

The PREV programming language

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1 Lexical structure

Programs in the PREV programming language are written in ASCII character set (no additional characters denoting post-alveolar consonants are allowed).

Programs in the PREV programming language consist of the following lexical elements:

- *Literals*:
 - literals of type void: **none**
 - literals of type bool: **true false**
 - literals of type char:
An character with the character code in decimal range 32...126 (from space to ~) enclosed in single quotes (').
 - literals of type int:
A nonempty finite string of digits (0...9) optionally preceded by a sign (+ or -).
 - literals of pointer types: **null**
- *Symbols*:
`! | ^ & == != <= >= < > + - * / % $ @ = . , : ; [] () { }`
- *Keywords*:
`arr bool char del do else end fun if int new ptr rec then typ var void where while`
- *Identifiers*:
A nonempty finite string of letters (A...Z and a...z), digits (0...9), and underscores (_) that (a) starts with either a letter or an underscore and (b) is not a keyword.
- *Comments*:
A string of characters starting with a hash (#) and extending to the end of line.
- *White space*:
Space, horizontal tab (HT), line feed (LF) and carriage return (CR). Line feed alone denotes the end of line within a source file.

Lexical elements should be recognised from left to right using the longest match approach.

2 Syntax structure

The concrete syntax of the PREV programming language is defined by context free grammar with the start symbol *expr* and productions

(literal)	$expr \rightarrow literal$
(unary expression)	$expr \rightarrow unop\ expr$
(binary expression)	$expr \rightarrow expr\ binop\ expr$
(variable access)	$expr \rightarrow identifier$
(function call)	$expr \rightarrow identifier([expr\ \{, expr\}])$
(element access)	$expr \rightarrow expr[expr]$
(component access)	$expr \rightarrow expr.identifier$
(type cast)	$expr \rightarrow [type]\ expr$
(memory allocation)	$expr \rightarrow new\ type$
(memory deallocation)	$expr \rightarrow del\ expr$
(compound expression)	$expr \rightarrow \{ stmt\ \{; stmt\} : expr\ [where\ decl\ \{; decl\}] \}$
(enclosed expression)	$expr \rightarrow (expr)$
(atomic type)	$type \rightarrow void\ \ bool\ \ char\ \ int$
(array type)	$type \rightarrow arr\ [expr]\ type$
(record type)	$type \rightarrow rec\ (identifier : type\ \{, identifier : type\})$
(pointer type)	$type \rightarrow ptr\ type$
(named type)	$type \rightarrow identifier$
(expression)	$stmt \rightarrow expr$
(assignment)	$stmt \rightarrow expr = expr$
(conditional)	$stmt \rightarrow if\ expr\ then\ stmt\ \{; stmt\} [else\ stmt\ \{; stmt\}] end$
(loop)	$stmt \rightarrow while\ expr\ do\ stmt\ \{; stmt\} end$
(type declaration)	$decl \rightarrow typ\ identifier : type$
(variable declaration)	$decl \rightarrow var\ identifier : type$
(function declaration)	$decl \rightarrow fun\ identifier([identifier : type\ \{, identifier : type\}]) : type [=expr]$

where *literal* denotes any literal, *unop* denotes an unary operator (any of `!`, `+`, `-`, `$` and `@`) and *binop* denotes a binary operator (any of `|`, `^`, `&`, `==`, `!=`, `<=`, `>=`, `<`, `>`, `+`, `-`, `*`, `/` and `%`). In the grammar above, braces typeset as `{}` enclose sentential forms that can repeated zero or more times, brackets typeset as `[]` enclose sentential forms that can be present or not while braces and brackets typeset as `{}` and `[]` denote characters that are a part of the program text.

Relational operators are non-associative, all other binary operators are left associative.

The precedence of operators is as follows:

<code> ^</code>	THE LOWEST PRECEDENCE
<code>&</code>	
<code>== != <= >= < ></code>	
<code>+ -</code>	(binary <code>+</code> and <code>-</code>)
<code>* / %</code>	
<code>! + - \$ @ new del type-cast</code>	(unary <code>+</code> and <code>-</code>)
<code>array-access component-access</code>	THE HIGHEST PRECEDENCE

3 Semantic structure

3.1 Name binding

Let function $\llbracket \cdot \rrbracket_{\text{BIND}}$ binds a name to its declaration according to the rules of namespaces and scopes as described below. Hence, the value of function $\llbracket \cdot \rrbracket_{\text{BIND}}$ depends on the context of its argument.

Namespaces. There are two kinds of a namespaces:

1. Names of types, functions, variables and parameters belong to one single global namespace.
2. Names of record components belong to record-specific namespaces, i.e., each record defines its own namespace containing names of its components.

Scopes. A new scope is created in two ways:

1. Compound expression

$$\{ \textit{stmt} \{; \textit{stmt}\} : \textit{expr} [\textbf{where} \textit{decl} \{; \textit{decl}\}] \}$$

creates a new scope. The scope starts right after $\{$ and ends just before $\}$.

2. Function declaration

$$\textbf{fun } \textit{identifier} ([\textit{identifier} : \textit{type} \{, \textit{identifier} : \textit{type}\}]) : \textit{type} [= \textit{expr}]$$

creates a new scope. The name of a function, the types of parameters and the type of a result belong to the outer scope while the names of parameters and the expression denoting the function body belong to the scope created by the function declaration.

All names declared within a given scope are visible in the entire scope unless hidden by a declaration in the nested scope. A name can be declared within the same scope at most once.

3.2 Constant subexpressions

Let $I = \{(-2^{63}) \dots (2^{63} - 1)\}$. Semantic function

$$\llbracket \cdot \rrbracket_{\text{VAL}} : \mathcal{P} \rightarrow I$$

maps phrases of PREV to the integer values they denote. It is defined by the following rules:

$$\frac{\textit{lexeme}(\text{INTEGER}) \in I}{\llbracket \text{INTEGER} \rrbracket_{\text{VAL}} = \textit{lexeme}(\text{INTEGER})} \quad \frac{\llbracket \textit{expr} \rrbracket_{\text{VAL}} = n}{\llbracket (\textit{expr}) \rrbracket_{\text{VAL}} = n}$$

$$\frac{\llbracket \textit{expr} \rrbracket_{\text{VAL}} = n \quad \text{op} \in \{+, -\}}{\llbracket \text{op } \textit{expr} \rrbracket_{\text{VAL}} = \text{op } n} \quad \frac{\llbracket \textit{expr}_1 \rrbracket_{\text{VAL}} = n_1 \quad \llbracket \textit{expr}_2 \rrbracket_{\text{VAL}} = n_2 \quad \text{op} \in \{+, -, *, /, \%\}}{\llbracket \textit{expr}_1 \text{ op } \textit{expr}_2 \rrbracket_{\text{VAL}} = n_1 \text{ op } n_2}$$

In all other cases the value of $\llbracket \cdot \rrbracket_{\text{VAL}}$ is undefined (denoted by \perp).

3.3 Lvalues

Semantic function

$$\llbracket \cdot \rrbracket_{\text{LVAL}} : \mathcal{P} \rightarrow \{\textbf{true}, \textbf{false}\}$$

marks phrases representing lvalues. It is defined by the following rules:

$$\frac{\llbracket \text{IDENTIFIER} \rrbracket_{\text{BIND}} \in \{(\textit{variable declaration}), (\textit{parameter declaration})\}}{\llbracket \text{IDENTIFIER} \rrbracket_{\text{LVAL}} = \textbf{true}}$$

$$\frac{\llbracket \textit{expr} \rrbracket_{\text{LVAL}} = \textbf{true}}{\llbracket \textbf{@ } \textit{expr} \rrbracket_{\text{LVAL}} = \textbf{true}} \quad \frac{\llbracket \textit{expr} \rrbracket_{\text{LVAL}} = \textbf{true}}{\llbracket \textit{expr} [\textit{expr}'] \rrbracket_{\text{LVAL}} = \textbf{true}} \quad \frac{\llbracket \textit{expr} \rrbracket_{\text{LVAL}} = \textbf{true}}{\llbracket \textit{expr} . \text{IDENTIFIER} \rrbracket_{\text{LVAL}} = \textbf{true}}$$

In all other cases the value of $\llbracket \cdot \rrbracket_{\text{LVAL}}$ equals **false**.

3.4 Type system

A set

$$\begin{aligned}
T_d = & \{\mathbf{void}, \mathbf{bool}, \mathbf{char}, \mathbf{int}\} && \text{(atomic types)} \\
& \cup \{\mathbf{arr}(n \times \tau) \mid n \in I \wedge \tau \in T_d\} && \text{(arrays)} \\
& \cup \{\mathbf{rec}(\tau_1, \dots, \tau_n) \mid n \in I \wedge \tau_1, \dots, \tau_n \in T_d\} && \text{(records)} \\
& \cup \{\mathbf{ptr}(\tau) \mid \tau \in T_d\} && \text{(pointers)}
\end{aligned}$$

denotes a set of all data types of PREV. A set

$$\begin{aligned}
T = & T_d && \text{(data types)} \\
& \cup \{(\tau_1, \dots, \tau_n) \rightarrow \tau \mid n \geq 0 \wedge \tau_1, \dots, \tau_n, \tau \in T_d\} && \text{(functions)}
\end{aligned}$$

denotes a set of all types of PREV.

Two types are equal if they share the same structure.

Type expressions. Semantic function

$$\llbracket \cdot \rrbracket_{\text{ISTYPE}}: \mathcal{P} \rightarrow T_d$$

maps phrases of PREV to types (as it is defined using $\llbracket \cdot \rrbracket_{\text{BIND}}$ it depends on the context of its argument). It is defined by the following rules:

$$\overline{\llbracket \mathbf{void} \rrbracket_{\text{ISTYPE}}} = \mathbf{void} \quad \overline{\llbracket \mathbf{bool} \rrbracket_{\text{ISTYPE}}} = \mathbf{bool} \quad \overline{\llbracket \mathbf{char} \rrbracket_{\text{ISTYPE}}} = \mathbf{char} \quad \overline{\llbracket \mathbf{int} \rrbracket_{\text{ISTYPE}}} = \mathbf{int}$$

$$\frac{\llbracket expr \rrbracket_{\text{VAL}} = n \quad \llbracket type \rrbracket_{\text{ISTYPE}} = \tau}{\llbracket \mathbf{arr}[expr] type \rrbracket_{\text{ISTYPE}} = \mathbf{arr}(n \times \tau)} \quad \frac{\llbracket type \rrbracket_{\text{ISTYPE}} = \tau}{\llbracket \mathbf{ptr} type \rrbracket_{\text{ISTYPE}} = \mathbf{ptr}(\tau)}$$

$$\frac{n > 0 \quad \llbracket type_1 \rrbracket_{\text{ISTYPE}} = \tau_1, \dots, \llbracket type_n \rrbracket_{\text{ISTYPE}} = \tau_n}{\llbracket \mathbf{rec}\{\text{IDENTIFIER}_1 : type_1, \dots, \text{IDENTIFIER}_n : type_n\} \rrbracket_{\text{ISTYPE}} = \mathbf{rec}(\tau_1, \dots, \tau_n)}$$

$$\frac{\llbracket \text{IDENTIFIER} \rrbracket_{\text{BIND}} = \mathbf{typ} \text{ decl} \quad \llbracket decl \rrbracket_{\text{TYPED}} = \tau}{\llbracket \text{IDENTIFIER} \rrbracket_{\text{ISTYPE}} = \tau}$$

In all other cases the value of $\llbracket \cdot \rrbracket_{\text{ISTYPE}}$ is undefined.

Value expressions and statements. Semantic function

$$\llbracket \cdot \rrbracket_{\text{OFTYPE}}: \mathcal{P} \rightarrow T_d$$

maps phrases of PREV to types (as it is defined using $\llbracket \cdot \rrbracket_{\text{BIND}}$ it depends on the context of its argument). It is defined by the following rules:

$$\overline{\llbracket \mathbf{none} \rrbracket_{\text{OFTYPE}}} = \mathbf{void} \quad \overline{\llbracket \mathbf{null} \rrbracket_{\text{OFTYPE}}} = \mathbf{ptr}(\mathbf{void})$$

$$\overline{\llbracket \mathbf{BOOLEAN} \rrbracket_{\text{OFTYPE}}} = \mathbf{bool} \quad \overline{\llbracket \mathbf{CHAR} \rrbracket_{\text{OFTYPE}}} = \mathbf{char} \quad \overline{\llbracket \mathbf{INTEGER} \rrbracket_{\text{OFTYPE}}} = \mathbf{int}$$

$$\frac{\llbracket expr \rrbracket_{\text{OFTYPE}} = \mathbf{bool}}{\llbracket ! expr \rrbracket_{\text{OFTYPE}} = \mathbf{bool}} \quad \frac{\llbracket expr \rrbracket_{\text{OFTYPE}} = \mathbf{int} \quad \text{op} \in \{+, -\}}{\llbracket \text{op} expr \rrbracket_{\text{OFTYPE}} = \mathbf{int}}$$

$$\frac{\llbracket expr_1 \rrbracket_{\text{OFTYPE}} = \mathbf{bool} \quad \llbracket expr_2 \rrbracket_{\text{OFTYPE}} = \mathbf{bool} \quad \text{op} \in \{!, \wedge, \&\}}{\llbracket expr_1 \text{ op } expr_2 \rrbracket_{\text{OFTYPE}} = \mathbf{bool}}$$

$$\begin{array}{c}
\frac{\llbracket expr_1 \rrbracket_{\text{OFTYPE}} = \mathbf{int} \quad \llbracket expr_2 \rrbracket_{\text{OFTYPE}} = \mathbf{int} \quad \text{op} \in \{+, -, *, /, \%\}}{\llbracket expr_1 \text{ op } expr_2 \rrbracket_{\text{OFTYPE}} = \mathbf{int}} \\
\\
\frac{\llbracket expr_1 \rrbracket_{\text{OFTYPE}} = \tau \quad \llbracket expr_2 \rrbracket_{\text{OFTYPE}} = \tau \quad \text{op} \in \{=, !=, <, >, <=, >=\} \\ \tau \in \{\mathbf{bool}, \mathbf{char}, \mathbf{int}\} \cup \{\mathbf{ptr}(\tau) \mid \tau \in T_d\}}{\llbracket expr_1 \text{ op } expr_2 \rrbracket_{\text{OFTYPE}} = \mathbf{bool}} \\
\\
\frac{\llbracket expr \rrbracket_{\text{OFTYPE}} = \tau \quad \tau \neq \mathbf{void} \quad \llbracket expr \rrbracket_{\text{LVAL}} = \mathbf{true}}{\llbracket \$ expr \rrbracket_{\text{OFTYPE}} = \mathbf{ptr}(\tau)} \quad \frac{\llbracket expr \rrbracket_{\text{OFTYPE}} = \mathbf{ptr}(\tau) \quad \tau \neq \mathbf{void}}{\llbracket @ expr \rrbracket_{\text{OFTYPE}} = \tau} \\
\\
\frac{\llbracket type \rrbracket_{\text{ISTYPE}} = \tau \quad \tau \neq \mathbf{void}}{\llbracket \mathbf{new type} \rrbracket_{\text{OFTYPE}} = \mathbf{ptr}(\tau)} \quad \frac{\llbracket expr \rrbracket_{\text{OFTYPE}} = \mathbf{ptr}(\tau) \quad \tau \neq \mathbf{void}}{\llbracket \mathbf{del expr} \rrbracket_{\text{OFTYPE}} = \mathbf{void}} \\
\\
\frac{\llbracket type \rrbracket_{\text{ISTYPE}} = \tau_1 \quad \llbracket expr \rrbracket_{\text{OFTYPE}} = \tau_2 \\ \langle \tau_1, \tau_2 \rangle \in \{\langle \mathbf{void}, \tau \rangle \mid \tau \in T_d\} \cup \\ \{\langle \mathbf{int}, \mathbf{int} \rangle, \langle \mathbf{int}, \mathbf{char} \rangle, \langle \mathbf{int}, \mathbf{bool} \rangle\} \cup \\ \{\langle \mathbf{ptr}(\tau), \mathbf{ptr}(\mathbf{void}) \rangle \mid \tau \in T_d\}}{\llbracket [type] expr \rrbracket_{\text{OFTYPE}} = \tau_1} \\
\\
\frac{\llbracket \text{IDENTIFIER} \rrbracket_{\text{BIND}} = \mathbf{var decl} \quad \llbracket decl \rrbracket_{\text{TYPED}} = \tau}{\llbracket \text{IDENTIFIER} \rrbracket_{\text{OFTYPE}} = \tau} \\
\\
\frac{n \geq 0 \quad \llbracket expr_1 \rrbracket_{\text{OFTYPE}} = \tau_1, \dots, \llbracket expr_n \rrbracket_{\text{OFTYPE}} = \tau_n \\ \llbracket \text{IDENTIFIER} \rrbracket_{\text{BIND}} = \mathbf{fun decl} \quad \llbracket decl \rrbracket_{\text{TYPED}} = (\tau_1, \dots, \tau_n) \rightarrow \tau}{\llbracket \text{IDENTIFIER}(expr_1, \dots, expr_n) \rrbracket_{\text{OFTYPE}} = \tau} \\
\\
\frac{\llbracket expr_1 \rrbracket_{\text{OFTYPE}} = \mathbf{arr}(n \times \tau) \quad \llbracket expr_2 \rrbracket_{\text{VAL}} = n}{\llbracket expr_1 [expr_2] \rrbracket_{\text{OFTYPE}} = \tau} \\
\\
\frac{\llbracket expr \rrbracket_{\text{OFTYPE}} = \mathbf{rec}(\tau_1, \dots, \tau_n) \quad \llbracket \text{IDENTIFIER} \rrbracket_{\text{BIND}} = decl \quad \llbracket decl \rrbracket_{\text{TYPED}} = \tau}{\llbracket expr.\text{IDENTIFIER} \rrbracket_{\text{OFTYPE}} = \tau} \\
\\
\frac{\llbracket stmts \rrbracket_{\text{OFTYPE}} = \tau \quad \llbracket expr \rrbracket_{\text{OFTYPE}} = \tau}{\llbracket \{stmts : expr\} \rrbracket_{\text{OFTYPE}} = \tau} \quad \frac{\llbracket stmts \rrbracket_{\text{OFTYPE}} = \tau \quad \llbracket expr \rrbracket_{\text{OFTYPE}} = \tau}{\llbracket \{stmts : expr \text{ where } decls\} \rrbracket_{\text{OFTYPE}} = \tau} \\
\\
\frac{\llbracket expr \rrbracket_{\text{OFTYPE}} = \tau}{\llbracket (expr) \rrbracket_{\text{OFTYPE}} = \tau} \\
\\
\frac{\llbracket expr \rrbracket_{\text{OFTYPE}} = \mathbf{void} \quad expr = stmt}{\llbracket stmt \rrbracket_{\text{OFTYPE}} = \mathbf{void}} \\
\\
\frac{\llbracket expr_1 \rrbracket_{\text{OFTYPE}} = \tau \quad \llbracket expr_2 \rrbracket_{\text{OFTYPE}} = \tau \quad \llbracket expr_1 \rrbracket_{\text{LVAL}} = \mathbf{true}}{\llbracket expr_1 = expr_2 \rrbracket_{\text{OFTYPE}} = \mathbf{void}} \\
\\
\frac{\llbracket expr \rrbracket_{\text{OFTYPE}} = \mathbf{bool} \quad \llbracket stmts \rrbracket_{\text{OFTYPE}} = \mathbf{void}}{\llbracket \mathbf{if expr then stmts end} \rrbracket_{\text{OFTYPE}} = \mathbf{void}} \\
\\
\frac{\llbracket expr \rrbracket_{\text{OFTYPE}} = \mathbf{bool} \quad \llbracket stmts_1 \rrbracket_{\text{OFTYPE}} = \mathbf{void} \quad \llbracket stmts_2 \rrbracket_{\text{OFTYPE}} = \mathbf{void}}{\llbracket \mathbf{if expr then stmts_1 else stmts_2 end} \rrbracket_{\text{OFTYPE}} = \mathbf{void}}
\end{array}$$

$$\frac{\llbracket expr \rrbracket_{\text{OFTYPE}} = \mathbf{bool} \quad \llbracket stmts \rrbracket_{\text{OFTYPE}} = \mathbf{void}}{\llbracket \mathbf{while} \ expr \ \mathbf{do} \ stmts \ \mathbf{end} \rrbracket_{\text{OFTYPE}} = \mathbf{void}}$$

$$\frac{\llbracket stmt_1 \rrbracket_{\text{OFTYPE}} = \mathbf{void}, \dots, \llbracket stmt_n \rrbracket_{\text{OFTYPE}} = \mathbf{void}}{\llbracket stmt_1; \dots; stmt_n \rrbracket_{\text{OFTYPE}} = \mathbf{void}}$$

In all other cases the value of $\llbracket \cdot \rrbracket_{\text{OFTYPE}}$ is undefined.

Declarations. Semantic function

$$\llbracket \cdot \rrbracket_{\text{TYPED}}: \mathcal{P} \rightarrow T$$

maps phrases of PREV to types (as it is defined using $\llbracket \cdot \rrbracket_{\text{BIND}}$ it depends on the context of its argument). It is defined by the following rules:

$$\frac{\llbracket type \rrbracket_{\text{ISTYPE}} = \tau}{\llbracket \text{IDENTIFIER} : type \rrbracket_{\text{TYPED}} = \tau}$$

$$\frac{n \geq 0 \quad \llbracket decl_1 \rrbracket_{\text{TYPED}} = \tau_1, \dots, \llbracket decl_n \rrbracket_{\text{TYPED}} = \tau_n \quad \llbracket type \rrbracket_{\text{ISTYPE}} = \tau \quad \tau_1, \dots, \tau_n, \tau \in \{\mathbf{bool}, \mathbf{char}, \mathbf{int}\} \cup \{\mathbf{ptr}(\tau) \mid \tau \in T_d\}}{\llbracket \text{IDENTIFIER}(decl_1, \dots, decl_n) : type \rrbracket_{\text{TYPED}} = (\tau_1, \dots, \tau_n) \rightarrow \tau}$$

In all other cases the value of $\llbracket \cdot \rrbracket_{\text{TYPED}}$ is undefined.