# Worksheet 05 Group 2

Andrea Staub Emanuel Mauch Holly Vuarnoz Jan Hohenheim Sophie Haldemann

```
library(glue)
library(rjags)
library(INLA)
library(MASS)
library(ggplot2)
library(patchwork)
library(coda)
library(stableGR)
source("05ess.r")
```

#### Exercise 3

Run the code provided in the file 05normal\_example\_JAGS.R and explore the interfaces in R to JAGS. Comment your findings. -> The comments can be found below the code chunks.

clearing environment, set.seed for reproducibility and set path to .txt file with model

#### Interface in R to JAGS: rjags

## 1 base::Variance

```
## 2
                      TRUE
         base::Mean
## 3
        base::Trace
                      TRUE
list.factories(type = "sampler")
##
               factory status
## 1
      bugs::BinomSlice
                          TRUE
## 2
             bugs::RW1
                          TRUE
## 3
        bugs::Censored
                          TRUE
## 4
             bugs::Sum
                          TRUE
## 5
            bugs::DSum
                          TRUE
## 6
       bugs::Conjugate
                          TRUE
## 7
       bugs::Dirichlet
                          TRUE
## 8
                          TRUE
         bugs::MNormal
## 9
          base::Finite
                          TRUE
## 10
           base::Slice
                          TRUE
set.factory(name = "base::Slice", type = "sampler", state = FALSE)
## NULL
list.factories(type = "sampler")
##
               factory status
## 1
     bugs::BinomSlice
                          TRUE
## 2
             bugs::RW1
                          TRUE
## 3
        bugs::Censored
                          TRUE
## 4
                          TRUE
             bugs::Sum
## 5
            bugs::DSum
                          TRUE
## 6
       bugs::Conjugate
                          TRUE
## 7
                          TRUE
       bugs::Dirichlet
## 8
                          TRUE
         bugs::MNormal
## 9
          base::Finite
                          TRUE
## 10
           base::Slice FALSE
set.factory(name = "base::Slice", type = "sampler", state = TRUE)
## NULL
list.factories(type = "sampler")
##
               factory status
## 1
                          TRUE
     bugs::BinomSlice
## 2
             bugs::RW1
                          TRUE
## 3
                          TRUE
        bugs::Censored
## 4
             bugs::Sum
                          TRUE
## 5
                          TRUE
            bugs::DSum
## 6
       bugs::Conjugate
                          TRUE
## 7
       bugs::Dirichlet
                          TRUE
## 8
         bugs::MNormal
                          TRUE
## 9
                          TRUE
          base::Finite
## 10
           base::Slice
                          TRUE
list.modules()
## [1] "basemod" "bugs"
load.module("glm")
```

```
## module glm loaded
list.modules()

## [1] "basemod" "bugs" "glm"

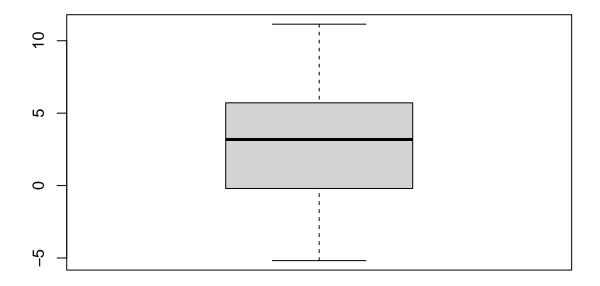
unload.module("glm")

## Module glm unloaded
list.modules()
```

```
## [1] "basemod" "bugs"
```

With list.factories a data frame with two columns is returned, the first column shows the names of the factory objects in the currently loaded modules, and the second column is a logical vector indicating whether the corresponding factory is active or not. With list.modules() the loaded modules can be listed. With load.module("module\_name") and unload.module("module\_name") modules can be loaded or unloaded.

```
######################
## Introduction
####################
# generating data
#mu <- 4
#sigma2 <- 16
#n <- 30
#y <- rnorm(n=n, mean=mu, sd=sqrt(sigma2))</pre>
# Load the data
# round(y,3)
y \leftarrow c(3.048, 2.980, 2.029, 7.249, -0.259, 3.061, 4.059, 6.370, 7.902, 1.926,
       9.094,10.489,-0.384,-3.096,2.315,5.830,-1.542,-1.544,5.714,
       -5.182,3.828,-4.038,2.169,5.087,-0.201,4.880,3.302,3.859,
       11.144,5.564)
par(mfrow = c(1, 1))
boxplot(y)
```



```
## Min. 1st Qu. Median Mean 3rd Qu. Max.
## -5.1820 0.3307 3.1815 3.1884 5.6765 11.1440

sd(y)

## [1] 4.046692

# Define the parameters of the prior distributions
mu0 <- -3
sigma2_0 <- 4
a0 <- 1.6
b0 <- 0.4</pre>
```

random datapoints were generated from a normal distribution with mean =4 and standard deviation =4. The parameters of the prior distribution are defined. Mean value from summary is with 3.1884333 not that close to mean =4.

```
list(prec = list(prior="loggamma",param=c(a0,b0)))),
control.fixed = list(mean.intercept=mu0, prec.intercept=1/sigma2_0))
```

As input for INLA the previously defined parameters and the random sampled datapoints are used. INLA is used to approximate distribution.

```
##############################
# Step 2: JAGS model file as a string in rjags with coda
##############################
set.seed(44566)
library(rjags)
library(coda)
#sessionInfo()
wb_data <- list( N=30,
                 y=c(3.048,2.980,2.029,7.249,-0.259,3.061,4.059,6.370,7.902,1.926,
                     9.094,10.489,-0.384,-3.096,2.315,5.830,-1.542,-1.544,5.714,
                     -5.182,3.828,-4.038,2.169,5.087,-0.201,4.880,3.302,3.859,
                     11.144,5.564)
)
wb_inits <- list( mu=-0.2381084, inv_sigma2=0.3993192 )</pre>
modelString = " # open quote for modelString
model{
# likelihood
for (i in 1:N){
y[i] ~ dnorm( mu, inv_sigma2 )
# Priors
mu ~ dnorm( -3, 0.25 ) # prior for mu N(mu0, prec=1/sigma2_0)
inv_sigma2 ~ dgamma( 1.6, 0.4 ) # prior for precision G(a0, b0)
# transformations
# deterministic definition of variance
sigma2 <- 1/inv_sigma2
# deterministic definition of standard deviation
sigma <- sqrt(sigma2)</pre>
" # close quote for modelString
writeLines(modelString, con="TempModel.txt") # write to a file
```

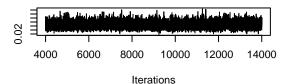
The input for JAGS is defined as a list. The model is printed to a new .txt file. N is set to 30 and N samples are drawn from a normal distribution with mean mu and the precision as standard deviation. Mu follows a normal prior and the precision a gamma prior. The variance and then the standard deviation are estimated from the precision.

```
# model initiation
model.jags <- jags.model(</pre>
 file = "TempModel.txt",
 data = wb_data,
 inits = wb_inits,
 n.chains = 1,
  n.adapt = 4000
## Compiling model graph
##
      Resolving undeclared variables
##
      Allocating nodes
## Graph information:
##
      Observed stochastic nodes: 30
##
      Unobserved stochastic nodes: 2
##
      Total graph size: 41
##
## Initializing model
str(model.jags)
## List of 8
## $ ptr :function ()
## $ data :function ()
## $ model :function ()
## $ state :function (internal = FALSE)
## $ nchain :function ()
## $ iter
              :function ()
## $ sync
               :function ()
## $ recompile:function ()
## - attr(*, "class") = chr "jags"
class(model.jags)
## [1] "jags"
attributes (model. jags)
## $names
## [1] "ptr"
                    "data"
                                "model"
                                             "state"
                                                         "nchain"
                                                                      "iter"
                    "recompile"
## [7] "sync"
## $class
## [1] "jags"
list.samplers(model.jags)
## $`bugs::ConjugateNormal`
## [1] "mu"
##
## $`bugs::ConjugateGamma`
## [1] "inv_sigma2"
```

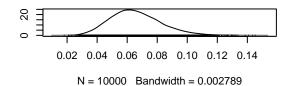
A jags model with only one chain is initiated. The previously generated TempModel.txt file is used. The number of iterations for adaption is set to 4000.

```
# burn-in
update(model.jags, n.iter = 4000)
# sampling
fit.jags.coda <- coda.samples(</pre>
 model = model.jags,
 variable.names = c("mu", "sigma2", "inv_sigma2"),
 n.iter = 10000,
 thin = 1
str(fit.jags.coda)
## List of 1
## $ : 'mcmc' num [1:10000, 1:3] 0.0607 0.1019 0.0835 0.0568 0.1072 ...
    ..- attr(*, "dimnames")=List of 2
##
    ....$ : NULL
   ....$ : chr [1:3] "inv_sigma2" "mu" "sigma2"
## ..- attr(*, "mcpar")= num [1:3] 4001 14000 1
## - attr(*, "class")= chr "mcmc.list"
class(fit.jags.coda)
## [1] "mcmc.list"
attributes(fit.jags.coda)
## $class
## [1] "mcmc.list"
summary(fit.jags.coda)
##
## Iterations = 4001:14000
## Thinning interval = 1
## Number of chains = 1
## Sample size per chain = 10000
## 1. Empirical mean and standard deviation for each variable,
##
     plus standard error of the mean:
##
##
                            SD Naive SE Time-series SE
## inv_sigma2 0.06572 0.01677 0.0001677 0.0001798
              2.44852 0.70995 0.0070995
                                              0.0076083
             16.27816 4.46477 0.0446477
## sigma2
                                              0.0483250
## 2. Quantiles for each variable:
##
##
                 2.5%
                         25%
                                   50%
                                            75%
                                                97.5%
## inv_sigma2 0.03686 0.0539 0.06425 0.07614 0.1025
             0.98945 1.9902 2.46585 2.92163 3.8129
## sigma2
             9.75956 13.1336 15.56520 18.55397 27.1266
#print(fit.jags.coda)
plot(fit.jags.coda)
```

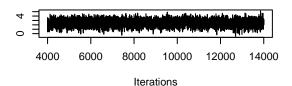
#### Trace of inv\_sigma2



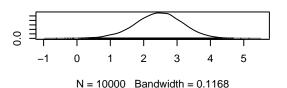
#### Density of inv\_sigma2



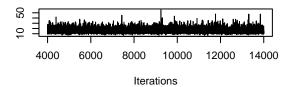
#### Trace of mu



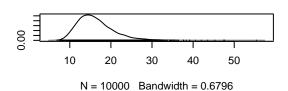
#### Density of mu



## Trace of sigma2



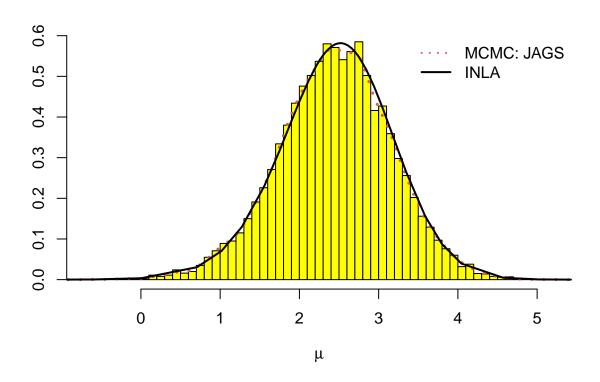
## Density of sigma2



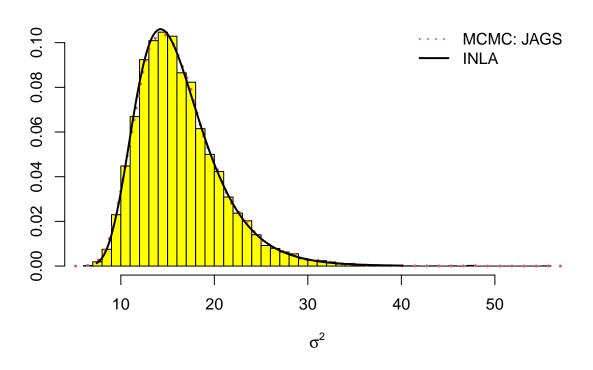
```
# store samples for each parameter from the chain into separate objects
m.fit.jags.coda <- as.matrix(fit.jags.coda)
mu.sim <- m.fit.jags.coda[,"mu"]
sigma2.sim <- m.fit.jags.coda[,"sigma2"]
inv_sigma2.sim <- m.fit.jags.coda[,"inv_sigma2"]

library(MASS)

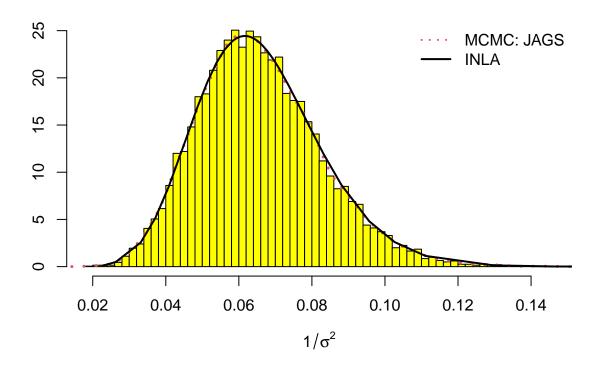
par(mfrow=c(1,1))
# plot for mean
rg <- range(inla.output$marginals.fixed$"(Intercept)"[,2])
truehist(mu.sim, prob=TRUE, col="yellow", xlab=expression(mu),ylim=rg)
lines(density(mu.sim),lty=3,lwd=3, col=2)
lines(inla.output$marginals.fixed$"(Intercept)",lwd=2)
legend("topright",c("MCMC: JAGS","INLA"),lty=c(3,1),lwd=c(2,2),col=c(2,1),cex=1.0,bty="n")</pre>
```



```
# plot for variance
m_var <-inla.tmarginal(function(x) 1/x, inla.output$marginals.hyperpar[[1]])
rg <- range(m_var[,2])
truehist(sigma2.sim, prob=TRUE, col="yellow", xlab=expression(sigma^2),ylim=rg)
lines(density(sigma2.sim),lty=3,lwd=3, col=2)
lines(m_var,lwd=2)
legend("topright",c("MCMC: JAGS","INLA"),lty=c(3,1),lwd=c(2,2),col=c(2,1),cex=1.0,bty="n")</pre>
```



```
# plot for precision
truehist(inv_sigma2.sim, prob=TRUE, col="yellow", xlab=expression(1/sigma^2))
lines(density(inv_sigma2.sim),lty=3,lwd=3, col=2)
lines(inla.output$marginals.hyperpar[[1]],lwd=2)
legend("topright",c("MCMC: JAGS","INLA"),lty=c(3,1),lwd=c(2,2),col=c(2,1),cex=1.0,bty="n")
```



The burn in period is set to 4000. After the burn in 10000 iterations are done to fit the model. The traceplots look good and stable. When looking at the traceplots we can see that the approximations for mu and sigma^2 from JAGS and INLA look similar but differ just a little bit.

```
# JAGS several chains
wb_inits <- function() {</pre>
 list(mu = rnorm(1),
     inv_sigma2 = runif(1)
 )
}
\# model initialisation
model.jags <- jags.model(</pre>
 file = "TempModel.txt",
 data = wb_data,
 inits = wb inits,
 n.chains = 4,
 n.adapt = 4000
)
##
  Compiling model graph
##
    Resolving undeclared variables
##
    Allocating nodes
## Graph information:
```

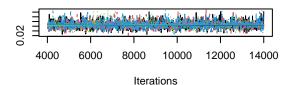
```
##
      Observed stochastic nodes: 30
##
      Unobserved stochastic nodes: 2
##
      Total graph size: 41
##
## Initializing model
# burn-in
update(model.jags, n.iter = 4000)
# sampling/monitoring
fit.jags.coda <- coda.samples(</pre>
 model = model.jags,
 variable.names = c("mu", "sigma2", "inv_sigma2"),
 n.iter = 10000,
 thin = 10
)
\#n.thin < -floor((n.iter-n.adapt)/500)
#floor((10000-4000)/500)=12
```

Now again JAGS is used with the same model but instead of only one chain, 4 chains are used instead. The burn in period is again 4000.

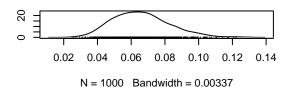
```
summary(fit.jags.coda)
##
## Iterations = 4010:14000
## Thinning interval = 10
## Number of chains = 4
## Sample size per chain = 1000
## 1. Empirical mean and standard deviation for each variable,
##
      plus standard error of the mean:
##
                            SD Naive SE Time-series SE
##
                  Mean
## inv_sigma2 0.06595 0.01683 0.000266
                                             0.0002821
               2.47872 0.71987 0.011382
                                             0.0110102
## mu
              16.21930 4.43271 0.070087
                                             0.0751751
## sigma2
##
## 2. Quantiles for each variable:
##
                 2.5%
                           25%
                                    50%
                                             75%
                                                   97.5%
## inv_sigma2 0.03758 0.05393 0.06465 0.07631 0.1027
              0.98807 2.00657 2.48768 2.96169 3.8591
## sigma2
              9.73704 13.10448 15.46830 18.54279 26.6125
```

plot(fit.jags.coda)

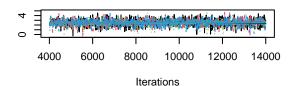
## Trace of inv\_sigma2



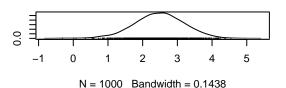
#### Density of inv\_sigma2



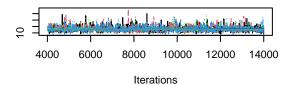
#### Trace of mu



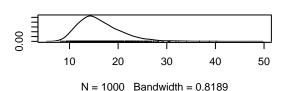
#### Density of mu



## Trace of sigma2

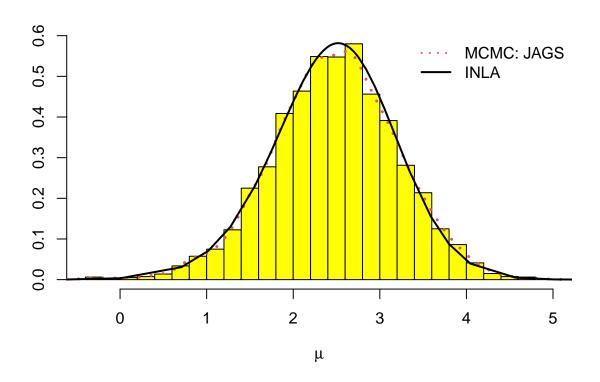


## Density of sigma2

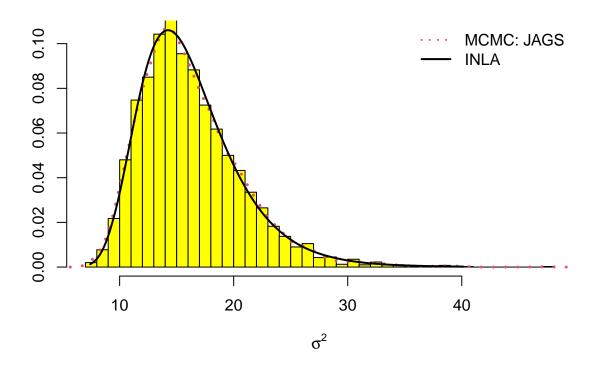


```
# store samples for each parameter from the chains into separate vectors
m.fit.jags.coda <-as.matrix(fit.jags.coda)
mu.sim <- m.fit.jags.coda[,"mu"]
sigma2.sim <- m.fit.jags.coda[,"sigma2"]
inv_sigma2.sim <- m.fit.jags.coda[,"inv_sigma2"]

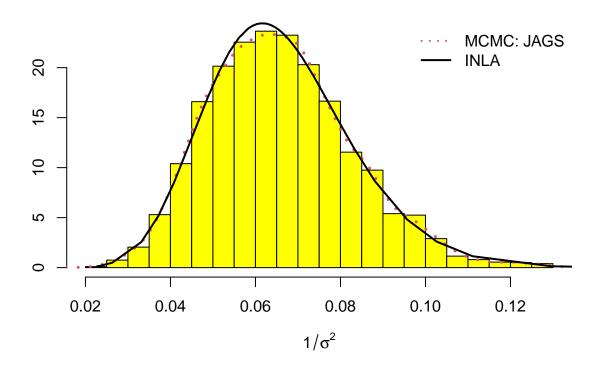
par(mfrow=c(1,1))
# plot for mean
rg <- range(inla.output$marginals.fixed$"(Intercept)"[,2])
truehist(mu.sim, prob=TRUE, col="yellow", xlab=expression(mu),ylim=rg)
lines(density(mu.sim),lty=3,lwd=3, col=2)
lines(inla.output$marginals.fixed$"(Intercept)",lwd=2)
legend("topright",c("MCMC: JAGS","INLA"),lty=c(3,1),lwd=c(2,2),col=c(2,1),cex=1.0,bty="n")</pre>
```



```
# plot for variance
m_var <-inla.tmarginal(function(x) 1/x, inla.output$marginals.hyperpar[[1]])
rg <- range(m_var[,2])
truehist(sigma2.sim, prob=TRUE, col="yellow", xlab=expression(sigma^2),ylim=rg)
lines(density(sigma2.sim),lty=3,lwd=3, col=2)
lines(m_var,lwd=2)
legend("topright",c("MCMC: JAGS","INLA"),lty=c(3,1),lwd=c(2,2),col=c(2,1),cex=1.0,bty="n")</pre>
```



```
# plot for precision
truehist(inv_sigma2.sim, prob=TRUE, col="yellow", xlab=expression(1/sigma^2))
lines(density(inv_sigma2.sim),lty=3,lwd=3, col=2)
lines(inla.output$marginals.hyperpar[[1]],lwd=2)
legend("topright",c("MCMC: JAGS","INLA"),lty=c(3,1),lwd=c(2,2),col=c(2,1),cex=1.0,bty="n")
```



```
## CODA
#summary(fit.jags.coda)
#effectiveSize(fit.jags.coda)
#lapply(fit.jags.coda, effectiveSize)
#gelman.diag(fit.jags.coda,autoburnin=TRUE)
#gelman.plot(fit.jags.coda,autoburnin=TRUE)
#qeweke.diaq(fit.jaqs.coda)
#geweke.plot(fit.jags.coda)
#heidel.diaq(fit.jaqs.coda)
#raftery.diag(fit.jags.coda)
#coda:::traceplot(fit.jags.coda)
# "DIC" penalised expected deviance computation
dic1<-dic.samples(model=model.jags, n.iter=1000, type="popt")</pre>
#dic2<-dic.samples(model=model.jags2, n.iter=1000, type="popt")</pre>
# "DIC" penalised expected deviance comparison
# There is no absolute scale for DIC comparison
# SE is very helpful
#diffdic(dic1,dic2)
```

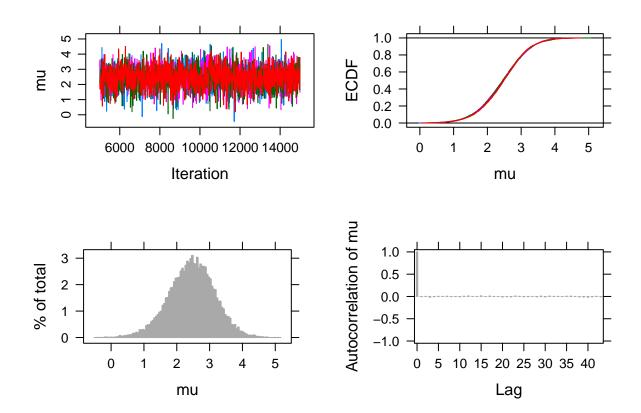
The traceplots of the four chains are superimposed on each other. They look alright. Also this time the results from approximation with JAGS and INLA look quite similar.

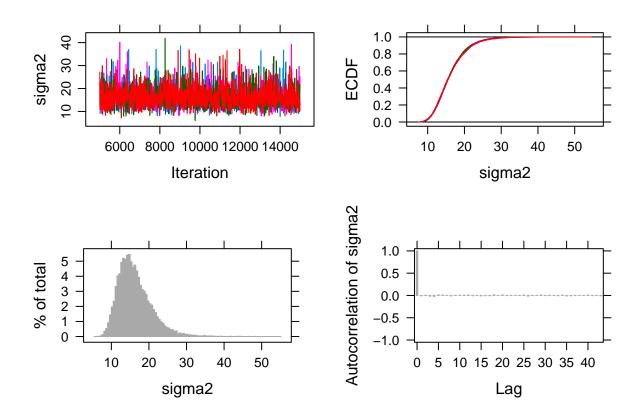
#### Interface in R to JAGS: runjags

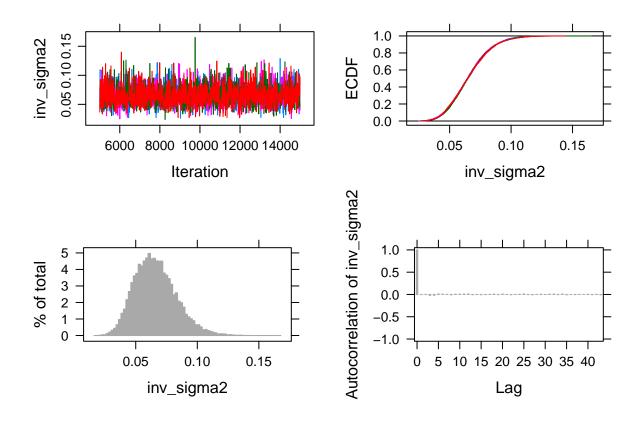
## Generating plots...

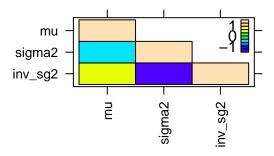
```
######
# Additional sampling in several chains, preparation for BGR/Gelman
# with runjags
######
library(runjags)
## Warning: package 'runjags' was built under R version 4.3.3
###############
# runjags interface with a link to a file
##############
wb_data <- list( N=30,
                 y=c(3.048,2.980,2.029,7.249,-0.259,3.061,4.059,6.370,7.902,1.926,
                     9.094,10.489,-0.384,-3.096,2.315,5.830,-1.542,-1.544,5.714,
                     -5.182,3.828,-4.038,2.169,5.087,-0.201,4.880,3.302,3.859,
                     11.144,5.564)
)
wb_inits <- function() {</pre>
 list(mu = rnorm(1),
       inv_sigma2 = runif(1)
}
fit.runjags<-run.jags(model=paste(path,"05normal_exmple_JAGS.txt",sep=""),</pre>
                      monitor=c("mu", "sigma2", "inv sigma2"),
                      data=wb_data,
                      inits=wb inits,
                      n.chains=4,
                      burnin=4000,
                      sample=5000,
                      adapt=1000,
                      thin=2)
## Compiling rjags model...
## Calling the simulation using the rjags method...
## Note: the model did not require adaptation
## Burning in the model for 4000 iterations...
## Running the model for 10000 iterations...
## Simulation complete
## Calculating summary statistics...
## Calculating the Gelman-Rubin statistic for 3 variables....
## Finished running the simulation
plot(fit.runjags)
```

17









```
print(fit.runjags)
##
## JAGS model summary statistics from 20000 samples (thin = 2; chains = 4; adapt+burnin = 5000):
##
##
                        Median Upper95
                                                                     MCerr MC%ofSD
              Lower95
                                            Mean
                                                       SD Mode
## mu
                1.041
                        2.4689 3.8062
                                          2.4526
                                                                  0.004857
                                                                               0.7
                                                  0.69999
               8.7965
                        15.468 24.965
                                          16.217
                                                   4.4475
                                                                  0.031513
                                                                               0.7
## sigma2
## inv_sigma2 0.03487 0.064648 0.09957 0.065974 0.016868
                                                            -- 0.00011849
                                                                               0.7
##
##
              SSeff
                         AC.20
                                 psrf
## mu
              20770 -0.0089682 1.0001
              19919 0.0049786 1.0003
## sigma2
## inv_sigma2 20265 0.0061126 1.0003
##
## Total time taken: 1.3 seconds
# CODA
fit.runjags.coda<-as.mcmc.list(fit.runjags)</pre>
summary(fit.runjags.coda)
##
## Iterations = 5001:14999
## Thinning interval = 2
## Number of chains = 4
## Sample size per chain = 5000
##
```

```
## 1. Empirical mean and standard deviation for each variable,
##
      plus standard error of the mean:
##
##
                            SD Naive SE Time-series SE
                  Mean
## mu
               2.45263 0.69999 0.0049497
                                              0.0048595
              16.21750 4.44754 0.0314488
                                              0.0315398
## sigma2
## inv sigma2 0.06597 0.01687 0.0001193
                                              0.0001187
##
## 2. Quantiles for each variable:
##
##
                 2.5%
                           25%
                                    50%
                                             75%
                                                    97.5%
                                                  3.7884
              1.01469 1.99579
                                2.46895 2.91999
## mu
## sigma2
              9.70196 13.08395 15.46842 18.60047 26.7184
## inv_sigma2 0.03743 0.05376 0.06465 0.07643 0.1031
# conduct CODA
```

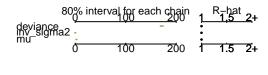
Another interface is runjags. Now the .txt file 05normal\_exmple\_JAGS.txt is used where the model is specified. Four chains are used the burnin period is again set to 4000 afterwards 5000 additional samples are taken. In the burnin the adaptive iterations to use for the simulation are not included. Thinning is set to 2. Here burnin is directly specified in the model instead of using update(). The traceplots look ok. We also get an empirical cumulative distribution function plot and an autocorrelation plot for the parameters and an additional plot showing the correlations between the parameters. The autocorrelation plots look good for all parameters.

#### Interface in R to JAGS: R2jags

A third interface is R2jags.

```
#define parameters
params<-c("mu", "sigma2", "inv_sigma2")</pre>
# define inits
inits1 <- list(mu=rnorm(1), inv_sigma2=runif(1),</pre>
                .RNG.name="base::Super-Duper", .RNG.seed=1)
inits2 <- list(mu=rnorm(1), inv_sigma2=runif(1),</pre>
                .RNG.name="base::Wichmann-Hill", .RNG.seed=2)
wb_inits <- list(inits1,inits2)</pre>
fit.R2jags<-jags(data=wb_data,</pre>
                  inits=wb_inits,
                  parameters.to.save=params,
                  model.file=paste(path, "05normal_exmple_JAGS.txt", sep=""),
                  n.chains=2,
                  n.iter=50000,
                  n.burnin=4000,
                  n.thin=5,
                  DIC = TRUE,
                  jags.seed = 321,
                  refresh =100,
                  digits = 4,
                  jags.module = c("glm","dic"))
## module glm loaded
## Compiling model graph
##
      Resolving undeclared variables
##
      Allocating nodes
## Graph information:
      Observed stochastic nodes: 30
      Unobserved stochastic nodes: 2
##
##
      Total graph size: 41
##
## Initializing model
# Standard plots of the monitored variables
plot(fit.R2jags)
```

Bugs model at "05normal\_exmple\_JAGS.txt", fit using jags, 2 chains, each with 50000 iterations (first 4000 discarded)

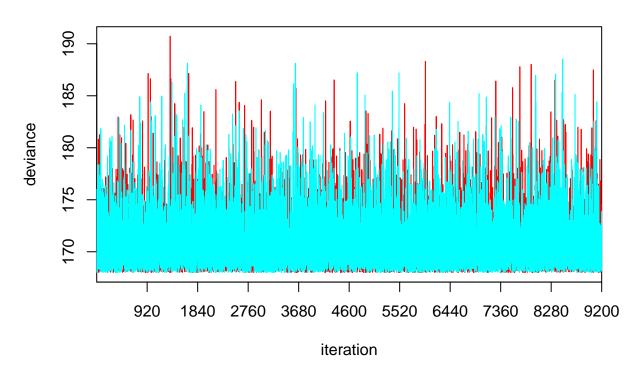


medians and 80% intervals

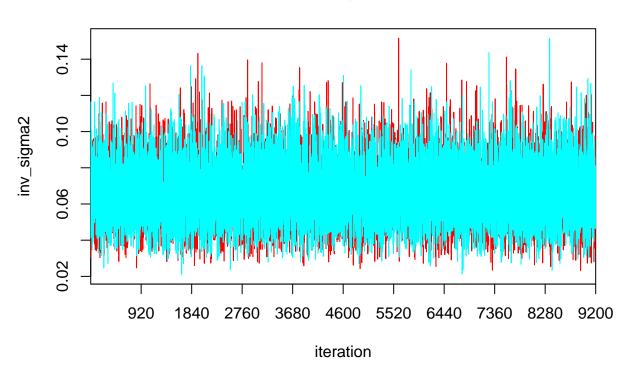
```
# Display summary statistics
print(fit.R2jags)
```

```
## Inference for Bugs model at "O5normal_exmple_JAGS.txt", fit using jags,
   2 chains, each with 50000 iterations (first 4000 discarded), n.thin = 5
   n.sims = 18400 iterations saved
##
              mu.vect sd.vect
                                          25%
                                                  50%
                                                          75%
                                                                97.5% Rhat n.eff
                                 2.5%
## inv_sigma2
                0.066
                        0.017
                                0.037
                                        0.054
                                                0.064
                                                        0.076
                                                                0.102 1.001 18000
## mu
                2.451
                                        1.991
                                                2.466
                                                        2.933
                                                                3.823 1.001 6200
                        0.715
                                0.993
              16.290
                        4.445
                                9.778
                                      13.131 15.558
                                                      18.664 27.093 1.001 18000
## sigma2
## deviance
              170.904
                        2.687 168.076 168.928 170.161 172.092 178.005 1.001 9300
## For each parameter, n.eff is a crude measure of effective sample size,
## and Rhat is the potential scale reduction factor (at convergence, Rhat=1).
##
## DIC info (using the rule, pD = var(deviance)/2)
## pD = 3.6 and DIC = 174.5
## DIC is an estimate of expected predictive error (lower deviance is better).
# traceplot
traceplot(fit.R2jags)
```

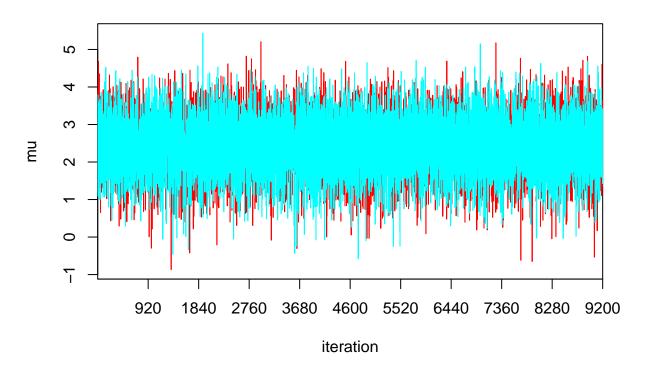
# deviance



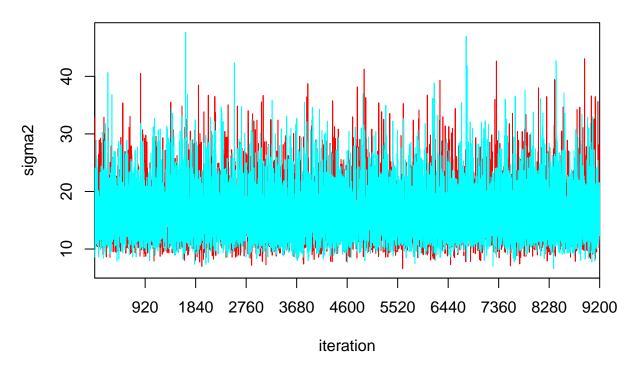
# inv\_sigma2



# mu



## sigma2



```
# CODA
fit.R2jags.coda<-as.mcmc(fit.R2jags)</pre>
summary(fit.R2jags.coda)
##
## Iterations = 4001:49996
## Thinning interval = 5
## Number of chains = 2
  Sample size per chain = 9200
##
##
   1. Empirical mean and standard deviation for each variable,
##
      plus standard error of the mean:
##
##
                              SD Naive SE Time-series SE
                   Mean
                                                0.0196358
              170.90404 2.68651 0.0198052
## deviance
                0.06567 0.01677 0.0001236
                                                0.0001266
## inv_sigma2
                2.45117 0.71547 0.0052745
## mu
                                                0.0052335
               16.28987 4.44454 0.0327656
                                                0.0327655
##
  sigma2
##
##
  2. Quantiles for each variable:
##
##
                                         50%
                                                    75%
                                                           97.5%
                   2.5%
                               25%
              168.07627 168.92819 170.16068 172.09243 178.0055
## deviance
## inv_sigma2
                0.03691
                           0.05358
                                     0.06428
                                                0.07616
                                                          0.1023
## mu
                0.99271
                           1.99140
                                     2.46569
                                                2.93277
                                                          3.8229
                9.77825
                        13.13110 15.55786
                                              18.66396 27.0926
## sigma2
```

## # conduct CODA

Now 2 Markov chains are used and a burnin of 4000. This time n.iter = 50000 includes the burnin period. The thinning is set to 5 to save memory and computation time. Also the model is called from the 05normal\_exmple\_JAGS.txt file. Again burnin is set directly instead of updating the model. Also this time the traceplots look alright.

## Exercise 4

Extend the code available in the file 05normal\_example\_JAGS.R to deal with the logistic regression example for mice data from Collett (2003, p.71) provided in Table 1.

Compare the output provided by the classic logistic regression and the Bayesian inference. What are the differences?

```
remove(list=ls())
rm(.Random.seed, envir=globalenv())
set.seed(44566)

# Load data
y <- c(26,9,21,9,6,1)
n <- c(28,12,40,40,40,40)
x <- c(0.0028, 0.0028, 0.0056, 0.0112, 0.0225, 0.0450)

# Priors
mu0 <- 0
prec_0 <- 1.0E-04</pre>
```

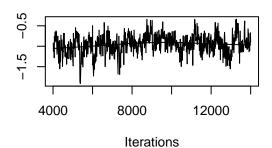
#### **INLA**

#### JAGS: one chain

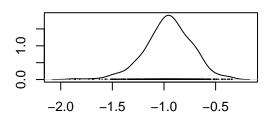
```
mice_data <- list(Y = y, x = x - mean(x), n = n)
inits_1chain <- list(a = 0, b = 0, .RNG.name = "base::Wichmann-Hill", .RNG.seed = 123456)
modelString = " # open quote for modelString
model {
    # likelihood
    for(i in 1:length(Y)) {
        Y[i] ~ dbin(p[i], n[i])
        logit(p[i]) <- a+b*x[i]
}
# priors
a ~ dnorm(0, 1.0E-4)
b ~ dnorm(0, 1.0E-4)
}
" # close quote for modelString</pre>
```

```
writeLines(modelString, con="MiceModel.txt") # write to a file
# model initiation
model.jags <- jags.model(</pre>
  file = "MiceModel.txt",
  data = mice_data,
 inits = inits_1chain,
 n.chains = 1,
  n.adapt = 4000
# burn-in
update(model.jags, n.iter = 4000)
# sampling
fit.jags.coda <- coda.samples(</pre>
  model = model.jags,
  variable.names = c("a", "b"),
 n.iter = 10000,
  thin = 10
#summary(fit.jags.coda)
plot(fit.jags.coda)
```

## Trace of a

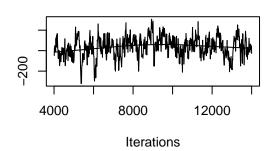


# Density of a

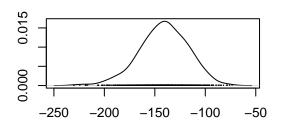


N = 1000 Bandwidth = 0.05669

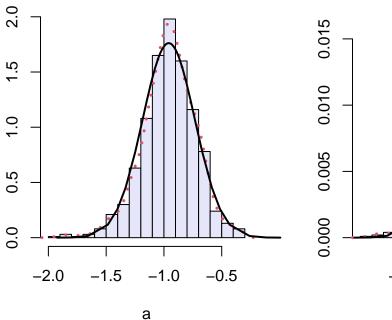
## Trace of b

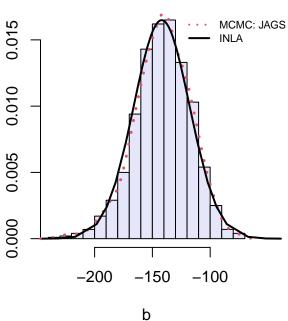


## Density of b



N = 1000 Bandwidth = 6.453



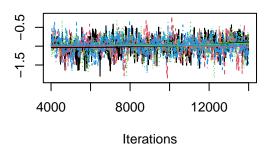


```
## Compiling model graph
## Resolving undeclared variables
## Allocating nodes
## Graph information:
## Observed stochastic nodes: 6
## Unobserved stochastic nodes: 2
## Total graph size: 37
##
```

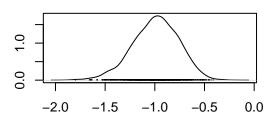
#### JAGS: several chains

```
inits_4chain <- list(</pre>
 list(a=0, b = 0, .RNG.name = "base::Super-Duper", .RNG.seed = 12345),
 list(a=0, b = 0, .RNG.name = "base::Super-Duper", .RNG.seed = 123456),
 list(a=0, b = 0, .RNG.name = "base::Super-Duper", .RNG.seed = 1234567),
 list(a=0, b = 0, .RNG.name = "base::Super-Duper", .RNG.seed = 12345678))
# model initialisation
model.jags <- jags.model(</pre>
 file = "MiceModel.txt",
 data = mice_data,
 inits = inits_4chain,
 n.chains = 4,
 n.adapt = 4000
# burn-in
update(model.jags, n.iter = 4000)
# sampling/monitoring
fit.jags.coda <- coda.samples(</pre>
 model = model.jags,
 variable.names = c("a", "b"),
 n.iter = 10000,
 thin = 10
)
model.jags$iter()
summary(fit.jags.coda)
plot(fit.jags.coda)
```

## Trace of a

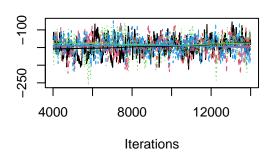


## Density of a

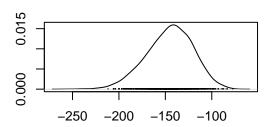


N = 1000 Bandwidth = 0.04678

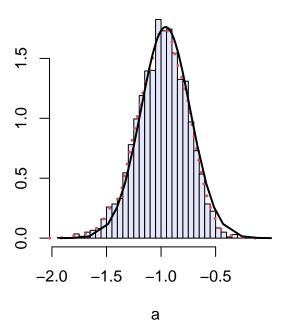
#### Trace of b

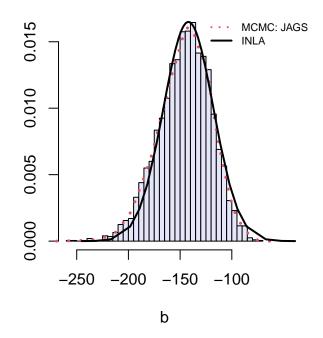


## Density of b



N = 1000 Bandwidth = 5.105





```
## Compiling model graph
##
      Resolving undeclared variables
##
      Allocating nodes
## Graph information:
      Observed stochastic nodes: 6
##
##
      Unobserved stochastic nodes: 2
##
      Total graph size: 37
##
   Initializing model
##
##
## [1] 14000
##
## Iterations = 4010:14000
## Thinning interval = 10
## Number of chains = 4
## Sample size per chain = 1000
##
## 1. Empirical mean and standard deviation for each variable,
##
      plus standard error of the mean:
##
##
                   SD Naive SE Time-series SE
         Mean
       -0.992 0.2318 0.003666
                                       0.01011
## a
## b -145.596 25.2995 0.400020
                                       1.32299
##
## 2. Quantiles for each variable:
##
```

## 2.5% 25% 50% 75% 97.5% ## a -1.483 -1.143 -0.9819 -0.8301 -0.57 ## b -199.094 -161.784 -143.9363 -127.6517 -100.05 Classical logistic regression model

## dosage\_centered -146.6927209 26.3629619 -5.564349 2.631328e-08

#### Conclusion/Comparison:

The estimates for the intercept a and slope b from the JAGS model are actually relatively similar compared to the classical logistic regression with the function glm(). Since we estimated the distribution of the slope and intercept, we can even obtain quantiles of a and b, which is not possible with the classical approach. Furthermore, we have a quantification of the computational MCMC error with the naive se and time-series se, which do not exist in the classical framework. Finally, we can see the fundamental differences between the classical and Bayesian statistics, reflected in the standard error of the estimates in the classical approach, and the empirical standard deviation in the Bayesian model.

# Exercise 5

## Exercise 6

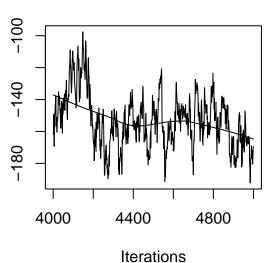
Run the code from the previous exercise with mice data with only one chain monitoring beta under the following two conditions:

#### 1

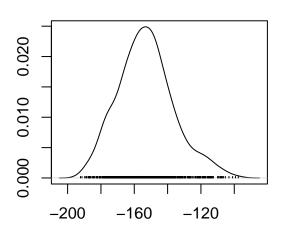
After an adaptation phase of 1000 and a burn-in of 4000 draw a sample of 1000 observations in one chain with thinning set to 1.

```
set.seed(44566)
inits_1chain <- list(a = 0, b = 0, .RNG.name = "base::Wichmann-Hill", .RNG.seed = 123456)
# model initiation
model.jags <- jags.model(</pre>
  file = "MiceModel.txt",
  data = mice_data,
  inits = inits_1chain,
  n.chains = 1,
  n.adapt = 1000)
## Compiling model graph
      Resolving undeclared variables
##
##
      Allocating nodes
## Graph information:
      Observed stochastic nodes: 6
##
##
      Unobserved stochastic nodes: 2
##
      Total graph size: 37
##
## Initializing model
# burn-in
update(model.jags, n.iter = 4000)
# sampling
fit.jags.coda_1 <- coda.samples(</pre>
  model = model.jags,
  variable.names = "b",
  n.iter = 1000,
  thin = 1)
#summary(fit.jags.coda)
par(mfrow=c(1,2), mar=c(10,2,4,3))
plot(fit.jags.coda_1)
```





# Density of b



N = 1000 Bandwidth = 4.219

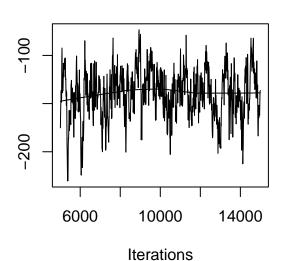
## 2

After an adaptation phase of 1000 and a burn-in of 4000 draw a sample of 10000 observations in one chain with thinning set to 10.

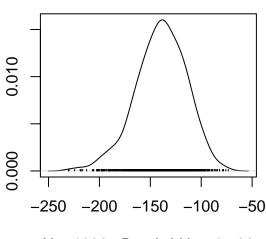
```
# sampling
fit.jags.coda_2 <- coda.samples(
   model = model.jags,
   variable.names = "b",
   n.iter = 10000,
   thin = 10)

#summary(fit.jags.coda)
par(mfrow=c(1,2), mar=c(10,2,4,3))
plot(fit.jags.coda_2)</pre>
```

## Trace of b



## Density of b



N = 1000 Bandwidth = 6.599

## (a)

For which of the above conditions the ESS estimates will be larger and why?

Without thinning, the samples are dependent on preceding samples since the Markov Chain is kept intact. With thinning, only every x'th sample is chosen, so this dependence is disrupted, and autocorrelation is reduced. Which lower autocorrelation, the resulting ESS is higher.

## (b)

To check your answer: Apply both the 05ess.R code and the function effectiveSize from the coda package. Compare the ESS estimates with those obtained with the n.eff function from package stableGR (Vats and Knudson, 2021). Please report your findings.

```
ess_t1 <- ess(fit.jags.coda_1[[1]], 1000)
ess_t10 <- ess(fit.jags.coda_2[[1]], 1000)

coda_ess_t1 <- as.numeric(effectiveSize(fit.jags.coda_1))
coda_ess_t10 <- as.numeric(effectiveSize(fit.jags.coda_2))

stableGR_ess_t1 <- as.numeric(n.eff(fit.jags.coda_1)$n.eff)
stableGR_ess_t10 <- as.numeric(n.eff(fit.jags.coda_2)$n.eff)</pre>
```

Setting	custom function	coda::effectiveSize	stableGR::n.eff
n.iter = 1000, thin = 1	21.01	26.67	17.54
n.iter = 10000, thin = 10	65.411	83.97	65.049

Indeed, the effective sample sizes are higher with thinning. The different packages don't all return exactly the same values, but they're in comparable ranges.