Worksheet 05 Group 2

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```
library(glue)
library(rjags)
library(INLA)
library(MASS)
library(ggplot2)
library(patchwork)
library(coda)
library(stableGR)
source("05ess.r")
```

Exercise 3

Run the code provided in the file 05normal_example_JAGS.R and explore the interfaces in R to JAGS. Comment your findings. -> The comments can be found below the code chunks.

clearing environment, set.seed for reproducibility and set path to .txt file with model

Interface in R to JAGS: rjags

1 base::Variance

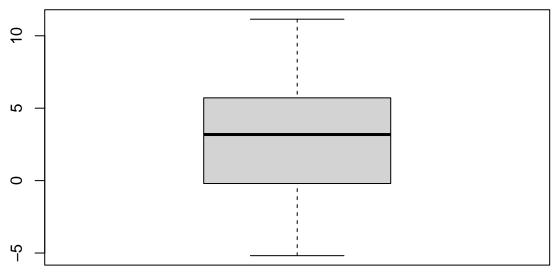
```
## 2
                      TRUE
         base::Mean
## 3
        base::Trace
                      TRUE
list.factories(type = "sampler")
##
               factory status
## 1
      bugs::BinomSlice
                          TRUE
## 2
             bugs::RW1
                          TRUE
## 3
        bugs::Censored
                          TRUE
## 4
             bugs::Sum
                          TRUE
## 5
            bugs::DSum
                          TRUE
## 6
       bugs::Conjugate
                          TRUE
## 7
       bugs::Dirichlet
                          TRUE
## 8
                          TRUE
         bugs::MNormal
## 9
          base::Finite
                          TRUE
## 10
           base::Slice
                          TRUE
set.factory(name = "base::Slice", type = "sampler", state = FALSE)
## NULL
list.factories(type = "sampler")
##
               factory status
## 1
     bugs::BinomSlice
                          TRUE
## 2
             bugs::RW1
                          TRUE
## 3
        bugs::Censored
                          TRUE
## 4
                          TRUE
             bugs::Sum
## 5
            bugs::DSum
                          TRUE
## 6
       bugs::Conjugate
                          TRUE
## 7
                          TRUE
       bugs::Dirichlet
## 8
                          TRUE
         bugs::MNormal
## 9
          base::Finite
                          TRUE
## 10
           base::Slice FALSE
set.factory(name = "base::Slice", type = "sampler", state = TRUE)
## NULL
list.factories(type = "sampler")
##
               factory status
## 1
                          TRUE
     bugs::BinomSlice
## 2
             bugs::RW1
                          TRUE
## 3
                          TRUE
        bugs::Censored
## 4
             bugs::Sum
                          TRUE
## 5
                          TRUE
            bugs::DSum
## 6
       bugs::Conjugate
                          TRUE
## 7
       bugs::Dirichlet
                          TRUE
## 8
         bugs::MNormal
                          TRUE
## 9
                          TRUE
          base::Finite
## 10
           base::Slice
                          TRUE
list.modules()
## [1] "basemod" "bugs"
load.module("glm")
```

```
## module glm loaded
list.modules()
## [1] "basemod" "bugs" "glm"
unload.module("glm")
## Module glm unloaded
```

```
list.modules()
## [1] "basemod" "bugs"
```

With list.factories a data frame with two columns is returned, the first column shows the names of the factory objects in the currently loaded modules, and the second column is a logical vector indicating whether the corresponding factory is active or not. With list.modules() the loaded modules can be listed. With load.module("module_name") and unload.module("module_name") modules can be loaded or unloaded.

```
######################
## Introduction
####################
# generating data
#mu <- 4
#sigma2 <- 16
#n <- 30
#y <- rnorm(n=n, mean=mu, sd=sqrt(sigma2))</pre>
# Load the data
# round(y,3)
y \leftarrow c(3.048, 2.980, 2.029, 7.249, -0.259, 3.061, 4.059, 6.370, 7.902, 1.926,
       9.094,10.489,-0.384,-3.096,2.315,5.830,-1.542,-1.544,5.714,
       -5.182,3.828,-4.038,2.169,5.087,-0.201,4.880,3.302,3.859,
       11.144,5.564)
par(mfrow = c(1, 1))
boxplot(y)
```



```
## Min. 1st Qu. Median Mean 3rd Qu. Max.
## -5.1820 0.3307 3.1815 3.1884 5.6765 11.1440

sd(y)

## [1] 4.046692

# Define the parameters of the prior distributions
mu0 <- -3
sigma2_0 <- 4
a0 <- 1.6
b0 <- 0.4</pre>
```

30 random datapoints were generated from a normal distribution with mean = 4 and standard deviation = 4. The parameters of the prior distribution are defined. Mean value from summary is with 3.1884333 not that close to mean = 4.

As input for INLA the previously defined parameters and the random sampled datapoints are used. INLA is used to approximate distribution.

```
##############################
# Step 2: JAGS model file as a string in rjags with coda
##############################
set.seed(44566)
library(rjags)
library(coda)
#sessionInfo()
wb_data <- list( N=30,
                 y=c(3.048,2.980,2.029,7.249,-0.259,3.061,4.059,6.370,7.902,1.926,
                     9.094,10.489,-0.384,-3.096,2.315,5.830,-1.542,-1.544,5.714,
                     -5.182,3.828,-4.038,2.169,5.087,-0.201,4.880,3.302,3.859,
                     11.144,5.564)
)
wb_inits <- list( mu=-0.2381084, inv_sigma2=0.3993192 )</pre>
modelString = " # open quote for modelString
model{
```

```
# likelihood
for (i in 1:N){
y[i] ~ dnorm( mu, inv_sigma2 )
}
# Priors
mu ~ dnorm( -3, 0.25 ) # prior for mu N(mu0, prec=1/sigma2_0)
inv_sigma2 ~ dgamma( 1.6, 0.4 ) # prior for precision G(a0, b0)

# transformations
# deterministic definition of variance
sigma2 <- 1/inv_sigma2

# deterministic definition of standard deviation
sigma <- sqrt(sigma2)
}
" # close quote for modelString
writeLines(modelString, con="TempModel.txt") # write to a file</pre>
```

The input for JAGS is defined as a list. The model is printed to a new .txt file. N is set to 30 and N samples are drawn from a normal distribution with mean mu and the precision as standard deviation. Mu follows a normal prior and the precision a gamma prior. The variance and then the standard deviation are estimated from the precision.

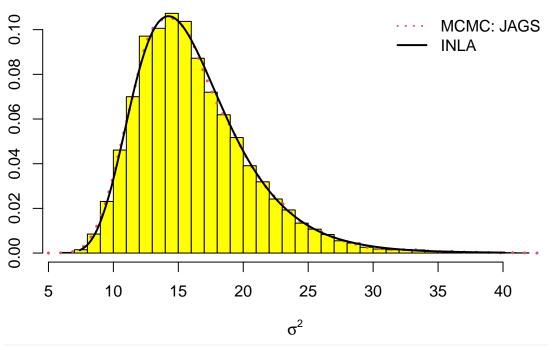
```
# JAGS only one chain
# model initiation
model.jags <- jags.model(</pre>
 file = "TempModel.txt",
 data = wb_data,
 inits = wb_inits,
 n.chains = 1,
 n.adapt = 4000
)
## Compiling model graph
##
     Resolving undeclared variables
##
     Allocating nodes
## Graph information:
     Observed stochastic nodes: 30
##
##
     Unobserved stochastic nodes: 2
##
     Total graph size: 41
##
## Initializing model
str(model.jags)
## List of 8
            :function ()
## $ ptr
## $ data
            :function ()
## $ model
            :function ()
            :function (internal = FALSE)
## $ state
## $ nchain
            :function ()
```

```
## $ iter
               :function ()
## $ sync
               :function ()
## $ recompile:function ()
## - attr(*, "class")= chr "jags"
class(model.jags)
## [1] "jags"
attributes(model.jags)
## $names
## [1] "ptr"
                    "data"
                                "model"
                                             "state"
                                                         "nchain"
                                                                      "iter"
                    "recompile"
## [7] "sync"
##
## $class
## [1] "jags"
list.samplers(model.jags)
## $`bugs::ConjugateNormal`
## [1] "mu"
## $`bugs::ConjugateGamma`
## [1] "inv_sigma2"
A jags model with only one chain is initiated. The previously generated TempModel.txt file is used. The
number of iterations for adaption is set to 4000.
# burn-in
update(model.jags, n.iter = 4000)
# sampling
fit.jags.coda <- coda.samples(</pre>
 model = model.jags,
 variable.names = c("mu", "sigma2", "inv_sigma2"),
 n.iter = 10000,
 thin = 1
)
str(fit.jags.coda)
## List of 1
## $ : 'mcmc' num [1:10000, 1:3] 0.0865 0.0682 0.0831 0.0641 0.0816 ...
     ..- attr(*, "dimnames")=List of 2
##
    ....$ : NULL
    ....$ : chr [1:3] "inv_sigma2" "mu" "sigma2"
##
     ..- attr(*, "mcpar")= num [1:3] 4001 14000 1
## - attr(*, "class")= chr "mcmc.list"
class(fit.jags.coda)
## [1] "mcmc.list"
attributes(fit.jags.coda)
## $class
## [1] "mcmc.list"
```

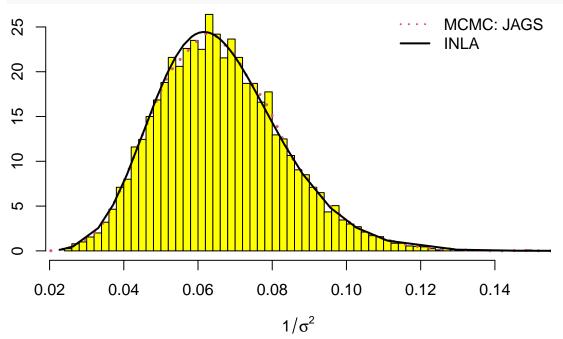
```
summary(fit.jags.coda)
##
## Iterations = 4001:14000
## Thinning interval = 1
## Number of chains = 1
## Sample size per chain = 10000
##
##
   1. Empirical mean and standard deviation for each variable,
##
      plus standard error of the mean:
##
##
                   Mean
                               SD Naive SE Time-series SE
## inv_sigma2 0.06615 0.01677 0.0001677
                                                   0.0001809
##
                2.44749 0.70381 0.0070381
                                                   0.0074615
               16.15654 4.37608 0.0437608
                                                   0.0478448
   sigma2
##
##
##
   2. Quantiles for each variable:
##
##
                   2.5%
                              25%
                                        50%
                                                  75%
                                                        97.5%
## inv_sigma2 0.03757
                         0.05401
                                   0.06474
                                             0.07663
                                                       0.1027
## mu
               0.98865
                         1.99425
                                   2.47361
                                             2.91217
## sigma2
               9.73916 13.04939 15.44625 18.51423 26.6161
#print(fit.jags.coda)
plot(fit.jags.coda)
            Trace of inv_sigma2
                                                             Density of inv_sigma2
                                                 20
                                                      0.02  0.04  0.06  0.08  0.10  0.12  0.14  0.16
   4000
          6000
                 8000
                       10000
                              12000
                                     14000
                                                           N = 10000 Bandwidth = 0.002817
                   Iterations
                Trace of mu
                                                                 Density of mu
                                                 0.0
   4000
          6000
                 8000
                       10000
                              12000
                                     14000
                                                          0
                                                                1
                                                            N = 10000 Bandwidth = 0.1151
                   Iterations
              Trace of sigma2
                                                               Density of sigma2
                                                 0.00
                                                          10
          6000
                                                                   20
                                                                            30
                                                                                     40
   4000
                 8000
                       10000
                              12000
                                     14000
                                                            N = 10000 Bandwidth = 0.6851
                   Iterations
# store samples for each parameter from the chain into separate objects
m.fit.jags.coda <- as.matrix(fit.jags.coda)</pre>
mu.sim <- m.fit.jags.coda[,"mu"]</pre>
```

```
sigma2.sim <- m.fit.jags.coda[,"sigma2"]</pre>
inv_sigma2.sim <- m.fit.jags.coda[,"inv_sigma2"]</pre>
library(MASS)
par(mfrow=c(1,1))
# plot for mean
rg <- range(inla.output$marginals.fixed$"(Intercept)"[,2])
truehist(mu.sim, prob=TRUE, col="yellow", xlab=expression(mu),ylim=rg)
lines(density(mu.sim),lty=3,lwd=3, col=2)
lines(inla.output$marginals.fixed$"(Intercept)",lwd=2)
legend("topright",c("MCMC: JAGS","INLA"),lty=c(3,1),lwd=c(2,2),col=c(2,1),cex=1.0,bty="n")
9.0
                                                                 MCMC: JAGS
S
                                                                 INLA
o.
0.4
0.3
0.2
0.1
0.0
             0
                           1
                                       2
                                                    3
                                                                  4
                                                                              5
                                          μ
```

```
# plot for variance
m_var <-inla.tmarginal(function(x) 1/x, inla.output$marginals.hyperpar[[1]])
rg <- range(m_var[,2])
truehist(sigma2.sim, prob=TRUE, col="yellow", xlab=expression(sigma^2),ylim=rg)
lines(density(sigma2.sim),lty=3,lwd=3, col=2)
lines(m_var,lwd=2)
legend("topright",c("MCMC: JAGS","INLA"),lty=c(3,1),lwd=c(2,2),col=c(2,1),cex=1.0,bty="n")</pre>
```



```
# plot for precision
truehist(inv_sigma2.sim, prob=TRUE, col="yellow", xlab=expression(1/sigma^2))
lines(density(inv_sigma2.sim),lty=3,lwd=3, col=2)
lines(inla.output$marginals.hyperpar[[1]],lwd=2)
legend("topright",c("MCMC: JAGS","INLA"),lty=c(3,1),lwd=c(2,2),col=c(2,1),cex=1.0,bty="n")
```



The burn in period is set to 4000. After the burn in 10000 iterations are done to fit the model. The traceplots look good and stable. When looking at the traceplots we can see that the approximations for mu and sigma^2 from JAGS and INLA look similar but differ just a little bit.

```
wb_inits <- function() {</pre>
  list(mu = rnorm(1),
       inv_sigma2 = runif(1)
  )
}
# model initialisation
model.jags <- jags.model(</pre>
  file = "TempModel.txt",
  data = wb_data,
  inits = wb_inits,
  n.chains = 4,
  n.adapt = 4000
## Compiling model graph
##
      Resolving undeclared variables
##
      Allocating nodes
## Graph information:
##
      Observed stochastic nodes: 30
##
      Unobserved stochastic nodes: 2
##
      Total graph size: 41
## Initializing model
# burn-in
update(model.jags, n.iter = 4000)
# sampling/monitoring
fit.jags.coda <- coda.samples(</pre>
  model = model.jags,
  variable.names = c("mu", "sigma2", "inv_sigma2"),
  n.iter = 10000,
  thin = 10
)
\#n.thin < -floor((n.iter-n.adapt)/500)
#floor((10000-4000)/500)=12
```

Now again JAGS is used with the same model but instead of only one chain, 4 chains are used instead. The burn in period is again 4000.

```
##
## Iterations = 4010:14000
## Thinning interval = 10
## Number of chains = 4
## Sample size per chain = 1000
##
## 1. Empirical mean and standard deviation for each variable,
## plus standard error of the mean:
##
```

Mean

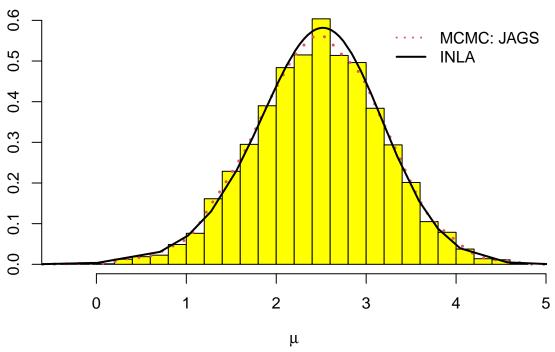
##

SD Naive SE Time-series SE

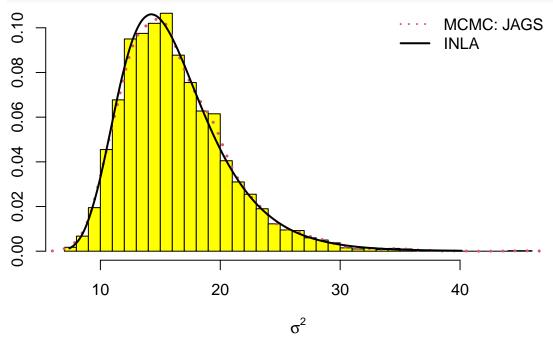
```
0.0002614
## inv sigma2 0.06555 0.01653 0.0002613
## mu
                  2.46498 0.71127 0.0112461
                                                        0.0104817
##
   sigma2
                 16.28801 4.37532 0.0691800
                                                        0.0680909
##
##
   2. Quantiles for each variable:
##
                    2.5%
                                25%
                                          50%
                                                     75%
                                                             97.5%
##
## inv_sigma2 0.03741
                                                0.07599
                                                           0.1013
                           0.05346
                                      0.0642
                 1.05023 1.99200
                                      2.4772
                                                2.95551
                 9.87495 13.16041 15.5763 18.70592 26.7328
## sigma2
plot(fit.jags.coda)
                                                                   Density of inv_sigma2
             Trace of inv_sigma2
                                                      20
           تسلخوانون بأحرين وامانون فالغانين وفهرنا فطرف فانك بالكاما بزوري
   4000
           6000
                  8000
                         10000
                                 12000
                                        14000
                                                            0.02  0.04  0.06  0.08  0.10  0.12  0.14
                     Iterations
                                                                 N = 1000 Bandwidth = 0.003335
                  Trace of mu
                                                                       Density of mu
      ومرتفق لياله للمراطي المرموس المراول والمالية والمراوية والمراوية والمراوية والمراولة والمراولة والمراولة والمراولة
                                                                 0
                                                                              2
                                                                                    3
   4000
           6000
                  8000
                         10000
                                 12000
                                        14000
                                                                                                 5
                                                          -1
                                                                  N = 1000 Bandwidth = 0.1435
                    Iterations
               Trace of sigma2
                                                                     Density of sigma2
                                                                10
                                                                        20
                                                                                 30
           6000
                                                                                         40
                                                                                                  50
   4000
                  8000
                         10000
                                 12000
                                                                  N = 1000 Bandwidth = 0.8351
                    Iterations
# store samples for each parameter from the chains into separate vectors
m.fit.jags.coda <-as.matrix(fit.jags.coda)</pre>
mu.sim <- m.fit.jags.coda[,"mu"]</pre>
sigma2.sim <- m.fit.jags.coda[,"sigma2"]</pre>
inv_sigma2.sim <- m.fit.jags.coda[,"inv_sigma2"]</pre>
par(mfrow=c(1,1))
# plot for mean
rg <- range(inla.output$marginals.fixed$"(Intercept)"[,2])</pre>
truehist(mu.sim, prob=TRUE, col="yellow", xlab=expression(mu),ylim=rg)
lines(density(mu.sim),lty=3,lwd=3, col=2)
```

legend("topright",c("MCMC: JAGS","INLA"),lty=c(3,1),lwd=c(2,2),col=c(2,1),cex=1.0,bty="n")

lines(inla.output\$marginals.fixed\$"(Intercept)",lwd=2)



```
# plot for variance
m_var <-inla.tmarginal(function(x) 1/x, inla.output$marginals.hyperpar[[1]])
rg <- range(m_var[,2])
truehist(sigma2.sim, prob=TRUE, col="yellow", xlab=expression(sigma^2),ylim=rg)
lines(density(sigma2.sim),lty=3,lwd=3, col=2)
lines(m_var,lwd=2)
legend("topright",c("MCMC: JAGS","INLA"),lty=c(3,1),lwd=c(2,2),col=c(2,1),cex=1.0,bty="n")</pre>
```



plot for precision
truehist(inv_sigma2.sim, prob=TRUE, col="yellow", xlab=expression(1/sigma^2))
lines(density(inv_sigma2.sim),lty=3,lwd=3, col=2)

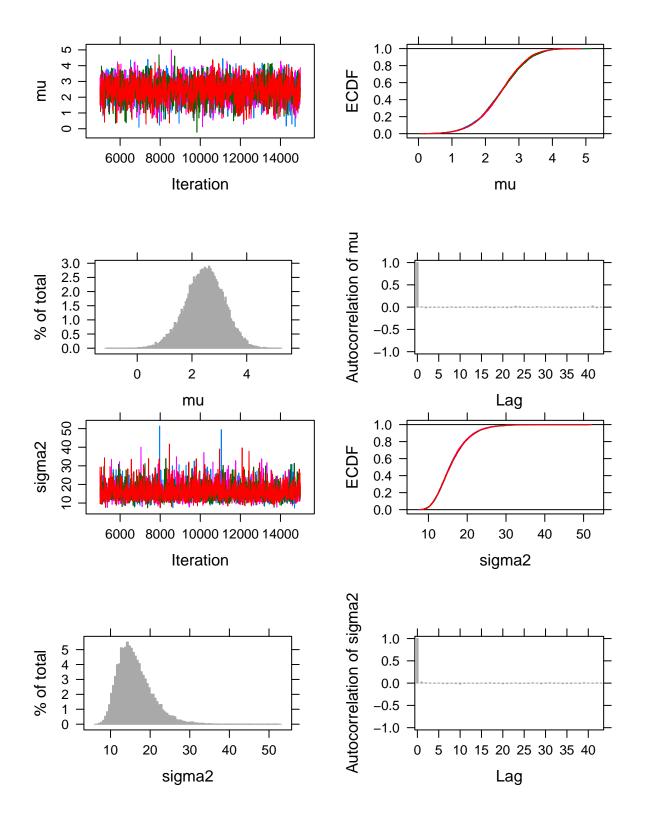
```
lines(inla.output$marginals.hyperpar[[1]],lwd=2)
legend("topright",c("MCMC: JAGS","INLA"),lty=c(3,1),lwd=c(2,2),col=c(2,1),cex=1.0,bty="n")
                                                               MCMC: JAGS
                                                               INLA
20
5
10
2
0
                                                           0.12
     0.02
                0.04
                           0.06
                                      80.0
                                                 0.10
                                                                      0.14
                                       1/\sigma^2
```

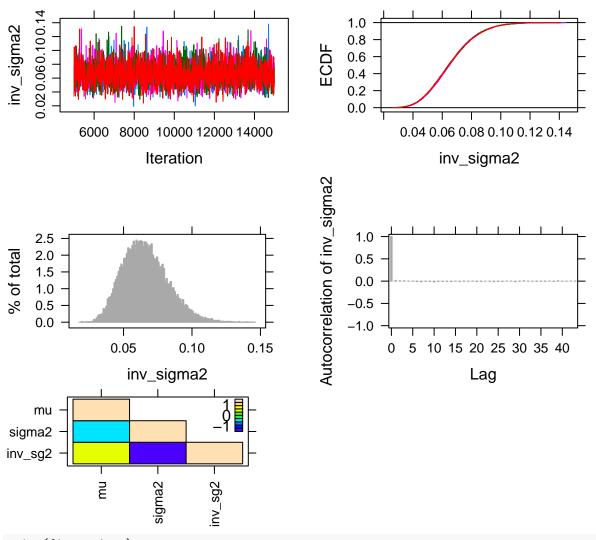
```
## CODA
#summary(fit.jags.coda)
#effectiveSize(fit.jags.coda)
#lapply(fit.jags.coda, effectiveSize)
#qelman.diaq(fit.jaqs.coda,autoburnin=TRUE)
#gelman.plot(fit.jags.coda,autoburnin=TRUE)
#qeweke.diaq(fit.jaqs.coda)
#geweke.plot(fit.jags.coda)
#heidel.diag(fit.jags.coda)
#raftery.diag(fit.jags.coda)
#coda:::traceplot(fit.jags.coda)
# "DIC" penalised expected deviance computation
dic1<-dic.samples(model=model.jags, n.iter=1000, type="popt")</pre>
#dic2<-dic.samples(model=model.jags2, n.iter=1000, type="popt")</pre>
# "DIC" penalised expected deviance comparison
# There is no absolute scale for DIC comparison
# SE is very helpful
#diffdic(dic1,dic2)
```

The traceplots of the four chains are superimposed on each other. They look alright. Also this time the results from approximation with JAGS and INLA look quite similar.

Interface in R to JAGS: runjags

```
# Additional sampling in several chains, preparation for BGR/Gelman
# with runjags
######
library(runjags)
###############
# runjags interface with a link to a file
##############
wb_data <- list( N=30,</pre>
                 y=c(3.048,2.980,2.029,7.249,-0.259,3.061,4.059,6.370,7.902,1.926,
                      9.094, 10.489, -0.384, -3.096, 2.315, 5.830, -1.542, -1.544, 5.714,
                     -5.182,3.828,-4.038,2.169,5.087,-0.201,4.880,3.302,3.859,
                     11.144,5.564)
)
wb_inits <- function() {</pre>
 list(mu = rnorm(1),
       inv_sigma2 = runif(1)
  )
}
fit.runjags<-run.jags(model=paste(path,"05normal_exmple_JAGS.txt",sep=""),</pre>
                      monitor=c("mu", "sigma2", "inv_sigma2"),
                       data=wb_data,
                       inits=wb_inits,
                      n.chains=4,
                      burnin=4000,
                      sample=5000,
                       adapt=1000,
                      thin=2)
## Compiling rjags model...
## Calling the simulation using the rjags method...
## Note: the model did not require adaptation
## Burning in the model for 4000 iterations...
## Running the model for 10000 iterations...
## Simulation complete
## Calculating summary statistics...
## Calculating the Gelman-Rubin statistic for 3 variables....
## Finished running the simulation
plot(fit.runjags)
## Generating plots...
```





```
print(fit.runjags)
```

```
##
  JAGS model summary statistics from 20000 samples (thin = 2; chains = 4; adapt+burnin = 5000):
##
##
##
               Lower95
                          Median
                                  Upper95
                                               Mean
                                                           SD Mode
                                                                         MCerr MC%ofSD
## mu
                 1.0481
                          2.4783
                                    3.8363
                                             2.4611
                                                      0.70933
                                                                     0.0049874
                                                                                   0.7
                 8.7181
                          15.471
                                    24.703
                                              16.19
                                                       4.3685
                                                                      0.031849
                                                                                   0.7
  sigma2
##
  inv_sigma2 0.035783 0.064637 0.099303 0.065975 0.016683
                                                                -- 0.00012045
                                                                                   0.7
##
##
##
              SSeff
                          AC.20
                                   psrf
## mu
              20227 -0.0067601 1.0002
                      -0.021053
## sigma2
              18814
                                      1
## inv_sigma2 19183
                      -0.019742
                                      1
##
## Total time taken: 0.1 seconds
# CODA
fit.runjags.coda<-as.mcmc.list(fit.runjags)</pre>
summary(fit.runjags.coda)
```

##

```
## Iterations = 5001:14999
## Thinning interval = 2
## Number of chains = 4
## Sample size per chain = 5000
##
  1. Empirical mean and standard deviation for each variable,
      plus standard error of the mean:
##
##
##
                  Mean
                            SD Naive SE Time-series SE
               2.46114 0.70933 0.005016
## mu
                                             0.0049892
## sigma2
              16.19003 4.36846 0.030890
                                              0.0318761
  inv_sigma2  0.06597  0.01668  0.000118
                                             0.0001205
##
##
## 2. Quantiles for each variable:
##
##
                 2.5%
                           25%
                                     50%
                                             75%
                                                   97.5%
              1.01050 1.99733 2.47826 2.9437
                                                 3.8038
## mu
              9.77993 13.08924 15.47105 18.5402 26.4400
## inv_sigma2 0.03782 0.05394 0.06464 0.0764 0.1023
```

conduct CODA

Another interface is runjags. Now the .txt file 05normal_exmple_JAGS.txt is used where the model is specified. Four chains are used the burnin period is again set to 4000 afterwards 5000 additional samples are taken. In the burnin the adaptive iterations to use for the simulation are not included. Thinning is set to 2. Here burnin is directly specified in the model instead of using update(). The traceplots look ok. We also get an empirical cumulative distribution function plot and an autocorrelation plot for the parameters and an additional plot showing the correlations between the parameters. The autocorrelation plots look good for all parameters.

Interface in R to JAGS: R2jags

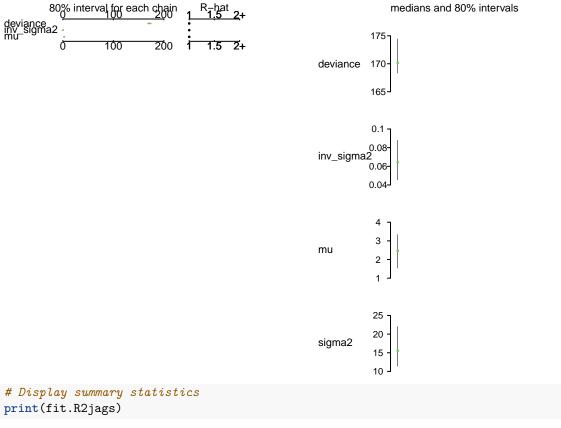
```
# R2jags wrapper to rjags interface to JAGS several chains
library(R2jags)
## Attaching package: 'R2jags'
## The following object is masked from 'package:coda':
##
##
    traceplot
#rm(list=ls())
```

A third interface is R2jags.

```
###############
# R2jags wrapper with a link to a file
##############
wb_data <- list( N=30,
```

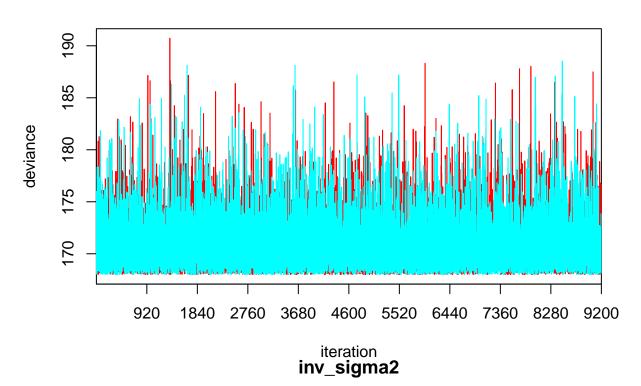
```
y=c(3.048,2.980,2.029,7.249,-0.259,3.061,4.059,6.370,7.902,1.926,
                      9.094, 10.489, -0.384, -3.096, 2.315, 5.830, -1.542, -1.544, 5.714,
                      -5.182,3.828,-4.038,2.169,5.087,-0.201,4.880,3.302,3.859,
                      11.144,5.564)
#define parameters
params<-c("mu", "sigma2", "inv_sigma2")</pre>
# define inits
inits1 <- list(mu=rnorm(1), inv_sigma2=runif(1),</pre>
                .RNG.name="base::Super-Duper", .RNG.seed=1)
inits2 <- list(mu=rnorm(1), inv_sigma2=runif(1),</pre>
                .RNG.name="base::Wichmann-Hill", .RNG.seed=2)
wb_inits <- list(inits1,inits2)</pre>
fit.R2jags<-jags(data=wb_data,</pre>
                  inits=wb_inits,
                  parameters.to.save=params,
                  model.file=paste(path, "05normal_exmple_JAGS.txt", sep=""),
                  n.chains=2,
                  n.iter=50000,
                  n.burnin=4000,
                  n.thin=5,
                  DIC = TRUE,
                  jags.seed = 321,
                  refresh =100,
                  digits = 4,
                  jags.module = c("glm", "dic"))
## module glm loaded
## Compiling model graph
##
      Resolving undeclared variables
##
      Allocating nodes
## Graph information:
##
      Observed stochastic nodes: 30
      Unobserved stochastic nodes: 2
##
##
      Total graph size: 41
##
## Initializing model
# Standard plots of the monitored variables
plot(fit.R2jags)
```

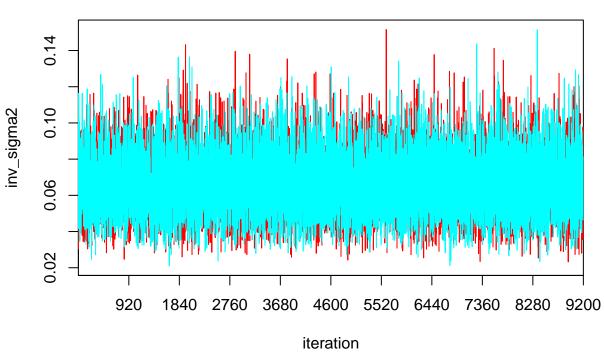
Bugs model at "05normal_exmple_JAGS.txt", fit using jags, 2 chains, each with 50000 iterations (first 4000 discarded)



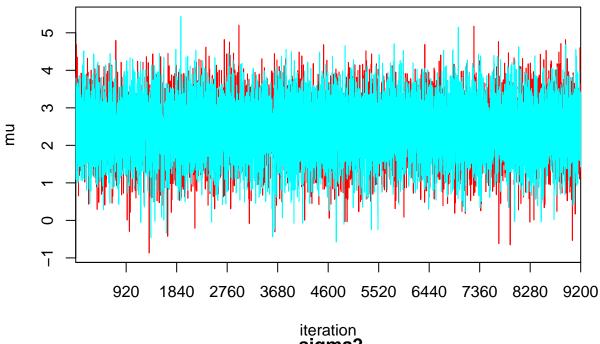
```
## Inference for Bugs model at "O5normal_exmple_JAGS.txt", fit using jags,
   2 chains, each with 50000 iterations (first 4000 discarded), n.thin = 5
   n.sims = 18400 iterations saved
                                          25%
                                                  50%
                                                           75%
                                                                 97.5% Rhat n.eff
              mu.vect sd.vect
                                 2.5%
                                        0.054
## inv_sigma2
                0.066
                        0.017
                                0.037
                                                0.064
                                                         0.076
                                                                 0.102 1.001 18000
## mu
                2.451
                        0.715
                                0.993
                                        1.991
                                                2.466
                                                         2.933
                                                                 3.823 1.001 6200
## sigma2
               16.290
                        4.445
                                9.778
                                       13.131
                                               15.558
                                                       18.664 27.093 1.001 18000
## deviance
              170.904
                        2.687 168.076 168.928 170.161 172.092 178.005 1.001 9300
##
## For each parameter, n.eff is a crude measure of effective sample size,
## and Rhat is the potential scale reduction factor (at convergence, Rhat=1).
## DIC info (using the rule, pD = var(deviance)/2)
## pD = 3.6 and DIC = 174.5
## DIC is an estimate of expected predictive error (lower deviance is better).
# traceplot
traceplot(fit.R2jags)
```

deviance

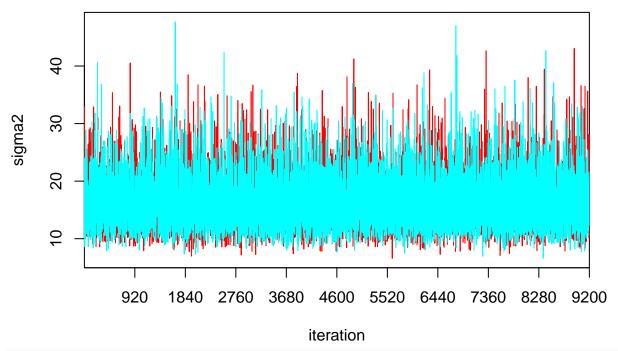




mu



iteration **sigma2**



CODA fit.R2jags.coda<-as.mcmc(fit.R2jags)</pre> summary(fit.R2jags.coda)

Iterations = 4001:49996

```
## Thinning interval = 5
## Number of chains = 2
## Sample size per chain = 9200
##
##
   1. Empirical mean and standard deviation for each variable,
##
      plus standard error of the mean:
##
##
                    Mean
                              SD
                                 Naive SE Time-series SE
                                                 0.0196358
## deviance
              170.90404 2.68651 0.0198052
   inv_sigma2
                0.06567 0.01677 0.0001236
                                                 0.0001266
##
  mu
                2.45117 0.71547 0.0052745
                                                 0.0052335
               16.28987 4.44454 0.0327656
##
   sigma2
                                                 0.0327655
##
## 2. Quantiles for each variable:
##
##
                    2.5%
                               25%
                                          50%
                                                    75%
                                                           97.5%
              168.07627 168.92819 170.16068 172.09243 178.0055
## deviance
## inv_sigma2
                0.03691
                           0.05358
                                     0.06428
                                                0.07616
                                                          0.1023
## mu
                                                2.93277
                                                          3.8229
                0.99271
                           1.99140
                                     2.46569
## sigma2
                9.77825
                          13.13110
                                    15.55786
                                               18.66396
                                                         27.0926
```

conduct CODA

Now 2 Markov chains are used and a burnin of 4000. This time n.iter = 50000 includes the burnin period. The thinning is set to 5 to save memory and computation time. Also the model is called from the 05normal_exmple_JAGS.txt file. Again burnin is set directly instead of updating the model. Also this time the traceplots look alright.

Exercise 4

Extend the code available in the file 05normal_example_JAGS.R to deal with the logistic regression example for mice data from Collett (2003, p.71) provided in Table 1.

Compare the output provided by the classic logistic regression and the Bayesian inference. What are the differences?

```
remove(list=ls())
rm(.Random.seed, envir=globalenv())
set.seed(44566)

# Load data
y <- c(26,9,21,9,6,1)
n <- c(28,12,40,40,40,40)
x <- c(0.0028, 0.0028, 0.0056, 0.0112, 0.0225, 0.0450)

# Priors
mu0 <- 0
prec_0 <- 1.0E-04</pre>
```

INLA

JAGS: one chain

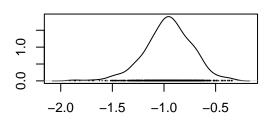
```
mice_data <- list(Y = y, x = x - mean(x), n = n)
inits_1chain <- list(a = 0, b = 0, .RNG.name = "base::Wichmann-Hill", .RNG.seed = 123456)
modelString = " # open quote for modelString
model {
    # likelihood
    for(i in 1:length(Y)) {
        Y[i] ~ dbin(p[i], n[i])
        logit(p[i]) <- a+b*x[i]
}
# priors
a ~ dnorm(0, 1.0E-4)
b ~ dnorm(0, 1.0E-4)
}
" # close quote for modelString</pre>
```

```
writeLines(modelString, con="TempModel.txt") # write to a file
# model initiation
model.jags <- jags.model(</pre>
  file = "TempModel.txt",
  data = mice_data,
 inits = inits_1chain,
 n.chains = 1,
  n.adapt = 4000
# burn-in
update(model.jags, n.iter = 4000)
# sampling
fit.jags.coda <- coda.samples(</pre>
  model = model.jags,
  variable.names = c("a", "b"),
  n.iter = 10000,
  thin = 10
#summary(fit.jags.coda)
plot(fit.jags.coda)
```

Trace of a

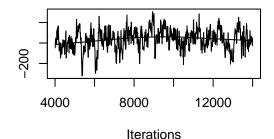
4000 8000 12000 Iterations

Density of a

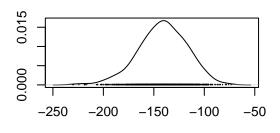


N = 1000 Bandwidth = 0.05669

Trace of b

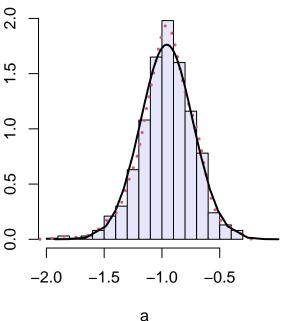


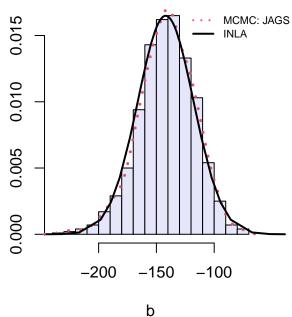
Density of b



N = 1000 Bandwidth = 6.453

```
# store samples for each parameter from the chain into separate objects
m.fit.jags.coda <- as.matrix(fit.jags.coda)
a.sim <- m.fit.jags.coda[,"a"]
b.sim <- m.fit.jags.coda[,"b"]</pre>
```





```
## Compiling model graph
## Resolving undeclared variables
## Allocating nodes
## Graph information:
## Observed stochastic nodes: 6
## Unobserved stochastic nodes: 2
## Total graph size: 37
##
## Initializing model
```

JAGS: several chains

```
inits_4chain <- list(
    list(a=0, b = 0, .RNG.name = "base::Super-Duper", .RNG.seed = 12345),
    list(a=0, b = 0, .RNG.name = "base::Super-Duper", .RNG.seed = 123456),
    list(a=0, b = 0, .RNG.name = "base::Super-Duper", .RNG.seed = 1234567),
    list(a=0, b = 0, .RNG.name = "base::Super-Duper", .RNG.seed = 12345678))

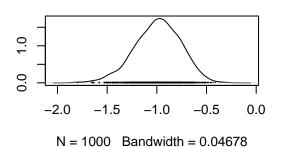
# model initialisation
model.jags <- jags.model(</pre>
```

```
file = "TempModel.txt",
  data = mice_data,
  inits = inits_4chain,
  n.chains = 4,
  n.adapt = 4000
# burn-in
update(model.jags, n.iter = 4000)
# sampling/monitoring
fit.jags.coda <- coda.samples(</pre>
  model = model.jags,
  variable.names = c("a", "b"),
  n.iter = 10000,
  thin = 10
model.jags$iter()
summary(fit.jags.coda)
plot(fit.jags.coda)
```

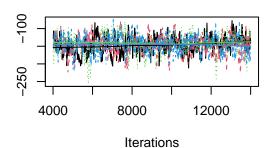
Trace of a

4000 8000 12000 Iterations

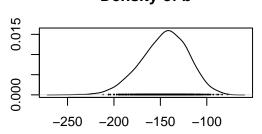
Density of a



Trace of b



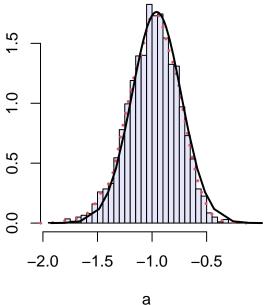
Density of b



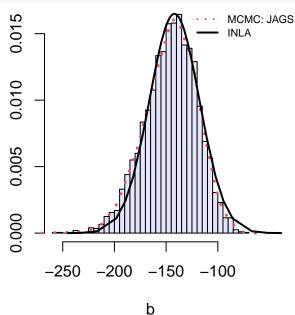
N = 1000 Bandwidth = 5.105

```
# store samples for each parameter from the chain into separate objects
m.fit.jags.coda <- as.matrix(fit.jags.coda)
a.sim <- m.fit.jags.coda[,"a"]
b.sim <- m.fit.jags.coda[,"b"]

par(mfrow=c(1,2), mar=c(6.1, 3.1, 4.1, 2.1), xpd=TRUE)
# plot for intercept
truehist(a.sim, prob=TRUE, col="lavender", xlab=expression(a))</pre>
```



##



```
## Compiling model graph
      Resolving undeclared variables
##
##
      Allocating nodes
  Graph information:
##
##
      Observed stochastic nodes: 6
##
      Unobserved stochastic nodes: 2
##
      Total graph size: 37
##
## Initializing model
##
## [1] 14000
##
## Iterations = 4010:14000
## Thinning interval = 10
## Number of chains = 4
## Sample size per chain = 1000
##
## 1. Empirical mean and standard deviation for each variable,
##
      plus standard error of the mean:
##
                   SD Naive SE Time-series SE
##
         Mean
       -0.992 0.2318 0.003666
                                       0.01011
## b -145.596 25.2995 0.400020
                                       1.32299
```

```
## 2. Quantiles for each variable:
##
## 2.5% 25% 50% 75% 97.5%
## a -1.483 -1.143 -0.9819 -0.8301 -0.57
## b -199.094 -161.784 -143.9363 -127.6517 -100.05
```

Classical logistic regression model

```
df <- data.frame("dosage" = x, "numtot" = n, "prop" = y/n)

# Centering dosages
df$dosage_centered <- df$dosage - mean(df$dosage)

glm.model <- glm(prop ~ dosage_centered, df, family= "binomial", weight= n)

summary(glm.model)$coef

## Estimate Std. Error z value Pr(>|z|)
## (Intercept) -0.9800475 0.2399331 -4.084669 4.413963e-05
## dosage_centered -146.6927209 26.3629619 -5.564349 2.631328e-08
```

Conclusion/Comparison:

. . .

Exercise 5

Exercise 6

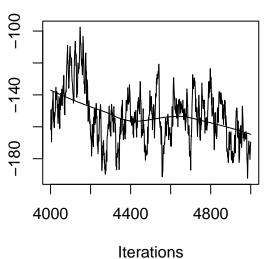
Run the code from the previous exercise with mice data with only one chain monitoring beta under the following two conditions:

1

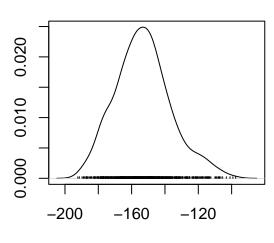
After an adaptation phase of 1000 and a burn-in of 4000 draw a sample of 1000 observations in one chain with thinning set to 1.

```
set.seed(44566)
inits_1chain <- list(a = 0, b = 0, .RNG.name = "base::Wichmann-Hill", .RNG.seed = 123456)
# model initiation
model.jags <- jags.model(</pre>
  file = "TempModel.txt",
  data = mice_data,
  inits = inits_1chain,
  n.chains = 1,
  n.adapt = 1000)
## Compiling model graph
      Resolving undeclared variables
##
##
      Allocating nodes
## Graph information:
      Observed stochastic nodes: 6
##
##
      Unobserved stochastic nodes: 2
##
      Total graph size: 37
##
## Initializing model
# burn-in
update(model.jags, n.iter = 4000)
# sampling
fit.jags.coda_1 <- coda.samples(</pre>
  model = model.jags,
  variable.names = "b",
  n.iter = 1000,
  thin = 1)
#summary(fit.jags.coda)
par(mfrow=c(1,2), mar=c(10,2,4,3))
plot(fit.jags.coda_1)
```





Density of b



N = 1000 Bandwidth = 4.219

$\mathbf{2}$

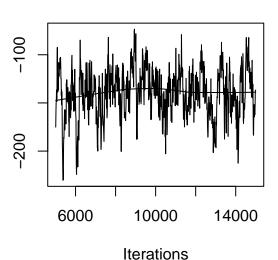
After an adaptation phase of 1000 and a burn-in of 4000 draw a sample of 10000 observations in one chain with thinning set to 10.

```
set.seed(44566)

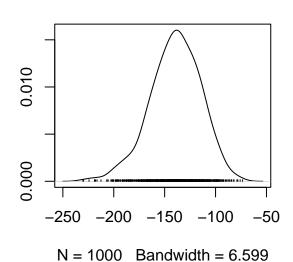
# sampling
fit.jags.coda_2 <- coda.samples(
    model = model.jags,
    variable.names = "b",
    n.iter = 10000,
    thin = 10)

#summary(fit.jags.coda)
par(mfrow=c(1,2), mar=c(10,2,4,3))
plot(fit.jags.coda_2)</pre>
```





Density of b



(a)

For which of the above conditions the ESS estimates will be larger and why?

Without thinning, the samples are dependent on preceding samples since the Markov Chain is kept intact. With thinning, only every x'th sample is chosen, so this dependence is disrupted, and autocorrelation is reduced. Which lower autocorrelation, the resulting ESS is higher.

(b)

To check your answer: Apply both the 05ess.R code and the function effectiveSize from the coda package. Compare the ESS estimates with those obtained with the n.eff function from package stableGR (Vats and Knudson, 2021). Please report your findings.

```
ess_t1 <- ess(fit.jags.coda_1[[1]], 1000)
ess_t10 <- ess(fit.jags.coda_2[[1]], 1000)

coda_ess_t1 <- as.numeric(effectiveSize(fit.jags.coda_1))
coda_ess_t10 <- as.numeric(effectiveSize(fit.jags.coda_2))

stableGR_ess_t1 <- as.numeric(n.eff(fit.jags.coda_1)$n.eff)
stableGR_ess_t10 <- as.numeric(n.eff(fit.jags.coda_2)$n.eff)</pre>
```

Setting	custom function	coda::effectiveSize	stableGR::n.eff
n.iter = 1000, thin = 1	21.01	26.67	17.54
n.iter = 10000, thin = 10	65.411	83.97	65.049

Indeed, the effective sample sizes are higher with thinning. The different packages don't all return exactly the same values, but they're in comparable ranges.