Practicum - Consultation: 29.02.2024, 09-11

Please send your Group solutions to corneliafranziska.richter@vetpharm.uzh.ch on time.

What	File name	When
Group solutions	"01worksheet-Group-Name.zip"	04.03.2024 at 7 am.

Please upload all files to OLAT on time.

What	File name	When
Individual project	"01worksheet-Your-Name.zip"	04.03.2024 at 7 am.
Group contribution	"o2contribution-Group-Name.zip"	05.03.2024 at 22 pm.

Individual tasks

Your of worksheet-Your-Name.zip file contains reproducible code necessary to generate your results and your report together with the resulting pdf-file.

Exercise 1 (Individual project (Part 1))

This individual exercise has 3 steps.

- (a) Explain the main goal of the study by Baeten et al. (2013).
- (b) Apply classical methods to analyse the data in Table 1.
- (c) Compute the optimal sample size for a 1:1 design for comparison of 60% (Secukinumab) and 25% (Placebo) with power 80% and significance level 5%.

Table 1: ASAS20 responders at week 6: data provided explicitly and implicitly in Table 2 of Baeten et al. (2013).

Group	п	Responders
		x (%)
Secukinumab	23	14 (60.9%)
Placebo	6	1 (16.7%)

Report your results.

Exercise 2 (Individual task: elicitation of your personal opinion)

Consider the height of adult Swiss females. What is your personal opinion about the location (mean) and the spread (standard deviation) of this distribution (in cm)? Report the values of both the mean and the standard deviation.

Exercise 3 (Individual task: installation of programs)

Given the system you are working with, follow the instructions to download and install the following programs and packages:

- 1. R: https://www.r-project.org/
- 2. RStudio: https://posit.co/
- 3. JAGS: https://mcmc-jags.sourceforge.io/
- 4. R-packages: rjags, coda, bayesmeta

Please report: Were you able to successfully download and install these programs and packages? Did you face any difficulties?

Exercise 4 (Individual task: your expectations)

Please answer the following questions.

- 1. What is your motivation to attend this course?
- 2. What would you like to learn in this course and why?
- 3. Have you already learned or used Bayesian methods?
- 4. If yes, which Bayesian methods and programs are you familiar with?
- 5. What is your experience with scientific writing?

Check the content of the diagram and summarize your thoughts on the typical structure of a scientific report.

Group tasks

Your of worksheet-Group-Name.zip (one per group) file contains reproducible code necessary to generate your results and your report together with the resulting pdf-file, which can contain scans of your handwritten solutions. List the names of students who contributed to the solution of group tasks.

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Exercise 5 (Bayes theorem)

Prove the conditional Bayes theorem:

$$P[A|B,I] = \frac{P[B|A,I]P[A|I]}{P[B|I]}$$

Exercise 6 (Application of the Bayes theorem)

Consider a diagnostic test with sensitivity $P[T^+|D^+] = 0.95$ and specificity $P[T^-|D^-] = 0.94$. What is the probability that someone tested positive T^+ actually is healthy $P[D^-|T^+]$ given that the prevalence of the disease is $P[D^+] = 0.001$. Discuss your findings.

Exercise 7 (Monte Carlo: random sample vs the true distribution)

Let the random variable X follow the target $N(\mu, \sigma^2)$ distribution with $\mu = 160$ and $\sigma = 20$. For set.seed(44566), use the rnorm() function in R and generate a Monte Carlo sample (*i.i.d* realisations of X) of size M = 1000 stored in the vector Xs.

Accomplish the following tasks given the MC sample in *Xs*:

- 1. Report the true values of the expectation (mean), standard deviation, variance, median, and (0.025, 0.5, 0.975) quantiles of *X*;
- 2. Plot the traceplot of the MC sample in *Xs*;
- 3. Plot the histogram of the MC sample in Xs with the overlayed true density curve;
- 4. Summarize the MC sample in *Xs* by computing sample mean, standard deviation, variance and (0.025, 0.5, 0.975) quantiles and compare them with the true values;
- 5. Use the MC sample in Xs to estimate the probabilities that P[X > 175] and P[150 < X < 180] and compare both estimates with the true values obtained with the pnorm() function.

Exercise 8 (Bayes Factor)

Let $Y|\mu \sim N(\mu, \kappa^{-1})$ with known variance κ^{-1} . For H_0 , $\mu = \mu_0$. For H_1 , we suppose that the parameter μ is known with prior distribution $\mu \sim N(\nu, \lambda^{-1})$, with ν and λ fixed.

(a) Show that

$$f(y|H_1) = \frac{1}{\sqrt{2\pi}} \sqrt{\frac{\kappa \lambda}{\kappa + \lambda}} \exp\left\{-\frac{\kappa \lambda}{2(\kappa + \lambda)} (y - \nu)^2\right\}$$



- (b) Determine analytically the Bayes factor $BF_{01}(y)$.
- (c) Show that $BF_{01}(y)$ tends to ∞ as λ tends to 0 ($BF_{01}(y) \xrightarrow{\lambda \to 0} \infty$).
- (d) Compute the posterior probability of H_0 , denoted by $P[H_0|y]$, if $P[H_0] = P[H_1] = 0.5$, $\mu_0 = 0$, $\kappa = 1$, $\nu = 2$, $\lambda = 1/2$, and $\nu = 1$. Interpret this result.

Exercise 9 (Calibration of *p*-values: pCalibrate)

Use the twoby2Calibrate function of pCalibrate to compute the minimum Bayes factor (BF) and p-values from Fisher's exact test applied to data provided in Table 1 of Exercise 1. To get the result for a confirmative test, assume that the alternative is simple. Format this BF with function formatBF (Held and Ott, 2018). Is BF increasing or decreasing the prior odds of no effect $P[H_0]$? Assume that the prior probability of no effect $P[H_0]$ is equal 50%. Compute the posterior probability $P[H_0|\text{data}]$ with function BF2pp and interpret the result.

Group contributions to the "Big picture"

Exercise 10 (Group contributions for the lecture on 07.03.2024)

Please prepare a group contribution, which your group will present (ca. 5 min) during the next lecture.

- (2.1) History of the Beta distribution and its properties (expectation, variance, functions in R, animation).
- (2.2) History of the Binomial distribution and its properties (expectation, variance, functions in R).
- (2.3) History of the Normal distribution and its properties (expectation, variance, functions in R).
- (2.4) Discuss the meaning of confidence intervals (Held and Sabanés Bové (2020, p. 57) and animation) and list procedures in R for the computation of confidence intervals for binary data. Demonstrate the use of the BinomCI function from the DescTools package.

Make sure that the file o2contribution-Group-Name.zip (one per group) contains the file and the R code you want to present.

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References

Baeten, D., X. Baraliakos, J. Braun, J. Sieper, P. Emery, D. van der Heijde, I. McInnes, J. van Laar, R. Landewé, P. Wordsworth, J. Wollenhaupt, H. Kellner, J. Paramarta, J. Wei, A. Brachat, S. Bek, D. Laurent, Y. Li, Y. Wang, A. Bertolino, S. Gsteiger, A. Wright, and W. Hueber (2013). Anti-interleukin-17A monoclonal antibody secukinumab in treatment of ankylosing spondylitis: a randomised, double-blind, placebo-controlled trial. *The Lancet* 382, 1705–1713.

Held, L. and M. Ott (2018). On p-values and Bayes Factors. *Annual Review of Statistics and Its Application* 5, 393–419.

Held, L. and D. Sabanés Bové (2020). *Likelihood and Bayesian Inference: With Applications in Biology and Medicine*. Springer (https://link.springer.com/book/10.1007/978-3-662-60792-3, https://github.com/lheld/HSB).

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