a8dec27b343dca4a
        # For use in Colab. For local, just use jupyter nbconvert directly
        import os
        # @title Convert Notebook to PDF. Save Notebook to given directory
        NOTEBOOKS DIR = "/content/drive/My Drive/CS441/24SP/hw1" # @param {type:"str
        NOTEBOOK_NAME = "CS441_SP24_HW1_Solution.ipynb" # @param {type:"string"}
        from google.colab import drive
        drive.mount("/content/drive/", force_remount=True)
        NOTEBOOK PATH = f"{NOTEBOOKS DIR}/{NOTEBOOK NAME}"
        assert os.path.exists(NOTEBOOK PATH), f"NOTEBOOK NOT FOUND: {NOTEBOOK PATH}"
        !apt install -y texlive-xetex texlive-fonts-recommended texlive-plain-generi
        !jupyter nbconvert "$NOTEBOOK_PATH" -- to pdf > /dev/null 2>&1
        NOTEBOOK_PDF = NOTEBOOK_PATH.rsplit('.', 1)[0] + '.pdf'
        assert os.path.exists(NOTEBOOK_PDF), f"ERROR MAKING PDF: {NOTEBOOK_PDF}"
        print(f"PDF CREATED: {NOTEBOOK_PDF}")
```