#### Introduction to Data Science (IDS) course

### **Decision Tree**

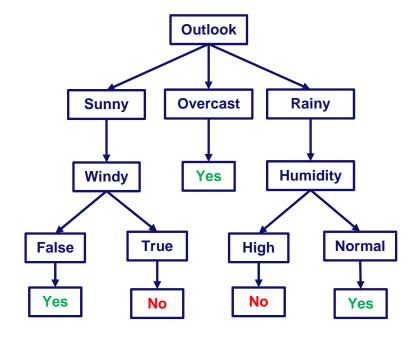
Lecture 3 Instruction

IDS-I-L3





|          |      | Target Feature |       |           |
|----------|------|----------------|-------|-----------|
| Outlook  | Temp | Humidity       | Windy | Play Golf |
| Rainy    | Hot  | High           | False | No        |
| Rainy    | Hot  | High           | True  | No        |
| Overcast | Hot  | High           | False | Yes       |
| Sunny    | Mild | High           | False | Yes       |
| Sunny    | Cool | Normal         | False | Yes       |
| Sunny    | Cool | Normal         | True  | No        |
| Overcast | Cool | Normal         | True  | Yes       |
| Rainy    | Mild | High           | False | No        |
| Rainy    | Cool | Normal         | False | Yes       |
| Sunny    | Mild | Normal         | False | Yes       |
| Rainy    | Mild | Normal         | True  | Yes       |
| Overcast | Mild | High           | True  | Yes       |
| Overcast | Hot  | Normal         | False | Yes       |
| Sunny    | Mild | High           | True  | No        |





#### 1. Calculate entropy of the target feature.

| Outlook  | Temp | Humidity | Windy | Play Golf |
|----------|------|----------|-------|-----------|
| Rainy    | Hot  | High     | False | No        |
| Rainy    | Hot  | High     | True  | No        |
| Overcast | Hot  | High     | False | Yes       |
| Sunny    | Mild | High     | False | Yes       |
| Sunny    | Cool | Normal   | False | Yes       |
| Sunny    | Cool | Normal   | True  | No        |
| Overcast | Cool | Normal   | True  | Yes       |
| Rainy    | Mild | High     | False | No        |
| Rainy    | Cool | Normal   | False | Yes       |
| Sunny    | Mild | Normal   | False | Yes       |
| Rainy    | Mild | Normal   | True  | Yes       |
| Overcast | Mild | High     | True  | Yes       |
| Overcast | Hot  | Normal   | False | Yes       |
| Sunny    | Mild | High     | True  | No        |

$$E = -\sum_{i=1}^{k} p_i \, \log_2(p_i)$$

| Play Golf |   |  |  |  |
|-----------|---|--|--|--|
| Yes No    |   |  |  |  |
| 9         | 5 |  |  |  |

$$Entropy (PlayGolf) = -(0.36log_20.36) - (0.64log_20.64) = 0.94$$



#### 2. Entropy after splitting by "Outlook".

| k                                |   |
|----------------------------------|---|
| $E = -\sum_{i} p_i  \log_2(p_i)$ | ) |
| i=1                              |   |

|         |          | Play Golf |    |    |
|---------|----------|-----------|----|----|
|         |          | Yes       | No |    |
| Outlook | Sunny    | 3         | 2  | 5  |
|         | Overcast | 4         | 0  | 4  |
|         | Rainy    | 2         | 3  | 5  |
|         |          |           |    | 14 |

$$E(3,2) = -(0.6log_20.6) - (0.4log_20.4) = 0.97$$
  
 $E(4,0) = -(1log_21) - (0log_20) = 0$   
 $E(2,3) = E(3,2) = 0.97$ 

Entropy (PlayGolf)  
= 
$$P(Sunny) \times E(3,2) + P(Overcast) \times E(4,0) + P(Rainy) \times E(2,3)$$
  
=  $\left(\frac{5}{14}\right) \times 0.97 + \left(\frac{4}{14}\right) \times 0 + \left(\frac{5}{14}\right) \times 0.97 = 0.69$ 

Information Gain = 0.94 - 0.69 = 0.25



#### 3. Calculate information gain after splitting by each descriptive feature.

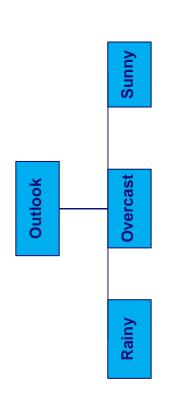
|         |          |     | Play Golf |    |   |
|---------|----------|-----|-----------|----|---|
|         |          | Yes |           | No |   |
| Outlook | Sunny    |     | 3         |    | 2 |
|         | Overcast |     | 4         |    | 0 |
|         | Rainy    |     | 2         |    | 3 |
| Gain    |          |     | = 0.25    |    |   |

|       |             | Play | Golf |  |  |
|-------|-------------|------|------|--|--|
|       |             | Yes  | No   |  |  |
| Temp. | Hot         | 2    | 2    |  |  |
|       | Mild        | 4    | 2    |  |  |
|       | Cool        | 3    | 1    |  |  |
|       | Gain = 0.02 |      |      |  |  |

|             |        | Play Golf |    |  |
|-------------|--------|-----------|----|--|
|             |        | Yes       | No |  |
| Humidity    | High   | 3         | 4  |  |
|             | Normal | 6         | 1  |  |
| Gain = 0.15 |        |           |    |  |

|             |             | Play Golf |    |  |  |
|-------------|-------------|-----------|----|--|--|
|             |             | Yes       | No |  |  |
| Windy False |             | 6         | 2  |  |  |
|             | True        | 3         | 3  |  |  |
|             | Gain = 0.04 |           |    |  |  |



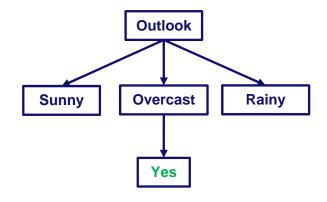


| Outlook | Temp | Humidity | Windy | Play Golf |
|---------|------|----------|-------|-----------|
| Sunny   | Mild | High     | False | Yes       |
| Sunny   | Cool | Normal   | False | Yes       |
| Sunny   | Cool | Normal   | True  | No        |
| Sunny   | Mild | Normal   | False | Yes       |
| Sunny   | Mild | High     | True  | No        |

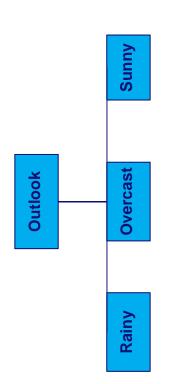
| Overcast | Hot  | High   | False | Yes |
|----------|------|--------|-------|-----|
| Overcast | Cool | Normal | True  | Yes |
| Overcast | Mild | High   | True  | Yes |
| Overcast | Hot  | Normal | False | Yes |

| Rainy | Hot  | High   | False | No  |
|-------|------|--------|-------|-----|
| Rainy | Hot  | High   | True  | No  |
| Rainy | Mild | High   | False | No  |
| Rainy | Cool | Normal | False | Yes |
| Rainy | Mild | Normal | True  | Yes |

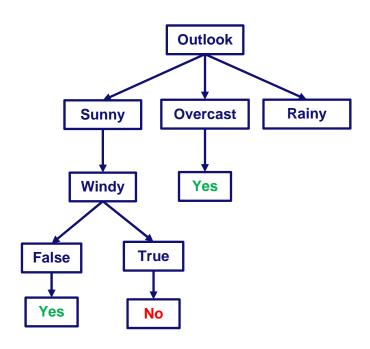
4. Split data based on the feature which has the maximum gain, and repeat steps 1-3 for each part.



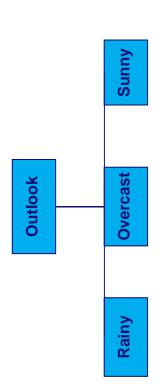




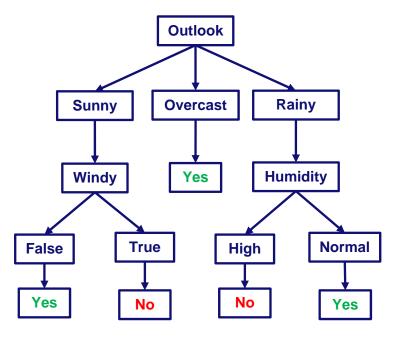
| Outlook  | Temp | Humidity | Windy | Play Golf |
|----------|------|----------|-------|-----------|
| Sunny    | Mild | High     | False | Yes       |
| Sunny    | Cool | Normal   | False | Yes       |
| Sunny    | Cool | Normal   | True  | No        |
| Sunny    | Mild | Normal   | False | Yes       |
| Sunny    | Mild | High     | True  | No        |
|          |      |          |       |           |
| Overcast | Hot  | High     | False | Yes       |
| Overcast | Cool | Normal   | True  | Yes       |
| Overcast | Mild | High     | True  | Yes       |
| Overcast | Hot  | Normal   | False | Yes       |
|          |      |          |       |           |
| Rainy    | Hot  | High     | False | No        |
| Rainy    | Hot  | High     | True  | No        |
| Rainy    | Mild | High     | False | No        |
| Rainy    | Cool | Normal   | False | Yes       |
| Rainy    | Mild | Normal   | True  | Yes       |







| Outlook  | Temp | Humidity | Windy | Play Golf |
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| Sunny    | Cool | Normal   | True  | No        |
| Sunny    | Mild | Normal   | False | Yes       |
| Sunny    | Mild | High     | True  | No        |
|          |      |          |       |           |
| Overcast | Hot  | High     | False | Yes       |
| Overcast | Cool | Normal   | True  | Yes       |
| Overcast | Mild | High     | True  | Yes       |
| Overcast | Hot  | Normal   | False | Yes       |
|          |      |          |       |           |
| Rainy    | Hot  | High     | False | No        |
| Rainy    | Hot  | High     | True  | No        |
| Rainy    | Mild | High     | False | No        |
| Rainy    | Cool | Normal   | False | Yes       |
| Rainy    | Mild | Normal   | True  | Yes       |





### Q2. Your Turn

• Suppose that the following data is about accepting or rejecting job applications based on "Experience", "Degree", and type of the job ("Job") that applicants applied for it. What is the decision tree for the following data set based on entropy?

| Experience | Degree | Job   | Class |
|------------|--------|-------|-------|
| Exp >10    | HS     | Board | No    |
| 5< Exp <10 | Uni    | Board | Yes   |
| Exp >10    | HS     | Board | No    |
| 5< Exp <10 | HS     | Hcare | Yes   |
| Exp < 5    | HS     | Hcare | Yes   |
| Exp < 5    | HS     | Board | No    |
| Exp < 5    | None   | Edu   | No    |
| Exp >10    | None   | Hcare | No    |
| Exp < 5    | Uni    | Edu   | Yes   |
| Exp >10    | Uni    | Board | Yes   |



# **Q3. Numerical Descriptive Features**

• What are possible categories for "Experience" feature?

| Experience | Degree | Job   | Class |
|------------|--------|-------|-------|
| 12         | HS     | Board | No    |
| 20         | Uni    | Board | Yes   |
| 15         | HS     | Board | No    |
| 10         | HS     | Hcare | Yes   |
| 3          | HS     | Hcare | No    |
| 7          | HS     | Board | Yes   |
| 5          | None   | Edu   | No    |
| 2          | None   | Hcare | No    |
| 6          | Uni    | Edu   | Yes   |
| 11         | Uni    | Board | Yes   |



## **Q4. Numerical Target Feature**

• Suppose that we have the following leaves after splitting the data set. Which classification is better and why?

**Target Features** 

| Descriptive readures range readures |        |     |            |
|-------------------------------------|--------|-----|------------|
| Experience                          | Degree | Job | Salary (K) |
| *                                   | *      | *   | 20         |
| *                                   | *      | *   | 40         |
| *                                   | *      | *   | 50         |
| *                                   | *      | *   | 65         |
| *                                   | *      | *   | 70         |
| *                                   | *      | *   | 25         |
| *                                   | *      | *   | 95         |
| *                                   | *      | *   | 100        |
| *                                   | *      | *   | 110        |
| *                                   | *      | *   | 45         |

**Descriptive Features** 

| Leaf 1 | 20 | 100 40  | 95  |
|--------|----|---------|-----|
| Leaf 2 | 50 | 65 70   | 110 |
| Leaf 3 | 45 | 25      |     |
| Leaf 1 | 70 | 100 110 | 95  |
| Leaf 2 | 40 | 45 65   | 50  |
| Leaf 3 | 25 | 20      |     |

$$var(a) = \frac{\sum_{i=1}^{n} (a_i - \overline{a})^2}{n-1}$$



### Q5. Homework

- We would like to predict the sex of a person based on two binary attributes: leg-cover (pants or skirts) and facial-hair (some or none). We have a data set of 1000 individuals, half male and half female. 50% of females wear skirt, and no male wears skirt. 75% of males and 25% of females have facial hair.
- Which attribute should be used as the root of the decision tree based on Entropy?

